Formulas Α

Solution for quadratic equations

$$ax^2 + bx + c = 0$$
 \Rightarrow $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Properties of dynamic models of robots

Given the following dynamic system

$$B(q)\ddot{q} + C(q,\dot{q})\dot{q} + F\dot{q} + g(q) = u$$

The following properties hold

$$\dot{q}^T \left(\dot{B} - 2C \right) \dot{q} = 0$$
 $B = B^T$
 $q^T B q > 0$
 $q^T F q > 0$

Linear algebra

A matrix is symmetric if it satisfies the condition

$$\boldsymbol{A} = \boldsymbol{A}^T$$

For symmetric matrices the following holds

$$\boldsymbol{x}^T \boldsymbol{A} \boldsymbol{y} = \boldsymbol{y}^T \boldsymbol{A} \boldsymbol{x}$$

A skew-symmetric matrix is from the vector $\mathbf{x} = [x \ y \ z]^T$ is defined as

$$\mathbf{S}(\mathbf{x}) = \begin{bmatrix} 0 & -z & y \\ z & 0 & -x \\ -y & x & 0 \end{bmatrix}$$
 (10)

Trigonometry

Definitions

$$\sin \theta = \frac{opposite}{hypotenuse}$$
 $\cos \theta = \frac{adjacent}{hypotenuse}$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{opposite}{adjacent}$$

Addition formulas

$$\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y$$
$$\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$$

Derivatives

$$\frac{d}{dx}\sin x = \cos x \tag{11}$$

$$\frac{d}{dx}\cos x = -\sin x \tag{12}$$

$$\frac{d}{dx}\cos x = -\sin x\tag{12}$$