The background image shows a wide-angle view of a modern architectural complex at TU Delft. In the foreground, a large, light-colored concrete staircase with many steps leads up a grassy slope. Numerous people are sitting and walking on the stairs and the grass. In the background, a tall, cylindrical concrete structure with a lattice of thin metal poles and cables rises into a clear blue sky. The overall scene is bright and sunny, with green trees visible on the right side.

# Triogen Turbine Optimization

*Euler turbine model analysis*

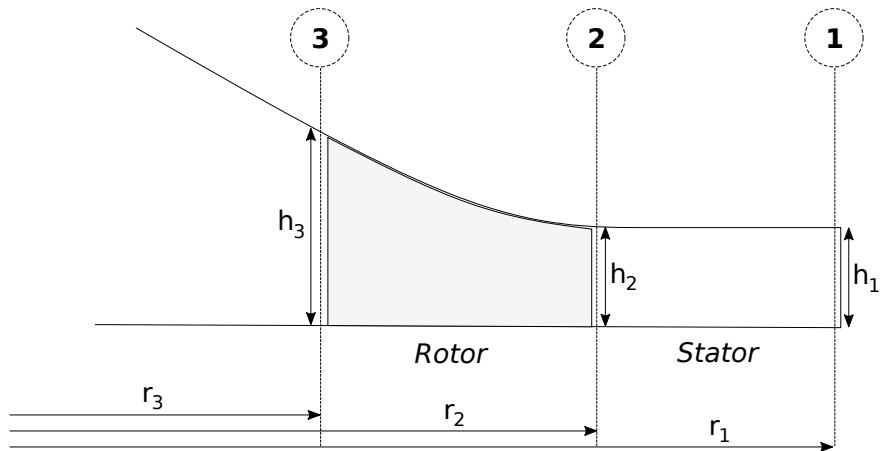
Delft University of Technology

Stephan Smit  
August 14, 2018

# Euler Turbine model

- 0-D model for Centripetal Radial Turbine
- Solves for each position in the turbine:
  - Total thermodynamic conditions (TC)
  - Static thermodynamic conditions (SC)
  - Velocity triangle (VT)
- Three main modelling assumptions:
  - Mass conservation at all turbine states
  - Conservation of total enthalpy between stator inlet and outlet
  - Conservation of rothalpy between rotor inlet and outlet
- Properties of Toluene included using Coolprop
- Written in Python (including parallized solution domain solving)

# Model schematic



# Euler Turbine model inputs

- Radial position and height at each state  $h_n, r_n$  for  $n = 1, 2, 3$
- Total conditions at inlet stator and the direction and magnitude of the velocity  $P_{01}, T_{01}, ||\bar{c}_1||, \alpha_1$
- Absolute velocity angle at inlet rotor  $\alpha_2$
- Static pressure at the outlet of the rotor  $P_3$
- Degree of reaction  $R$
- Speed of rotation  $\omega$

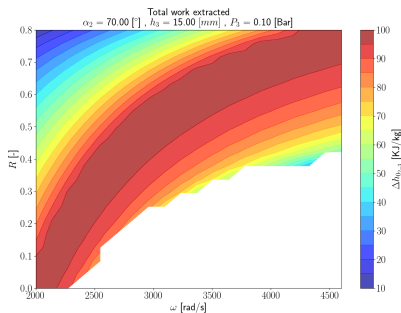
## Recap important equations

- Massflow:  $\dot{m} = \rho A c_r$
- Total Enthalpy:  $h_0 = h + \frac{||\bar{c}||^2}{2}$
- Rothalpy:  $I = h + \frac{||\bar{w}||^2}{2} - \frac{||\bar{U}||^2}{2}$
- Degree of reaction:  $R = \frac{h_2 - h_3}{h_1 - h_3}$
- Velocity triangles:  $\bar{c} = \bar{w} + \bar{U}$
- Angular velocity:  $\bar{U} = [U_r, U_\theta]^T = [0, \omega r]^T$
- Specific work  $w = U_{\theta-2} c_{\theta-2} - U_{\theta-3} c_{\theta-3}$

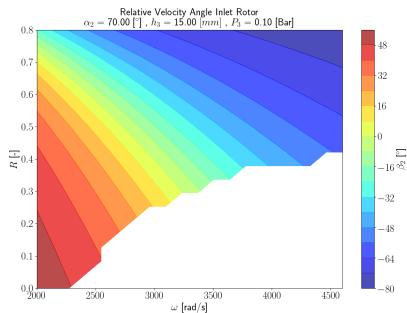
# Model solving procedure

- 1 Calculate  $U_2$  and  $U_3$  using  $\omega$ ,  $r_2$ , and  $r_3$
- 2 Calculate  $TC|_1$ ,  $SC|_1$  and  $VT|_1$ , using  $P_{01}$ ,  $T_{01}$ ,  $||\bar{c}_1||$  and  $\alpha_1$
- 3 Calculate  $m_1$  with  $A_1$ ,  $SC|_1$  and  $VT|_1$
- 4 Assuming  $s_3 = s_1$ , calculate  $SC|_3$  using  $P_3$
- 5 Assuming  $s_2 = s_1$ , calculate  $SC|_2$  by means of  $R$  and  $SC|_3$
- 6 Assuming  $TC|_1 = TC|_2$ , calculate  $||\bar{c}_2||$  using  $SC|_2$
- 7 Given  $\alpha_2$ , calculate  $VT|_2$
- 8 Given  $VT|_2$  find  $h_2$  such that  $\dot{m}_2 = \dot{m}_1$
- 9 Given  $l_2 = l_3$ ,  $SC|_2$  and  $SC|_3$  calculate  $\bar{w}_3$
- 10 Given the  $\dot{m}_3 = \dot{m}_2$  and the  $SC_3$  calculate  $c_{r-3}$
- 11 Using  $c_{r-3}$  and  $\bar{w}_3$  calculate the  $VT|_3$
- 12 Calculate  $h_{03}$  using the Eulerian work formula and  $VT|_2$  and  $VT|_3$
- 13 Calculate  $TC|_3$  with  $h_{03}$  and  $s_3$

