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- Nvidia Corporation

Outline

- 1 Why GPU Scripting?
- 2 Scripting CUDA
- 3 GPU Run-Time Code Generation
- 4 DG on GPUs
- 5 Perspectives





- 1 Why GPU Scripting?
 - Combining two Strong Tools
- 2 Scripting CUDA
- 3 GPU Run-Time Code Generation
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- 5 Perspectives





How are High-Performance Codes constructed?

- "Traditional" Construction of High-Performance Codes:
 - C/C++/Fortran
 - Libraries
- "Alternative" Construction of High-Performance Codes:
 - Scripting for 'brains'
 - GPUs for 'inner loops'
- Play to the strengths of each programming environment.







Why GPU Scripting? ○●○○○

Scripting: Means



A scripting language. . .

- is discoverable and interactive.
- has comprehensive built-in functionality.
- manages resources automatically.
- is dynamically typed.
- works well for "gluing" lower-level blocks together.

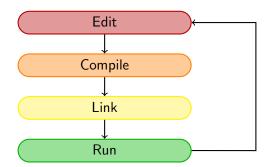




Why GPU Scripting? ○○●○○

Scripting: Interpreted, not Compiled

Program creation workflow:



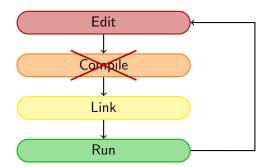




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Program creation workflow:

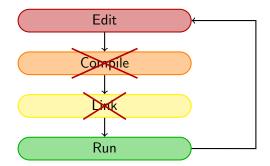




Why GPU Scripting? ○○●○○

Scripting: Interpreted, not Compiled

Program creation workflow:







Scripting: Python

One example of a scripting language: Python

- Mature
- Large and active community
- Emphasizes readability
- Written in widely-portable C
- A 'multi-paradigm' language







Why do Scripting for GPUs?

- GPUs are everything that scripting languages are not.
 - Highly parallel
 - Very architecture-sensitive
 - Built for maximum FP/memory throughput
 - → complement each other







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 - Scripting fast enough







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- CPU: largely restricted to control tasks (~1000/sec)
 - Scripting fast enough
- Python + CUDA = PyCUDA







Outline

- 1 Why GPU Scripting?
- 2 Scripting CUDA
 - Whetting your Appetite
 - Under the Hood
 - Fun with GPU Arrays
- 3 GPU Run-Time Code Generation
- 4 DG on GPUs
- 5 Perspectives





Whetting your appetite

```
import pycuda.driver as cuda
import pycuda.autoinit
import numpy

a = numpy.random.randn(4,4).astype(numpy.float32)
a_gpu = cuda.mem_alloc(a.nbytes)
cuda.memcpy_htod(a_gpu, a)
```

[This is examples/demo.py in the PyCUDA distribution.]





Whetting your appetite

```
mod = cuda.SourceModule("""
         __global__ void twice(float *a)
10
11
12
           int idx = threadIdx.x + threadIdx.y*4;
13
          a[idx] *= 2;
14
        """ )
15
16
17
    func = mod.get_function("twice")
18
    func(a_gpu, block=(4,4,1))
19
20
    a_doubled = numpy.empty_like(a)
    cuda.memcpy_dtoh(a_doubled, a_gpu)
21
22
    print a_doubled
23
    print a
```

9

11

14

17

18

21

22

Whetting your appetite

```
mod = cuda.SourceModule("""
10
         __global__ void twice(float *a)
                                                    Compute kernel
12
          int idx = threadIdx.x + threadIdx.y*4;
13
          a[idx] *= 2;
15
        11 11 11
16
    func = mod.get_function("twice")
    func(a_gpu, block=(4,4,1))
19
20
    a_doubled = numpy.empty_like(a)
    cuda.memcpy_dtoh(a_doubled, a_gpu)
    print a_doubled
23
    print a
```

Whetting your appetite, Part II

Did somebody say "Abstraction is good"?





