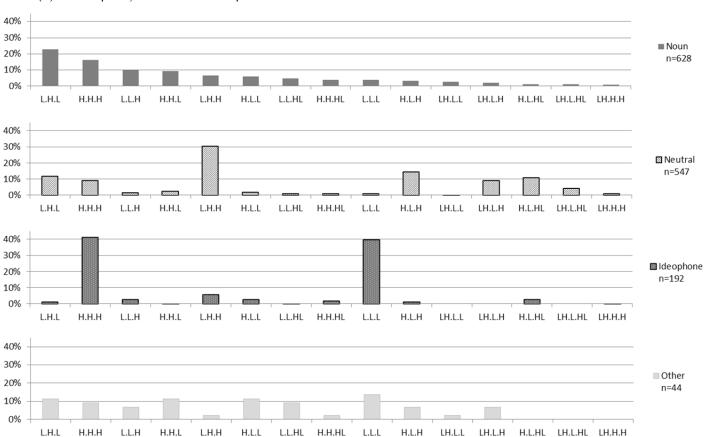
Morphologically-conditioned tonotactics in multilevel Maximum Entropy grammar

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1 Introduction

- This talk presents a case of lexically-conditioned tonotactics variation from Mende (Mande, Sierra Leone).
- (1) Top trisyllabic surface tone patterns in the Mende lexicon



- Part of speech-sensitive patterns =
 - different lexical classes can exhibit different phonological patterns.
 - noted cross-linguistically: e.g., English noun versus verb stress patterns
 - applications in e.g., comprehension, parsing
- Two hypotheses about how lexical class-conditioned sensitivity could work:
 - A. Lexical class differences are limited by the grammar/UG.
 - differences only in faithfulness, not markedness (e.g., Ito & Mester 1995; Alderete 2001; Smith 2011)
 - preferential classes, e.g., nouns // verbs will show a subset of noun patterns (Smith 2011)
 - B. Lexical classes can each have their own completely independent phonological profiles (e.g., Ito & Mester 1995; Inkelas & Zoll 2007; Anttila 2002; Pater 2009).

This talk:

- quantitatively models space of lexically-conditioned variation and frequency of variation across the corpus,
- using a 'varying slopes' approach in Maximum Entropy Harmonic Grammar (MaxEnt; Goldwater & Johnson 2003; Wilson 2006; Jäger 2007; Hayes & Wilson 2008; a.o.).
- This approach directly addresses the overarching problem in morphophonology of how to quantify the heterogeneity that morphological conditioning can engender in a phonological system.

2 MENDE TONOTACTICS

2.1 History, early generative accounts

- Early generative accounts of Mende noticed common tone patterns recurrent in the language, particularly in nouns (Leben 1978) → 'tone melodies' (see also Hyman 1987 for similar tone melodies in Kukuya),
- In Autosegmental Phonology, these surface tone patterns were modeled using
 - geometric association conventions of Autosegmental Phonology
 - 5 underlying tone melodies (H, L, HL, LH, LHL) as source of all surface patterns.
- But, subsequent work pointed out many surface patterns that deviate from the supposed five melodies or their "universal" autosegmental association principles (Dwyer 1978; Conteh et al. 1983; Zoll 2003; Zhang 2007).

2.2 Data

- Mende dictionary: n=5,412 (Innes 1969)
- 1 to 3-syllable words: *n*=4,989
 - Morpheme breaks are not indicated in Innes, but a primary source of morphological complexity (in nouns, at least) appears to be total reduplication in 4-syllable words, which we're not looking at here.
- Parts of speech

- Nouns 2,494

- Neutrals 1,442 (verbs, adjectives)

- Ideophones 762

- Other 291 (pronouns, conjunctions, interjections, adverbs, etc.)

