

# Moving Home: Non-Market Housing and Labour Market Risk

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# Introduction

## New empirical evidence (Health and Retirement Study)

- ▶ Children who lose their job are more likely to move home with parents
  - ▶ NEW Effect is present both at young adulthood and into middle age
  - ▶ Kaplan (2012): evidence for men 17-22, NLSY97
- ▶ Effect is robust to controlling for income, eldercare, and parent characteristics

## Research questions

1. How does parental coresidence affect job market search among adult children?
2. How does welfare from coresidence interact with the optimal level of UI?

# Contribution

## **Empirical:** Health and Retirement Study

- ▶ Children are more likely to move home when transitioning into unemployment
  - ▶ NEW Observed for children into middle age

## **Quantitative:** structural lifecycle model of job search and coresidence

- ▶ Consumers with the option to move home search in higher-wage submarkets
- ▶ Welfare from the move home option is decreasing in the size of the UI benefit

## HRS Data Selection: Definition of Cross-wave Flows

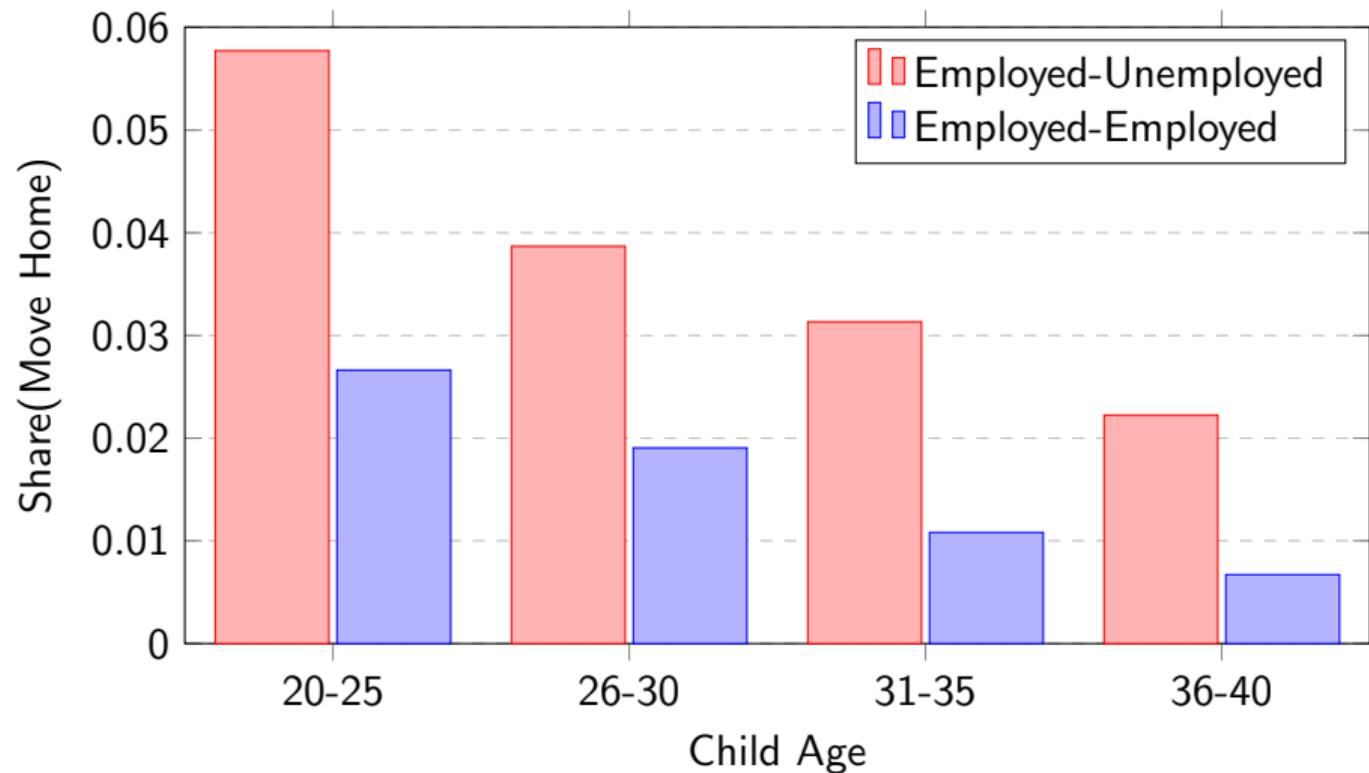
**Employment:** two types of job transitions

1. Employed-Employed: working in two subsequent waves
2. Employed-Unemployed: working in the previous wave but not in the current wave

**Coresidence:** child lives independently previously and coresides in the current wave

- ▶ If parent is a homeowner and child is not: child moves home
- ▶ If child is a homeowner and parent is not: child hosts parent
- ▶ Neither (or both) parent and child are homeowners: ambiguous coresidence

## HRS: E-U children are more likely to move home at all working ages



# Probit: Average Marginal Effects on Share(Move Home)

**Dependent variable:** indicator for moving home after living independently

| <b>Independent Variable</b> | Child Age   |           |           |           |
|-----------------------------|-------------|-----------|-----------|-----------|
|                             | (1) 20-25   | (2) 26-30 | (3) 31-35 | (4) 36-40 |
| Employed-Unemployed         | .0312***    | .0194***  | .0169***  | .0050*    |
| Transfer from Parent        | .0096*      | .0130***  | .0078***  | .0044***  |
| Child Income                |             |           |           |           |
| <10K                        | <i>Base</i> |           |           |           |
| 10-35K                      | -.0173***   | -.0036    | -.0137*** | -.0076**  |
| 35-70K                      | -.0387***   | -.0051    | -.0245*** | -.0147*** |
| 70-100K                     | -.0205      | -.0068    | -.0268*** | -.0154*** |
| 100K+                       | .           | -.0039    | -.0274*** | -.0168*** |
| Child Gender (Female)       | .0039       | -.0013    | -.0074*** | -.0048*** |
| Child Marital Status        | -.0655***   | -.0328*** | -.0201*** | -.0134*** |
| Child Parental Status       | .0162**     | -.0050*   | .0064***  | .0010     |
| <b>Mean Share(MH)</b>       | .0301       | .0147     | .0100     | .0071     |