Whetting your appetite, Part II

```
import numpy
import pycuda.autoinit
import pycuda.gpuarray as gpuarray

a_gpu = gpuarray.to_gpu(
    numpy.random.randn(4,4).astype(numpy.float32))

a_doubled = (2*a_gpu).get()
print a_doubled
print a_gpu
```





PyCUDA Philosophy



- Provide complete access
- Automatically manage resources
- Provide abstractions
- Allow interactive use
- Check for and report errors automatically
- Integrate tightly with numpy





PyCUDA: Completeness



PyCUDA exposes all of CUDA.

For example:

- Arrays and Textures
- Pagelocked host memory
- Memory transfers (asynchronous, structured)
- Streams and Events
- Device queries
- GL Interop





PyCUDA: Completeness

PyCUDA supports every OS that CUDA supports.

Scripting CUDA 00000000000000

- Linux
- Windows
- OS X

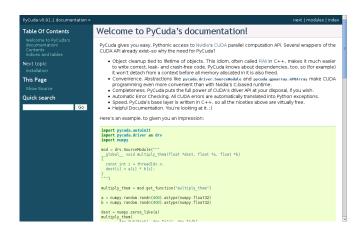








PyCUDA: Documentation

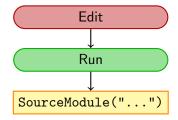




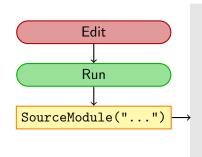








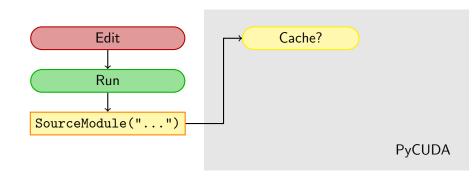




PyCUDA

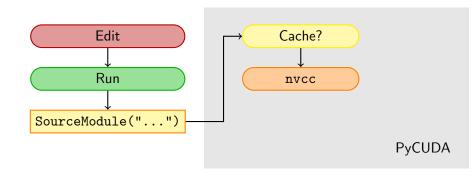






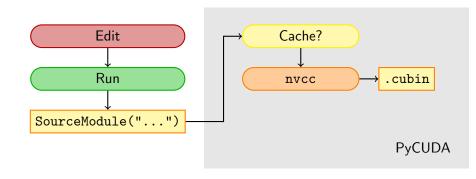






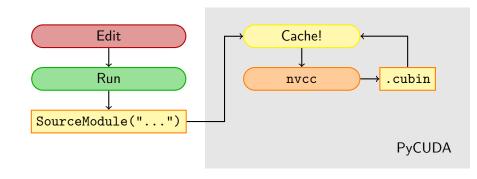






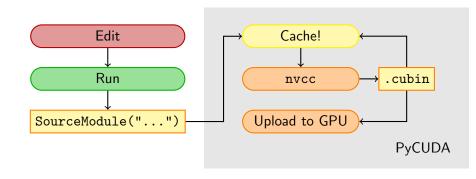






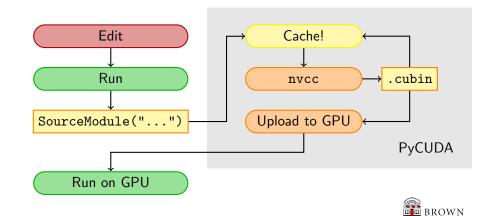














Automatic Cleanup

- Reachable objects (memory, streams, ...) are never destroyed.
- Once unreachable, released at an unspecified future time.
- Scarce resources (memory) can be explicitly freed. (obj.free())
- Correctly deals with multiple contexts and dependencies.







gpuarray: Simple Linear Algebra

pycuda.gpuarray:

- Meant to look and feel just like numpy.
 - gpuarray.to_gpu(numpy_array)
 - numpy_array = gpuarray.get()
- +, -, *, /, fill, sin, exp, rand, basic indexing, norm, inner product, ...
- Mixed types (int32 + float32 = float64)
- print gpuarray for debugging.
- Allows access to raw bits
 - Use as kernel arguments, textures, etc.







gpuarray: Elementwise expressions

Avoiding extra store-fetch cycles for elementwise math:

