

HY448 FM Radio



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February 10, 2023



Contents

1	Introduction	3
2	Requirements	4
2.1	Gnu-Radio Companion	4
2.2	Installing PlutoSDR Drivers	4
2.2.1	libiio	4
2.2.2	libad9361-iio	4
2.2.3	pyadi-iio	5
2.3	"Hacking" Adalm-Pluto SDR to increase RF Range	5
2.4	Installing and building gr-rds blocks from Source-GitHub	5
3	FM Station	6
4	FM Receiver	8
5	FM Stereo Receiver	10
6	RDS STANDARDS	13
6.1	Data channel (Physical layer)	13
6.2	Baseband coding (Data-link layer)	13
6.3	Method Of Modulation	13
6.4	Clock Frequency and Data Rate	13
6.5	Differential Encoding	14
6.6	Manchester Encoding	14
6.7	Matched Filter	15
7	FM-RDS Decoding	16
7.1	Signal Demodulation and RDS Bandwidth Isolation	17
7.2	Matched Filter and Symbol-Timing Synchronization	18
7.3	Carrier Recovery, BPSK Demodulation, Differential and RDS Data Decoding	20
8	FM-RDS Encoding	21
8.1	Building the Mono-Audio and Stereo Audio	22
8.2	RDS Encoding, Differential Encoding, Manchester Encoding, Shaped Filter	22
8.3	Frequency Modulation of our Signal and Transmit via PlutoSDR	23

1 Introduction

FM-Radio is a broadcast technology that uses frequency modulation to transmit sound over radio waves. It provides high-fidelity audio transmission and is commonly used for music and talk radio programs. FM radio operates in the frequency range of 87.5 to 108 MHz and is widely available in many countries around the world. It is popular due to its ease of use, portability and the availability of FM receivers in many devices, including cars and smartphones. A typical spectrum of composite base-band FM signal is shown in Figure 1:

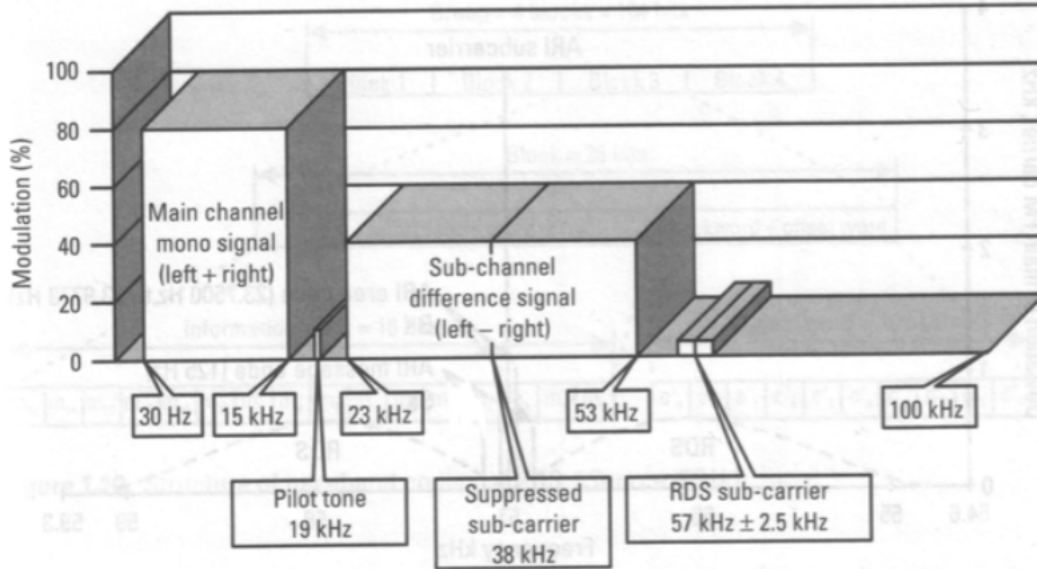


Figure 1: FM Spectrum

As we can observe, the FM spectrum consists of:

- L + R signal (Left + Right Channel), Bandwidth: 30 Hz - 15 kHz, and its called Mono Audio.
- A tone located at 19 kHz, which called Pilot Tone.
- L - R signal (Left - Right Channel), Bandwidth: 23 kHz - 53 kHz, centered at 38kHz, called Stereo Audio.
- RDS Signal(RDS stands for Radio Data System), Bandwidth: 54.6 kHz - 59.4 kHz, centred at 57 kHz.

In this project, we are going to implement an FM - Radio and some of its functionalities. using Gnu-Radio Companion(GRC), which is a Software Defined Radio platform that enables experimentation and education in wireless communications, along with Adalm-Pluto(SDR) Analog Device. More specifically, we will focus on:

- Creating an FM station, using our laptop's microphone as input
- Creating an FM receiver, using our laptop's speakers as output
- Receiving an FM station which broadcasts stereo
- Decoding FM-RDS packets
- Encoding FM-RDS packets

2 Requirements

2.1 Gnu-Radio Companion

Gnu-Radio Companion(GRC) installed in Ubuntu 22.04.1 LTS(64-bit), by typing the command:

```
sudo apt-get install gnuradio
```

The version is 3.10.1.1 .

2.2 Installing PlutoSDR Drivers

Three libraries required:

- **libiio**, Analog Device’s “cross-platform” library for interfacing hardware
- **libad9361-iio**, AD9361 is the specific RF chip inside the PlutoSDR
- **pyadi-iio**, the Pluto’s Python API

2.2.1 libiio

Libiio is a library that has been developed by Analog Devices to ease the development of software interfacing Linux Industrial I/O (IIO) devices. The library abstracts the low-level details of the hardware, and provides a simple yet complete programming interface that can be used for advanced projects. The installation commands:

- `sudo apt-get install build-essential git libxml2-dev bison flex libcdk5-dev cmake python3-pip libusb-1.0-0-dev libavahi-client-dev libavahi-common-dev libaio-dev`
- `cd` (to home directory)
- `git clone -branch v0.23 https://github.com/analogdevicesinc/libiio.git`
- `cd libiio`
- `mkdir build`
- `cd build`
- `cmake -DPYTHON_BINDINGS=ON ..`
- `make -j$(nproc)`
- `sudo make install`
- `sudo ldconfig`

2.2.2 libad9361-iio

A library for filter design/handling and multi-chip sync. The installation commands:

- `cd` (to home directory)
- `git clone https://github.com/analogdevicesinc/libad9361-iio.git`
- `cd libad9361-iio`
- `mkdir build`
- `cd build`
- `cmake ..`
- `make -j$(nproc)`
- `sudo make install`
- `sudo ldconfig`

2.2.3 pyadi-iio

The pyadi-iio library is used simplify the use of different devices a python package was created interface with the different IIO drivers. The module pyadi-iio, provides device-specific APIs built on top of the current libIIO python bindings. The installation commands:

- `cd` (to home directory)
- `git clone --branch v0.0.14 https://github.com/analogdevicesinc/pyadi-iio.git`
- `cd pyadi-iio`
- `pip3 install --upgrade pip`
- `pip3 install -r requirements.txt`
- `sudo python3 setup.py install`

2.3 "Hacking" Adalm-Pluto SDR to increase RF Range

When we plugged in Adalm-Pluto to our PC, a "config.txt" file appears in his folder. Here, we can define its IP (we set it to "192.168.2.1").

Open a terminal and:

- `ssh root@192.168.2.1`
- password: analog

Now, we can check our Adalm-Pluto's Firmware version. For version 0.32 and higher, type:

- `fw_setenv compatible ad9364`
- `reboot`

Now, we are able to tune up to 6 GHz and down to 70 MHz.

2.4 Installing and building gr-rds blocks from Source-GitHub

Since Gnu-Radio Companion does not provide us any blocks for RDS Decoding-Encoding, we need to install and build them. Specifically, a pretty good repository that contain these blocks is [this](#). The installation and build of this repository, requires also the installation of the Boost.Locale library, by typing:

```
sudo apt-get install libboost-all-dev
```

The installation commands for installing and building gr-rds blocks (GnuRadio Version: 3.10):

- `cd` (to our home directory)
- `git clone --branch=maint-3.10 https://github.com/bastibl/gr-rds.git`
- `cd gr-rds`
- `mkdir build`
- `cd build`
- `-cmake ..` (that requires Boost.Locale library to produce the Makefile)
- `make`
- `sudo make install`
- `sudo ldconfig`

Now, we are ready to begin our implementations.

3 FM Station

To build an FM-Station in GnuRadio-Companion, using Adalm-Pluto SDR, first we need to find frequencies that are not used. In my case, I'm transmitting in 107.6 MHz. The GRC Flow Graph of an FM-Station is shown in Figure 2. The variable **audio_rate** represents the sampling rate of the block **Audio Source**. This specific

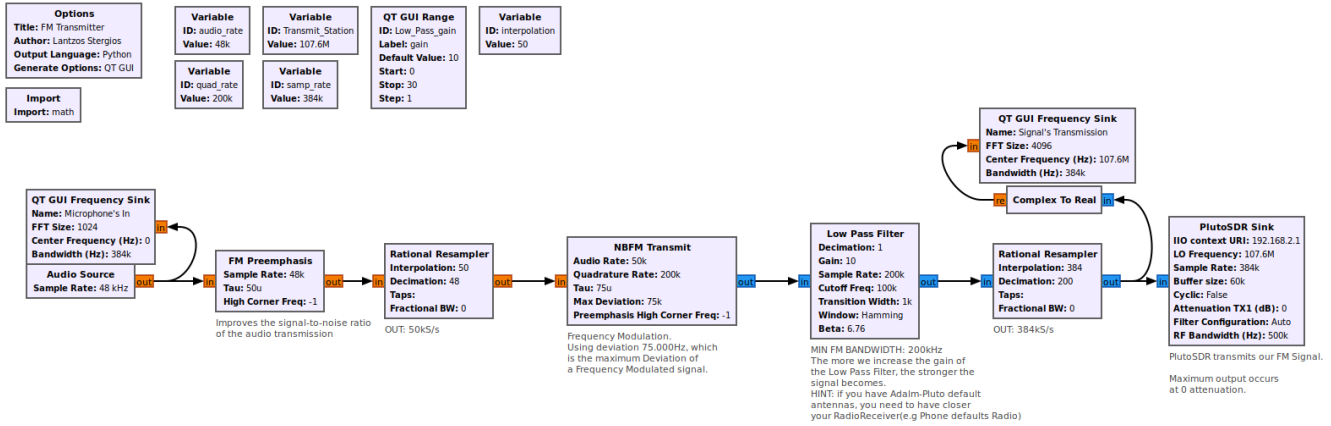


Figure 2: FM-Station Flow Graph

sampling rate is supported by the most common hardware. If we tap in this block, we can see four fields:

- Sample Rate : set to 48kHz
- Device Name : left it blank (it detects our PC's microphone by itself). If its not, use: plughw:0,0 or hw:0,0
- OK to Block : select "NO"
- Num Outputs : set it to 1

Its important to mention that Audio Source with 1 Output, in my PC, it didn't work at first. I managed to make it work properly, Via pavucontrol(sudo apt-get install pavucontrol and then type "pavucontrol"), configuring my mic's settings like Figure 3:

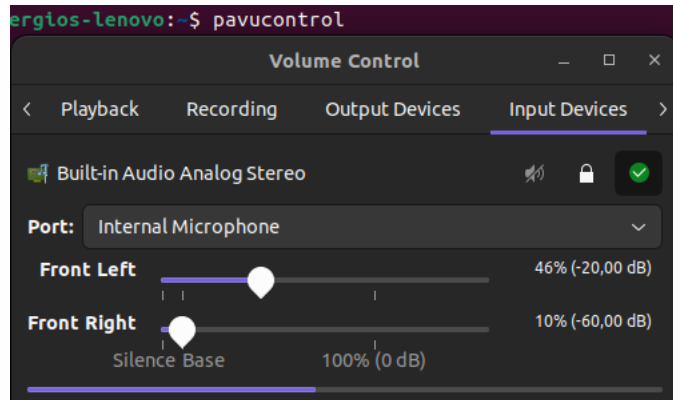


Figure 3: Pavucontrol Settings for my Mic

Basically, all i did, is to mute the Front Right(by moving it inside the Silence Base), and now Audio Source is working perfect! If i left it as default, Audio Source required at least two outputs.

So, Audio Source takes input from our microphone. **FM Preemphasis** follows, that is used for the transmission sessions. Its main functionality is to improve the signal-to-noise ratio(SNR) of the audio transmission(remember: SNR is defined as the ratio of signal power to the noise power). A **Rational Resampler** interpolates our sampling rate, giving us a new sampling rate of 50kS/s. Then, i used a **NBFM**(Narrow Band Frequency Modulation), that produces a single FM modulated complex base-band output, ready to be transmitted. At first, instead of NBFM block for the signal modulation, i used the WBFM(Wide Band Frequency Modulation). WBFM is more proper for high-quality music transmission, and NBFM works better for speech communications. Since i'm using my laptop's microphone, NBFM had a better performance. Its fields:

- Audio Rate: Input Sample Rate(for this scheme is 50kHz).
- Quadrature Rate: Sample Rate of the output stream. Needs to be multiple of Audio Rate. Because we want a typical Bandwidth of 200kHz, a Quadrature Rate of 200kS/s works fine.
- Tau: 75e-6 default value.
- Max Deviation: 75.000 Hz, which corresponds FM-Radios max allowable deviation.

A **Low Pass Filter** follows. Its main goal is to make stronger our signal and a little-bit more clear than before. Its fields:

- Decimation: 1
- Gain: is set by the variable Low_Pass_gain, so we can manually change it to find the proper gain required. Gain set to 10 as default.
- Sample Rate: the Quadrature Rate at 200kS/s.
- Cutoff Frequency: 100 kHz, keeping the 200 kHz bandwidth of FM standards, because this bandwidth is doubled, resulting the total FM-Bandwidth, which minimum value should be 200 kHz. Also, we are okay with the Nyquist-Sample Theorem, because we are sampling at 200kS/s and the highest frequencies that our signal passes from are 100kHz.
- Transition Width: 1000Hz.

Another **Rational Resampler** follows, that interpolates our sampling rate to match the Adalm-Pluto's one, at 384kS/s .

Finally, the last block is the **PlutoSDR Sink** which transmits our signal through TX Antenna, which most important fields are:

The plot of the FM-Station Flow Graph is represented in Figure 4.

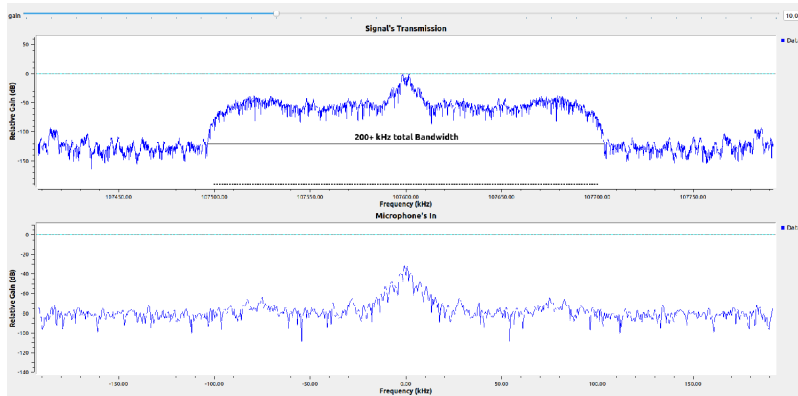


Figure 4: FM-Transmitted Signal at 107.6 MHz

As we can see, we have a total 200+ kHz signal bandwidth, that matches the minimum requirement bandwidth of FM. Also, the higher we set the gain of our Low Pass Filter, the more powerful the signal becomes. The FM-Station can be tested, by using our phone and lock into the frequency we transmit. It is important to mention that Adalm-Pluto's default antennas has a low TX Range, so if we want to hear what are we transmitting, we need to have our phone close to Adalm-Pluto, for achieving a better performance.

4 FM Receiver

Now we are ready to proceed with the FM-Receiver implementation. The Flow Graph of the FM-Receiver is illustrated in Figure 5. A **GT GUI Chooser** block, allows us to set frequencies of our desire(Like Radio Stations

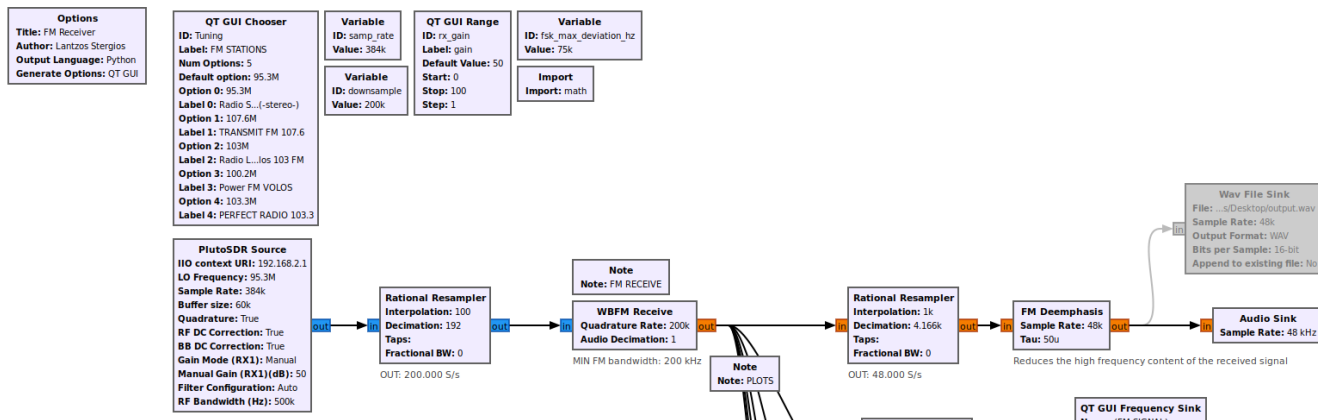


Figure 5: FM-Receiver Flow Graph

Frequencies et.c), with purpose to lock into them. In City of Volos, i found four Radio-Stations that broadcast FM Signals, and entered their frequencies in the fields of QT GUI Chooser, for tuning.

Beginning from the start of the Flow Graph, the very first block we meet is **PlutoSDR Source**. This block's fields are quite similar to PlutoSDR Sink, which explained in the section of the FM-Station. PlutoSDR Source LO(Local Oscillator) value is set to QT GUI Chooser's ID("Tuning"). From this point, PlutoSDR is capable to lock into these frequencies that QT GUI Chooser contains. We begin with a sample rate of 384 kHz.

The second block we are faced of, is a **Rational Resampler**, which is decimating our sampling rate. In this case, we want to a sample rate of 200kHz(FM-Bandwidth standards), so we multiply 384kS/s with 100 and divide by 192, giving us a sample rate of 200kS/s.

Moving forward, a **WBFM Receive** appears to demodulate the signal we are receiving via PlutoSDR Source. Its main field:

- Quadrature Rate: Input sample rate of complex baseband input. In our case, is 200kHz.

This block outputs the demodulated audio, that we need to send to our speakers to hear what we are receiving.

At this stage, another **Rational Resampler** follows which decimates our sampling rate to exactly 48kHz, as much as my hardware can support. Last but not least, as we did with the FM-Station(adding FM-Preemphasis), now we add **FM-Deemphasis**, which reduces the high frequency content of the signal, too. Now, the demodulated audio is fed to our Speakers, through **Audio Sink** block. This block parameters are used exactly as the Audio Source from the previous section.

