Stepan Gordeev Texas Christian University Sudhir Singh University of Rochester

Nov 2, 2024

NEUDC

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how does heterogeneous product choice affect aggregate misallocation cost?

DATA

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COMPARED TO THE MULTI-PRODUCT MODEL, STANDARD 1-PRODUCT MODELS:

· overstate frictions in data

PRFVIFW

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 - → understate total cost of misallocation

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 - ▶ why
 - but mechanisms apply equally to other sectors

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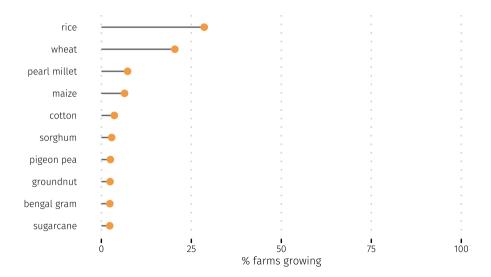
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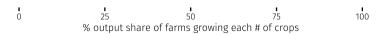
MULTI-PRODUCT FARMS IN INDIA

CROP CHOICE IS HETEROGENEOUS



MANY FARMS GROW MULTIPLE CROPS, MAINLY ACROSS SEASONS





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· 3 agricultural seasons: Kharif (monsoon), Rabi (winter/spring), Zaid (summer/dry)

PRODUCTION FUNCTIONS

$$y_{f,i,t} = z_{f,i,t} l_{f,i,t}^{\gamma_i} x_{labor,f,i,t}^{\alpha_{labor,i}} x_{inter,f,i,t}^{\alpha_{inter,i}}$$

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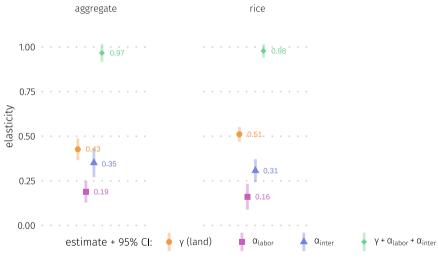
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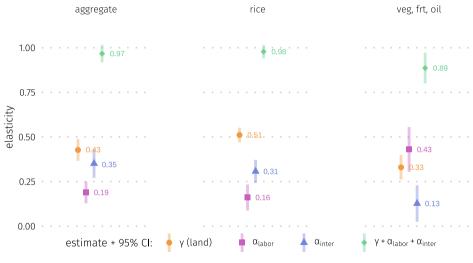
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· OBJECTIVES:

model multi-product farm decisions in presence of distortions

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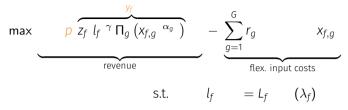
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- add multi-product farms choosing among heterogeneous products



• profit-maximizing farm f: sells output py_f , pays for inputs

$$\max \underbrace{p \underbrace{\frac{y_f}{Z_f l_f} \, {}^{\gamma} \, \Pi_g \left(x_{f,g} \, {}^{\alpha_g} \, \right)}_{\text{revenue}} - \underbrace{\sum_{g=1}^G r_g}_{\text{flex. input costs}} X_{f,g}$$

$$\text{s.t.} \qquad l_f \qquad = L_f \quad (\lambda_f)$$

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- · land input l is in fixed supply L_f
 - almost no land market in India

FARM: DISTORTIONS

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- between farms: $\tau_{1,g} > \tau_{2,g} \ \forall g \ \rightarrow$ farm 1 is "too small" given its TFP z_f
- · L_f fixed \rightarrow land is also distorted unless distributed to equalize λ_f
 - e.g. lacking property rights, communal land distribution

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- · $\mathit{L_f}$ fixed ightarrow land is also distorted unless distributed to equalize λ_f
 - e.g. lacking property rights, communal land distribution
- distortions extracted from observed input, output choices
 - rationalize all heterogeneity in data ► details