# Model

## Model – Consumers

- ▶ Consumers are heterogeneous productivity, assets, and age
  - ▶ NEW option to coreside with a parent
  - ▶ Assumed to be purely altruistic: no strategic interaction b/t agents
  - ▶ **Tradeoff:** can avoid housing costs but lose out on utility from living independently
  - ▶ Independence utility subject to a Type-I extreme value shock
- ▶ When young, consumers choose:
  - ▶ Submarket (piece-rate) for search
  - ▶ Whether to coreside or live independently (up to age 40)
  - ▶ Saving for next period
- ▶ When old, consumers choose:
  - ▶ Saving for next period

## Consumer Preferences – Utility

$$U(j, a, \epsilon) = \frac{c^{1-\sigma}}{1-\sigma} + d_h \chi$$

Where:

- ▶  $j$ : age
- ▶  $a$ : assets
- ▶  $\epsilon$ : individual-specific productivity
- ▶  $\chi$ : independence utility

$d_h$  = 1 when a consumer lives independently, = 0 when they coreside

- ▶ Beyond age 40,  $d_h$  = 1 for all consumers

## Consumer Preferences – Budget Constraints

**Employed:**  $c + a' = (1 - \tau)\phi\epsilon_j + (1 + r)a - d_h\kappa_h$

**Unemployed:**  $c + a' = (1 - \tau)b + (1 + r)a - d_h\kappa_h$

**Retired:**  $c + a' = (1 - \tau)S + (1 + r)a - \kappa_h$

Where:

- ▶  $\phi$ : piece-rate determined by submarket choice
- ▶  $b$ : unemployment benefit
- ▶  $S$ : pension benefit
- ▶  $\kappa_h$ : cost of housing
- ▶  $\tau$ : proportional tax on income
- ▶  $r$ : interest rate
- ▶  $a'$ : savings choice

## Labour Market – Workers

- ▶ Directed search in submarkets on age  $j$ , piece-rate  $\phi$ , and worker productivity  $\epsilon$
- ▶ Den Haan matching function  $M(u, v) = \frac{uv}{(u^\alpha + v^\alpha)^{\frac{1}{\alpha}}}$  with market tightness  $\theta = \frac{v}{u}$
- ▶ Find job at rate  $f(\theta) = \frac{M(u,v)}{u}$
- ▶ Provide individual-specific productivity  $\epsilon$  to the firm
- ▶ Earn wage as an after-tax share of output:  $w = (1 - \tau)\phi\epsilon_j$
- ▶ Proportional tax on output finances unemployment benefit  $b$

## Labour Market – Firms

- ▶ Hire worker at rate  $q(\theta) = \frac{M(u,v)}{v}$  after paying posting cost  $\kappa_p$
- ▶ Match is destroyed in each subsequent period with probability  $\delta$

**Firm's value function:**

$$V_f(j, \epsilon, \phi) = \epsilon_j(1 - \phi) + \beta(1 - \delta)V(j + 1, \epsilon, \phi)$$

**Vacancy posting decision:**  $\max\{V_f(j, \epsilon, \phi) - \kappa_p, 0\} \quad \forall j, \epsilon, \phi$

[Search Equilibrium](#)

## Value Functions – Young Consumers

$$V_s(j, a, \epsilon) = \max_{\phi} \{ f(\theta(j, a, \epsilon)) V_u(j, a, \epsilon) + [1 - f(\theta(j, a, \epsilon))] V_e(j, a, \epsilon, \phi) \}$$

$$V_u(j, a, \epsilon) = \max \mathbf{E}_{\xi^c, \xi^i} \{ V_u^{cores}(j, a, \epsilon) + \xi^c, V_u^{ind}(j, a, \epsilon) + \xi^i \}$$

$$V_e(j, a, \epsilon, \phi) = \max \mathbf{E}_{\xi^c, \xi^i} \{ V_e^{cores}(j, a, \epsilon, \phi) + \xi^c, V_e^{ind}(j, a, \epsilon, \phi) + \xi^i \}$$

Where:

- ▶  $V_u^{cores}(j, a, \epsilon), V_u^{ind}(j, a, \epsilon)$ : consumer's value of coresiding and living independently while unemployed
- ▶  $V_e^{cores}(j, a, \epsilon, \phi), V_e^{ind}(j, a, \epsilon, \phi)$ : consumer's values while employed
- ▶  $\xi^{cores}, \xi^{ind}$  are Type-I extreme value shocks on the coresidence choice

## Value of Unemployment

$$V_u(j, a, \epsilon) = \max \mathbf{E}_{\xi_c, \xi_i} \left\{ V_u^{cores}(j, a, \epsilon) + \xi_c, V_u^{ind}(j, a, \epsilon) + \xi_i \right\}$$

$$V_u^{cores}(j, a, \epsilon) = \max_{a' \geq 0} \left\{ \frac{[b + (1+r)a - a']^{1-\sigma}}{1-\sigma} + \beta V_s(j+1, a', \epsilon) \right\}$$

$$V_u^{indep}(j, a, \epsilon) = \max_{a' \geq 0} \left\{ \frac{[b + (1+r)a - a' - \kappa_h]^{1-\sigma}}{1-\sigma} + \chi + \beta V_s(j+1, a', \epsilon) \right\}$$