For using both TX and RX and the same time, i suggest to right click on Audio Sink block and disable it, and enable the **Wav File Sink** block to record what you are receiving through PlutoSDR Source. The Flow Graph continues downwards with some Plots, using LowPass and BandPass Filters just to isolate and plot the Mono Audio, Pilot Tone, Stereo Audio and finally the RDS. Executing the receiver and tuning at a Station, we get these plots:

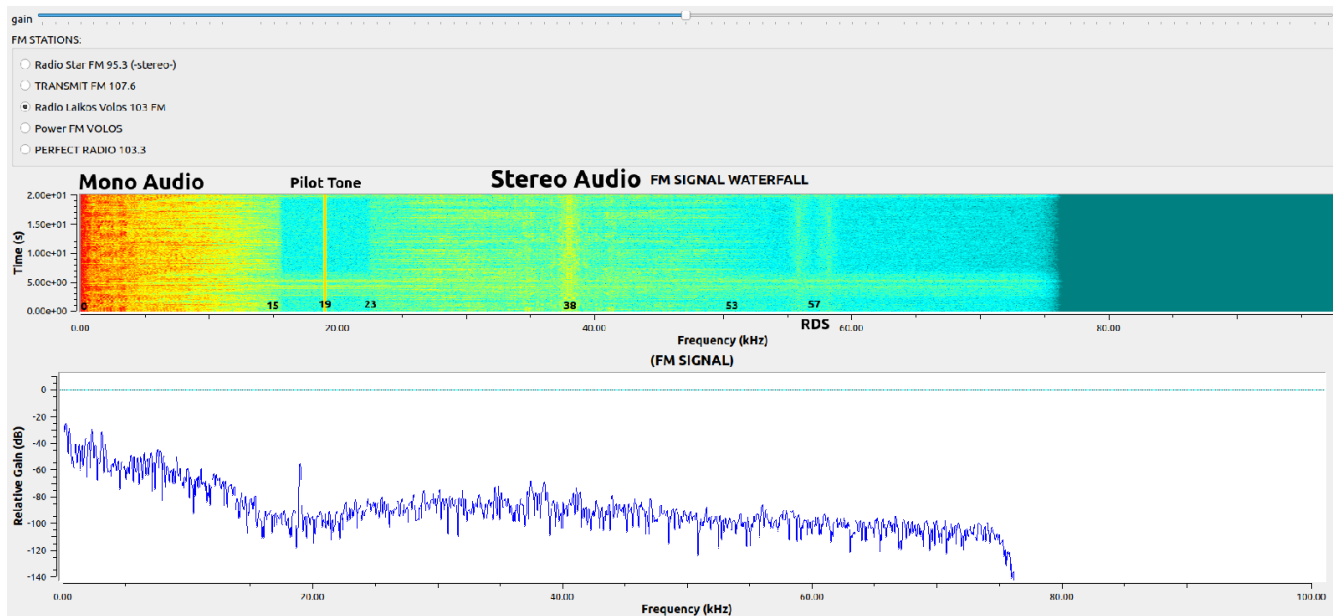


Figure 6: FM-Signal, FM-Waterfall

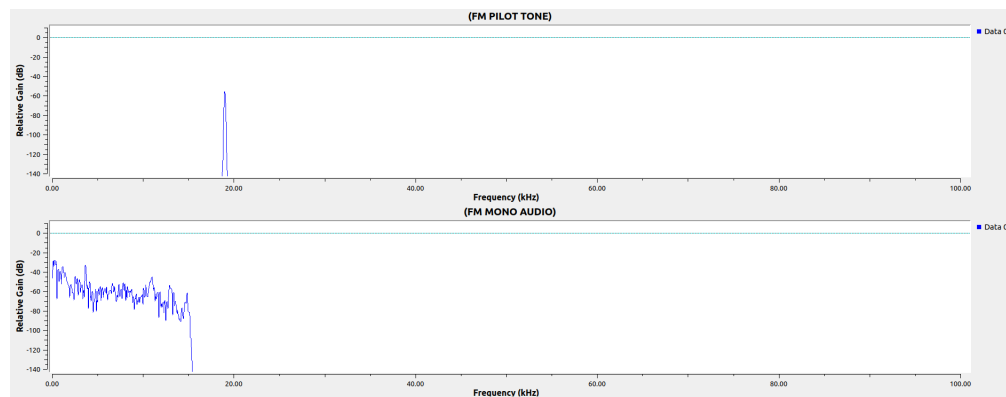


Figure 7: FM Pilot tone at 19kHz, FM Mono Audio at 0.03-15kHz

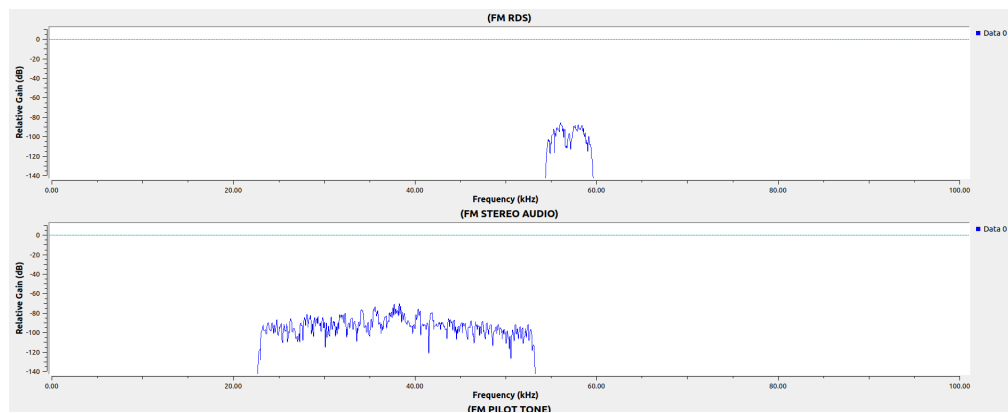


Figure 8: FM-Stereo Audio at 23-53kHz, FM-RDS at 54.6-59.4 kHz

As we expected(from the Introduction):

- The Mono Audio is located at: 0.03-15kHz
- The Pilot Tone at 19kHz
- The Stereo Audio at 23-53kHz, centered at 38kHz
- The RDS at 54.6-59.4kHz, centered at 57kHz

The Waterfall of the whole FM-Demodulated Signal, shows us how strong each signal is. The more hot is the color, the more powerful is the corresponding signal.

5 FM Stereo Receiver

Lets see how an FM-Stereo Decoder works and what are its functionalities. Our implementation is based in the scheme that is represented in the Figure 9:

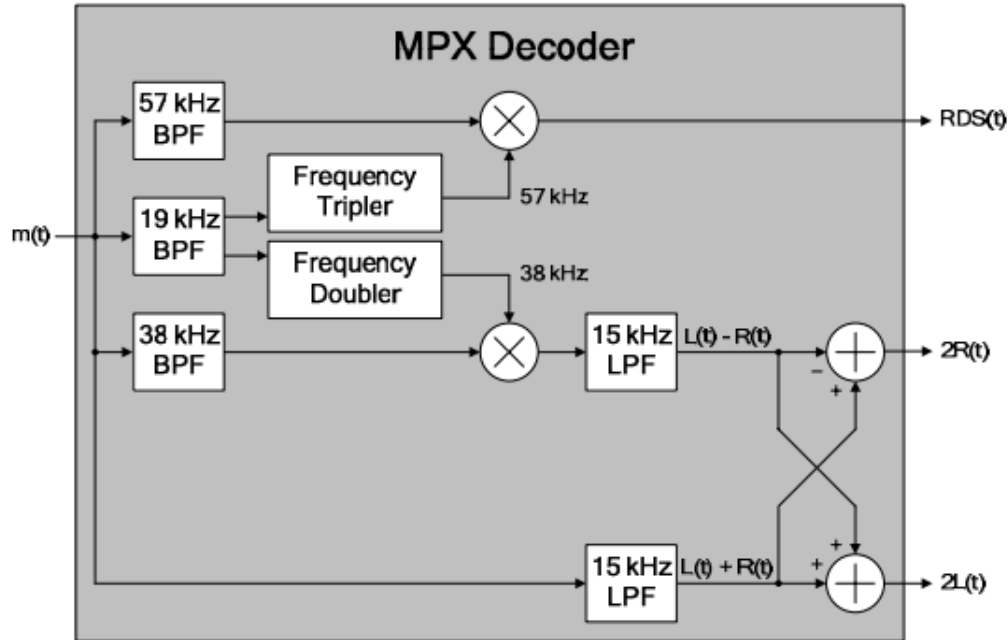


Figure 9: FM-Stereo Decoding Process

In this section, we will not deal with RDS, so the process is to:

- extract the L+R Signal from the Signal(Mono Audio), using LowPass Filter.
- generate a 38 kHz signal by frequency doubling the received 19 kHz Pilot. It will ensure that the 38 kHz signal is in phase with the 19 kHz signal(we will see how).
- demodulate the signals from 23 kHz to 53 kHz to get back the L-R channel(Stereo Audio), using a BandPass Filter.
- Build and use the L+R and the L-R signals to regenerate the original L and R signals.

The implementation of the FM-Stereo Receiver in GnuRadio:

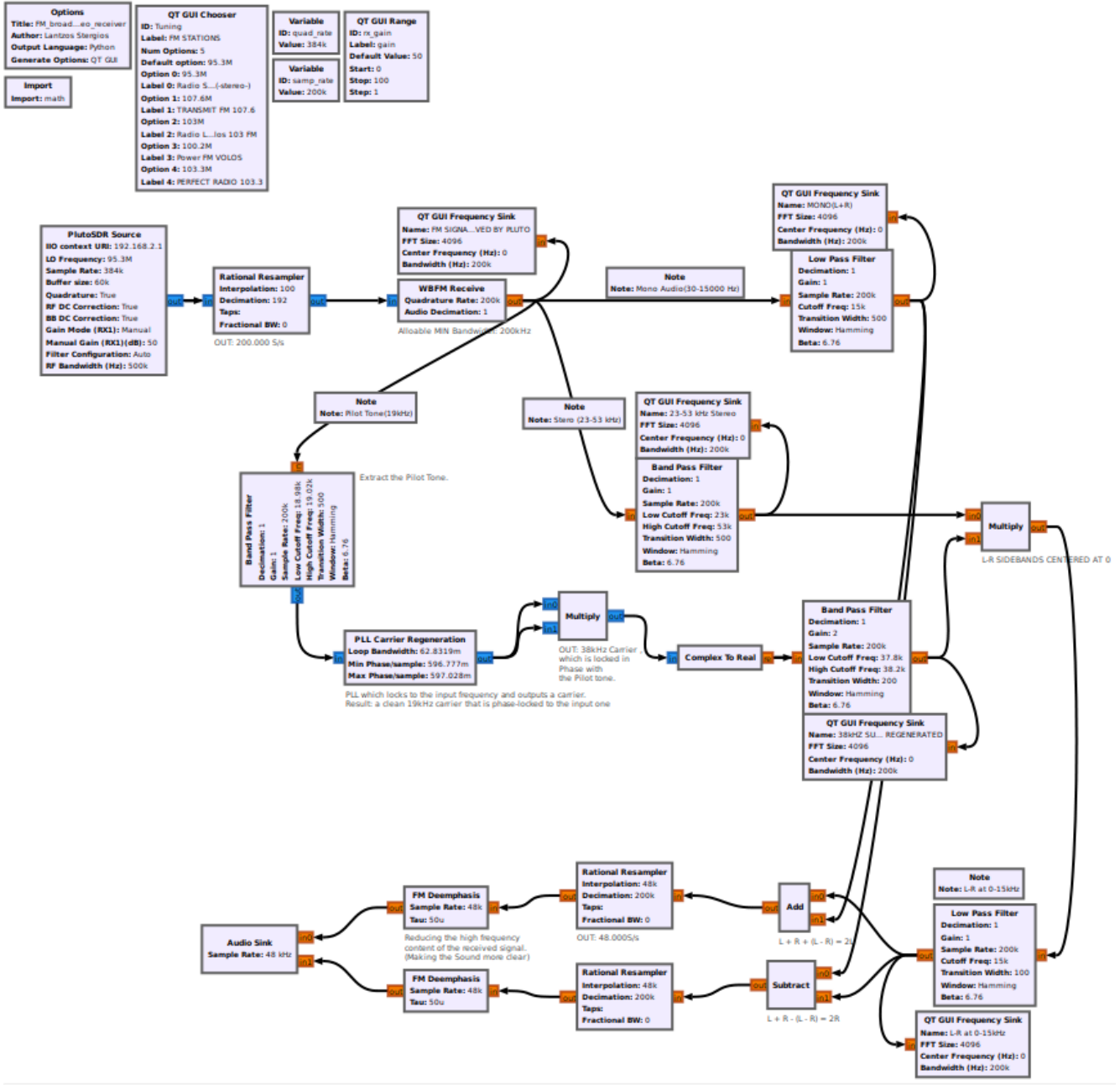


Figure 10: FM-Stereo Decoding Flow Graph in GnuRadio

Via **PlutoSDR Source**, we receive the Signal. A **Rational Resampler** is decimating our sampling rate to 200kS/s. The **WBFM Receive** demodulates our FM Signal, and now the process begins:

- **MONO AUDIO:** First of all, we extract the Mono Audio(Mono Audio locates at 0.03-15 kHz), using a **Low Pass Filter** with cutoff Frequency at 15 kHz. We direct it to the Add and Subtract Blocks, in purpose to build the L and R Channels.
- **STEREO AUDIO:** Now we need to do exactly the same process with the Stereo Audio. Extracting the Pilot Tone(which locates at 19kHz) using a **BandPass Filter**, with Low Cutoff Frequency at 18.90 kHz and High Cutoff Frequency at 19.02 kHz. We could now double it and regenerating the 38 kHz Carrier. But for better performance, we use the block **PLL Carrier Regeneration**. This block, locks into the

input frequency(19kHz Pilot tone in our case), and outputs a clean carrier, that is locked in-phase too. **Multiplying** by itself twice, we regenerate the 38 kHz carrier. Multiplying the Stereo Audio signal with the Pilot Tone ,allows us to extract the stereo information from the composite signal by removing the mono audio and recovering the original stereo audio. Meanwhile, we isolated the Stereo Audio from the Demodulated Signal(Stereo locates at 23-53kHz) using also a **BandPass Filter**, and we are **multiplying** it with the 38kHz carrier that we regenerated right now. The Stereo Audio is centered at 0 Hz now, and we are taking the Side-band(L-R) with a **Low Pass filter**, using cutoff Frequency at 15kHz.

Since we extracted successfully the L+R and the L-R side-bands, we need to build the channels(Right and Left). Using:

- **Add Block**: takes the L-R and adds it to L+R. The Result is the: $L+R + L - R = 2L$ (Left channel)
- **Subtract Block**: Subtracts the L-R from the L+R. The Result is the: $L+R - (L - R) = 2R$ (Right channel)

The last step, is to Downsample at 48kS/s and add the block **FM Deemphasis**. Left and Right channel are fed to **Audio Sink**, that plays the Stereo Audio in our Speakers.

6 RDS STANDARDS

FM RDS (Radio Data System) is a system for transmitting data over FM radio waves. It is widely used in many countries for providing listeners with additional information such as the name of the song or artist currently playing, station identification, and traffic reports. The technology allows stations to transmit text messages and digital signals, making it possible to provide a more interactive listening experience.

6.1 Data channel (Physical layer)

The RDS hardware first demodulates the 57 kHz RDS subcarrier signal to extract a differential Manchester encoded signal which contains both the bit clock and the differentially encoded bitstream. This allows the RDS decoder to tolerate phase inversion of its input.

6.2 Baseband coding (Data-link layer)

One RDS "group" (frame) is 104 bits long, comprised of 4 "blocks" of 26 bits each. A block includes the "information word" (16 bits) and the "checkword" (10 bits). There are 32 group types (0- 15, A or B) and the decoding of the infowords depends on the group type. This structure is illustrated in Figure 11:

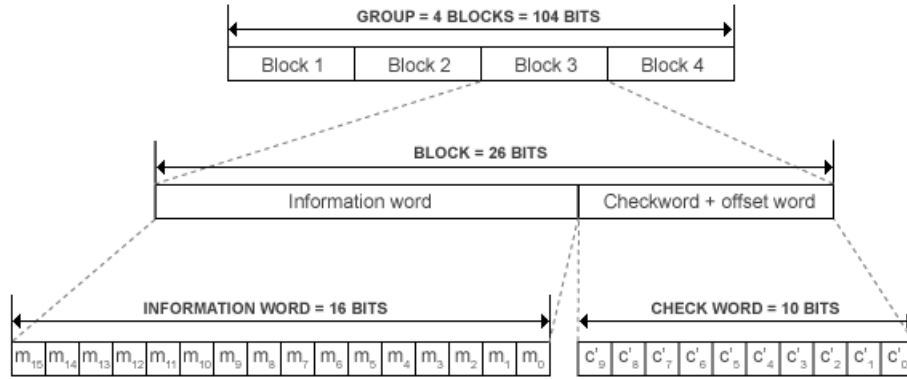


Figure 11: Structure of an RDS group

6.3 Method Of Modulation

The RDS sub-carrier at 57kHz (with a total bandwidth of 4.8kHz) is amplitude-modulated (AM) by the shaped and Bi-Phase (or Manchester) coded signal. It is also suppressed. The method of modulation RDS uses is BPSK (Binary Phase-shift keying). So, when the digital information changes from 1 to -1, the modulated signal changes from $\cos(t)$ to $\cos(-t)$, which equals to $\cos(t+\pi)$ or a phase inversion.

6.4 Clock Frequency and Data Rate

The basic clock frequency in FM RDS is actually derived from the division of a higher reference frequency, which is 57 kHz with 48. This division by 48 is used to generate the RDS subcarrier frequency because it provides a convenient frequency that falls within the acceptable range for a subcarrier in the FM band and can be used for efficient data transmission. The division of 57 kHz by 48 results in a subcarrier frequency of 1187.5 Hz. So, the basic data-rate of the system is 1187.5 \pm 0.125 bits/second. Also, the 57kHz is the 3rd harmonic of the Pilot Tone (19kHz). Since the Pilot tone has a \pm 2Hz deviation, the 57kHz subcarrier has a deviation of \pm 6Hz, because as we tripling the frequency, the deviation is tripled too.

6.5 Differential Encoding

RDS systems uses Differential Encoding. In differential encoding, the data is transmitted as the difference between the current data symbol and the previous one, instead of absolute values. Supposing "ti" is some arbitrary time, and "ti-1" is the time one data-clock period earlier, where data-clock period is equal to 1/1187.5 sec. When the input is 0, the output remains unchanged from the previous output bit, and when an input 1 occurs, the new output bit is the complement of the previous output bit. In conclusion, modulo 2 SUM(or X-OR) is performed(Figure 12).

Previous input (at time t_{i-1})	New input (at t_i)	New Output (at time t_i)
0	0	0
0	1	1
1	0	1
1	1	0

Figure 12: Differential Encoding

6.6 Manchester Encoding

Manchester encoding is a form of binary phase-shift keying (BPSK) that has gained wide acceptance as the modulation scheme for low-cost radio-frequency (RF) transmission of digital data. The encoding of digital data in Manchester format defines the binary states of "1" and "0" to be transitions rather than static values. So, instead of sending zeros and ones, the Manchester algorithm sends two symbols(they called "two halves") in one data-clock period. Replaces the logic "1" by a positive impulse at $t = 0$ and an opposite polarity pulse delayed by $t_d/2$, where t_d is the bit duration. For logic 0, the inverse method is used(Figure 13).

[1, -1] represents logic 1

[-1, 1] represents logic 0

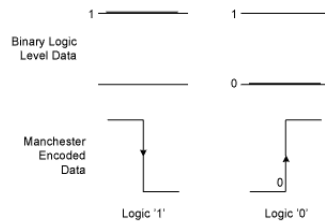


Figure 13: Manchester Encoding

Although the bit rate of the RDS is 1187.5 Bit/s, the Manchester encoding doubles this rate, resulting a new bit rate of 2375 Bit/s.

6.7 Matched Filter

A Pulse shaping filter to limit message spectrum and shape these impulses to smooth the signal, is added both in Transmitter and Receiver. This filter, we called "Root Raised Cosine Filter(RRC)", is used to improve the signal-to-noise ratio(SNR) of the received RDS signal and to reduce errors in decoding the data, providing also the required band limited spectrum. The combination of two RRC Filters is called a Raised Cosine Filter(RC), and is ideal for digital transmission and helps in reducing inter symbol interference (ISI). The Bi-Phase coded symbols are represented by the two below equations.

