Worksheet 4: Connecting V and \vec{E}

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0 Comments

Slightly different format this week; fewer problems, more background info. The goal is to *really* understand the problems done in session – this means solving them independently and ability to teach others how to solve them.

1 Kirchoff's Loop Law

Kirchoff's Loop Law states the sum of all potential differences encountered while moving around a closed loop is zero:

$$\Delta V_{\text{loop}} = \sum_{i} (\Delta V)_{i} = 0$$

Prove that this is just a statement of conservation of energy.¹

¹In other words, this law doesn't tell us anything we didn't know from 40A.

2 Parallel-Plate Capacitor

Earlier in the quarter, we learned that the electric field inside a parallel-plate capacitor is:

$$\vec{E} = \left(\frac{Q}{\epsilon_0 A}, + \to -\right)$$

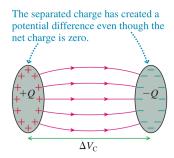
Let V = 0 at the negative plate. Find the **electric potential** inside the capacitor.

3 Capacitance

The figure below shows two electrodes charged to $\pm Q$. Although net charge is equal to zero, there is a potential difference ΔV between the electrodes. We define **capacitance** C to be the proportionality constant that relates charge² to potential:

$$Q = C\Delta V_C$$
 (charge on a capacitor)

Prove that capacitance depends only on the geometry of the electrodes.



 $^{^{2}}$ Here, this Q refers to the magnitude of the charge on one of the electrodes. The electrodes of a capacitor always have $equal\ but\ opposite$ charges.