## Value of Employment

$$V_e(j, a, \epsilon, \phi) = \max \mathbf{E}_{\xi_c, \xi_i} \{ V_e^{cores}(j, a, \epsilon, \phi) + \xi_c, V_{ind}^e(j, a, \epsilon, \phi) + \xi_i \}$$

$$\begin{aligned} V_e^{cores}(j, a, \epsilon, \phi) = \max_{a' \geq 0} & \left\{ \frac{[(1 - \tau)\epsilon_j \phi + (1 + r)a - a']^{1-\sigma}}{1 - \sigma} \right. \\ & \left. + \beta[(1 - \delta)V_e(j + 1, a', \epsilon, \phi) + \delta V_s^e(j + 1, a', \epsilon)] \right\} \end{aligned}$$

$$\begin{aligned} V_e^{indep}(j, a, \epsilon, \phi) = \max_{a' \geq 0} & \left\{ \frac{[(1 - \tau)\epsilon_j \phi + (1 + r)a - a' - \kappa_h]^{1-\sigma}}{1 - \sigma} + \chi \right. \\ & \left. + \beta[(1 - \delta)V_e(j + 1, a', \epsilon, \phi) + \delta V_s(j + 1, a', \epsilon)] \right\} \end{aligned}$$

## Value Functions – Old Consumers

$$V_r(j, a) = \max_{a'} \left\{ \frac{[S + (1+r)a - a' - \kappa_h]^{1-\sigma}}{1-\sigma} + \beta \psi_j V^r(j+1, a') \right\}$$

Where  $\psi_j$  is a survival probability that increases in age

## Government

The government provides an unemployment benefit ( $b$ ) and pension benefit ( $S$ ) by choosing income taxes ( $\tau$ ) such that:

$$\int \tau \epsilon_j \phi d\omega_e(j, a, \epsilon, \phi) = \int b d\omega_u(j, a, \epsilon) + \int S d\omega_r(j, a)$$

Where  $\omega_e, \omega_u, \omega_r$  are stationary distributions of employed, searchers, and retirees

# Equilibrium

Given initial distributions of assets and productivity there is an equilibrium such that:

1. Consumers solve their problem by choosing a piece-rate, coresidence, and saving
2. Firms face zero expected profits for each submarket in which they post
3. Government funds unemployment and pension benefits via a proportional tax

Solution Algorithm

# Results

## Calibration: Internal

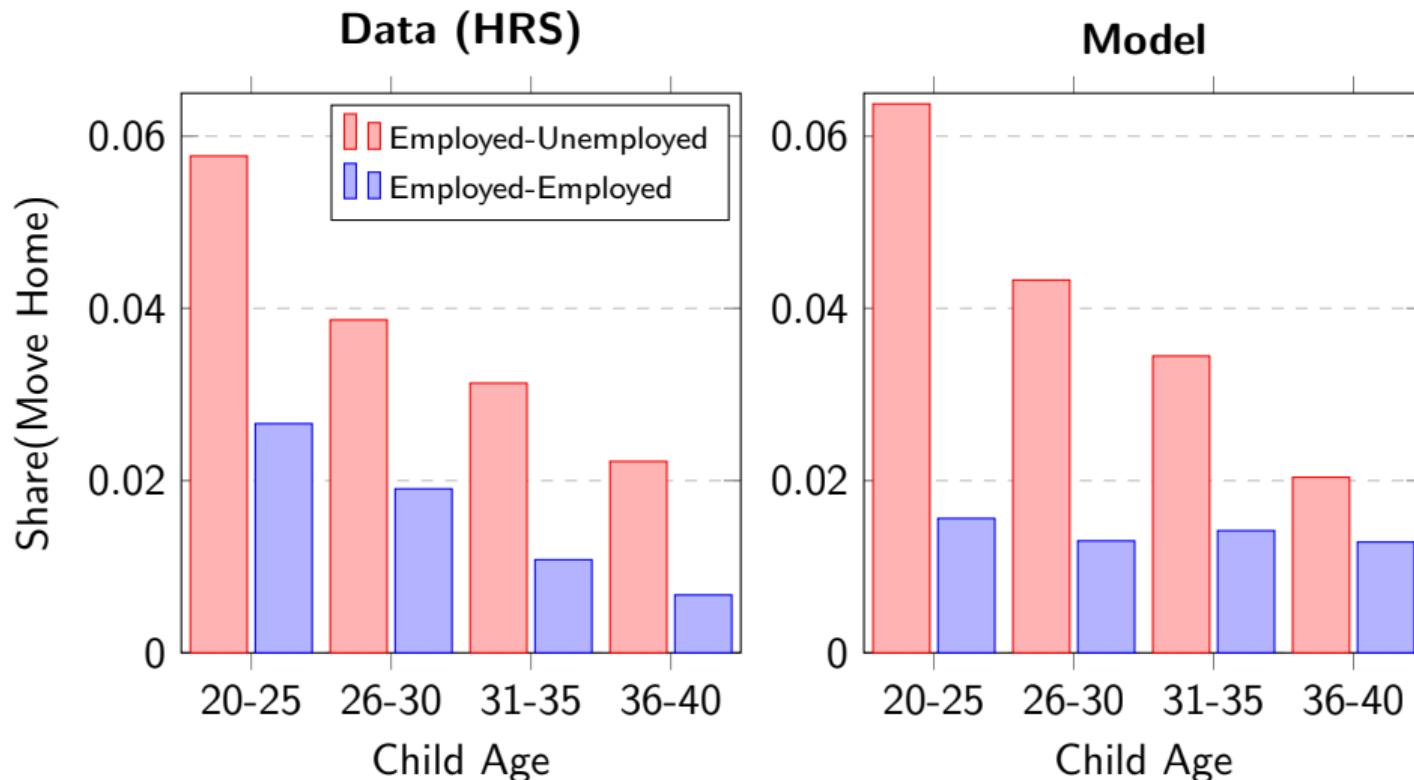
|                   | <b>Parameter</b>        | <b>Value</b> | <b>Target</b>                            | <b>Model</b> | <b>Data</b> |
|-------------------|-------------------------|--------------|--|--------------|-------------|
| $\kappa_h$        | Cost of Housing         | .1171        | Rent-to-Income Ratio                     | .0500        |             |
| $\chi$            | Independence Utility    | 4.703        | E-U Move Home Share                      | .0413        | .0413       |
| $\eta$            | EV Distribution Scale   | 1.000        | Coresidence Share                        | .0273        | .1460       |
| $\kappa_j$        | Cost of Posting         | .0034        | Unemployment Share <sup>1</sup>          | .0478        | .0420       |
| $b$               | UI Benefit              | .2454        | UI Exp. to Income Ratio <sup>2</sup>     | .0042        | .0042       |
| $S$               | Social Security Benefit | .7537        | SS Exp. to Income Ratio <sup>3</sup>     | .0525        | .0525       |
| $\sigma_\epsilon$ | St. Dev. Productivity   | .8868        | SD Log Earnings (Age 26-30) <sup>4</sup> | .9000        | .9000       |