Logic 1 is represented by:

$$e(t) = d(t) - d(t - td/2) = 1 - (-1) = 2 > 0 \text{ (positive value)} \quad (1)$$

and a logic 0:

$$e(t) = -d(t) + d(t - td/2) = -1 - (+1) = -2 < 0 \text{ (negative value)} \quad (2)$$

where t is an arbitrary time value, and the $d(t)$ and $d(t - td/2)$ are the two halves of one Manchester Encoded bit. So, according to equations (1),(2), a Bi-Phase Symbol which has a negative value is represented as zero, and for a positive is represented as 1. We can see it clearly in the figure 14:

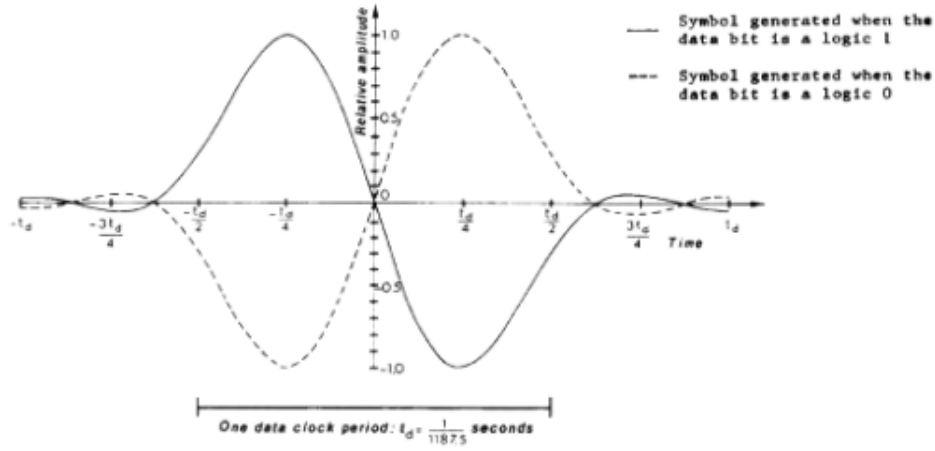


Figure 14: The RRC filter's response for one Manchester Symbol.

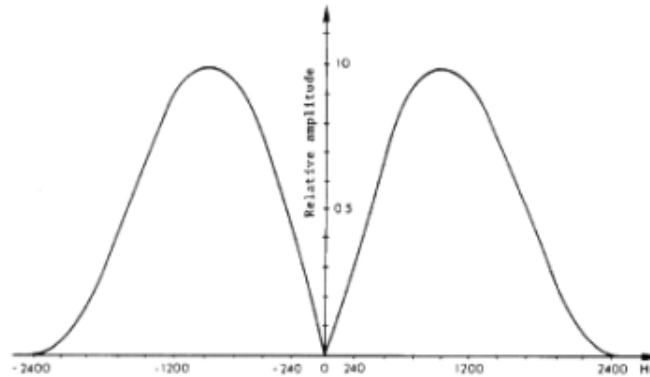


Figure 15: Spectrum of bi-phase coded radio-data signals. Notice the peak at 1187.5Hz !

7 FM-RDS Decoding

An FM-RDS Decoding process in GnuRadio Companion, is illustrated in Figure 16:

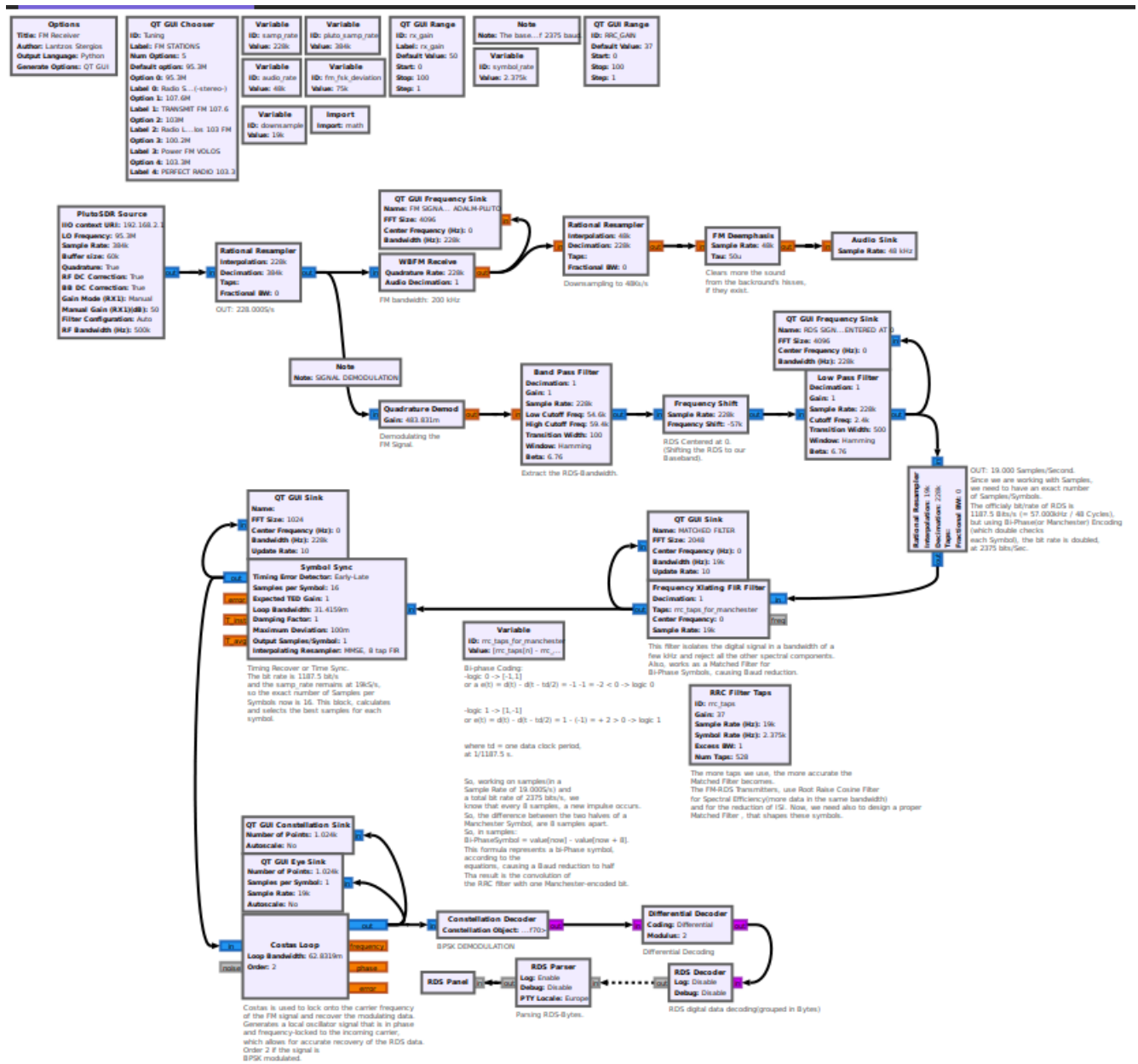


Figure 16: FM-RDS Decoder Flow Graph

Since the Flow Graph seems complicated, we are splitting it into three stages:

1. Signal Demodulation and RDS Bandwidth Isolation, centered at 0
2. Matched Filter and Symbol-Timing Synchronization, Baud Reduction
3. Carrier Recovery, BPSK Demodulation, Differential and RDS Data Decoding

7.1 Signal Demodulation and RDS Bandwidth Isolation

The first stage, demands the demodulation of our frequency modulated signal, playing the sound in our Speakers and isolating just the RDS Bandwidth. A Flow Graph that implements a scenario like this is illustrated in the Figure 17:

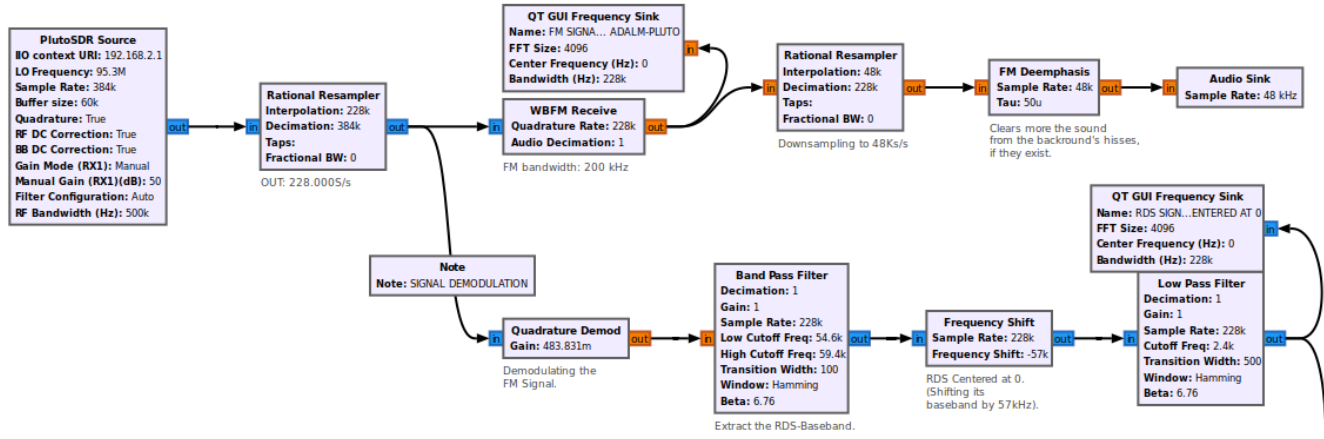


Figure 17: 1st Stage of the RDS Decoding Process

Receiving the Frequency Modulated Signal via **PlutoSDR Source** Block, which is tuning in the frequencies of our desire. A **Rational Resampler** follows to reduce our sampling rate at 228kS/s. Since FM-Signal Bandwidth requires at least 200kHz Bandwidth, this sampling rate meets these specifications. **WBFM Receive** demodulates our signal, and feeds it to another **Rational Resampler**, just to set the new sampling rate that our Sound Card's Hardware Supports(48kS/s).

