

TOF	d-TOF	<p>Pulsed modulation</p> <p>time of flight를 direct로 계산하는 방법</p> <p>high energy의 pulse 신호를 쏘주기 때문에 background illumination의 영향을 줄일 수 있음</p> <p>상대적으로 Optical power의 평균값은 작기 때문에 eye safety에 중요한 요소가 될 수 있음</p>
	i-TOF	<p>Continuous wave (CW) modulation</p>

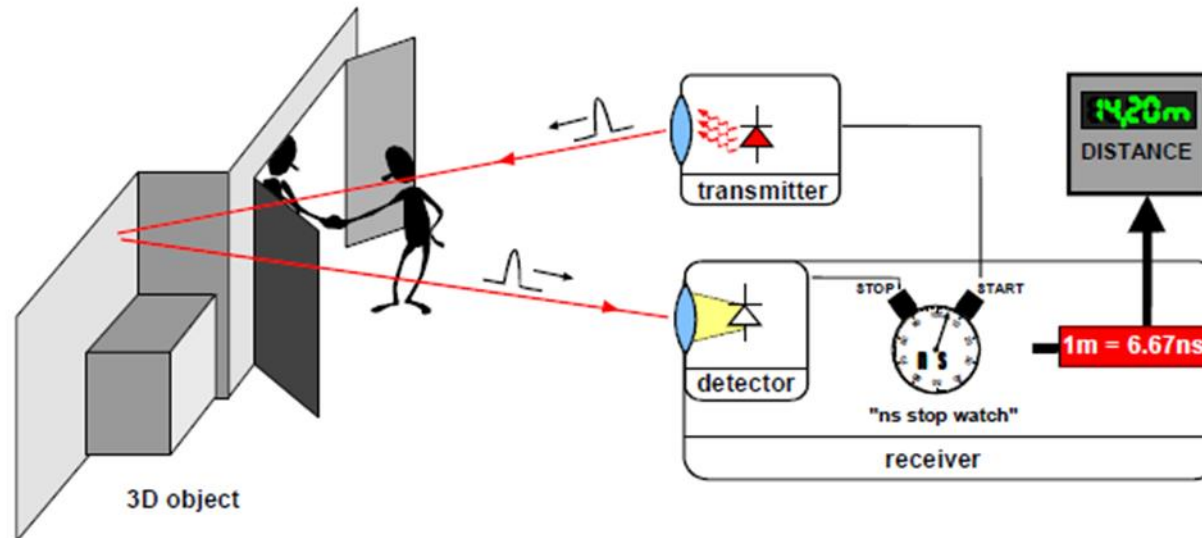


Figure 1.3 Basic principle of an (optical) TOF ranging system.

◆ Depth estimation

$$d = \frac{1}{2}ct$$

d: distance
c: speed of light
t: time of flight



time of flight를 직접적으로
 구하기 어려움
 → **phase shift**를 이용하여
 t를 계산하는 것이 목표.

◆ Relationship between phase shift and time of flight

$$\phi = 2\pi ft$$

ϕ : phase shift
f: modulation frequency
t: time of flight

$$d = \frac{1}{2f} c \frac{\phi}{2\pi}$$

```
UR=calib.speed_of_light./(2*Fmod);  

% rescale from rad to m and store in Distance  

Distance(iFmod,ifiber) = Phase * UR(iFmod)/(2*pi);
```