<sup>1</sup> BLS (2025) <sup>2,3</sup> BEA (2024) <sup>4</sup> Kuhn & Ríos-Rull (2013)

## Calibration: External

|          | <b>Parameter</b>     | <b>Value</b> | <b>Source</b>   |
|----------|----------------------|--------------|-----------------|
| $\alpha$ | Match Elasticity     | 1.27         | Den Haan (2000) |
| $\delta$ | Job Destruction Rate | 0.0192       | E-U Share (HRS) |
| $\sigma$ | Risk Aversion        | 2            |                 |
| $\beta$  | Discount Factor      | 0.96         |                 |
| $r$      | Interest Rate        | 0.04         |                 |

## Model Validation: Share who Move Home



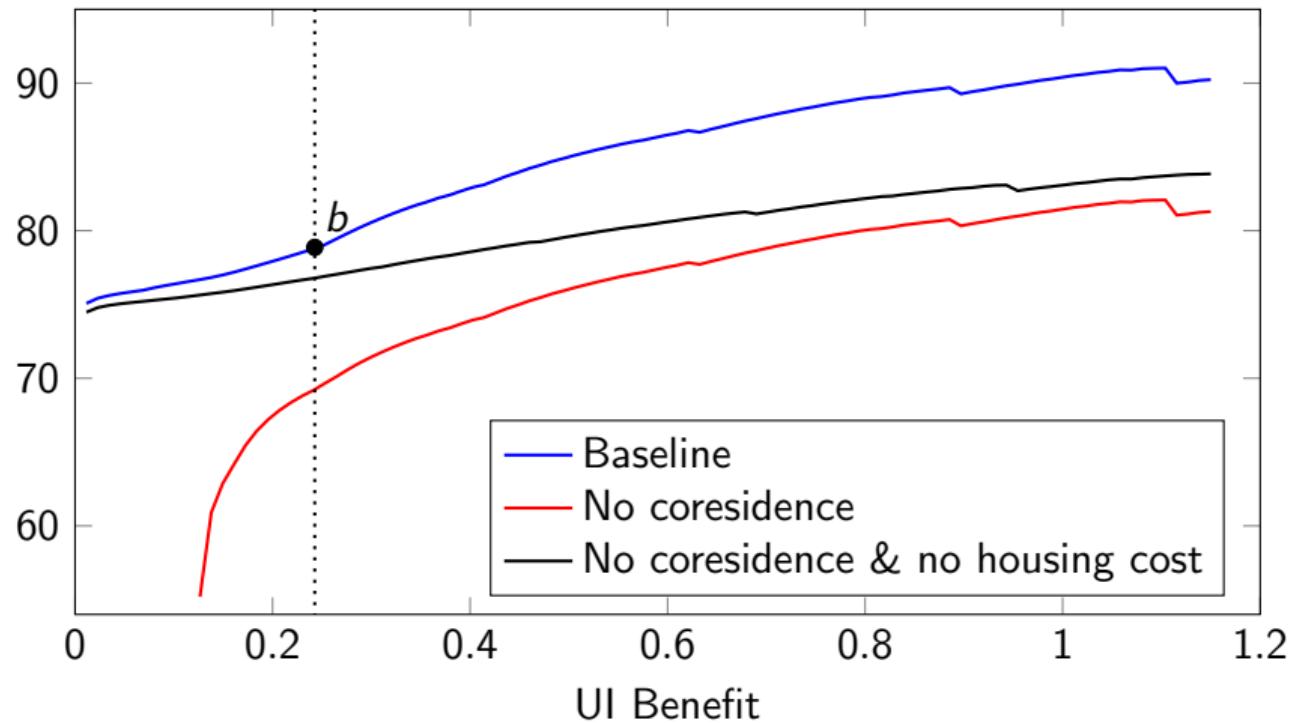
- Move home flows are larger for E-U consumers and are decreasing in age