On the other pattern, we used a **Quadrature Demod** that works similar to WBFM Receiver, but it takes a complex baseband as input, and outputs a signal frequency in relation to the sample rate, multiplied with the gain. The gain can be calculated by this formula:

$$\frac{\text{Sampling Rate}}{2 \times \pi \times \text{FM Deviation}}, \quad (3)$$

where FM maximum allowable Deviation is 75.000Hz. A **BandPassFilter** isolates the RDS signal from the whole demodulated signal. RDS Bandwidth ranges from (54.6-59.4)kHz and it is centered at 57kHz. Shifting the RDS Signal to our base-band(0 Hz), for furthermore processing. A **Low Pass Filter** is used for the better performance of our signal, with cutoff Frequency at 2.4 kHz, since the whole RDS bandwidth is 4.8kHz. The stage 1 is completed, and we can see it clearly in the Figure 18:

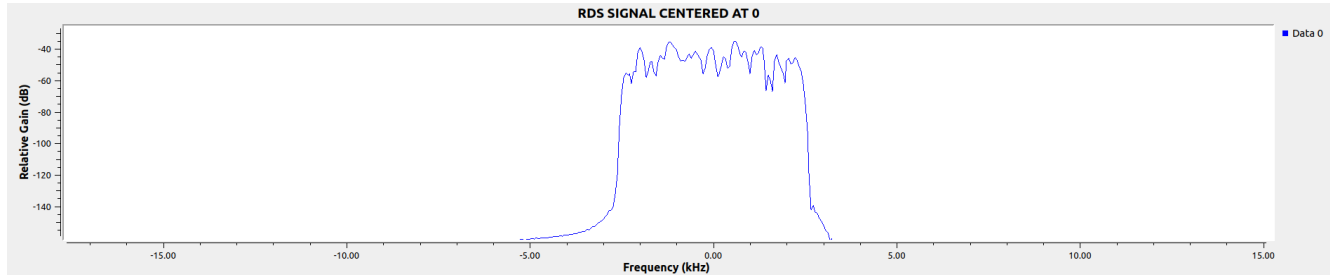


Figure 18: RDS Signal

7.2 Matched Filter and Symbol-Timing Synchronization

Now begins the stage 2(Figure 19), which is the most complicated part of the whole scenario. The RDS transmits

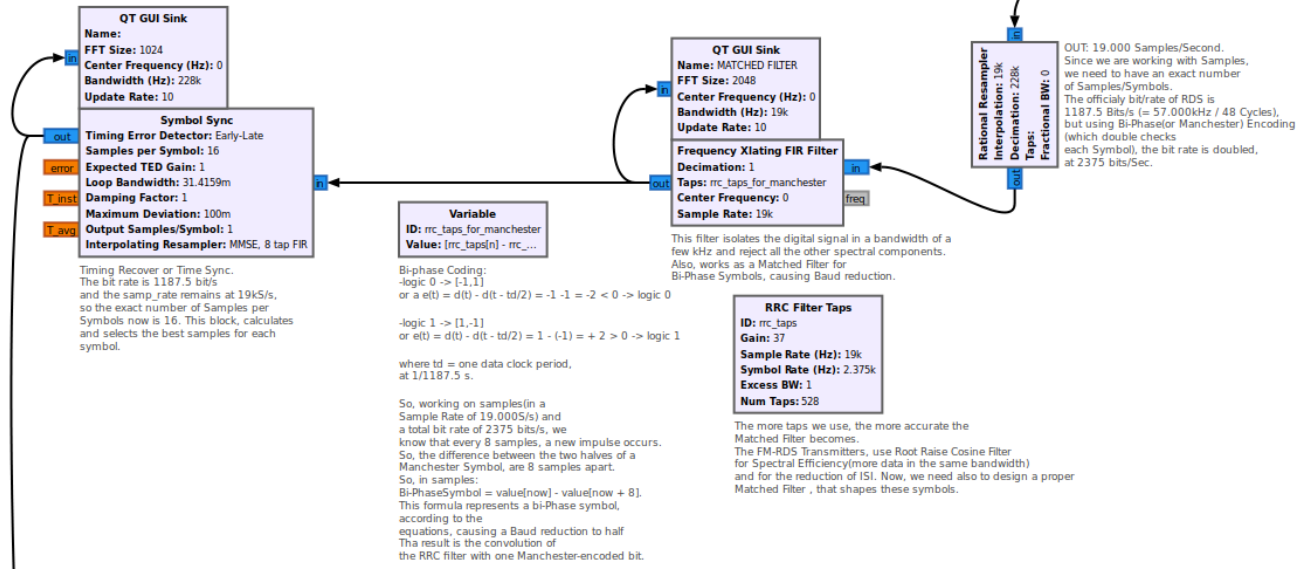


Figure 19: 2nd Stage of the RDS Decoding Process

the data, using a rate of 1187.5 Bits/sec. Also, the spectral efficiency of BPSK modulation described from this formula:

$$\text{BPSK Spectral Efficiency} = \log_2(M),$$

where $M = 2$. So the Spectral Efficiency is 1, and the transmission rate is:

$$\text{Tx Rate} = \text{Symbol Rate} \times \log_2(M),$$

which results a rate of 1187.5 symbols per second. Note that this number is the one-sixteenth of the Pilot Tone. So, a **Rational Resampler** reduces our Sampling Rate from 228kS/s, to 19kS/s. This allows us to have an exact number of Samples/Symbol, that makes the Symbol Sync more efficient, working on samples.

A **Frequency Xlating FIR Filter** follows, which removes the unwanted components, making more clear and strong the signal that is located in its centered Frequency. Also, this filter is a Matched filter for the Manchester's Encoded Symbols. As we said before, a Bi-Phase Symbol can be represented as:

$$e(t) = d(t) - d(t - td/2) \quad (4)$$

by means, subtracting the second half of the Manchester Symbol, from its first half. In order to make the Matched Filter, we need to transfer the equation (4), in samples. Our Sampling Rate is 19kS/s, and the Symbol Rate is 2375 bits/s. To make it more understandable:

$$\frac{\text{Sampling Rate}}{\text{Symbol Rate}} = \frac{19000 \text{ Samples per Seconds}}{2375 \text{ Symbols per Seconds}} = 16 \text{ Samples per Symbol}$$

That means that every 16 Samples a new Manchester Symbol is sent(or two halves are sent). So, splitting the 16 SpS, into two halves, we are getting 8 samples for the first half(the first bit[it could be 1 or -1]) and another 8 samples for the second half[the second bit[could be 1 or -1 too]]. So, it leads us to the conclusion that the two halves of a Manchester Symbols, in this scenario, are 8 samples apart(Using always 19.000S/s for our sampling rate).

So, the equation (4), in samples can be described by:

$$\text{Bi-Phase-Symbol} = \text{first_half} - \text{second_half} = \text{value}[\text{now}] - \text{value}[\text{now} + 8 \text{ samples}] \quad (5)$$

In common words, the value of the equation (5) could be either positive (represented as one), or negative (represented as zero). We know that before the Frequency Xlating FIR Filter, the incoming Manchester Symbols require 16 Samples each, and their two halves of them were 8 samples apart. So, the variable **rrc_taps_for_manchester** (which value is the equation(5)), in combination with **RRC Filter Taps** block, gives us the convolution of the RRC Filter for one Manchester Encoded bit, subtracting its second half (which is 8 samples apart), from the first one, resulting a new value for our Bi-Phase Symbols:

- Logic 1: $[1 - (-1) = 2]$
- Logic 0: $[-1 - (+1) = -2]$

In common words, now negative means zero and positive means one.

Before this Matched Filter, our Symbols were represented with two consecutive opposite-impulses, and from now on, each one of them is represented by one. This effect also causes a Baud reduction from 2375 impulses/sec, to 1187.5 impulses/second.

In the block RRC Filter Taps, we have added in the field "Gain", our Qt GUI Range, called RRC_GAIN, so we can manually changing the gain of the Matched Filter, for the better performance of BPSK, varying these values from $[-1, 1]$.

The final part in this stage, is the **Symbol Sync**, and its goal is to perform a Timing Recovery algorithm, by selecting the best samples that can perform each impulse/symbol. Its most important fields:

- Samples per Symbol: 16
- Output Samples/Symbol: 1
- Timing Error Detector: Early-Late

This block is performing the timing synchronization needed so that the signal is sampled at exactly the right moment in time, which is when each Bi-Phase's symbol/impulse is at its max value. Early-Late algorithm for Timing Error Detector, seems working good!

7.3 Carrier Recovery, BPSK Demodulation, Differential and RDS Data Decoding

Now, things are not complicated as before. After timing sync, now its time for the carrier recovery. The stage 3, which is the final, is illustrated in Figure 20. A **Costas Loop** Block is used to remove any residual frequency

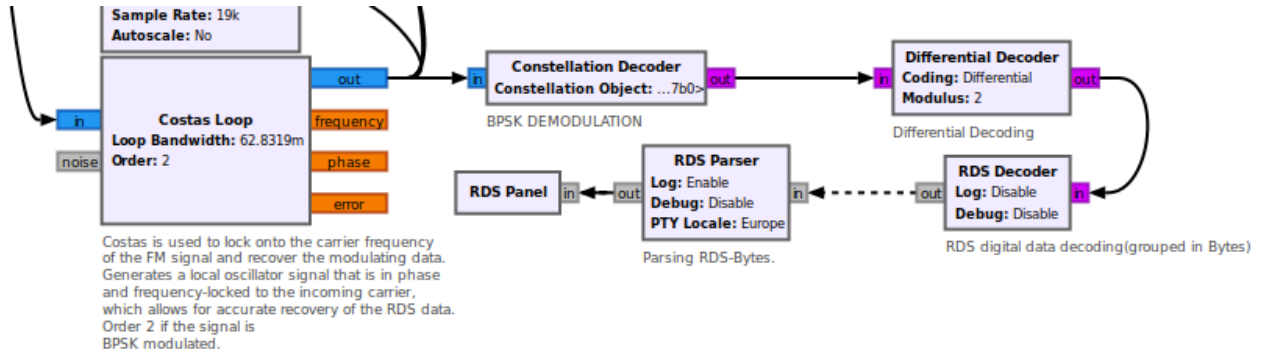


Figure 20: Final Stage of the RDS Decoding Process

offset. While the signal was previously base-banded, there may still exist a small frequency and phase offset that prohibits demodulating the BPSK signal. So Costas Loop, is a PLL circuit, that locks into the carrier frequency, by generating a LO that is locked in phase too. This allows us to continuously track the phase and frequency of the incoming FM signal, even in the presence of phase and frequency variations. A **Constellation Decoder** with "digital.constellation_bpsk().base()" in its only field, is used to perform the BPSK Demodulation in our signal. Feed its output to **Differential Decoder** with modulus 2, to perform the X-OR operation, as we discussed in the Section of Differential Encoding. The **RDS Decoder** follows, which performs the RDS digital data decoding, receiving raw bits and sending completed RDS frames(grouped in Bytes), and the **RDS Parser**, who is receiving these RDS frames and sends the Station/Song names to the **RDS Panel**. So, moving on with the plots:

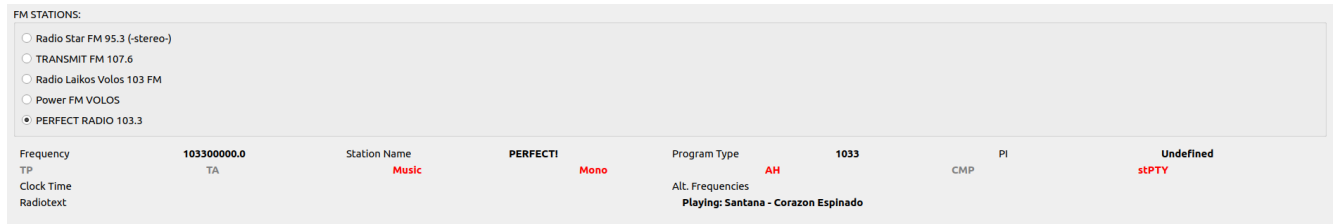


Figure 21: RDS Messages in our Panel

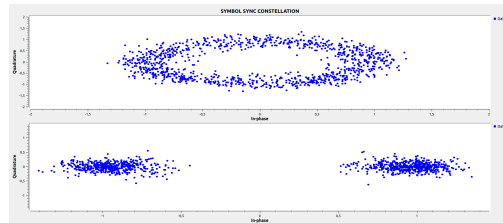


Figure 22: This Figure shows the actual constellations before and after carrier recovery. The received signal with a carrier frequency offset, causes a rotating or spinning constellation. Once Costas Loop lock's in the carrier's frequency and phase, this spinning effect is removed, since the small frequency offsets of our received carrier cause this cyclic-spinning move.

8 FM-RDS Encoder

The implementation of the FM-RDS Encoder, is illustrated in the Figure 23:

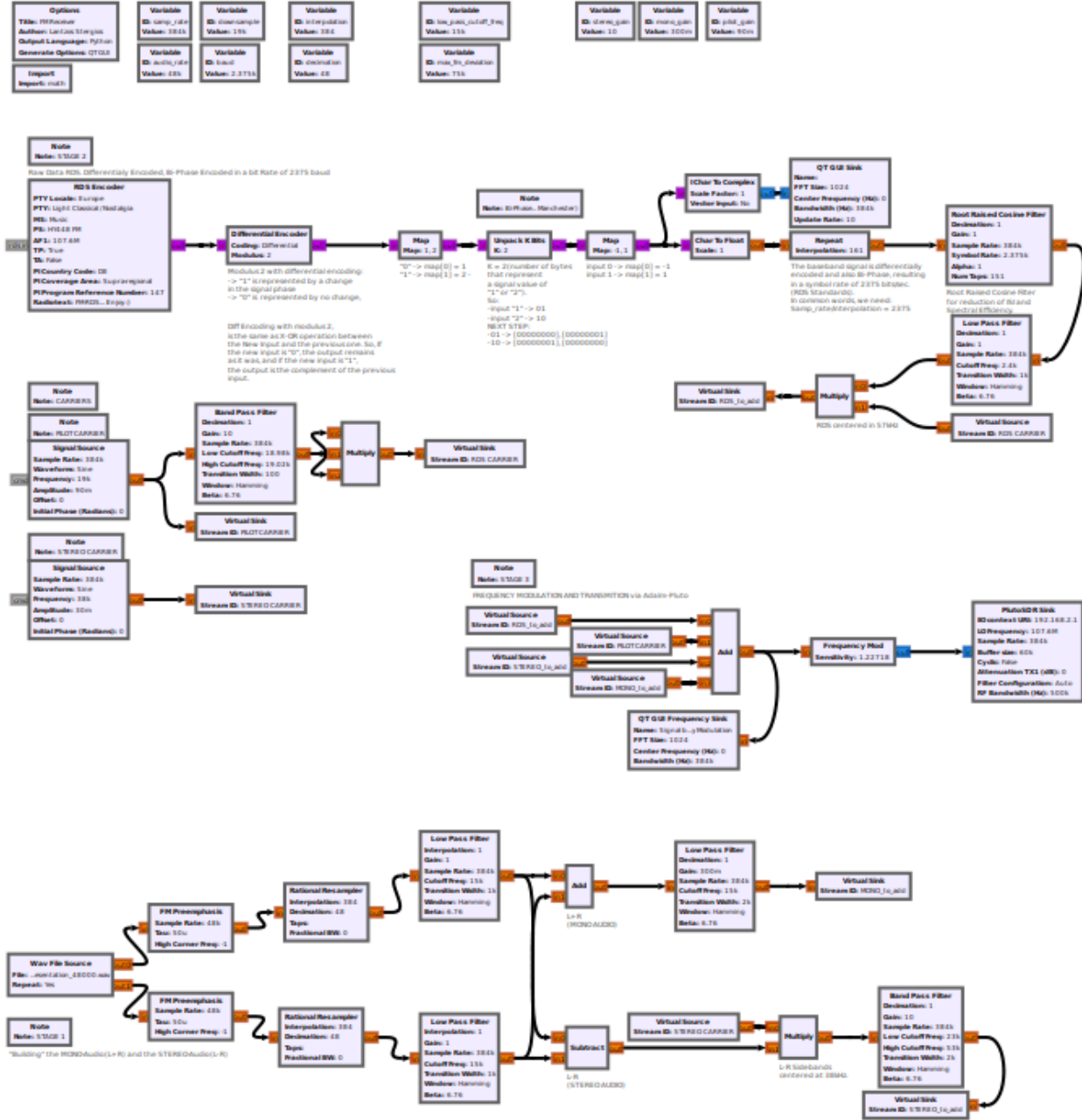


Figure 23: FM-RDS Encoder Flow Graph

For better understanding, we divided this implementation in 3 stages too:

- Building the Mono-Audio and Stereo-Audio
- RDS Encoding, Differential Encoded, Shaped Filter
- Frequency Modulation of our Signal and Transmit via PlutoSDR

8.1 Building the Mono-Audio and Stereo Audio

The first step, as you can see from the Figure 24, is to build the Mono and Stereo Audio.

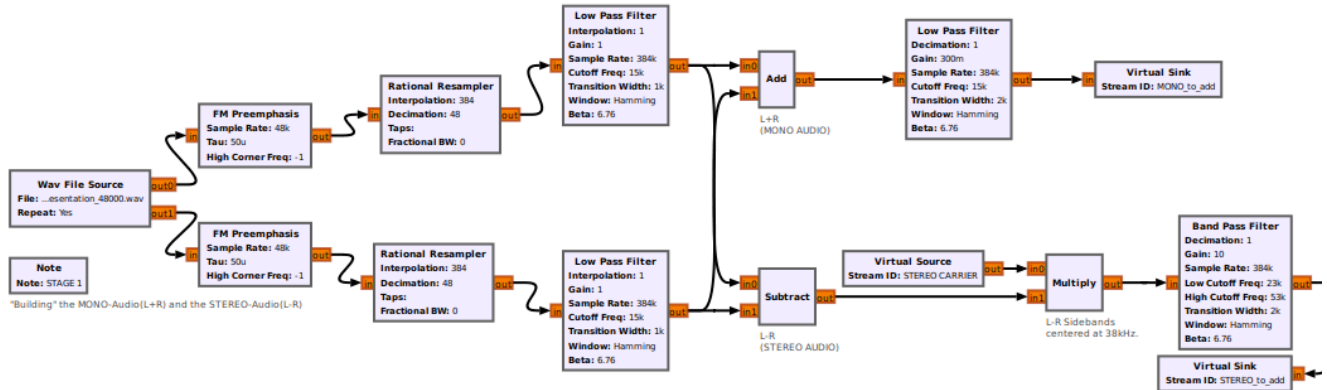


Figure 24: Mono and Stereo Audio

Used a **Wav File Source**, that's taking a .wav file and outputs a float stream. **FM Preemphasis** added for both Mono and Stereo Audio, since its reduces the high frequency components, making the sound little bit clear. **Both Rational Resamplers**, increases our sampling rate from 48kS/s to 384kS/S, which will be our sampling rate in the entire flow-graph. Also, the same **Low Pass Filters** added, with cutoff Frequencies at 15kHz(Mono Audio, and Stereo's each Side-band, have a bandwidth of 15 kHz). The **Add** block, outputs the L+R(which is the Mono Audio), and feeds its output to a **Low Pass Filter**, with cutoff Frequency at 15 kHz. Now, the part of the Mono Audio is done.

The **Subtract** block, builds the L-R Stereo side-bands, and its **multiplied** with the **Stereo Carrier** , in purpose to be centered at 38kHz. Using a **BandPass Filter**, with Low cutoff Frequency at 23kHz and High cutoff Frequency at 53 kHz, the Stereo Audio with its two side-bands is also ready.

