Long-distance interaction between caller and callee

Stephan Boyer and Esther Wang

```
t ::=
                                       term
                                       value
          v
                                        variable
          \boldsymbol{x}
          t t
                                        application
          provide S as \varepsilon in t
                                       provide
                                        value
v ::=
                                        constant
          \lambda x : \tau . t
                                        abstraction
S ::=
                                        effect handler
                                       empty handler
           \varnothing_S
          S, s = t
                                       handler extension
\Delta ::=
                                       effect map
                                       empty effect map
           \varnothing_\Delta
          \Delta, \varepsilon = \Gamma
                                       effect map extension
\tau ::=
                                        type
                                        type of constants
          \kappa
                                        arrow type
          \sigma \to \sigma
                                       type with effects
\sigma ::=
           E ! \tau
                                        effect annotation
E ::=
                                       effect set
                                       empty effect
          \varnothing_{arepsilon}
          E, \varepsilon
                                       effect extension
\Gamma \coloneqq
                                        context
                                       empty context
           \varnothing_{\Gamma}
          \Gamma, x : \tau
                                       variable binding
                      Figure 1: Syntax
```

$$\begin{array}{c} \Gamma \vdash t : \sigma \\ \hline \\ \Gamma \vdash c : \varnothing_{\varepsilon} \, ! \, \kappa \end{array} \text{(T-Constant)} \\ \hline \\ \frac{x : \sigma \in \Gamma}{\Gamma \vdash x : \sigma} \, \text{(T-Variable)} \\ \hline \\ \frac{\Gamma, x : \tau \vdash t : \sigma}{\Gamma \vdash \lambda x : \tau \cdot t : \tau \to \sigma} \, \text{(T-Abstraction)} \\ \hline \\ \frac{\Gamma \vdash t_1 : E_1 ! \, \tau_1 \qquad \Gamma \vdash t_2 : E_2 \, ! \, (\tau_1 \to E_3 \, ! \, \tau_2)}{\Gamma \vdash t_2 \, t_1 : E_1, E_2, E_3 \, ! \, \tau_2} \, \text{(T-Application)} \\ \hline \\ \frac{\Gamma \vdash t : E \, ! \, \tau}{\Gamma \vdash t : E, \varepsilon \, ! \, \tau} \, \text{(T-Weaken)} \\ \hline \\ S = (\varnothing_S, s_1 = t_1, \ldots, s_n = t_n) \\ \Gamma \vdash t_i : E_i \, ! \, \tau_i \\ \sigma_i = E_i, \varepsilon \, ! \, \tau_i \\ \sigma_i = E_i, \varepsilon \, ! \, \tau_i \\ \varepsilon = \varnothing_{\Gamma}, s_1 : \sigma_1, \ldots, s_n : \sigma_n \in \Delta \\ \underline{\Gamma, s_1 : \sigma_1, \ldots, s_n : \sigma_n \vdash t : E \, ! \, \tau}{\Gamma \vdash \text{provide } S \text{ as } \varepsilon \text{ in } t : E - \varepsilon \, ! \, \tau} \, \text{(T-Provide)} \\ \hline \end{array}$$

Figure 2: Typing rules