$$d_{amb} = \frac{1}{2f} c$$

ambiguity distance:
 해당 modulation으로 측정할 수 있는 최대 거리

80MHz: 1.8657m

60MHz: 2.4876m

◆ Cross correlation Function

- Emitted signal

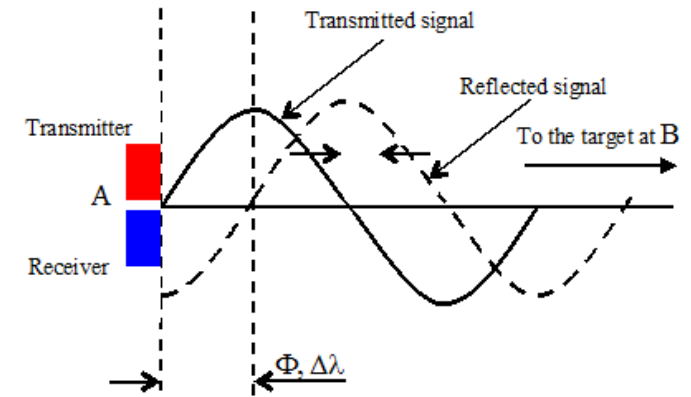
$$s(t) = \cos(2\pi ft)$$

- Received signal

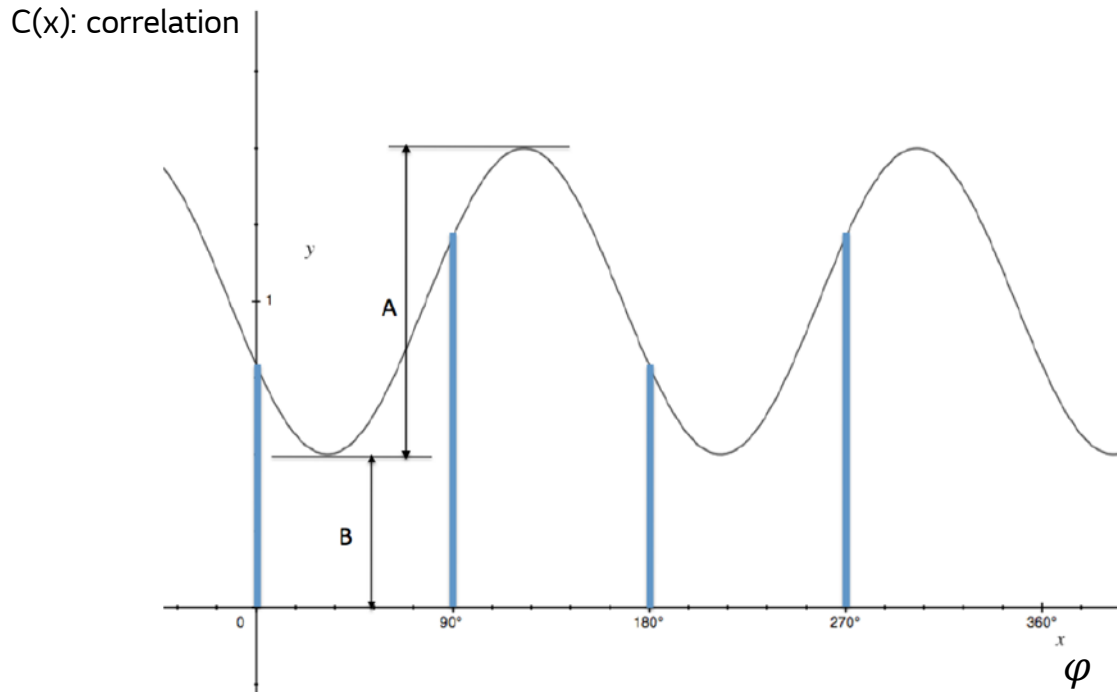
$$r(t) = A\cos(2\pi f(t - \tau)) + B$$

- Cross-correlation between emitted and received signals

$$\begin{aligned} C(x) &= \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} r(t)s(t+x)dt \\ &= \frac{A}{2} \cos(2\pi f\tau + 2\pi fx) + B \\ &= \frac{A}{2} \cos(\phi + \varphi) + B \end{aligned}$$



◆ 4-Bucket Method



$$C(x_0) = \frac{A}{2} \cos(\phi + 0) + B = \frac{A}{2} \cos(\phi) + B$$

$$C(x_1) = \frac{A}{2} \cos\left(\phi + \frac{\pi}{2}\right) + B = -\frac{A}{2} \sin(\phi) + B$$

$$C(x_2) = \frac{A}{2} \cos(\phi + \pi) + B = -\frac{A}{2} \cos(\phi) + B$$

$$C(x_3) = \frac{A}{2} \cos\left(\phi + \frac{3\pi}{2}\right) + B = \frac{A}{2} \sin(\phi) + B$$



$$\phi = 2\pi f\tau = \arctan\left(\frac{C(x_3) - C(x_1)}{C(x_0) - C(x_2)}\right)$$

$$A = \frac{1}{2} \sqrt{(C(x_3) - C(x_1))^2 + (C(x_0) - C(x_2))^2}$$

$$B = \frac{1}{4} (C(x_0) + C(x_1) + C(x_2) + C(x_3))$$

◆ PMD Raw data for calibration

[super frame]