FARM: MULTIPLE PRODUCTS

$$\max \underbrace{\sum_{i=1}^{N} p_{i} \underbrace{Z_{f,i} l_{f,i} \gamma_{i} \Pi_{g} \left(X_{f,g,i} \alpha_{g,i} \right)}_{\text{revenue}} - \underbrace{\sum_{g=1}^{G} r_{g} \tau_{f,g} \sum_{i=1}^{N} \tau_{f,g,i} X_{f,g,i}}_{\text{flex. input costs}}$$

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 - params of crop i change $o \lambda_f$ changes o inputs and outputs of crops -i change
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FARM: FIXED COST

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- fixed cost ω per produced crop
 - ightarrow farms choose $crop\ set$ in addition to $crop\ mix$
 - farms don't all produce everything
 - → fit observed heterogeneity in crop sets

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▶ reallocation exercise details ▶ sensitivity to concavity ▶ role of states, seasons



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 - products (crops) are ∼homogeneous across firms (farms)
- but mechanism applies to non-agricultural settings too
 - → relevant for *more* developed countries too



FARM SOLUTION EXPRESSIONS

$$\begin{split} \sum_{i \in l_f} \left(\lambda_f^{\frac{\eta \sum_g \alpha_{g,i} - 1}{1 - \eta \sum_g \alpha_{g,i} - \eta \gamma_i}} \right) \left(\left(p_i z_{f,i} \right)^{\eta} \eta \left(\frac{\gamma_i}{\tau_{f,l,i}} \right)^{1 - \eta \sum_g \alpha_{g,i}} \Pi_g \left(\frac{\alpha_{g,i}}{r_g \tau_{f,g} \tau_{f,g,i}} \right)^{\eta \alpha_{g,i}} \right)^{\frac{1}{1 - \eta \sum_g \alpha_{g,i} - \eta \gamma_i}} \tau_{f,l,i} = L_f \\ x_{f,g,i} &= \frac{\alpha_{g,i}}{r_g \tau_{f,g} \tau_{f,g,i}} \left(\frac{\gamma_i}{\lambda_f \tau_{f,l,i}} \right)^{\frac{1 - \eta \sum_g \alpha_{g,i} - \eta \gamma_i}{\alpha_{g,i} - \eta \gamma_i}} \left(\left(p_i z_{f,i} \right)^{\eta} \eta \Pi_h \left(\frac{\alpha_{h,i}}{r_h \tau_{f,h} \tau_{f,h,i}} \right)^{\eta \alpha_{h,i}} \right)^{\frac{1}{1 - \eta \sum_h \alpha_{h,i} - \eta \gamma_i}} \\ l_{f,i} &= \left(\left(p_i z_{f,i} \right)^{\eta} \eta \left(\frac{\gamma_i}{\lambda_f \tau_{f,l,i}} \right)^{1 - \eta \sum_g \alpha_{g,i}} \Pi_g \left(\frac{\alpha_{g,i}}{r_g \tau_{f,g} \tau_{f,g,i}} \right)^{\eta \alpha_{g,i}} \right)^{\frac{1}{1 - \eta \sum_g \alpha_{g,i} - \eta \gamma_i}} \end{split}$$

LIST OF CROPS

Crop list

Rice	Wheat	Other Cereals	Pulses	Oilseeds, Fruits and Vegetables		
		Barley Maize Sorghum Pearl millet Finger millet Others	Black gram Green peas Pigeon peas Horse gram Cowpea Kidney bean Lentil Chickpeas Others	Oilseeds Sesame Groundnut Castor Sunflower Niger Soybean Safflower Rapseed Linseed Others	Vegetables Ash gourd Beet root Bitter gourd Bottle gourd Eggplant Board bean Cabbage Cauliflower Carrot Potato Cucumber Peas	Fruits / Condiments Mango Papaya Grapes Plum Cardamom Chilli Cumin Dill seed Indian mustard Other