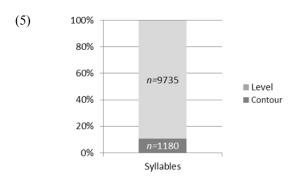
2.3 A fresh look at tone: the theoretical underpinnings

- Agreement by Correspondence Theory (ABC; Hansson 2001; Rose & Walker 2004; Bennett 2013; a.o.)
 - grounded in basic principles of similarity and proximity attraction, modeling instability in syntagmatic phonological relationships (Wayment 2009; Inkelas & Shih 2013).
 - Elements that are sufficiently similar/proximal interact in e.g., assimilation/dissimilation.
 - For simplicity in this talk, constraints are reformulated into more familiar phonotactic markedness format (but it's still ABC under the hood; cf. Hansson 2014).
- Q Theory (e.g., Shih & Inkelas 2014)
 - decomposes segments into strings of (2 or 3) smaller, temporally-sequenced, featurally-uniform subsegments, which bear tone features.

- (4) a. $Q \rightarrow (q^1 \quad q^2)$ b. $\check{a} \rightarrow (\grave{a} \, \acute{a})$ c. $\widehat{LH} \rightarrow (L \, H)$
- provides a more fine-grained point of reference for the grammar: crucial for e.g., contour tones.
- divorces issue of what are the minimal units that carry tone features versus what are the units that participate in tonal alternations/phenomena.
- Basic relevant differences between Autosegmentalism (e.g., Leben 1973) and ABC+Q for this talk:
 - Constraints grounded in principles of similarity- and proximity-based interaction.
 - No reliance on geometric, autosegmental 'line' representations
 - No reliance on operations that reference autosegmental 'lines': i.e., tone association rules.

2.4 Observed patterns for Mende surface tones

- Primary observations taken from Inkelas & Shih 2015.
- 2.4.1 Contour toned syllables (and tone transitions in general—except at syllable boundaries) are avoided.

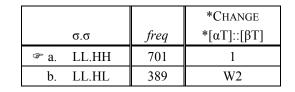


• Significantly fewer contour syllables than expected, if syllable tone patterns could be HH, LL, LH, and HL. χ^2 =6705.270, p<0.0001.

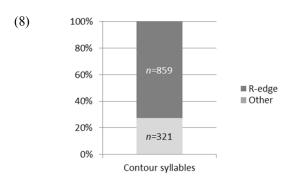
(6) $*[\alpha T]::[\beta T]$ (*Change)

(7)

Penalise every sequence of adjacent q's that are tonally non-identical.



2.4.2 If necessary, contour tones are tolerated at the right edge.



- The significant majority of contour syllables occur at the right edge of words.
- versus equal probability across all syllables: $\chi^2=353.407$, p<0.0001.

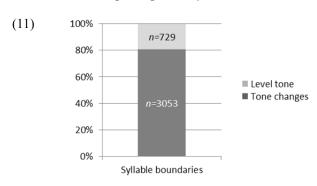
¹ This possibility was hinted at by Zoll (2003), but not fully explored.

- (9) $*([\alpha T]::[\beta T])_{\sigma w}$
- (*WeakContour)

Penalise every adjacent *q* sequence of non-identical tones within a weak (i.e., non-final) syllable. (cf. COINCIDE-CONTOUR; Zoll 2003)

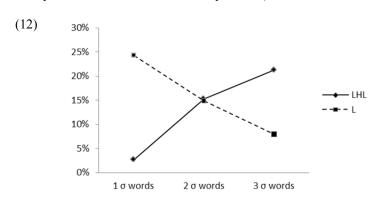
(10)			*WeakContour	*CHANGE
	σ.σ	freq	$*([\alpha T]::[\beta T])_{\sigma w}$	*[αT]::[βT]
	☞ a. LL.HL	389		2
	b. LH.LL	77	W1	2

2.4.3 Tone changes align with syllable boundaries



• Syllable boundaries coincide significantly with tone changes (in polysyllabic words that have non-level surface patterns) . χ^2 =1428.074, p<0.0001

Resulting prediction: tone melody complexity should correlate with the number of syllables in a word. More syllables → more non-level tone patterns (Inkelas & Shih 2015).