Sequence	0	1				2				3	4
Raw image	Gray Scale	0°	90°	180°	270°	0°	90°	180°	270°	Gray Scale	Gray Scale
Modulation Frequency [MHz]	60.24	80.32				60.24					
Duty Cycle (Illumination)	0% (OFF)	25%				25%				0% (OFF)	25%

◆ RAW data → Phase

modulation 별 각각의 phase 계산

```
function [Phase, Amplitude] = ProcessNPhase (Raw, Phaseshift)
    N_Raw=numel(Raw);
    for i=1:1:N_Raw
        if ~isfloat(Raw{i})
            Raw{i}=double(Raw{i});
        end
    end

    % initialize frames for real and imaginary parts
    Re=zeros(size(Raw{1}));
    Im=Re;

    % compile real and imaginary parts
    for i=1:1:N_Raw
        Re = Re - 2/N_Raw*Raw{i}*cosd(Phaseshift(i));
        Im = Im + 2/N_Raw*Raw{i}*sind(Phaseshift(i));
    end

    % calculate phase and amplitude values
    Phase = pi + atan2(Im, Re);
    Amplitude = sqrt(Im.^2 + Re.^2);
end
```

$$Re = 1/2 * (Raw(180^\circ) - Raw(0^\circ))$$

$$Im = 1/2 * (Raw(90^\circ) - Raw(270^\circ))$$

$$\phi = \pi + \arctan\left(\frac{Raw(x_1) - Raw(x_3)}{Raw(x_2) - Raw(x_0)}\right)$$

$$A = \frac{1}{2} \sqrt{(Raw(x_1) - Raw(x_3))^2 + (Raw(x_2) - Raw(x_0))^2}$$

tangent가 주기가 pi라 값은 같은 듯 한데 왜 pi를 더할까?

arctan2의 범위 (-pi, +pi) → (0, 2pi)

◆ Phase → Distance

```

for ifiber = 1:N_fiber
    if ~obj.FB.valid_fibers(ifiber)
        % skip invalid fibers
        continue;
    end

    % create a logical mask for this fiber (for FPPN values)
    Mask=false(obj.FB.FRDData.SensorROI([4,3]));
    Mask(obj.FB.FRDData.FPixel{1,ifiber},obj.FB.FRDData.FPixel{2,ifiber})=true;

    % iterate over all modulation frequencies
    for iFmod=1:N_Fmod modulation 별 각각의 distance 계산
        BPhase=obj.FB.FRDData.Phase{iFmod,ifiber};

        % apply wiggling compensation
        BPhase = BPhase + harmonics.apply(obj.PhaseWiggling{iFmod}, BPhase);

        % apply temperature drift compensation
        Delta_Temp = obj.FB.FRDData.illuminationTemperature - obj.TempCompensation{iFmod}(1);
        Delta_Distance = obj.TempCompensation{iFmod}(2) * Delta_Temp ...
            + obj.TempCompensation{iFmod}(3) * Delta_Temp.^2 ...
            + obj.TempCompensation{iFmod}(4) * Delta_Temp.^3; % in m
        Delta_Phase = Delta_Distance*(2*pi)/UR(iFmod); % in rad
        BPhase = BPhase - Delta_Phase; % in rad

        % apply FPPN
        BPhase = BPhase + obj.FPPN{iFmod}(Mask)*(2*pi)/UR(iFmod);

        % average over pixels in blob;
        Phase = mean(fix_unambiguous_range(BPhase));

        % rescale from rad to m and store in Distance
        Distance(iFmod,ifiber) = Phase * UR(iFmod)/(2*pi);
    end
end

```

Distance 계산

- 1) phase wiggling compensation
- 2) temperature drift compensation
- 3) FPPN compensation
- 4) rad to m

$$d = \frac{1}{2f} c \frac{\phi}{2\pi}$$

FiberLengths = CALC_2Freq(Distance(1,:),Distance(2,:),Fmod); 두 modulation에서 나온 거리를 이용하여 최종 거리 계산

◆ CALC_2Freq

```
function D=CALC_2Freq(d1,d2,Fmod)
    flong=lcm(Fmod(1),Fmod(2));
    UR=flong./[Fmod(1),Fmod(2)];
    [~,u,~]=gcd(UR(1),UR(2));
    fak=flong*2/calib.speed_of_light;

    d_diff=fak*(d2-d1);
    f=round(d_diff);
    D=f*u*UR(1)+fak*d1+(d_diff-f)/2; %주기 d1기준 위상차
    D=mod(D,prod(UR))/fak;
end
```