## Ex Ante Search Choice ( $j = 27, a = .16$ )



- ▶ Consumers without the coresidence option search in lower piece-rate submarkets

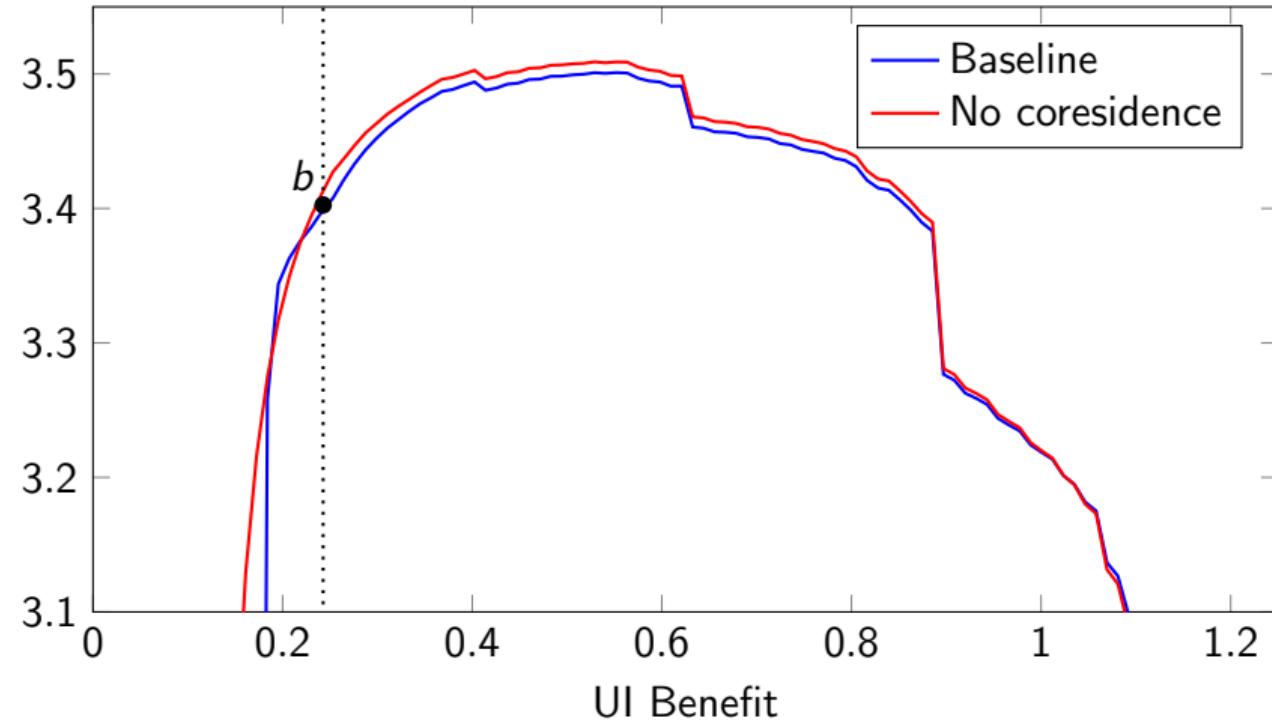
## Optimal UI Benefit: Expected Lifetime Utility



- ▶ Consumers prefer higher UI benefits until everyone selects into unemployment

Tax Rate

## Optimal UI Benefit: Equilibrium Utility



- ▶ Optimal UI under this welfare measure is roughly twice its calibrated value ( $b$ )

Tax Rate

# Conclusion

**Empirical observation:** E-U children are more likely to enter coresidence

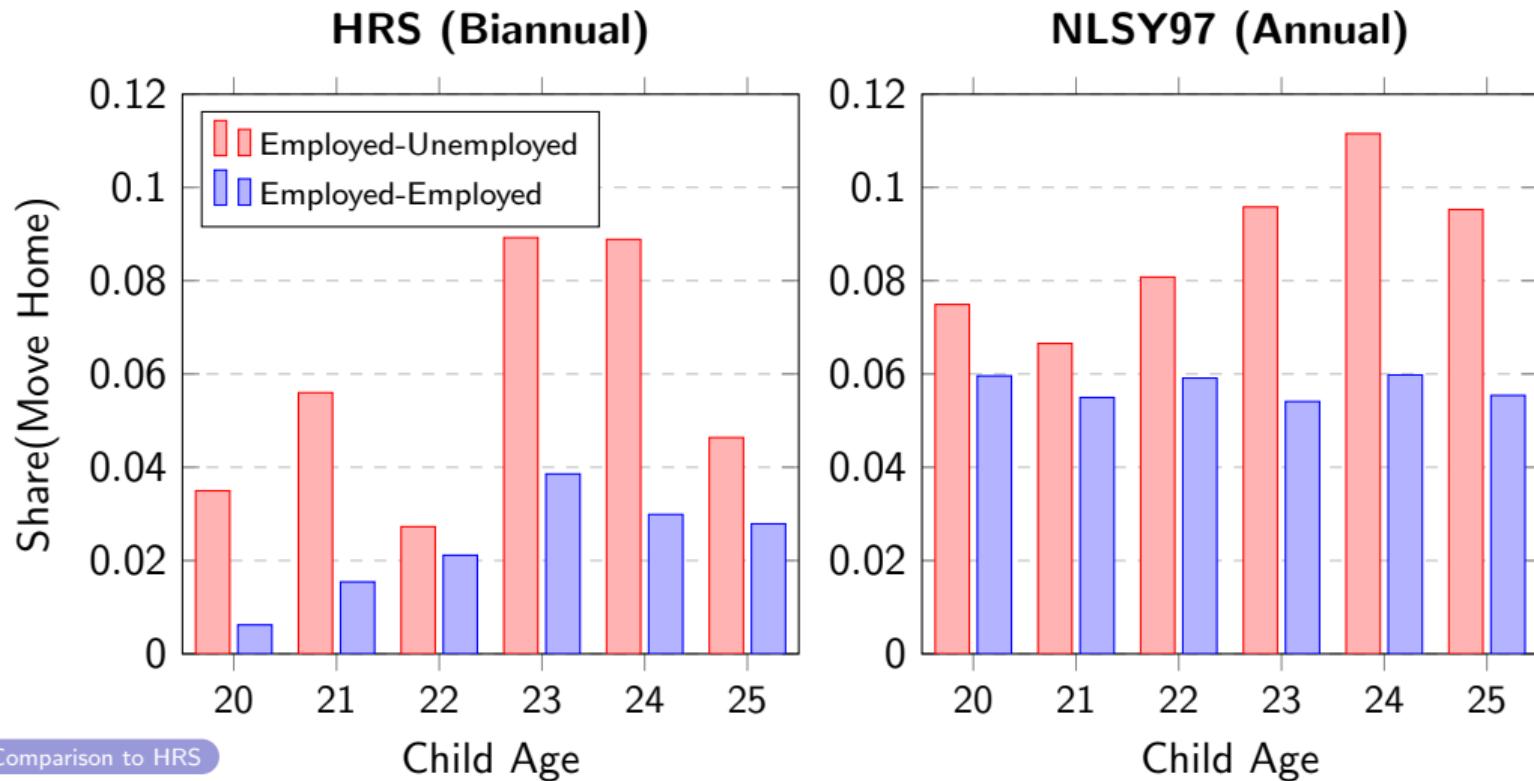
## Structural model:

