Chapter 1 Exercises

- 1.11 Assume a 15cm diameter wafer has a cost of 12, contains 84 dies, and has 0.020 defects/cm². Assume a 20cm diameter wafer has a cost of 15, contains 100 dies, and has 0.031 defects/cm².
- 1.11.1 Find the yield for both wafers.

$$yield = \frac{1}{(1 + (Defects per area \times Die area))^{N}}$$

Wafer 1:

- Wafer area₁ = $\pi r^2 = \pi (\frac{15}{2})^2 = \frac{\pi 225}{4}$
- Die area₁ = $\frac{\text{Wafer area}}{\text{Dies per wafer}} = \frac{(\pi 225)/4}{84} = \frac{\pi 75}{112}$
- Defects per area₁ = 0.020
- $N_1 = 2$

$$\mathrm{yield}_1 = \frac{1}{(1 + (0.020 \times \frac{\pi75}{112}))^2} = 0.9208... \Rightarrow 0.92$$

$$yield_1 = 0.92$$

Wafer 2:

- Wafer area₂ = $\pi r^2 = \pi (\frac{20cm}{2})^2 = \pi 100$
- Die area $_2=\frac{\text{Wafer area}}{\text{Dies per wafer}}=\frac{\pi 100}{100}=\pi$
- Defects per $area_2 = 0.031$
- $N_2 = 2$

$$yield_2 = \frac{1}{(1 + (0.031 \times \pi))^2} = 0.8303... \Rightarrow 0.83$$

$$yield_2 = 0.83$$

1.11.2 Find the cost per die for both wafers.

$$\label{eq:cost_per_die} \text{Cost per wafer} \\ \frac{\text{Cost per wafer}}{\text{Dies per wafer} \times \text{yield}}$$

Wafer 1:

- Cost per wafer₁ = 12
- Dies per wafer₁ = 84
- yeild₁ = 0.9208

$$\label{eq:cost_cost} \text{Cost per die}_1 = \frac{12}{84 \times 0.9208} = 0.1551... \Rightarrow 0.16$$

Cost per
$$die_1 = 0.16$$

Wafer 2:

- Cost per wafer _2 = 15
- Dies per wafer $_2=100$
- $\cdot \ \mathrm{yeild}_2 = 0.8303$

Cost per
$$\text{die}_2 = \frac{15}{100 \times 0.8303} = 0.1806... \Rightarrow 0.18$$

Cost per
$$die_2 = 0.18$$

1.11.3 If the number of dies per wafer is increased by 10% and the defects per area unit increases by 15%, find the die area and yeild.

Wafer 1:

- Dies per wafer₁ = $84 + (0.1 \times 84) = 92.4$
- Wafer area₁ = $\pi r^2 = \pi (\frac{15cm}{2})^2 = \frac{\pi 225}{4}$
- Defects per area _1 = 0.020 + (0.15 \times 0.020) = 0.023
- $N_1 = 2$
- Cost per wafer₁ = 12

$$\mbox{Die area}_1 = \frac{\mbox{Wafer area}}{\mbox{Dies per wafer}} = \frac{(\pi 225)/4}{92.4} = \frac{\pi 375}{616}$$

Die area₁ =
$$\frac{\pi 375}{616}$$

$$\mathrm{yield}_1 = \frac{1}{(1 + (0.023 \times \frac{\pi 375}{616}))^2} = 0.9175... \Rightarrow 0.92$$

$$yield_1 = 0.92$$

Wafer 2:

- Dies per wafer₂ = $100 + (0.1 \times 100) = 110$
- Wafer area₂ = $\pi r^2 = \pi (\frac{20cm}{2})^2 = \pi 100$

- Defects per area
_2 = 0.031 + (0.15
$$\times$$
 0.031) = 0.03565

•
$$N_2 = 2$$

Die area₂ =
$$\frac{\text{Wafer area}}{\text{Dies per wafer}} = \frac{\pi 100}{110} = \frac{\pi 10}{11}$$

Die area₂ =
$$\frac{\pi 10}{11}$$

$$\mathrm{yield}_2 = \frac{1}{(1 + (0.03565 \times \frac{\pi 10}{11}))^2} = 0.8237... \Rightarrow 0.82$$

$$yield_2 = 0.82$$

- 1.15 Assume a program requires the execution of 50×10^6 FP instructions. 110×10^6 INT instructions, 80×10^6 L/S instructions, and 10×10^6 branch instructions. The CPI for each type of instruction is 1, 1, 4, and 2, respectively. Assume the processor has 2GHz clock rate.
- 1.15.1 By how much must we improve the CPI of FP instructions if we want the program to run two times faster?

Total CPU clock cycles before optimization:

$$(50 \times 10^6)(1) + (110 \times 10^6)(1) + (80 \times 10^6)(4) + (16 \times 10^6)(2) = 512 \times 10^6$$

Total CPU execution time before optimization:

$$\frac{512 \times 10^6}{2 \mathrm{GHz}} = 256 \times 10^{-3} \mathrm{s}$$

Goal CPU execution time before optimization:

$$\frac{256\times 10^{-3}s}{2} = 128\times 10^{-3}s$$

Goal total cycles for FP:

$$128 \times 10^{-3} \text{s} \times 2 \text{GHz} = 256 \times 10^{6}$$

FP CPI:

FP CPI =
$$\frac{256 - 462}{50}$$

$$FP \ CPI = -4.12$$

It is not possible to improve the FP CPI to make the program run 2 times faster.

1.15.2 By how much must we improve the CPI of L/S instructions if we want the program to run two times faster?

Goal CPU execution time before optimization:

$$\frac{256 \times 10^{-3} \text{s}}{2} = 128 \times 10^{-3} \text{s}$$

Goal total cycles for L/S:

$$128 \times 10^{-3} \text{s} \times 2 \text{GHz} = 256 \times 10^{6}$$

L/S CPI:

$$(50 \times 10^6)(1) + (110 \times 10^6)(1) + (80 \times 10^6)(L/S \text{ CPI}) + (16 \times 10^6)(2) = 512 \times 10^6$$

L/S CPI =
$$\frac{256 - 192}{80}$$

$$\mathrm{FP}\ \mathrm{CPI} = 4.625$$

CPI Improvement:

$$4/0.8 = 5$$

L/S instructions must be 5 times faster

1.15.3 By how much is the execution time of the program improved if the CPI of INT and FP instructions is reduced by 40% and the CPI of L/S and Branch is reduced by 30%?

New CPI

• FP:
$$(1 - (1) \times 0.4) = 0.6$$

• INT:
$$(1 - (1) \times 0.4) = 0.6$$

• L/S:
$$(4 - (4) \times 0.3) = 2.8$$

• Branch:
$$(2 - (2) \times 0.3) = 1.4$$

New total CPU clock cycles

$$(50 \times 10^6)(0.6) + (110 \times 10^6)(0.6) + (80 \times 10^6)(2.8) + (16 \times 10^6)(1.4) = 342.4 \times 10^6$$

New CPU execution time

$$\frac{342.4\times10^6}{2\mathrm{GHz}}=171.2\times10^{-3}\mathrm{s}$$

CPU execution time improvement:

$$\frac{256\times10^{-3}}{171.2\mathrm{s}\times10^{-3}\mathrm{s}}\times100\%=149.5\%$$

The execution time is improved by 149.5%