80MHz와 60MHz의 최소공배수 = 240960000 = 240MHz

UR = [3, 4]

u = -1 / gcd = 최대 공약수 - [g, c, d] = GCD[A, B] → g = A*c+B*d

$$d = \frac{1}{2f} c \frac{\phi}{2\pi}$$

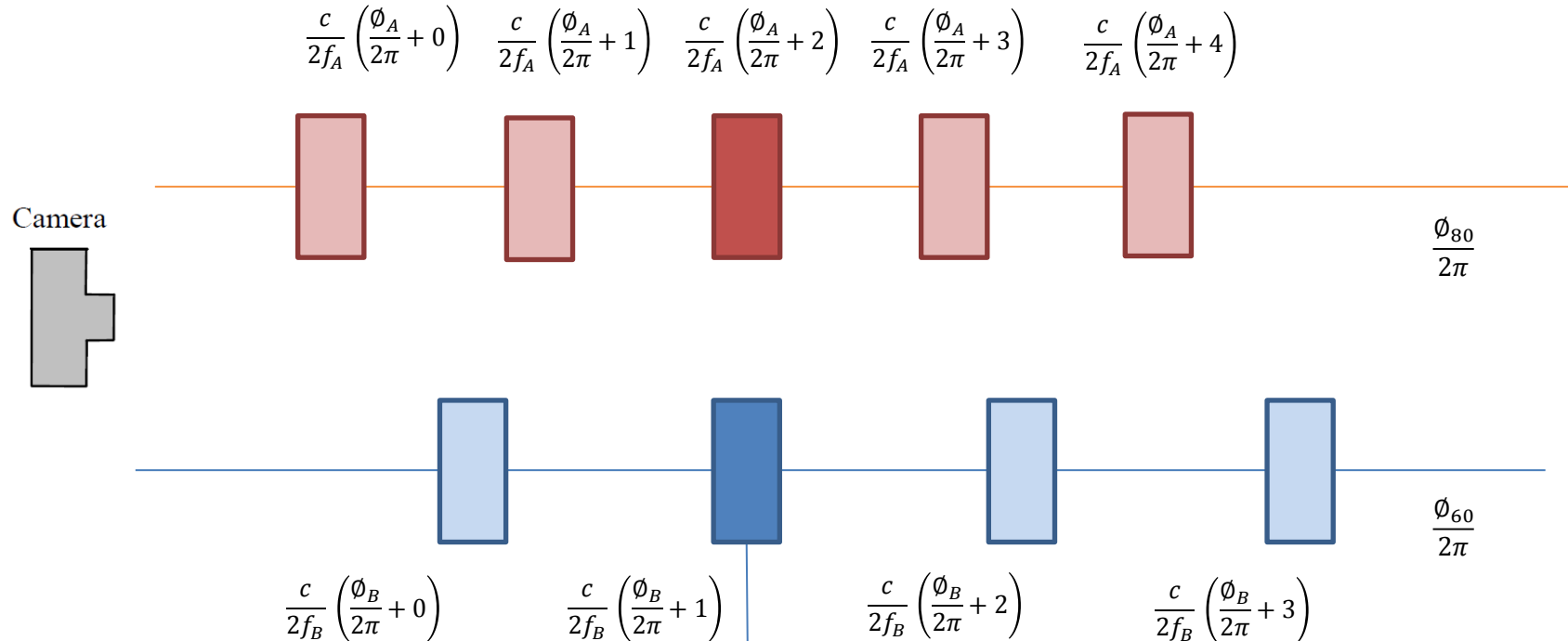
$$\begin{aligned} d_{diff} &= \frac{2f_{240}}{c} \frac{c}{2f_{60}} \frac{\phi_{60}}{2\pi} - \frac{2f_{240}}{c} \frac{c}{2f_{80}} \frac{\phi_{80}}{2\pi} \\ &= 4 \frac{\phi_{60}}{2\pi} - 3 \frac{\phi_{80}}{2\pi} \end{aligned}$$

$$d = \frac{c}{2f_{60}} \frac{\phi_{60}}{2\pi} = \frac{c}{2f_{240}} \frac{4\phi_{60}}{2\pi}$$

$$d = \frac{c}{2f_{80}} \frac{\phi_{80}}{2\pi} = \frac{c}{2f_{240}} \frac{3\phi_{80}}{2\pi}$$