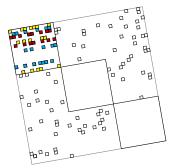
```
from pycuda.curandom import rand as curand
a_gpu = curand((50,))
b_gpu = curand((50,))
from pycuda elementwise import ElementwiseKernel
lin_comb = ElementwiseKernel(
        "float a, float *x, float b, float *y, float *z",
        "z[i] = a*x[i] + b*v[i]")
c_gpu = gpuarray.empty_like(a_gpu)
lin_comb(5, a_gpu, 6, b_gpu, c_gpu)
assert la.norm((c_gpu - (5*a_gpu+6*b_gpu)).get()) < 1e-5
```

gpuarray: Reduction made easy

Example: A scalar product calculation

Sparse Matrix-Vector on the GPU

- In development version:
 Sparse matrix-vector
 multiplication
- Uses "packeted format" by Garland and Bell (also includes parts of their code)
- Integrates with scipy.sparse.
- Optimized conjugate-gradients solver included







PyCUDA: Vital Information

- http://mathema.tician.de/ software/pycuda
- Complete documentation
- X Consortium License (no warranty, free for all use)
- Requires: numpy, Boost C++, Python 2.4+.
- Support via mailing list.







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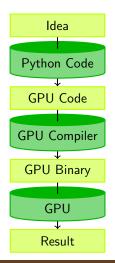


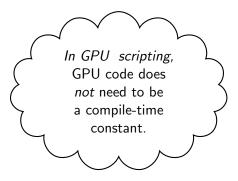
In GPU scripting,
GPU code does
not need to be
a compile-time
constant.

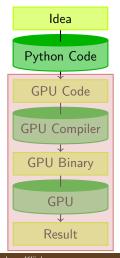


Idea

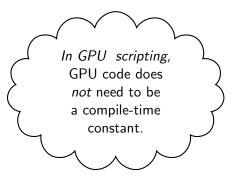


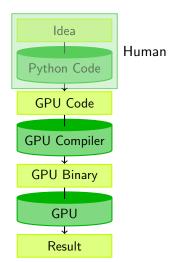




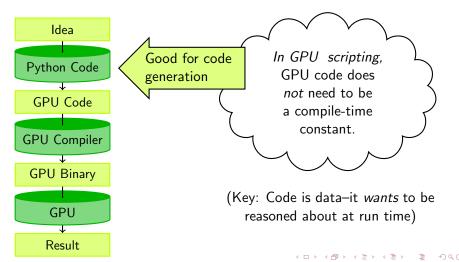


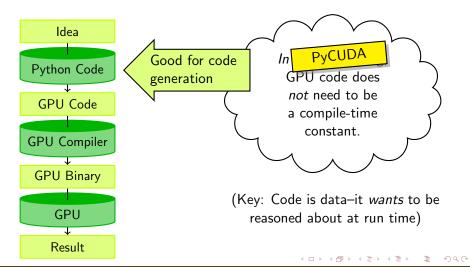
Machine











Machine-generated Code

Why machine-generate code?

- Automated Tuning (cf. ATLAS, FFTW)
- Data types
- Specialize code for given problem
- Constants faster than variables (→ register pressure)
- Loop Unrolling







PyCUDA: Support for Metaprogramming

- Access properties of compiled code: func.{num_regs,shared_size_bytes,local_size_bytes}
- Exact GPU timing via events
- Can calculate hardware-dependent MP occupancy
- codepy:
 - Build C syntax trees from Python
 - Generates readable, indented C
- Or use a templating engine (many available)





RTCG via Templates

```
from jinja2 import Template
tpl = Template("""
    __global__ void twice({{ type_name }} *tgt)
      int idx = threadIdx.x +
        {{ thread_block_size }} * {{ block_size }}
        * blockldx.x:
      {% for i in range(block_size) %}
          {% set offset = i* thread_block_size %}
          tgt[idx + {{ offset }}] *= 2;
      {% endfor %}
rendered_tpl = tpl.render(
    type_name="float", block_size = block_size,
    thread_block_size = thread_block_size )
smod = SourceModule(rendered_tpl)
```

