

CSC 421 A2P1 - Dana Wiltse V00867579

Q1.

0	X	0
X	0	
X		

Max

$\alpha = 0$
 $\beta = \infty$

0	X	0
X	0	
X		

Min

$\alpha = -\infty$
 $\beta = -1$

0	X	0
X	0	X
X		

$\alpha = -1$
 $\beta = -1$

0	X	0
X	0	
X	X	

$\alpha = -1$
 $\beta = 0$

0	X	0
X	0	
X		X

Max
 $\alpha = 0$
 $\beta = \infty$

0	X	0
X	0	X
X	0	X

0	X	0
X	0	X
X		0

utility = -1

0	X	0
X	0	
X	X	0

utility = -1

~~not explored~~

0	X	0
X	0	0
X	X	

utility = 1

$\alpha = 0$
 $\beta = \infty$

0	X	0
X	0	
X	0	X

utility = 0

$\alpha = \infty$
 $\beta = 1$

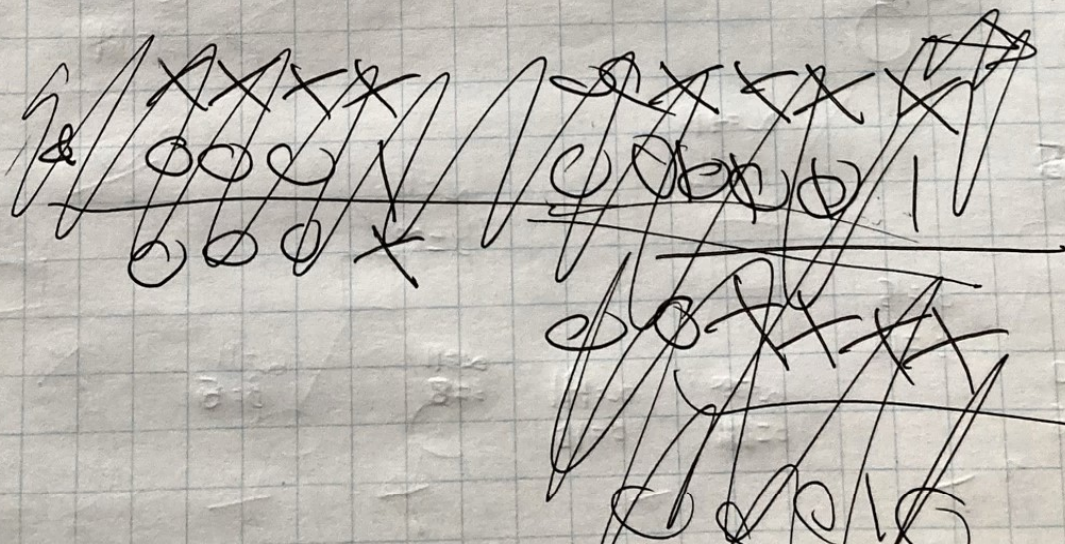
0	X	0
X	0	0
X	X	X

utility = 1

Min
 $\alpha = 0$
 $\beta = \infty$

0	X	0
X	0	X
X	0	X

utility = 0



Q2 b.

max

$$\alpha = -11$$

$$\beta = \infty$$

min

$$\alpha = -\infty$$

$$\beta = 3$$

$$\alpha = 3$$

$$\beta = 11$$

max

$$\alpha = 3$$

$$\beta = \infty$$

$$\alpha = 3$$

$$\beta = 3$$

$$\alpha = 11$$

$$\beta = \infty$$

$$\alpha = 11$$

$$\beta = 11$$

min

$$\alpha = -\infty$$

$$\beta = \infty$$

$$\alpha = 1$$

$$\beta = 3$$

$$\alpha = -\infty$$

$$\beta = 3$$

$$\alpha = 3$$

$$\beta = 9$$

$$\alpha = 9$$

$$\beta = 11$$

$$\alpha = 3$$

$$\beta = 11$$

1 2

3 4

5 6

7 8

9 10

11 12

13 14

15 16

6

Q2 a.