◆ CALC_2Freq

기본 concept: 두 주파수(f_A, f_B)에서 나올 수 있는 가능 거리가 동일한 거리 찾기

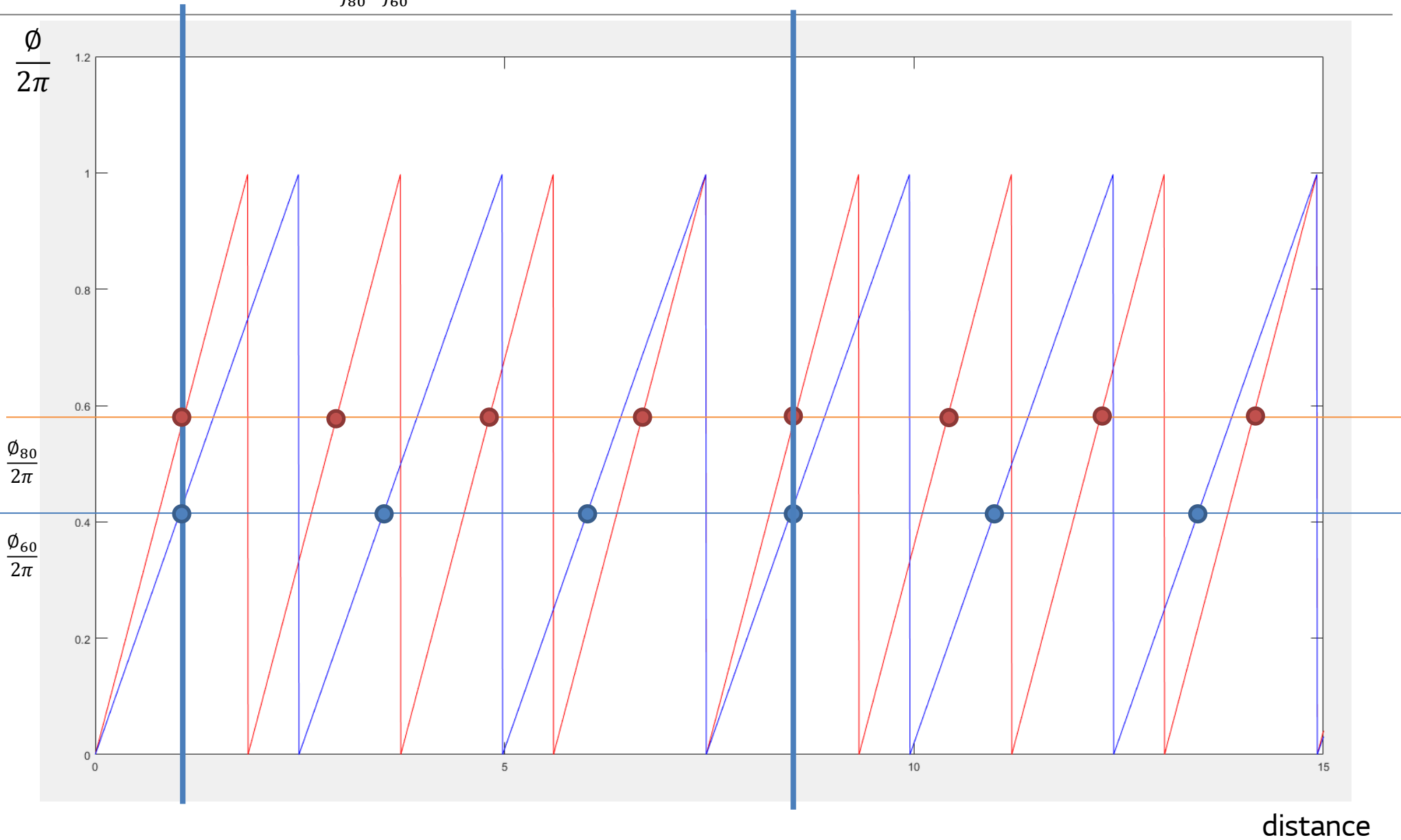


목표: 거리가 같게 나오는 n_A, n_B 구하기

$$d = \frac{c}{2f_A} \left(\frac{\phi_A}{2\pi} + n_A \right) = \frac{c}{2f_B} \left(\frac{\phi_B}{2\pi} + n_B \right)$$