RTCG via AST Generation

```
from codepy.cgen import *
from codepy.cgen.cuda import CudaGlobal
mod = Module([
    FunctionBody(
        CudaGlobal(FunctionDeclaration(
            Value("void", "twice"),
            arg_decls = [Pointer(POD(dtype, "tgt"))])),
        Block([
             Initializer (POD(numpy.int32, "idx"),
                "threadIdx.x + %d*blockIdx.x"
                % (thread_block_size * block_size )),
            1+[
            Assign("tgt[idx+%d]" % (o*thread_block_size),
                "2 *tgt[idx+%d]" % (o*thread_block_size))
            for o in range(block_size )]))])
smod = SourceModule(mod)
```

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 - Introduction
 - DG and Metaprogramming
 - Results







Let
$$\Omega := \bigcup_i \mathsf{D}_k \subset \mathbb{R}^d$$
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Goal

Solve a *conservation law* on Ω :

$$u_t + \nabla \cdot F(u) = 0$$

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Solve a *conservation law* on Ω :

$$u_t + \nabla \cdot F(u) = 0$$

Example

Maxwell's Equations: EM field: E(x,t), H(x,t) on Ω governed by

$$\partial_t E - \frac{1}{\varepsilon} \nabla \times H = -\frac{j}{\varepsilon},$$
$$\nabla \cdot E = \frac{\rho}{\varepsilon},$$

$$\partial_t H + \frac{1}{\mu} \nabla \times E = 0,$$

$$\nabla \cdot H = 0.$$

Multiply by test function, integrate by parts:

$$0 = \int_{D_k} u_t \varphi + [\nabla \cdot F(u)] \varphi \, dx$$

=
$$\int_{D_k} u_t \varphi - F(u) \cdot \nabla \varphi \, dx + \int_{\partial D_k} (\hat{n} \cdot F)^* \varphi \, dS_x,$$

Integrate by parts again, substitute in basis functions, introduce elementwise differentiation and "lifting" matrices D, L:

$$\partial_t u^k = -\sum_{\nu} D^{\partial_{\nu},k}[F(u^k)] + L^k[\hat{n} \cdot F - (\hat{n} \cdot F)^*]|_{A \subset \partial D_k}.$$

For straight-sided simplicial elements: Reduce $D^{\partial_{\nu}}$ and L to reference matrices.



- Specialize code for user-given problem:
 - Flux Terms





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 - Flux Terms
- Automated Tuning:
 - Memory layout
 - Loop slicing
 - Gather granularity





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- Constants instead of variables:
 - Dimensionality
 - Polynomial degree
 - Element properties
 - Matrix sizes





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- Specialize code for user-given problem:
 - Flux Terms (*)
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Metaprogramming DG: Flux Terms

$$0 = \int_{\mathsf{D}_k} u_t \varphi + [\nabla \cdot F(u)] \varphi \, \mathrm{d}x - \underbrace{\int_{\partial \mathsf{D}_k} [\hat{n} \cdot F - (\hat{n} \cdot F)^*] \varphi \, \mathrm{d}S_x}_{\mathsf{Flux \ term}}$$





Metaprogramming DG: Flux Terms

$$0 = \int_{\mathsf{D}_k} u_t \varphi + [\nabla \cdot F(u)] \varphi \, \mathrm{d}x - \underbrace{\int_{\partial \mathsf{D}_k} [\hat{n} \cdot F - (\hat{n} \cdot F)^*] \varphi \, \mathrm{d}S_x}_{\mathsf{Flux \ term}}$$

Flux terms:

- vary by problem
- expression specified by user
- evaluated pointwise





Metaprogramming DG: Flux Terms Example

Example: Fluxes for Maxwell's Equations

$$\hat{n} \cdot (F - F^*)_E := \frac{1}{2} \left[\hat{n} \times (\llbracket H \rrbracket - \alpha \hat{n} \times \llbracket E \rrbracket) \right]$$

Metaprogramming DG: Flux Terms Example

Example: Fluxes for Maxwell's Equations

$$\hat{n} \cdot (F - F^*)_E := \frac{1}{2} \left[\hat{n} \times (\llbracket H \rrbracket - \alpha \hat{n} \times \llbracket E \rrbracket) \right]$$