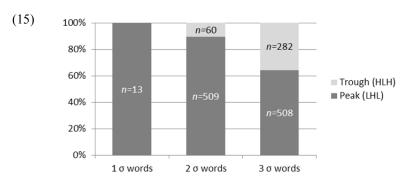
 As # of syllables in a word increases, so does the percentage of more complex melodies. Conversely, less complex, alllevel melodies decrease.

(13) $*[\alpha T]:$:[\alpha T]$ (Change@\$)

Penalise every adjacent, tonally-identical q sequence that is separated by a syllable boundary (\$). (cf. xx-Edge constraints; Bennett 2013)

(14)	σ.σ.σ	freq	Change@\$ *[αΤ]:\$:[αΤ]	*WeakContour *([αΤ]::[βΤ]) _{σw}	*Change *[αΤ]::[βΤ]
	☞ a. LL.HH.LL	233			2
	b. LL.HH.HH	218	W1		L1
	c. LL.LL.LL	112	W2		L
	d. LL.LL.HH	78	W1		L1
	e. LH.LL.HH	64		W1	W3
	f. LH.HH.LL	7	W1	W1	2

2.4.4 HLH troughs are avoided

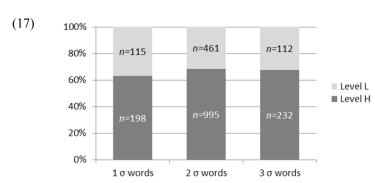


 Troughs are underrepresented, but their presence increases as the number of syllables in words increases.

(16) *Trough

Penalise any two H tones separated by any number of consecutive L tones. (Cahill 2007; a.o.)

2.4.5 Words preferably have at least one H tone



■ Level H tone patterns (e.g., HH.HH.HH) are more common than Level L tone patterns (e.g., LL.LL.LL).

(18) HAVEH

Penalise any word with no H tone.

2.5 Constraint summary

(19)	Constraint	Nickname	Definition
	*[αT]::[βT]	*CHANGE	Penalise every sequence of adjacent <i>q</i> 's that are tonally non-identical.
	$*([\alpha T]::[\beta T])_{\sigma w}$	*WeakContour	Penalise every adjacent <i>q</i> sequence of non-identical tones within a weak (i.e., non-final) syllable.
	*[α T]:\$:[α T]	CHANGE@\$	Penalise every adjacent, identical q sequence that is separated by a syllable boundary.
	*Trough	*Trough	Penalise any two H tones separated by any number of consecutive L tones.
	HAVEH	HAVEH	Penalise any word with no H tone.

• Note that no matter the OT analysis, the goal in this paper is to examine and model the variance of part-of-speech-specific tonotactics. (Almost) any constraint set would be fine for this, and the fact that there's lexically-conditioned differences (see (1)) doesn't change.

3 ANALYSIS

3.1 Maximum Entropy Harmonic Grammar

- Maximum Entropy Harmonic Grammar (MaxEnt) (Goldwater & Johnson 2003; Wilson 2006; Jäger 2007; Hayes & Wilson 2008; a.o.), fitted using MaxEnt Grammar Tool (Hayes et al. 2009).²
 - ranks probabilities (i.e., comparative grammaticality) of outcome candidates in variable data.
- Output = probability distribution over all possible surface tone pattern combinations of LL, HH, LH, HL syllables (LHL, HLH are found on monosyllables only)

3.2 Cophonologies/Indexed Constraints as Varying Slopes

- Varying slopes = additive weight adjustment for constraints in the Base Grammar, per each lexical class.
 - Such an approach has been hinted at before; e.g., Albright 2008; Coetzee & Pater 2011.