$f_{80}: f_{60} \rightarrow \frac{1}{f_{80}}: \frac{1}{f_{60}} \rightarrow 4:3 \rightarrow \text{둘이 만나는 주기 12}$

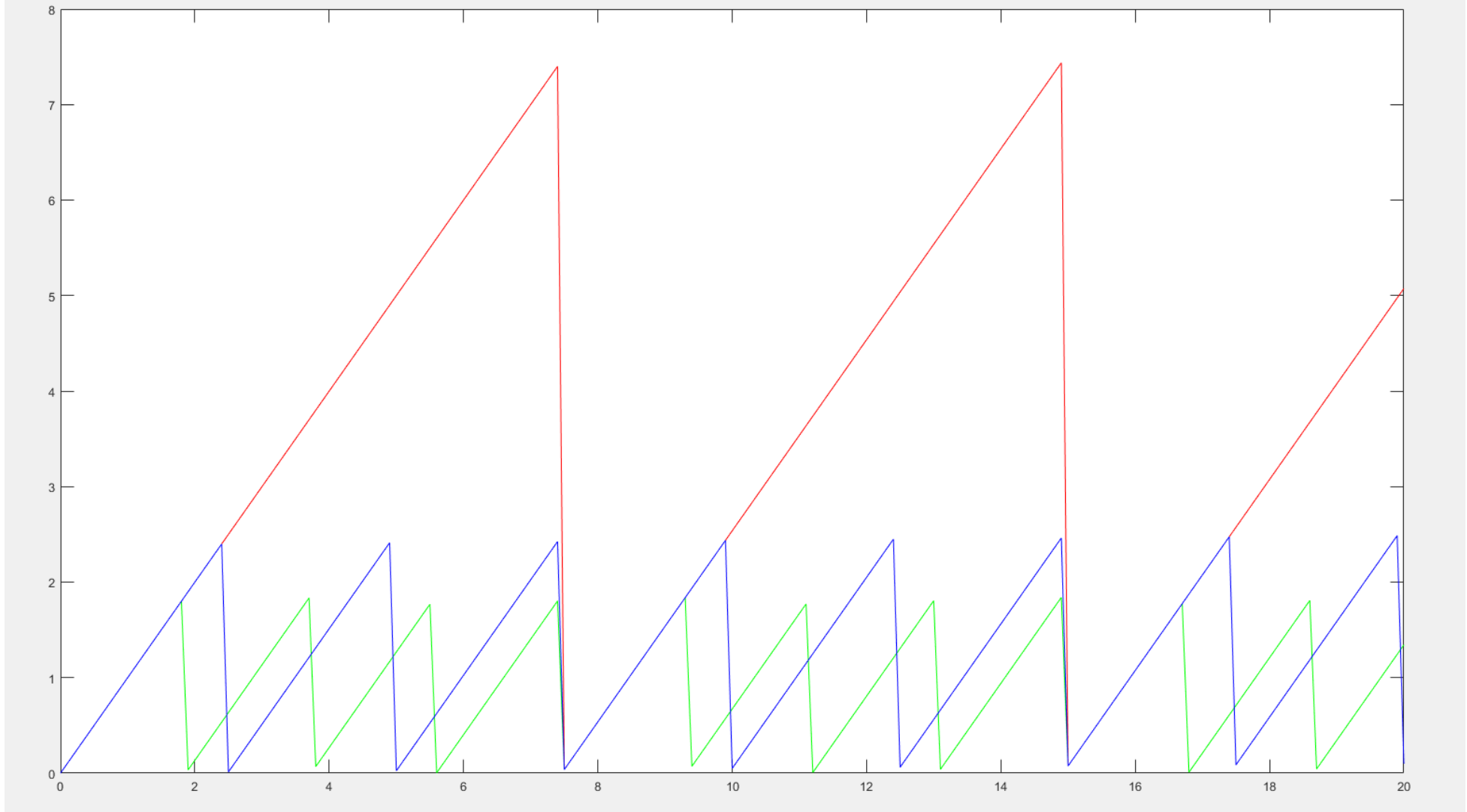
10/15



distance

---: distance 80MHz+60MHz
---: distance 80MHz
---: distance 60MHz

calculated distance



real distance

◆ CALC_2Freq

$$d = \frac{c}{2f_A} \left(\frac{\phi_A}{2\pi} + n_A \right) = \frac{c}{2f_B} \left(\frac{\phi_B}{2\pi} + n_B \right)$$