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- · output:
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- 2SLS first stage:

$$M_{j,i,t} = Z_{k \neq j,i,t} + \mu_{j,i,t}$$

- M = land, labor, intermediates
- $Z_{k \neq j,i,t}$: instruments from other plots within farm
 - > agricultural shocks interacted with plot characteristics
 - > household, community characteristics & shocks interacted with plot characteristics



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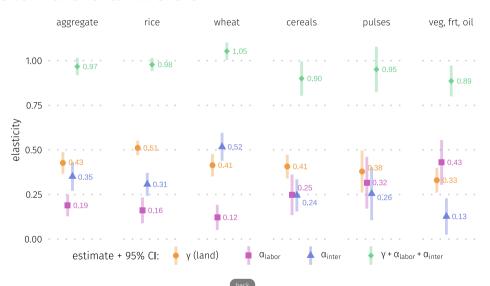
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- · → quality index = predicted price/acre
- quality-adjusted land = quality index × plot area

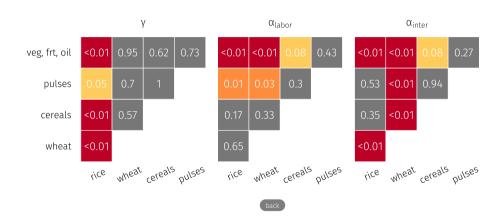
PRODUCTION FUNCTIONS: ALL CROPS



PRODUCTION FUNCTIONS: TABLE

	Aggregate	Rice	Wheat	Other Cereals	Pulses	Veg, Frt, Oil
Land	0.427	0.511	0.414	0.407	0.379	0.330
	(0.031)	(0.021)	(0.032)	(0.034)	(0.060)	(0.035)
Labor	0.189	0.161	0.122	0.248	0.316	0.430
	(0.031)	(0.037)	(0.036)	(0.058)	(0.074)	(0.064)
Intermediates	0.351	0.307	0.517	0.245	0.255	0.127
	(0.041)	(0.033)	(0.040)	(0.046)	(0.076)	(0.052)
Observations	14,705	4,807	3,566	2,779	1,128	2,338
R^2	0.624	0.742	0.713	0.590	0.417	0.572
Village FEs	Υ	Υ	Υ	Υ	Υ	Υ
Season FEs	Υ	Υ	Υ	Υ	Υ	Υ
	First Stage: F statistics					
Land	77.0	62.0	40.3	37.8	15.7	19.3
Labor	49.3	34.7	17.7	25.2	12.9	14.8
Intermediates	35.8	31.7	21.5	19.9	8.9	11.8
K-Paap Wald F statistic	51.1	40.4	16.0	30.8	12.4	12.7

PRODUCTION FUNCTIONS: PAIRWISE EQUALITY TEST P-VALUES



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- for each farm, pick profit-maximizing crop set



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$$r_{g}\tau_{f,g}\tau_{f,g,i} = \frac{\alpha_{g,i}\eta\left(p_{i}y_{f,i}\right)^{\eta}}{x_{f,g,i}} = mrpg_{f,i}$$
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 \cdot split of r_g from $au_{f,g}$ imposed by GE

ESTIMATE THE ELASTICITY OF SUBSTITUTION

· from consumption FOC:

$$\log\left(\frac{p_iC_i}{\sum_j p_jC_j}\right) = -\log\left(\sum_j \varphi_j^{\sigma} p_j^{1-\sigma}\right) + (1-\sigma)\log p_i + \sigma\log \varphi_i$$

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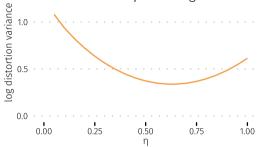
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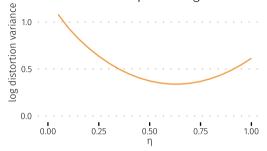
	$\log s_{h,i}$
σ	1.699
$\log p_{h,i}$	-0.699 (0.067)
Observations Kleibergen-Paap F stat	40,833 230.9