(20)
$$w_1C_1 + w_2(C_1 \times \text{NOUN}) + w_3(C_1 \times \text{NEUT}) + w_4(C_1 \times \text{ID}) + \dots + w_kC_{iN}$$
 (cf. fn 2)

Base grammar = $w_1 C_1$

Adjusted noun grammar = $w_1C_1 + w_2(C_1 \times \text{NOUN})$ Adjusted neutral grammar = $w_1C_1 + w_3(C_1 \times \text{NEUT})$ Adjusted ideophone grammar = $w_1C_1 + w_4(C_1 \times \text{ID})$

- Base Grammar predicts overall tonotactics for the language, and lexical class-specific tonotactics are predicted by the additive combination of weights of Base Grammar constraints and class-specific weights.
- Cophonologies ≅ bundles of Indexed Constraints.
- Because there is a finite set of lexical classes, varying slopes are formally executed here as interaction terms.³
 - for other previous uses of interaction terms in MaxEnt HG, usually as weighted constraint conjunction: see
 e.g., Hayes et al. 2012; Pater & Moreton 2012; Green & Davis 2014; Shih, to appear.

3.3 What is the base grammar?

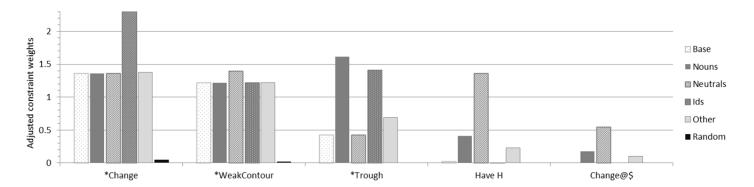
- Trained a base grammar on bootstrapped samples (*n*=2500 / sample) of possible tone melodies in Mende, drawn from the existing distribution.
 - mirrors a Mende speaker knowing word tone patterns but not (yet) part of speech.
 - did not want to a priori assume one lexical class as "default."
 - across base grammar samples, the results are stable; a representative result is reported here.
- A grammar trained without any data for base grammar provides very similar results (not reported here).
- Another baseline: grammar on a totally random tone patterns (*n*=5000), generated from random combinations of HH, LL, LH, and HL syllables for 1–3 syllable words is also provided here for comparison.

² \mathcal{H} armony $(x, i) = \sum_{k=1}^{N} w_k C_i(x) = \mathbf{w_k} \cdot \mathbf{C_i}$; where x = candidate for input i, $w_k =$ weight of constraint C_i , $C_i(x) =$ number of violations of C_i that x incurs, and N = vector of constraints $(C_{i1} \dots C_{iN})$.

³ For justification on the equivalency of interaction terms and random slopes in this situation, see e.g., Gelman & Hill 2007.

4 RESULTS

(21) Adjusted MaxEnt weights, in graphical form (adjusted wC_i = base wC_i + indexed wC_i)



(22) Adjusted MaxEnt weights, in numbers

	Base	Adjusted	Adjusted Grammars			
		Nouns	Neutrals	Ideophones	Other	
*CHANGE	1.356	1.356	1.356	2.537	1.374	0.047
*WeakContour	1.220	1.220	1.391	1.220	1.220	0.018
*Trough	0.426	1.612	0.426	1.409	0.691	0
HAVE H	0.017	0.411	1.361	0.017	0.232	0
CHANGE@\$	0	0.175	0.543	0	0.099	0

(23) Constraint weights by lexical class (top→bottom: highest weight→lowest weight)

Base	Cophonology Indexed Grammars						
	Nouns	Neutrals	Ideophones	Other			
*CHANGE	*Trough	*WeakContour	*CHANGE	*CHANGE			
*WeakCONTOUR	*CHANGE	HAVE H	*Trough	*WeakContour			
*Trough	*WeakContour	*CHANGE	*WeakContour	*Trough			
HAVE H	HAVE H	CHANGE@\$	CHANGE@\$	HAVE H			
CHANGE@\$	CHANGE@\$	*Trough	HAVE H	CHANGE@\$			

4.1 Results and observations

4.1.1 Sanity check

A MaxEnt grammar on completely random data yields constraint weights pretty close to 0.

4.1.2 Base grammar

- Reveals importance of general contour tone avoidance and R-edge contour tone alignment.
 - *CHANGE = 1.356
 - *WeakContour = 1.220
 - cf. "Random" model results, where weights are much lower, nearly at 0.
- These two constraints remain highly weighted across all lexical classes.
 - weight of *WeakContour stays stable across the lexicon, suggesting that it's a very general principle.
- Reflects universal dispreferences for (nonfinal) contour tones (e.g., Gordon 2001; Zhang 2004).