목표: 거리가 같게 나오는 n_A, n_B 구하기

$$\rightarrow \min \left| \frac{c}{2f_A} \left(\frac{\phi_A}{2\pi} + n_A \right) - \frac{c}{2f_B} \left(\frac{\phi_B}{2\pi} + n_B \right) \right|$$

거리가 같다 = 거리차 최소

$$\rightarrow \min \left| \frac{cM_B}{2f_A M_B} \left(\frac{\phi_A}{2\pi} + n_A \right) - \frac{cM_A}{2f_B M_A} \left(\frac{\phi_B}{2\pi} + n_B \right) \right|$$

최소 공배수

$$\rightarrow \min \left| M_B \left(\frac{\phi_A}{2\pi} + n_A \right) - M_A \left(\frac{\phi_B}{2\pi} + n_B \right) \right|$$

공통부분 없애기

$$\rightarrow \min |M_B(p_A + n_A) - M_A(p_B + n_B)|$$

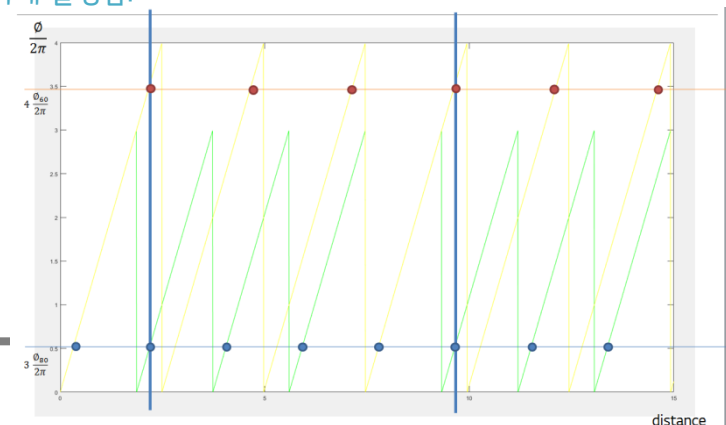
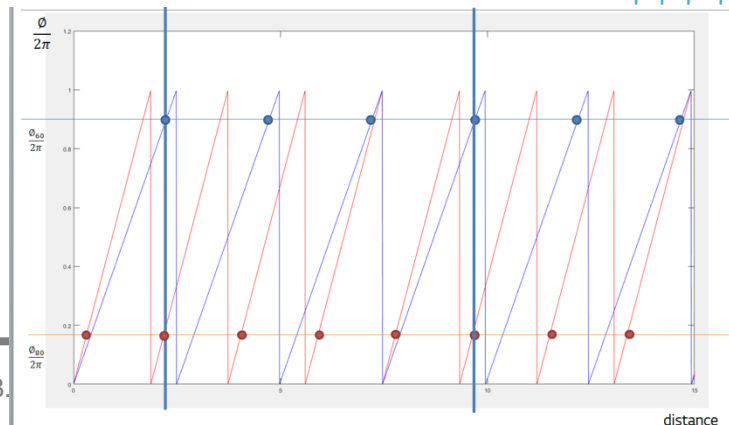
80:60 → 4:3

$$M_A = \frac{f_A}{\gcd(f_A, f_B)}, M_B = \frac{f_B}{\gcd(f_A, f_B)}$$

$$p_A = \frac{\phi_A}{2\pi}, p_B = \frac{\phi_B}{2\pi}$$

최소공배수로 phase를 맞추면
거리의 차가 일정하게 발생함.

$$d = \frac{c}{2f_{60}} \frac{\phi_{60}}{2\pi} = \frac{c}{2f_{240}} \frac{4\phi_{60}}{2\pi} \quad d = \frac{c}{2f_{80}} \frac{\phi_{80}}{2\pi} = \frac{c}{2f_{240}} \frac{3\phi_{80}}{2\pi}$$



◆ CALC_2Freq

$$\min |M_B(p_A + n_A) - M_A(p_B + n_B)|$$

solution1)

최소가 되는 n_A, n_B 조합을 경우의수로 찾아보는 방법

One naive approach is to evaluate all possible combinations of n_A and n_B and select the options that give the difference closest to zero. With values established for n_A and n_B , distance is computed by

$$d = \frac{c}{2} \left[\frac{w(n_A + p_A)}{f_A} + \frac{(1 - w)(n_B + p_B)}{f_B} \right] \quad (8)$$

where w is a weighting factor between 0 and 1 and is chosen to minimize the variance in the output distance estimate.