Village-level instruments: Elevation \times rain, ruggedness \times rain, pucca roads availability

 \cdot τ s reproducing data need to be extreme if η is too high or too low

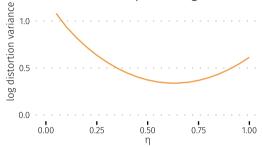


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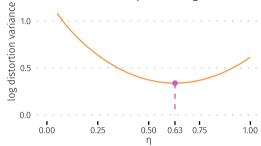
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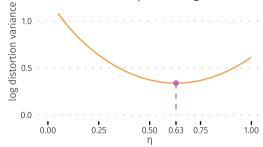
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- \rightarrow pick η that minimizes distortions required to explain observed output distribution
 - → conservative misallocation estimates

• τ s reproducing data need to be extreme if η is too high or too low



- · low η : farm, farm-crop output more uniformly distributed in efficient allocation
 - ightarrow data farm size "too varied", farms mix crops "too little" ightarrow extreme distortions
- high η : farm, farm-crop output more dispersed in efficient allocation
 - ightarrow data farm size "too uniform", farms mix crops "too much" ightarrow extreme distortions
- \rightarrow pick η that minimizes distortions required to explain observed output distribution
 - → conservative misallocation estimates
- ▶ details

• representative consumer buys crops, sells inputs, receives profit from owned farms

$$\max_{\{C_i\}_{i=1}^N} \left(\sum_i \varphi_i C_i^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

s.t.

$$\sum_{i} p_{i}C_{i} = \sum_{g} r_{g}X_{g}^{agg} + \Pi$$

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▶ profits details

· farm-crop revenue:

$$p_{i}y_{f,i} = \left(\underbrace{\left(\frac{1}{\lambda_{f}\tau_{f,m,i}}\right)^{\gamma_{i}}\Pi_{g}\left(\frac{1}{\tau_{f,g}\tau_{f,g,i}}\right)^{\alpha_{g,i}}}_{\text{composite distortion, } dist_{f,i}}\right)^{\frac{1}{1-\eta(\sum_{g}\alpha_{g,i}+\gamma_{i})}}\underbrace{\left(p_{i}Z_{f,i}\gamma_{i}^{\gamma_{i}}\eta^{\sum_{g}\alpha_{g,i}+\gamma_{i}}\Pi\left(\frac{\alpha_{g,i}}{r_{g}}\right)^{\alpha_{g,i}}\right)^{\frac{1}{1-\eta(\sum_{g}\alpha_{g,i}+\gamma_{i})}}}_{\text{"objective" factors}}$$

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· $Var(\log dist_{f,i})$ needed to match observed output dispersion depends on chosen η

GE PROFITS

$$\Pi = \sum_{f} \left[\sum_{i=1}^{N} p_{i} y_{f,i} - \sum_{g=1}^{G} r_{g} \sum_{i=1}^{N} x_{f,g,i} \right]$$

- distortions au, fixed costs ω , concavity η are not reflected in dividends sent to consumer
 - farmers act as if frictions they face had monetary representations
 - but these are non-monetary and not added/subtracted from dividends
- equivalent formulation: aus, ω s are monetary taxes/subsidies, administered by consumer
 - show up in dividends and consumer's BC as government revenue/expense
- choice is arbitrary: both formulations (or any mixture) produce identical equilibrium conditions

REALLOCATION

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- · compare reallocation gain between multi-product model and 1-product model
 - ► reallocation exercise details

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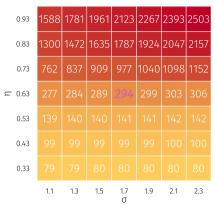
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 - ightarrow need to parameterize **unconditional** z, au distributions and calibrate to match observed **conditional** distributions