4.1.3 Syllable edge – Tone change alignment

- Only nouns and neutrals show an effect of syllable edge-tone transition alignment. → see adjusted weights for CHANGE@\$:
 - Change@ $$\times$ Noun = 0.175
 - Change@\$×Neut = 0.543
 - versus Change@ $$\times$ ID = 0
- Shows that ideophones often involve much simpler surface tone patterns than the other lexical classes.
 - e.g., vòvòlò 'creaking'
 - In addition, ideophones significantly increase the weight of *CHANGE

(24)			*Change×Id *[αT]::[βT]×Id	CHANGE@\$ \times ID *[α T]:\$:[α T] \times ID	
	σ.σ.σ, ID	freq	$w_{\rm adj} = 2.537$	$w_{\rm adj} = 0$	${\cal H}$
	a. LL.HH.LL	2	W2		5.073
	☞ b. LL.LL.LL	76		L2	0

4.1.4 HAVE H: a verb thing

- Neutrals in particular (but also nouns to a certain extent) show a much greater affinity for a requisite H tone than ideophones.
 - = level L surface patterns much more tolerated for Ideophones > Nouns > Neutrals.

(25)		σ.σ.σ, ΝΕυΤ	freq	HAVEH \times NEUT $w_{\text{adj}}=1.360656$	${\cal H}$
	a.	LL.LL.LL	5	1	1.36
		σ.σ.σ, Noun		HAVEH×NOUN w_{adj} =0.410611	
	b.	LL.LL.LL	25	1	0.41
		σ.σ.σ, ID		HAVEH×ID $w_{\rm adj}$ =0.016843	
	C.	LL.LL.LL	76	1	.02

4.1.5 *TROUGH: not a verb thing

- Neutrals also differ from Nouns and Ideophones by showing greater preference for tone transitions that align with syllable boundaries, even if these result in a HLH trough.
 - e.g., *húvùndí* 'be mouldy, mildewed'
 - = Greater dispreference of troughs in Nouns and Ideophones.
 - Much lower adjusted weight for *TROUGH in Neutrals than other lexical classes:
 - *TROUGH \times NEUT = 0.426
 - $*TROUGH \times NOUN = 1.612$
 - *TROUGH ×ID = 1.409

Perhaps a contrast maximization issue?

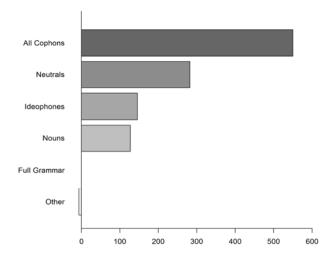
(26)						CHANGE@\$	
					*Trough×Neut	* $[\alpha T]$:\$: $[\alpha T]$ ×NEUT	
			σ.σ.σ, Neut	freq	$w_{\rm adj} = 0.426$	$w_{\rm adj} = 0.543$	${\cal H}$
	a.	♂ i.	HH.LL.HH	78	1		0.43
		ii.	НН.НН.НН	48		2	1.09

		σ.σ.σ, Noun		*TROUGH×NOUN w_{adj} =1.612	* $[\alpha T]$:\$: $[\alpha T]$ × NOUN w_{adj} =0.175	
b.	i.	HH.LL.HH	21	1		1.61
	☞ ii.	НН.НН.НН	101		2	0.35

		σ.σ.σ, ID		*TROUGH×ID w_{adj} =1.409	* $[\alpha T]$:\$: $[\alpha T]$ ×ID w_{adj} =0	
c.	i.	HH.LL.HH	2	1		1.41
	☞ ii.	НН.НН.НН	79		2	0.00

4.2 Importance of lexical conditioning

- Are the cophonology/indexed grammars contributing significantly to improving our base grammar?
- Tested here using Akaike Information Criterion (AIC_C) model comparison.⁴
 - How much information is lost when cophonology/indexed constraints are removed?
- (27) ΔAIC_C from full model for each cophonology removed = how much information is lost for each cophonology is in turn removed.⁵



- AIC_C comparison results show that lexical class-specific cophonologies/indexed constraints produce a better fit for the data.
 - Exception that is expected: the "Other" part of speech class, which is heterogeneous as is.
- Certain lexical classes provide more information on top of the baseline, suggesting 'distance' from the full model.
 - Neutral-specific cophonology contributes a lot of additional information to the grammar.
 - Interestingly, ideophones are *not* the most extreme lexical class.
- For future work: comparing individual indexed constraints versus entire cophonologies of indexed constraints.