User writes: Vectorial statement in math. notation

Metaprogramming DG: Flux Terms Example

Example: Fluxes for Maxwell's Equations

$$\hat{\mathbf{n}} \cdot (\mathbf{F} - \mathbf{F}^*)_{\mathbf{E}} := \frac{1}{2} \left[\hat{\mathbf{n}} \times (\llbracket \mathbf{H} \rrbracket - \alpha \hat{\mathbf{n}} \times \llbracket \mathbf{E} \rrbracket) \right]$$

We generate: Scalar evaluator in C $(6\times)$

```
 a\_flux \ += (\\ (((\ val\_a\_field5 \ - \ val\_b\_field5) * fpair -> normal[2] \\ - (\ val\_a\_field4 \ - \ val\_b\_field4) * fpair -> normal[0]) \\ + \ val\_a\_field0 \ - \ val\_b\_field0) * fpair -> normal[0] \\ - (((\ val\_a\_field4 \ - \ val\_b\_field4) * fpair -> normal[1] \\ - (\ val\_a\_field1 \ - \ val\_b\_field1) * fpair -> normal[2]) \\ + \ val\_a\_field3 \ - \ val\_b\_field3) * fpair -> normal[1] \\ )* value\_type (0.5);
```

Setting: *N* independent work units + preparation



Question: How should one assign work units to threads?



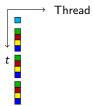


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 w_s : in sequence





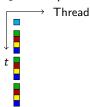


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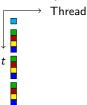


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 w_s : in sequence



w_i: "inline-parallel"





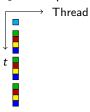


Setting: N independent work units + preparation

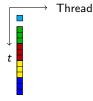
Preparation

Question: How should one assign work units to threads?

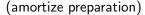
 w_s : in sequence



w_i: "inline-parallel"





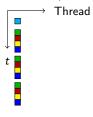




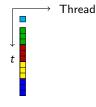
Setting: *N* independent work units + preparation

Question: How should one assign work units to threads?

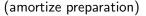
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 w_i : "inline-parallel"





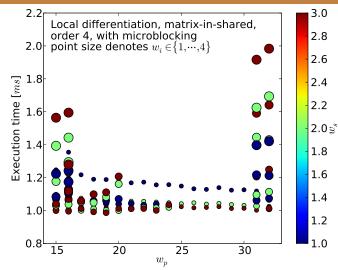


(exploit register space)

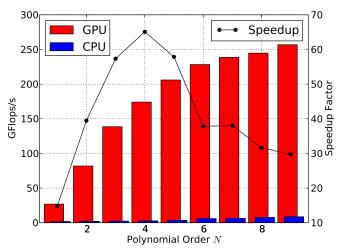




Loop Slicing for Differentiation





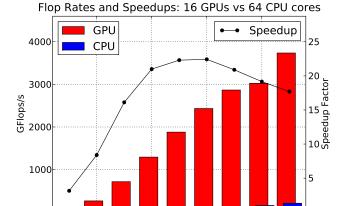






Results

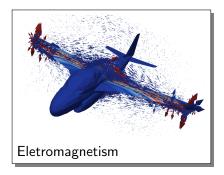
16 T10s vs. $64 = 8 \times 2 \times 4$ Xeon E5472