8.2 RDS Encoding, Differential Encoding, Manchester Encoding, Shaped Filter

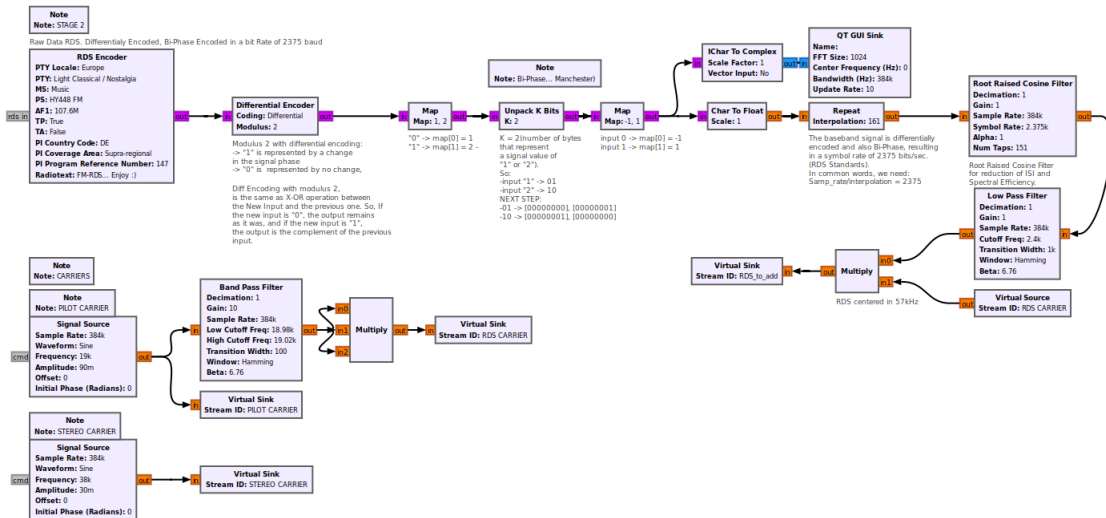


Figure 25: RDS Encoding, Differential Encoding and Manchester Encoding

The RDS Data for Transmission(RadioText, StationName et.c), are set in the **RDS Encoder** Block. **Differential Encoder** performs the differential Encoding, using modulus 2(X-OR). Now, the block **Map** is working like

this:

- If the input is 0, it maps 0 at map[0], which is 1
- If the input is 1, it maps 1 at map[1], which is 2

Unpack K Bits , with K = 2, stands for the representation of the input bit value with 2 bytes. In common words:

- If input is 1, represents 1 as [00000000], [00000001]
- If input is 2, represents 2 as [00000001], [00000000]

The last **Map Block**, does the Bi-Phase(or Manchester) encoding. More specifically:

- If input-Byte-value is 0, represents 0 as map[0] = -1
- If input-Byte-value is 1, represents 1 as map[1] = 1

So, in conclusion, a binary value "0" is represented as [-1,1], and the binary value "1" is represented as [1,-1]. This is the Manchester Encoding algorithm. The **Repeat** interpolation, defines the ratio that these symbols are sent. RDS bit rate is 1187.5 bit/s, but the Manchester encoding, doubles this rate, since each symbols is represented by two bits,resulting a new rate of 2375 Bits/s. We need to find the proper value to interpolate. Since we are sampling at 384kS/s, and the bit rate is 2375 Bits/s, the number we are searching for is:

$$\frac{\text{Sampling Rate}}{X} = \text{Symbol Rate}, \quad (6)$$

,providing to us a result of 161. Next, we are using a **Root Raised Cosine Filter**, for minimizing the ISI, and its output is fed to a **Low Pass Filter**, with cutoff Frequency of 2.4kHz, since the whole bandwidth of RDS is 4.8kHz. **Multiplying** the result of the Low Pass, with the **57kHz carrier**(by tripling the Pilot Tone), centers our RDS to 57kHz. Now, the RDS is ready to be added into the whole signal.

8.3 Frequency Modulation of our Signal and Transmit via PlutoSDR

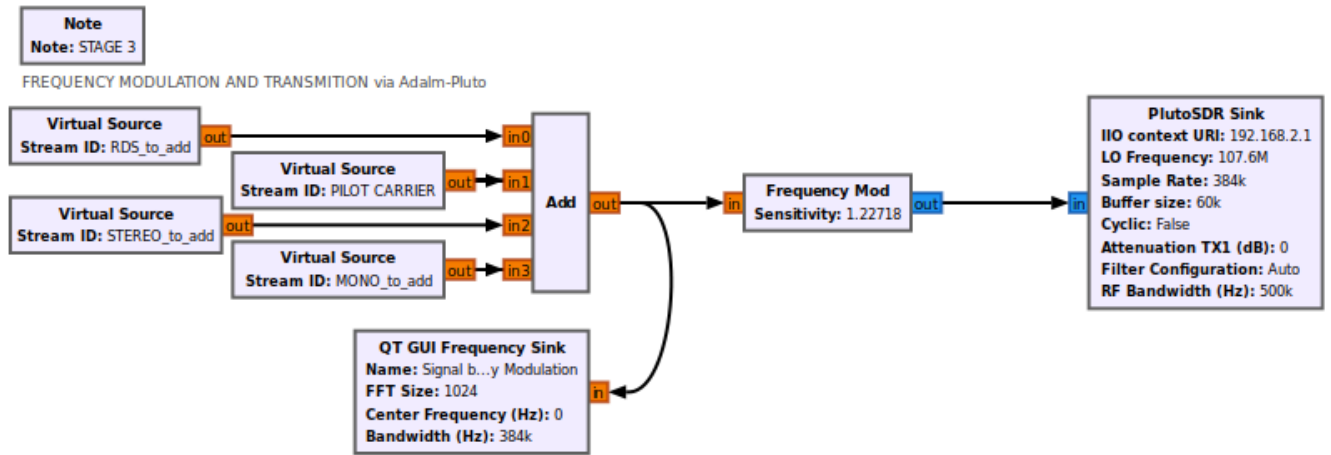


Figure 26: Frequency Modulation and Transmit

The last step, is to add all these frequency carriers, and modulates them into one, creating the FM-Signal. The **Frequency Mod** Block, modulates our signal in frequency, using the formula:

$$\text{Sensitivity} = \frac{2 \times \pi \times 75.000}{384.000}, \quad (7)$$

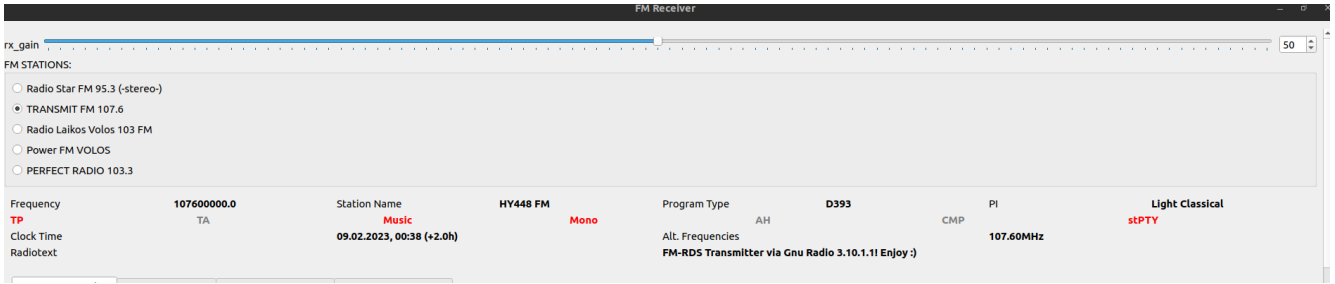


Figure 27: Text Messages in RDS Panel, received from the RDS Decoder Flow Graph

where 75.000 is the maximum allowable deviation and 384.000 is our sampling rate. The FM Signal, is fed to PlutoSDR for transmission, in the frequency of 107.6 MHz. The next step, to test this, requires the executing of the RDS Decoder and tuning it, in the frequency of 107.6MHz. Then, we will execute the RDS Encoder, and we will see what happens..

So, in the Figure 27, we can see that the data we set in the RDS Encoder Block, appear instantly in our panel. In the Figure 28, we can see its constellation, which responds to BPSK. Also, we can see the four possible transitions of the BPSK in the eye diagram: from +1 to +1, (ii) from +1 to -1, (iii) from -1 to +1, and (iv) from -1 to -1.

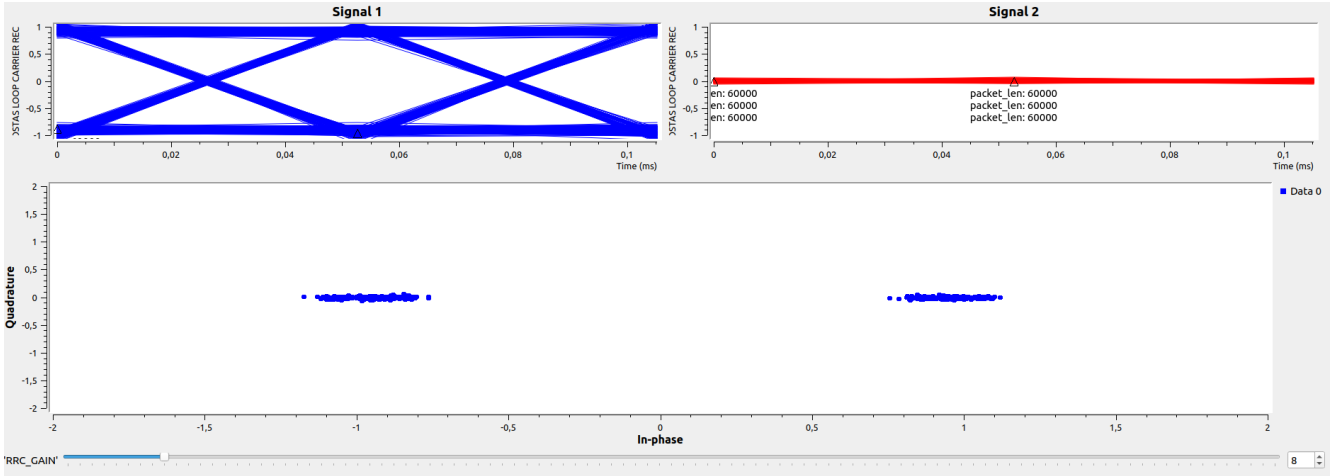


Figure 28: BPSK Constellation

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