⁴ Second-order AIC_C is used here, because it adjusts more strictly for differences in the number of constraints between comparison grammars. See e.g., Burnham & Anderson 2002 for justification of AIC_C -based model comparison. For use in comparing phonological grammars, see e.g., Shih, to appear (cf. Wilson & Obdeyn 2009).

 $^{^{5}}$ ∆AIC_C ≥ 10 is considered large (equivalent to 150:1 that the second best model has essentially no support of being as good as the best model).

5 IMPLICATIONS & CONCLUSION

Lexically-conditioned phonology

Part-of-speech phonological differences go beyond noun-adjective-verb distinctions (as observed by e.g., Smith 2011).

- → more closely resemble the complexity of morphophonological alternations and variation.
- Lexically-conditioned phonology is not just a matter of differential faithfulness (e.g., FAITH_{NOUN}» FAITH_{VERB}; Smith 2011).
- Overall, indexation of markedness constraints per lexical class gains better fit for the data.
- There are hints of markedness reversals of the kind that 'Grammar Dependence' (Alderete 2001) predicts impossible (cf. Pater 2009):
 - E.g., Across nearly all of the grammars (base and lexical class-specific) in Mende, *TROUGH is ranked fairly highly w/r/t the other constraints.
 - In Neutrals, however, *TROUGH is weighted at the bottom.
 - Therefore, a structure (e.g., HLH) that might otherwise be highly marked in the rest of the language is quite good and (comparatively) unmarked for Neutrals.

Quantifying morphological conditioning

- Our approach can quantify how much lexical class-specific phonotactics can differ from the rest of the lexicon.
 - E.g., how different can ideophone phonology be? → long standing issue for e.g., African languages (see Rose 2015 for recent summary).
 - Results show that ideophones operate within fairly conservative parameters of the overall Mende tonotactics grammar—cf., neutrals.
 - Potentially useful as a scale of ideophone idiosyncrasy (cf. Newman 2001 on Hausa ideophones).
- Because we *a priori* restrict standard HG/OT grammars to positive weights (i.e., to only penalise rather than reward structures), we're not really examining the full potential space of variation between cophonologies yet.
- In the future, this 'varying slopes' approach could extend to other types of morphology (e.g., affixation; dominant tone melodies): e.g., what are the tone patterns that are grammaticalised in a language as productive morphemes?

For the future

- What is the utility of these phonological differences between groups?
 - There's evidence from other languages that speakers are capable of learning these lexical statistics (e.g., Coetzee 2014).
 - and that such phonological differences help in e.g., acquisition, processing, information load (e.g., Monaghan et al. 2010).

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To save trees, references are available online.

http://cogsci.ucmerced.edu/shih/ShihInkelas_AMP2015handout.pdf

6 REFERENCES

ALBRIGHT, ADAM. 2008. How many grammars am I holding up? Discovering differences between word classes. *Proceedings of the 26th West Coast Conference on Formal Linguistics*, ed. by Charles B. Chang and Hannah J. Haynie, 1–20. Somerville, MA: Cascadilla Proceedings Project.

