Discussion Assignment #2

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Question 2(d) What are the observed data O? Factorize the observed data distribution P_0 according to the time-ordering.

N i.i.d. copies of $O = (L_0, A_0, L_1, A_1, L_2) \sim P_0$ (with Y as a subset of the Ls)

Basic Probability reminder for factoring:

- \triangleright $P(A,B) = P(A \cup B) = P(A|B)XP(B)$
- ▶ If we know that say 10% of the class drinks coffee, and that of coffee drinkers, 50% like ginger cookies, then 5% of the class drinks coffee AND likes ginger cookies.
- ▶ So then, P(A, B, C) = P(A|B, C)XP(B|C)XP(C)

Because we have something that is a function of the joint distribution (P_0) we can factorize it using probability rules into conditional distributions that we can use.

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$$P(L_0, A_0, L_1, A_1, L_2) = P(L_2|A_1 = a_1, L_1 = l_1, A_0 = a_0, L_0 = l_0)XP(A_1|L_1 = l_1, A_0 = a_0, L_0 = l_0)$$

$$XP(L_1|A_0 = a_0, L_0 = l_0)XP(A_0|L_0 = l_0)XP(L_0 = l_0)$$

$$\prod_{0} P(L_{k} = I_{k} | \bar{A}_{k-1} = \bar{a}_{k-1}, \bar{L}_{k-1} = \bar{I}_{k-1}) X$$

$$\prod_{0}^{1} P(A_{k} = a_{k} | \bar{A}_{k-1} = \bar{a}_{k-1}, \bar{L}_{k-1} = \bar{I}_{k-1})$$

 $P(L_0, A_0, L_1, A_1, L_2) =$

Question 2(d) What are the observed data O? Factorize the observed data distribution P_0 according to the time-ordering.

$$P(O = o) = \prod_{k=0}^{2} Q(L_{k} = I_{k} | \bar{A}_{k-1} = \bar{a}_{k-1}, \bar{L}_{k-1} = \bar{I}_{k-1}) X$$

$$\prod_{k=0}^{1} g(A_{k} = a_{k} | \bar{A}_{k-1} = \bar{a}_{k-1}, \bar{L}_{k-1} = \bar{I}_{k-1})$$

Question 2(e): What assumptions are needed to identify the causal parameter from the observed data distribution?

In order to identify our causal parameter from the observed data distribution, we must use the:

- Sequential Randomization assumption, which assumes each a is independent of y (and which allows us to control for a different set of covariates at each time point)
- Positivity assumption, which assumes that no strata have few or no observations.
- 3. No unmeasured confounding
- 4. Correct model is specified
- 5. No measurement error

Question 2(f): Specify the G-computation formula (i.e. the statistical estimand) for this example.

$$E(Y_{\bar{a}}) = \sum_{0}^{1} E(Y|\bar{A}_{K} = \bar{a}_{K}, \bar{L}_{K} = \bar{I}_{K})X$$

$$\prod_{0}^{1} P(L_{k} = I_{k}|\bar{A}_{k-1} = \bar{a}_{k-1}, \bar{L}_{k-1} = \bar{I}_{k-1})$$