max

$$\alpha = 11$$

$$\beta = \infty$$

min

$$\alpha = -\infty$$

$$\beta = 11$$

$$\alpha = 11$$

$$\beta = 11$$

max

$$\alpha = 15$$

$$\beta = \infty$$

$$\alpha = 11$$

$$\beta = 15$$

min

$$\alpha = -\infty$$

$$\beta = 15$$

$$\alpha = \infty$$

$$\beta = 11$$

$$\alpha = 11$$

$$\beta = 10$$

$$\alpha = 11$$

$$\beta = \infty$$

$$\alpha = 11$$

$$\beta = 6$$

16 15

14 13

12 11

10 9

8 7

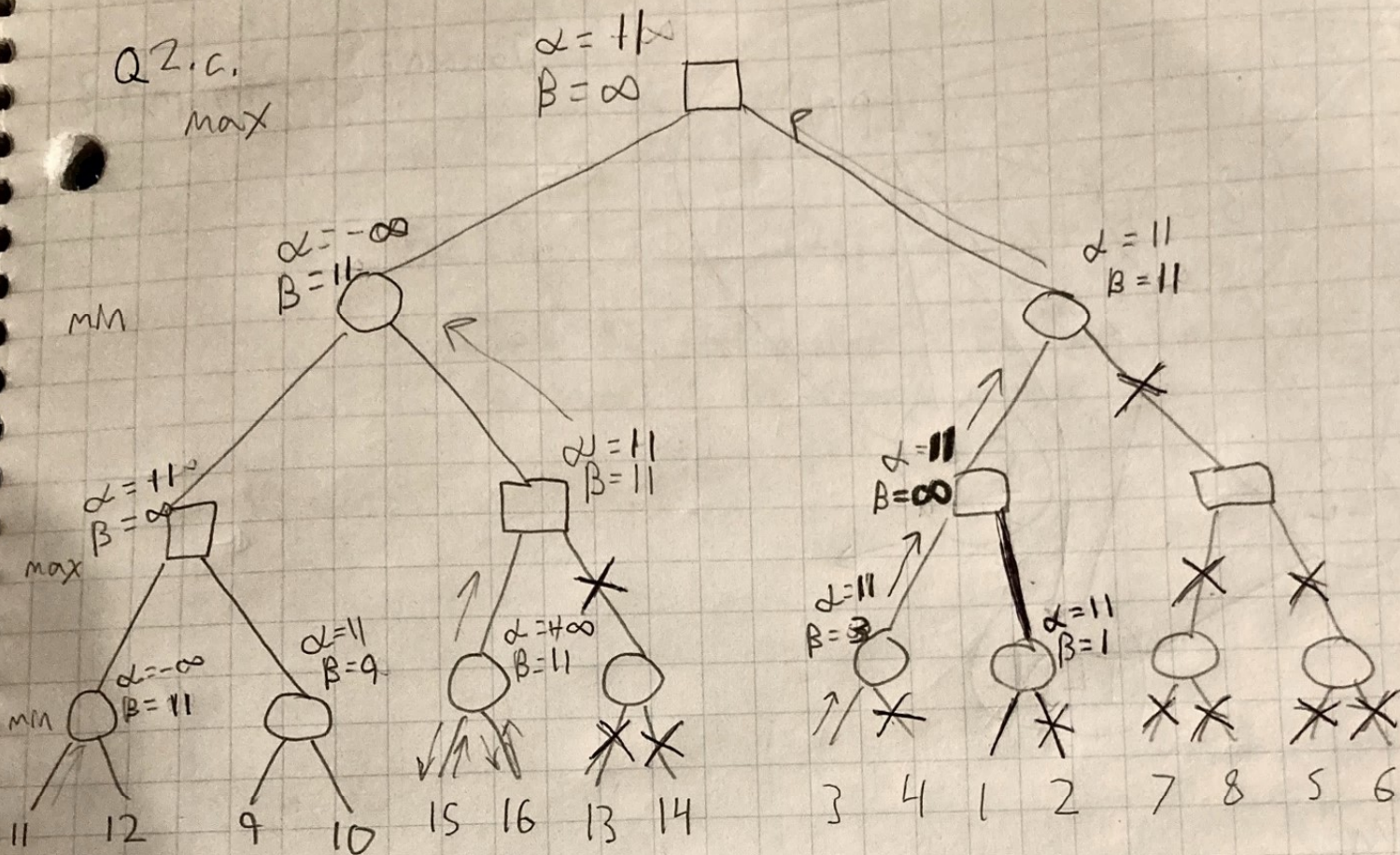
6 5

4 3

2 1

11

Q2.c.
max

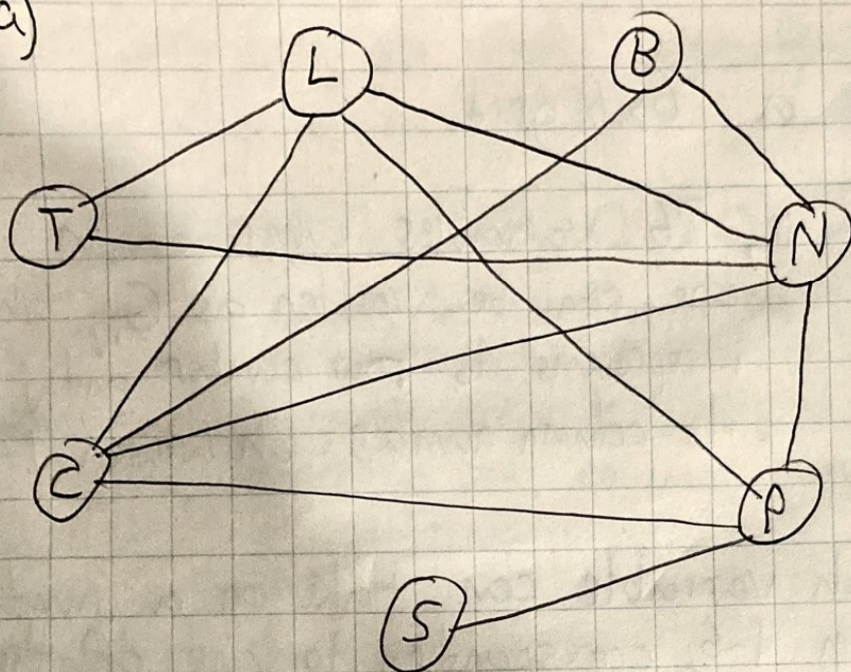


Q2 d. The order of the nodes does have a large effect on the efficacy of alphabeta pruning.

In 2a, we were able to avoid 6 nodes compared to 12 in 2c, a 50% increase in efficiency and on this small of an input.

~~It~~ It seems alpha-beta pruning performs poorly on inputs where the leaves are sorted in ascending order.

Q3. a)



Domains:

$$T = \{1\}$$

$$N = \{2-4\}$$

$$L = \{2-4\}$$

$$P = \{1-4\}$$

$$S = \{1-4\}$$

$$C = \{1-4\}$$

$$B = \{1-4\}$$