- ALDERETE, JOHN D. 2001. Dominance Effects as Transderivational Anti-Faithfulness. *Phonology* 18.201–253.
- ANTTILA, ARTO. 2002. Morphologically Conditioned Phonological Alternations. *Natural Language & Linguistic Theory* 20.1–42.
- BENNETT, WILLIAM G. 2013. Dissimilation, consonant harmony, and surface correspondence. New Brunswick, NJ: Rutgers, The State University of New Jersey ph.d. dissertation.
- BURNHAM, KENNETH P.; and DAVID R. ANDERSON. 2002. *Model Selection and Multimodel Inference: A Practical Information-Theoretic Approach*. 2nd edition. New York, NY: Springer-Verlag.
- CAHILL, MIKE. 2007. More universals of tone. Ms. SIL, ms.
- COETZEE, ANDRIES W; and JOE PATER. 2011. The place of variation in phonological theory. *The Handbook of Phonological Theory*, ed. by John A Goldsmith, Jason Riggle, and Alan C. L. Yu, 401–434. John Wiley & Sons.
- COETZEE, ANDRIES W. 2014. Grammatical change through lexical accumulation: Voicing cooccurrence restrictions in Afrikaans. *Language* 90.693–721.
- CONTEH, P.; E. COWPER; D. JAMES; K. RICE; and M. SZAMOSI. 1983. A reanalysis of tone in Mende. *Current Approaches to African Linguistics*, ed. by J. Kaye, H. Koopman, D. Sportiche, A. Dugas, J. Kaye, H. Koopman, D. Sportiche, and A. Dugas, 2:127–137. Dordrecht: Foris.
- DWYER, DAVID. 1978. What sort of tone language is Mende? Studies in African Linguistics 9.167–208.
- GELMAN, ANDREW; and JENNIFER HILL. 2007. *Data analysis using regression and multilevel/hierarchical models*. Analytic methods for social research. New York, NY: Cambridge University Press.
- GOLDWATER, SHARON; and MARK JOHNSON. 2003. Learning OT Constraint Rankings Using a Maximum Entropy Model. *Proceedings of the Stockholm Workshop on Variation within Optimality Theory*, ed. by Jennifer Spenader, Anders Eriksson, and Östen Dahl, 111–120. Stockholm: Stockholm University.
- GORDON, MATTHEW. 2001. A typology of contour tone restrictions. Studies in Language 25.405-444.
- GREEN, CHRISTOPHER; and STUART DAVIS. 2014. Superadditivity and Limitations on Syllable Complexity in Bambara Words. *Perspectives on Phonological Theory and Acquisition: Papers in Honor of Daniel Dinnsen*, ed. by Ashley W. Farris-Trimble and Jessica Barlow. Philadelphia/Amsterdam: John Benjamins Co.
- HANSSON, GUNNAR ÓLAFUR. 2001. Theoretical and Typological Issues in Consonant Harmony. University of California, Berkeley ph.d. dissertation.
- HANSSON, GUNNAR ÓLAFUR. 2014. (Dis)Agreement by (Non)Correspondence: Inspecting the foundations. *UC Berkeley Phonology Lab Annual Report: ABC Conference Archive*, 3–62. Berkeley, CA. http://linguistics.berkeley.edu/phonlab/annual_report/documents/2014/annual_report_2014_ABCC.html.
- HAYES, BRUCE; and COLIN WILSON. 2008. A maximum entropy model of phonotactics and phonotactic learning. *Linguistic Inquiry* 39.379–440.
- HAYES, BRUCE; COLIN WILSON; and BEN GEORGE. 2009. *Maxent Grammar Tool*. http://www.linguistics.ucla.edu/people/hayes/MaxentGrammarTool/.
- HAYES, BRUCE; COLIN WILSON; and ANNE SHISKO. 2012. Maxent grammars for the metrics of Shakespeare and Milton. *Language* 88.691–731.
- HYMAN, LARRY M. 1987. Prosodic Domains in Kukuya. Natural Language & Linguistic Theory 5.311–333.
- INKELAS, SHARON; and STEPHANIE S SHIH. 2013. Unstable surface correspondence as the source of local conspiracies. Paper presented at the NELS 2013, University of Connecticut. http://stanford.edu/~stephsus/InkelasShih NELS 2013 handout.pdf.
- INKELAS, SHARON; and STEPHANIE S SHIH. 2015. Tone melodies in the age of Surface Correspondence. Paper. Paper presented at the 51st Annual Meeting of the Chicago Linguistic Society (CLS), University of Chicago.
- INNES, GORDON. 1969. A Mende-English Dictionary. London and New York: Cambridge University Press.
- JÄGER, GERHARD. 2007. Maximum Entropy Models and Stochastic Optimality Theory. *Architectures, Rules, and Preferences: A Festschrift for Joan Bresnan*, ed. by Jane Grimshaw, Joan Maling, Chris Manning, Jane Simpson, and Annie Zaenen. Stanford, CA: CSLI.
- KULLBACK, SOLOMAN; and RICHARD A. LEIBLER. 1951. On Information and Sufficiency. *Annals of Mathematical Studies* 2.79–86.
- LEBEN, WILL. 1978. The representation of tone. *Tone: A Linguistic Survey*, ed. by Victoria Fromkin, 177–219. New York: Academic Press.
- LEBEN, WILLIAM R. 1973. Suprasegmental phonology. Cambridge, MA: Massachusetts Institute of Technology ph.d. dissertation.