# Effect of DOR and Rotational Speed

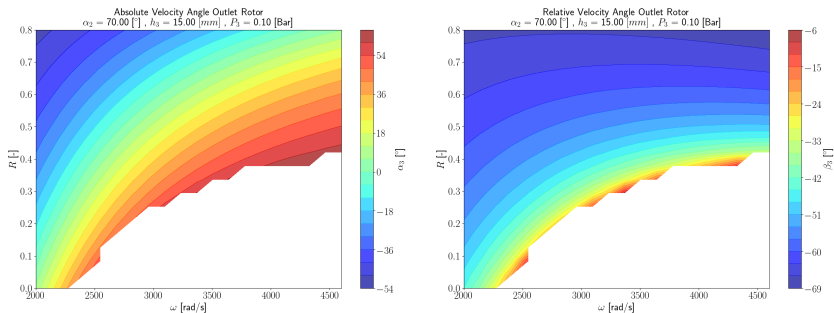


(a) Work extracted



(b) Relative Flow Angle Inlet Rotor

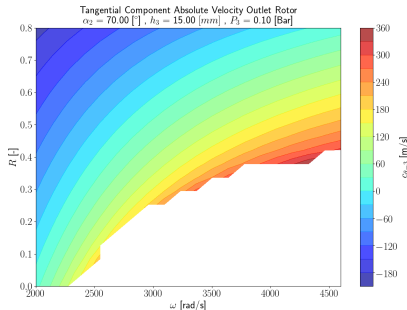
# Effect of DOR and Rotational Speed



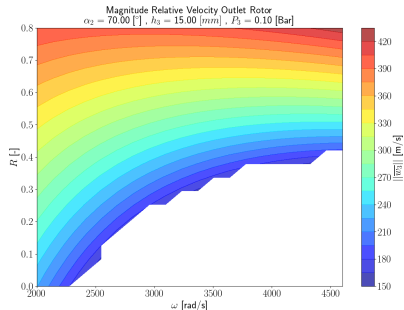
(a) Absolute Flow Angle Outlet Rotor (b) Relative Flow Angle Outlet Rotor



# Effect of DOR and Rotational Speed

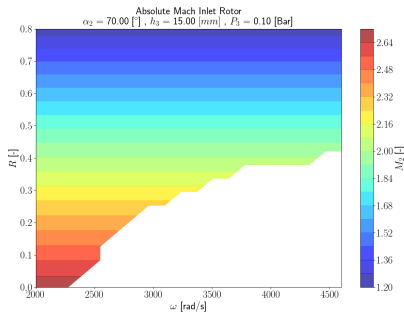


(a) Tangential Absolute Velocity  
Outlet Rotor

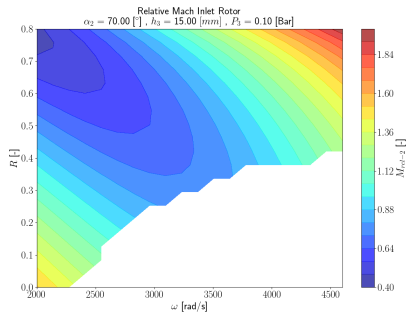


(b) Magnitude Relative Velocity  
Outlet Rotor

# Effect of DOR and Rotational Speed

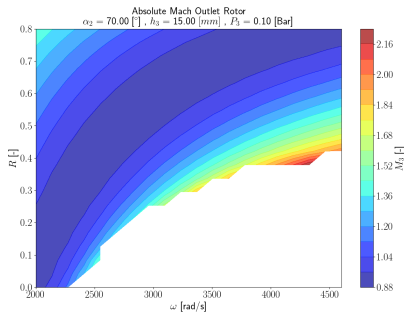


(a) Absolute Mach Inlet Rotor

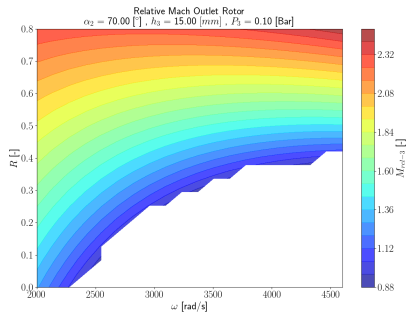


(b) Relative Mach Inlet Rotor

# Effect of DOR and Rotational Speed



(a) Absolute Mach Outlet Rotor



(b) Relative Mach Outlet Rotor

# Conclusion on the basis of 0-Model

- In simulations we saw that at higher rotational speed the relative outflow angle was not equal to the trailing angle (much smaller)
- 0-D model tells us that this is due to massflow conservation, the area is too small, therefore a large radial component is necessary, reducing the angle
- Can be resolved by increasing the area at the outlet of the rotor