	0.93	1588	1781	1961	2123	2267	2393	2503
	0.83	1300	1472	1635	1787	1924	2047	2157
	0.73	762	837	909	977	1040	1098	1152
=	0.63			289	294	299	303	306
	0.53							
	0.43							
	0.33							
		1.1	1.3	1.5	1.7 σ	1.9	2.1	2.3

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(a) reallocation gain, %



(b) single-product model error, %

- misallocation estimates are always sensitive to calibrated concavity
 - firms can expand grow more easily in reallocation \rightarrow greater gain
- $\boldsymbol{\cdot}$ sign and magnitude of single-product model's error also depends on calibration



REALLOCATION: ROLE OF STATES AND SEASONS

	main	within state	no split by season
multi-product:	294%	107%	314%
1-product:	212%	124%	260%

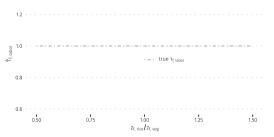
back

• 1-product model misinterprets crop heterogeneity as frictions

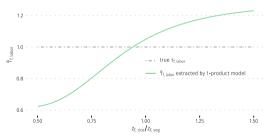
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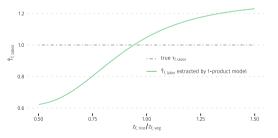


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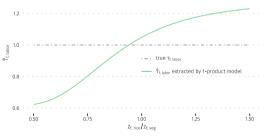


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 exercise to isolate: apply 1-product model to counterfactual reallocation data generated by multi-product model

• 1-product model understates TFP dispersion



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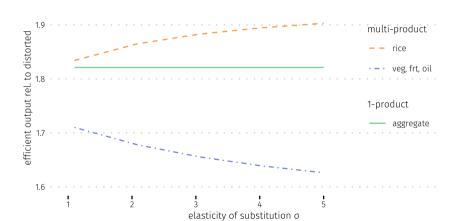
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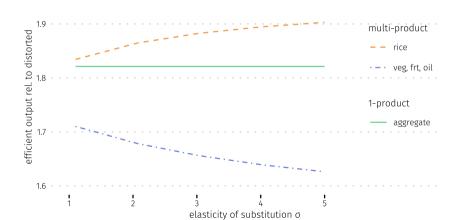
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- exercise to isolate: treat farm-crops as separate farms for 1-product model

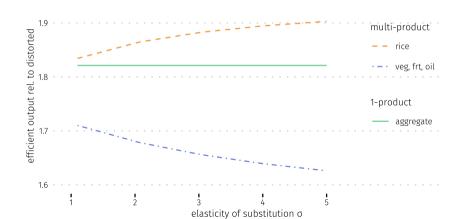
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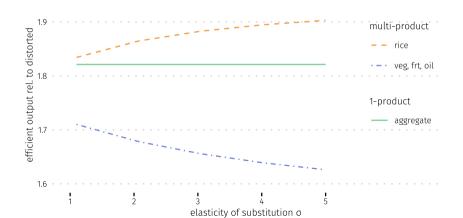
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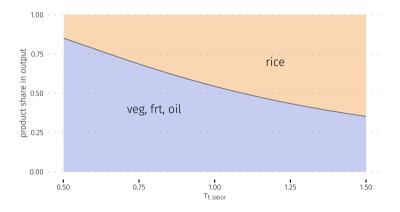
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 - exercise to isolate: rescale input elasticities to equalize returns to scale



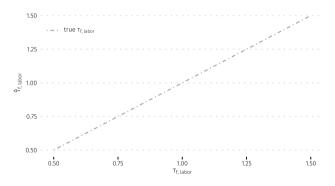
• simulated multi-product farm as labor distortion $\tau_{f,labor}$ is varied:



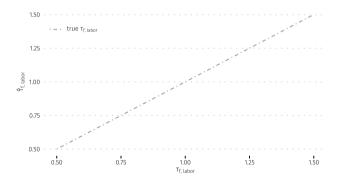
• $\tau_{f,labor} \uparrow \rightarrow$ shift from labor-intensive vegetables to land-intensive rice