MONAGHAN, PADRAIC; MORTEN H. CHRISTIANSEN; THOMAS A. FARMER; and STANKA A. FITNEVA. 2010. Measures of phonological typicality: Robust coherence and psychological validity. *The Mental Lexicon* 5.281–299.

- NEWMAN, PAUL. 2001. Are ideophones really as weird and extra-systematic as linguists make them to be? *Ideophones*, ed. by F. K. Erhard Voeltz and Christa Kilian-Hatz, 251–258. Typological Studies in Language 44. Amsterdam: John Benjamins.
- PATER, JOE. 2009. Morpheme-specific phonology: constraint indexation and inconsistency resolution. *Phonological argumentation: essays on evidence and motivation*, ed. by Steve Parker. Advances in Optimality Theory. Equinox.
- PATER, JOE; and ELLIOT MORETON. 2012. Structurally biased phonology: Complexity in learning and typology. *The English and Foreign Languages Journal* 3.1–44.
- ROSE, SHARON. 2015. Phonology of Ideophones in African Languages. Paper. Paper presented at the WOCAL 8, Kyoto University, Japan.
- ROSE, SHARON; and RACHEL WALKER. 2004. A Typology of Consonant Agreement by Correspondence. *Language* 80.475–531.
- SHIH, STEPHANIE S. to appear. Super additive similarity in Dioula tone harmony. *Proceedings of the West Coast Conference on Formal Linguistics 33*.
- SHIH, STEPHANIE S; and SHARON INKELAS. 2014. A subsegmental correspondence approach to contour tone (dis)harmony patterns. *Proceedings of Phonology 2013*. University of Massachusetts, Amherst. http://journals.linguisticsociety.org/proceedings/index.php/amphonology/article/view/22.
- SMITH, JENNIFER L. 2011. Category-specific effects. *The Blackwell Companion to Phonology*, ed. by Marc van Oostendorp, Colin Ewen, Elizabeth Hume, and Keren Rice, 2439–2463. Malden, MA: Wiley-Blackwell.
- WAYMENT, ADAM. 2009. Assimilation as attraction: Computing distance, similarity, and locality in phonology. Baltimore, MD: Johns Hopkins University ph.d. dissertation.
- WILSON, COLIN. 2006. Learning Phonology with Substantive Bias: An Experimental and Computational Study of Velar Palatalization. *Cognitive Science* 30.945–982.
- WILSON, COLIN; and MARIEKE OBDEYN. 2009. Simplifying subsidiary theory: statistical evidence from Arabic, Muna, Shona, and Wargamay.
- ZHANG, JIE. 2004. Contour tone licensing and contour tone representation. Language and Linguistics 5.925–968.
- ZHANG, JIE. 2007. Contour tone distribution is not an artifact of tonal melody mapping. *Studies in the Linguistic Sciences* 33.
- ZOLL, CHERYL. 2003. Optimal Tone Mapping. Linguistic Inquiry 34.225–268.