Polynomial Order N

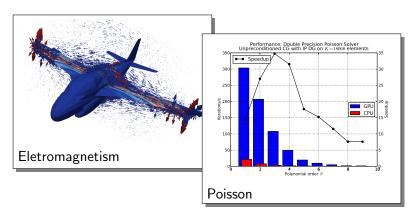






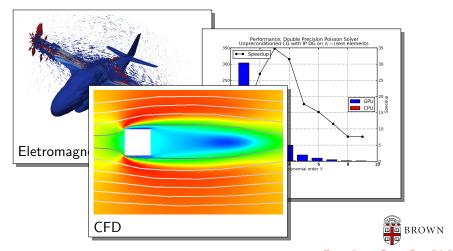


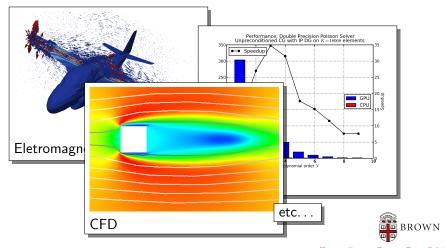












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 - Conclusions





Introducing... PyOpenCL

- PyOpenCL is "PyCUDA for OpenCL"
- Complete, mature API wrapper
- Features like PyCUDA: not yet
- Tested on all available Implementations, OSs
- http://mathema.tician.de/ software/pyopencl



OpenCL





Introducing... PyOpenCL

Same flavor, different recipe:

```
ctx = cl. create\_context\_from\_type (cl. device\_type .ALL)
queue = cl.CommandQueue(ctx)
a = numpy.random.rand(50000).astype(numpy.float32)
a_buf = cl. Buffer(ctx, cl.mem_flags.COPY_HOST_PTR, hostbuf=a)
prg = cl. Program(ctx, """
    __kernel void twice( __global float *x)
    \{ x [ get\_global\_id (0)] *= 2; \}""" \}. build ()
prg.twice(queue, a.shape, a_buf)
twice_a = numpy.empty_like(a)
cl . enqueue_read_buffer (queue, a_buf, twice_a). wait()
```

Automating GPU Programming

GPU programming can be time-consuming, unintuitive and error-prone.

- Obvious idea: Let the computer do it.
- One way: Smart compilers





Automating GPU Programming

GPU programming can be time-consuming, unintuitive and error-prone.

- Obvious idea: Let the computer do it.
- One way: Smart compilers
 - GPU programming requires complex tradeoffs
 - Tradeoffs require heuristics
 - Heuristics are fragile





Automating GPU Programming

GPU programming can be time-consuming, unintuitive and error-prone.

- Obvious idea: Let the computer do it.
- One way: Smart compilers
 - GPU programming requires complex tradeoffs
 - Tradeoffs require heuristics
 - Heuristics are fragile
- Another way: Dumb enumeration
 - Enumerate loop slicings
 - Enumerate prefetch options
 - Choose by running resulting code on actual hardware



Loo.py Example

Empirical GPU loop optimization:

```
a, b, c, i, j, k = [var(s) for s in "abcijk"]
n = 500
k = make_loop_kernel([
    LoopDimension("i", n),
    LoopDimension("j", n),
    LoopDimension("k", n),
    ], [
    (c[i+n*j], a[i+n*k]*b[k+n*j])
])

gen_kwargs = {
    "min_threads": 128,
    "min_blocks": 32,
}
```

→ Ideal case: Finds 160 GF/s kernel without human intervention.







Loo.py Status

Limited scope:

- Require input/output separation
- Kernels must be expressible using "loopy" model (i.e. indices decompose into "output" and "reduction")
- Enough for DG, LA, FD, ...







Loo.py Status

Limited scope:

- Require input/output separation
- Kernels must be expressible using "loopy" model (i.e. indices decompose into "output" and "reduction")
- Enough for DG, LA, FD, . . .
- Kernel compilation limits trial rate
- Non-Goal: Peak performance
- Good results currently for dense linear algebra and (some) DG subkernels







■ Fun time to be in computational science



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- Use Python and PyCUDA to have even more fun :-)
 - With no compromise in performance





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 - Enable Metaprogramming
- Further work in GPU-DG:
 - Other equations (Euler, Navier-Stokes)
 - Curvilinear Elements
 - Local Time Stepping





Where to from here?

More at...

→ http://mathema.tician.de/

CUDA-DG

AK, T. Warburton, J. Bridge, J.S. Hesthaven, "Nodal Discontinuous Galerkin Methods on Graphics Processors", J. Comp. Phys., 2009.

GPU RTCG

AK, N. Pinto et al. *PyCUDA: GPU Run-Time Code Generation for High-Performance Computing*, in prep.



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Thank you for your attention!

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