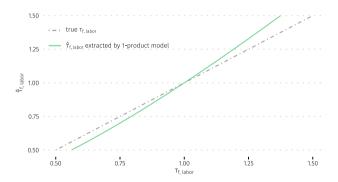
• apply **single**-product model to extract frictions from simulated **multi**-product data



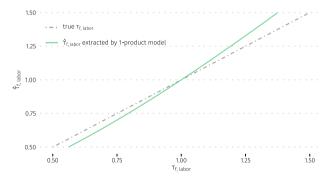
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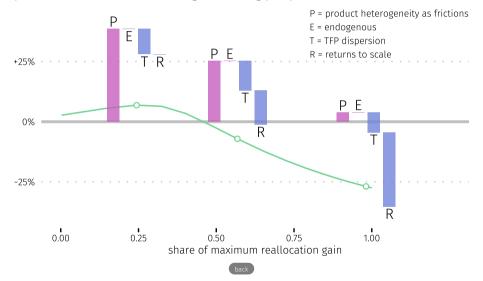


- exercise to isolate: prohibit farms in multi-product model to change product choice in counterfactuals
 - keep product sets fixed
 - keep input allocation across crops fixed: farm can choose $\sum_i x_{f,g,i}$ but $x_{f,g,i}$ gets a fixed share of total



Remove More Distortions → 1-Product Model Overstates

• 1-product error when conducting increasingly expansive reallocations:



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 - → understates misallocation
- **RETURNS TO SCALE** ▶ details
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- PRODUCT HETEROGENEITY AS FRICTIONS ► details
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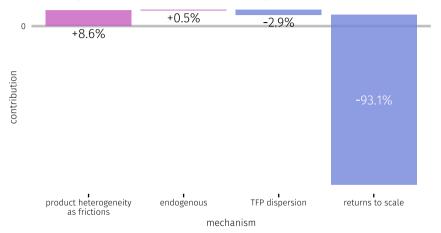


MECHANISMS DECOMPOSITION: BENCHMARK REALLOCATION

• benchmark: single-product model understates gain by 82 pp (28%)

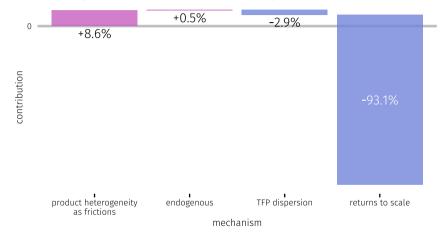
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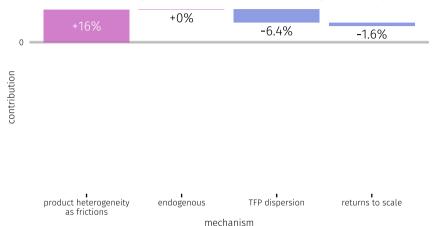
assess total drag of misallocation → firms' ability to expand matters most
 → single-product model understates misallocation

MECHANISMS DECOMPOSITION: "LEAST-DISTORTED STATE" REALLOCATION

• "least-distorted state": single-product model overstates gain by 10 pp (26%)

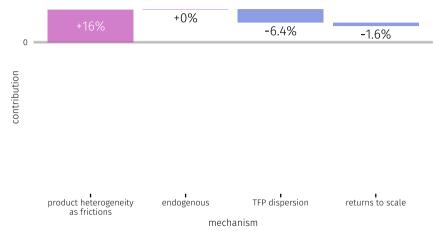
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- consider partial reallocations ightarrow estimation of frictions matters most
 - \rightarrow single-product model overstates misallocation \blacktriangleright details

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 - reflects aggr. TFP gain from better input allocation between farms
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- · compare reallocation gain between multi-product model and 1-product model
 - ▶ details