b)

Depth	C	S	P	N	B	L	T	
1	1-4	1-4	1-4	2-4	1-4	2-4	1	MRV, D(N=2), FC(B, L, C, P)
2	1,3,4	1-4	1,3,4	2	1,3,4	3,4	1	MRV(L=3) FC(C, P)
3	1,4	1-4	1,4	2	1,3,4	3	1	MRV, D, C and P are so C=1, FC(B, P)
4	1	1-4	4	2	3,4	3	1	MRV(B=4) FC(S)
5	1	1-3	4	2	3,4	3	1	MRV(B=3), FC
6	1	1-3	4	2	3	3	1	MRV(S=1)
7	1	1	4	2	3	3	1	

Q4.

Variables: a 6×6 grid.

ie, 36 variables where each one can be written as G_{ij} where i represents its row number and j represents its column number, each between 1-6.

Domain: each variable can take on a number from 1-6, corresponding to one of the six unique Greek characters.

Constraints:

- $G_{ij} \neq G_{kj}$ for $k \neq i$, $1 \leq k \leq 6, 1 \leq i \leq 6$
(no symbol in same ~~row~~ column)
- $G_{ij} \neq G_{ih}$ for $h \neq j$, $1 \leq j \leq 6, 1 \leq h \leq 6$
(no symbol in same ~~column~~ row)
- if $i = j$ then:
 - $G_{ij} \neq G_{i \pm k, j \pm k}$ $1 \leq k \leq 5$
 $1 \leq i \pm k \leq 6$
 $1 \leq j \pm k \leq 6$
(no symbol in main diagonals)