1. Children who can coreside search in submarkets with lower job-finding rates
  - ▶ Relative cost of unemployment is lower due to the coresidence option
  - ▶ Coresidence allows children to avoid housing cost  $\kappa_h$
2. Welfare benefits of coresidence are largest at lower unemployment benefits
  - ▶ Suggests coresidence and UI are complementary insurance mechanisms

# Thank you

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## HRS v. NLSY97: E-U young adults are more likely to move home



Comparison to HRS

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## HRS v. NLSY97

Health and Retirement Study (1998-2018):

- ▶ Biannual frequency, ages 18-45
- ▶ Categorical child income, no unemployment benefits
- ▶ **Coresidence and transfers in all years**

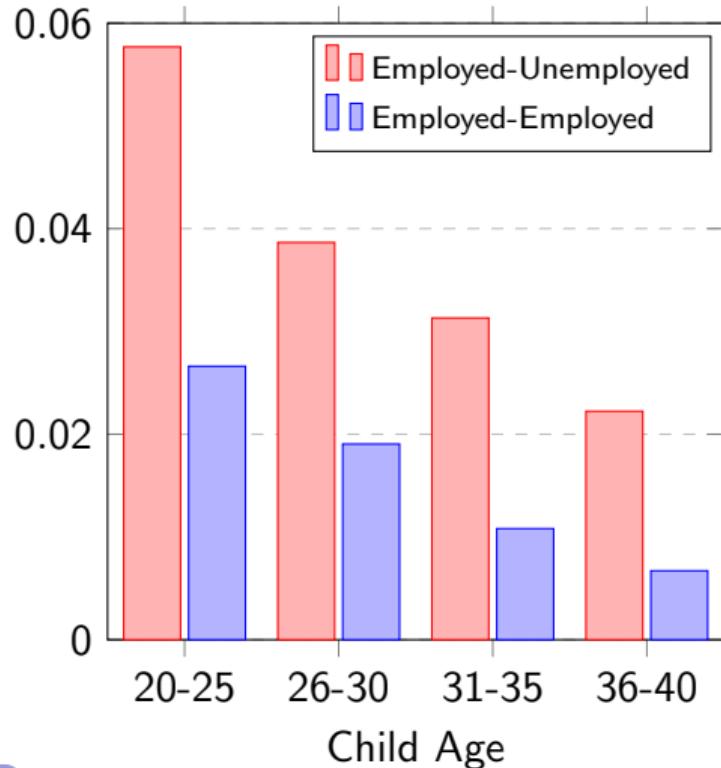
NLSY97 (1998-2021):

- ▶ Annual frequency, ages 18-42
- ▶ Child income, employment, and unemployment benefits
- ▶ **Key variables:**
  1. Coresidence: available until 2009 (age 26)
  2. Transfers: available until 2002 (22); extensive margin until 2011 (age 32)

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## Counterfactual: U-E children are more likely to move out

Share(Move Home)



Share(Move Out)



## HRS: Coresidence

- ▶ 8% of adult children (excluding students) live with their parents
- ▶ In any individual wave, 1.3% of adult children move home
  - ▶ 0.71% move in with parents
  - ▶ 0.15% host parents
  - ▶ 0.44% are ambiguous
- ▶ Children who move home tend to be younger and have less education
- ▶ Parents of children who move home have lower incomes but higher wealth

|                         | Move home | Stay independent |
|-------------------------|-----------|------------------|
| Child age               | 36.2      | 42.1             |
| Child education (years) | 12.4      | 13.8             |
| Parent income           | \$89,357  | \$79,104         |
| Parent assets           | \$465,707 | \$578,635        |

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## HRS: Transfers

Parents transfer choices and co-residence depend on child employment outcomes

- ▶ Children who have recently lost their jobs are more likely to receive transfers relative to those who stay employed
- ▶ The quantity of these transfers is also larger in both the unconditional average and intensive margin
- ▶ Job-losing children are also approximately 3.5 times more likely to move home

|                      | E-U      | E-E     |
|----------------------|----------|---------|
| Extensive margin     | 0.1932   | 0.1672  |
| Intensive margin     | \$10,336 | \$9,740 |
| Average transfer     | \$1,997  | \$1,628 |
| Share(Move home)     | 0.03773  | 0.01354 |
| Share(MH & Transfer) | 0.00683  | 0.00214 |

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## Linear Probability Model: Share(Move Home)

**Dependent variable:** indicator for moving home after living independently

| Independent Variable  | Child Age |           |           |           |
|-----------------------|-----------|-----------|-----------|-----------|
|                       | (1) 20-25 | (2) 26-30 | (3) 31-35 | (4) 36-40 |
| Employed-Unemployed   | .0315***  | .0202***  | .0205***  | .00814**  |
| Transfer from Parent  | .0091*    | .0144***  | .0092***  | .0045**   |
| Child Income          |           |           |           |           |
| <10K                  | Base      |           |           |           |
| 10-35K                | -.0186*** | -.0056    | -.0206*** | -.0208**  |
| 35-70K                | -.0354*** | -.0054    | -.0313*** | -.0284*** |
| 70-100K               | -.0226    | -.0067    | -.0321*** | -.0286*** |
| 100K+                 | -.0541*** | -.0061    | -.0334*** | -.0282*** |
| Child Gender (Female) | .0046     | -.0018    | -.0068*** | -.0058*** |
| Child Marital Status  | -.0418*** | -.0312*** | -.0235*** | -.0174*** |
| Child Parental Status | .0118     | -.0044*   | .0075***  | .0037*    |
| Mean Share(MH)        | .0301     | .0147     | .0100     | .0071     |

\*\*\* 99%, \*\* 95%, \* 90%

## Search Equilibrium

Value for a firm with a match:

$$V_f(j, \epsilon, \phi) = \epsilon(1 - \phi) + \beta(1 - \delta)V_f(j + 1, \epsilon, \phi)$$

Free entry condition:

$$q(\theta(j, \epsilon, \phi))V_f(j, \epsilon, \phi) = \kappa_p \quad \forall j, \epsilon, \phi$$

If  $V_f(j, \epsilon, \phi) < \kappa_j \rightarrow \theta = 0$  since the firm does not post in submarket  $(j, \epsilon, \phi)$

Otherwise:

$$q(\theta) = \frac{\kappa_p}{V_f} = \frac{M(u, v)}{v} = \frac{u}{(u^\alpha + v^\alpha)^{\frac{1}{\alpha}}}$$

$$u = \frac{\kappa_p}{V_f}(u^\alpha + v^\alpha)^{\frac{1}{\alpha}} \Rightarrow \frac{u^\alpha}{u^\alpha + v^\alpha} = \left(\frac{\kappa_p}{V_f}\right)^\alpha$$

$$1 + \theta^\alpha = \left(\frac{V_f}{\kappa_p}\right)^\alpha \Rightarrow \theta^\alpha = \left(\frac{V_f}{\kappa_p}\right)^\alpha - 1 \Rightarrow \theta = \left[\left(\frac{V_f}{\kappa_p}\right)^\alpha - 1\right]^{\frac{1}{\alpha}} \quad \forall j, \epsilon, \phi$$

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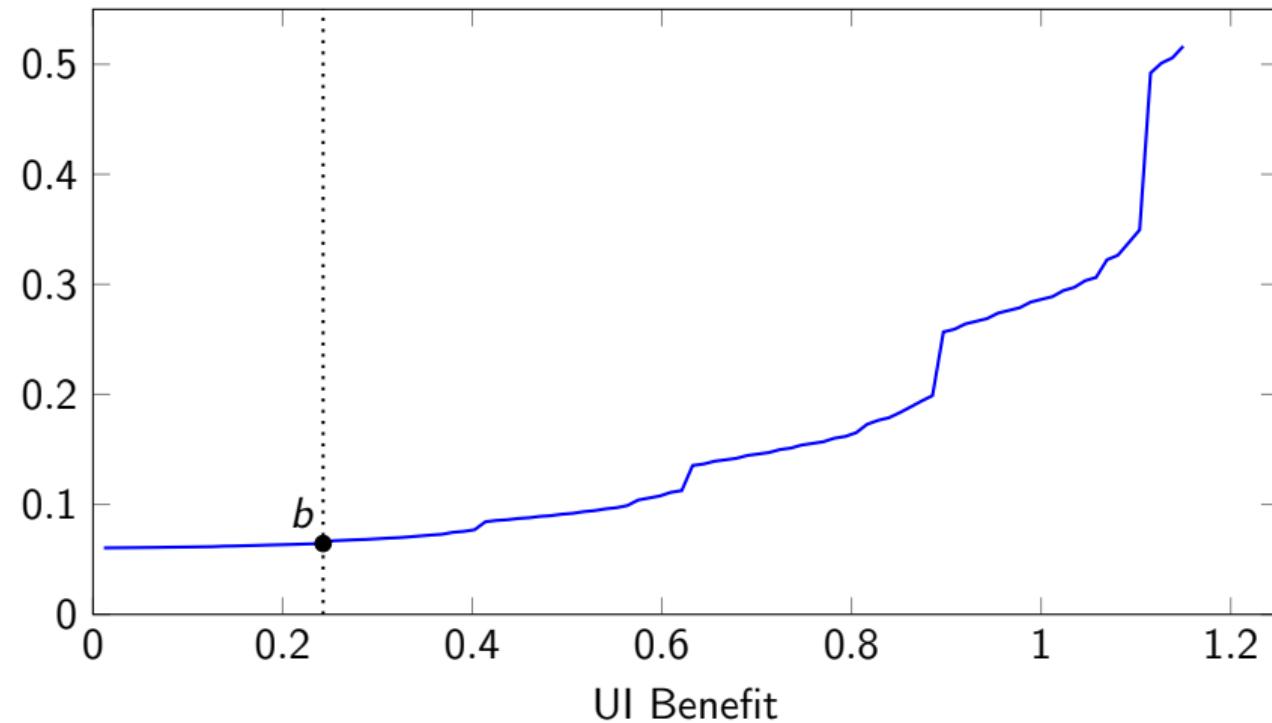
## Solution Algorithm

Assuming an initial distribution of consumers ( $\omega_s$ ) at  $j = 1 \forall a, \epsilon$

- (1) Guess labour income tax rate  $\tau \in \{0, 1\}$
- (2) Firm: solve for  $V_f(j, \epsilon, \phi)$  where  $V_f(J, \epsilon, \phi) = 0 \forall \epsilon, \phi$ 
  - ▶ Using  $V_f(j, \epsilon, \phi)$ , compute market tightness  $\theta$
- (3) Consumer: using  $V^r(J, a) = 0 \forall a$ , compute
  - ▶  $V_r(j, a) \forall a$  and  $j \in \{65, \dots, J - 1\}$
  - ▶  $V_u(j, a, \epsilon)$ ,  $V_u^{indep}(j, a, \epsilon)$ , and  $V_u^{cores}(j, a, \epsilon) \forall a, \epsilon$  and  $j \in \{0, \dots, 64\}$
  - ▶  $V_e(j, a, \epsilon, \phi)$ ,  $V_e^{indep}(j, a, \epsilon, \phi)$ , and  $V_e^{cores}(j, a, \epsilon, \phi) \forall a, \epsilon, \phi$  and  $j \in \{0, \dots, 64\}$
  - ▶  $V_s(j, a, \epsilon) \forall a, \epsilon$  and  $j \in \{0, \dots, 64\}$
- (4) Compute distributions for workers  $\omega_s(j, a, \epsilon)$ ,  $\omega_e(j, a, \epsilon, \phi)$  and retirees  $\omega_r(j, a)$
- (5) Compute tax rate to balance the government's budget constraint; update guess
- (6) Iterate on (2) – (5) until convergence

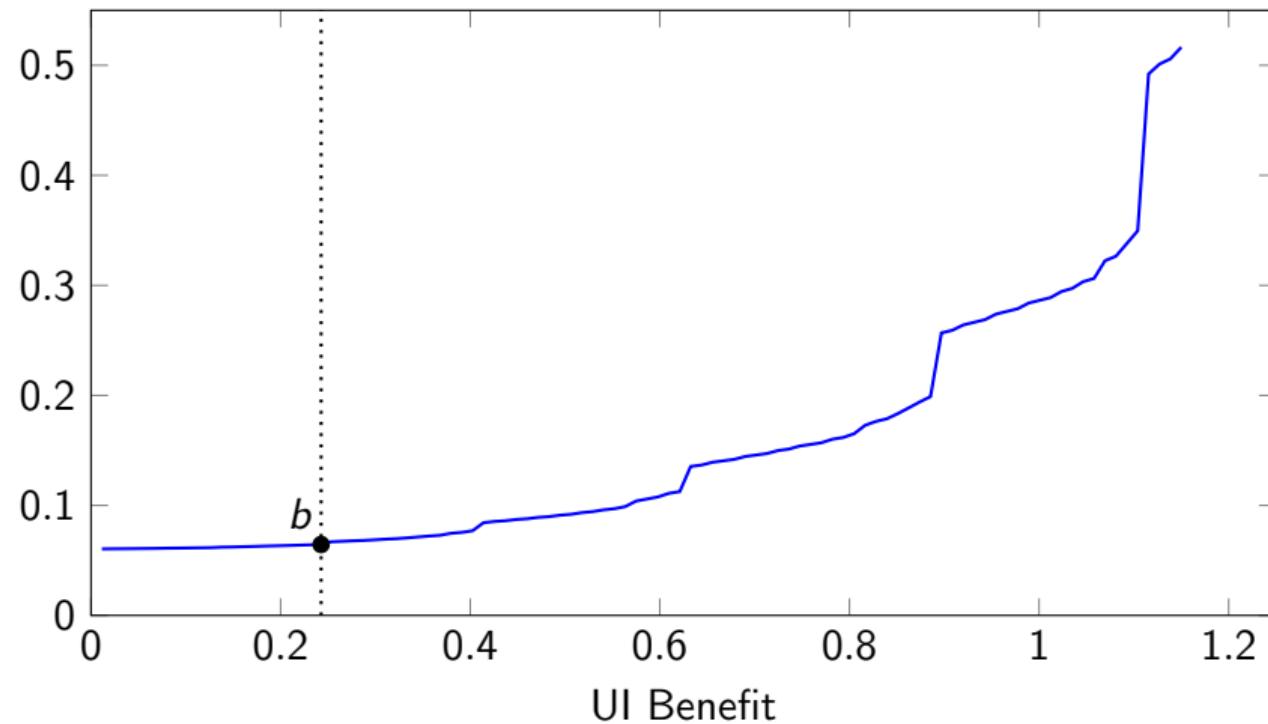
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## Tax Rate: Expected Lifetime Utility



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## Tax Rate: Equilibrium Utility



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