◆ CALC_2Freq

$$\min |M_B(p_A + n_A) - M_A(p_B + n_B)|$$

solution2)

residue to binary converter을 이용한 방법

step1. Chinese remainder theorem을 이용한 n_B 계산

$$e = p_A M_B - p_B M_A = d_diff$$

$$n_B = \text{mod} [k_0 \text{round}(e), M_B] \quad (9)$$

마이너스 위상차 보상

step2. scale 전 거리 계산

$$\begin{aligned} X &= w M_B(n_A + p_A) + (1 - w) M_A(n_B + p_B) \\ &= M_A n_B + M_A p_B + w(e - \text{round}(e)). \end{aligned} \quad (10)$$

$$\text{UR}(1) * f * u \quad fak * d1 \quad 1/2 * (d_diff - f)$$

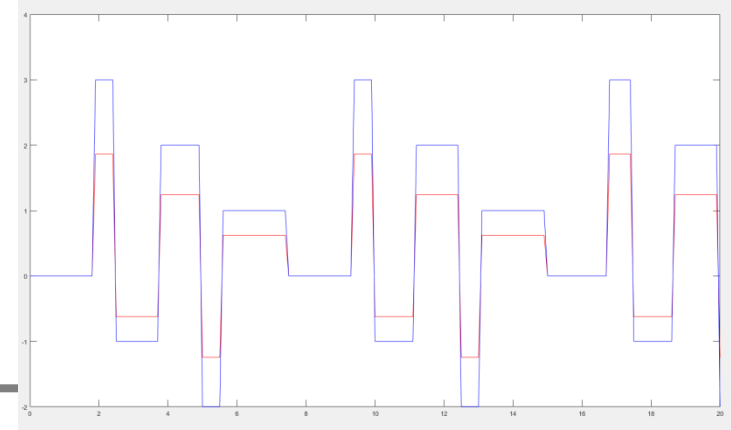
step3. scaling

$$d = d_E \cdot \frac{X}{M_A M_B} \cdot D / fak$$

```
function D=CALC_2Freq(d1,d2,Fmod)
flong=lcm(Fmod(1),Fmod(2));
UR=flong./[Fmod(1),Fmod(2)];
[~,u,~]=gcd(UR(1),UR(2));
fak=flong*2/calib.speed_of_light;

d_diff=fak*(d2-d1);
f=round(d_diff);
D=f*u*UR(1)+fak*d1+(d_diff-f)/2; %주기 d1기준 위상차
D=mod(D,prod(UR))/fak;
end
```

마이너스 위상차 보상



◆ CALC_2Freq

$$\min |M_B(p_A + n_A) - M_A(p_B + n_B)|$$

solution2)

residue to binary converter을 이용한 방법

step1. Chinese remainder theorem을 이용한 n_B 계산

$$e = p_A M_B - p_B M_A = d_{\text{diff}} = 3 \frac{\phi_{80}}{2\pi} - 4 \frac{\phi_{60}}{2\pi}$$

$$n_B = \text{mod} [k_0 \text{round}(e), M_B] \quad (9)$$

0, 1, 2 → 반복되는 주파수를 제거하고서 몇 번째 주기인지 찾는 부분

step2. scale 전 거리 계산

$$\begin{aligned} X &= w M_B (n_A + p_A) + (1 - w) M_A (n_B + p_B) \\ &= M_A n_B + M_A p_B + w (e - \text{round}(e)). \end{aligned} \quad (10)$$

step3. scaling

$$d = d_E \cdot \frac{X}{M_A M_B} \cdot \frac{D}{fak}$$

$$d = \frac{c}{2f_B} \left(\frac{\phi_B}{2\pi} + n_B \right) = \frac{c}{2f_B M_A} \left(\frac{\phi_B M_A}{2\pi} + n_B M_A \right)$$

```
function D=CALC_2Freq(d1,d2,Fmod)
    flong=lcm(Fmod(1),Fmod(2));
    UR=flong./[Fmod(1),Fmod(2)];
    [~,u,~]=gcd(UR(1),UR(2));
    fak=flong*2/calib.speed_of_light;

    d_diff=fak*(d2-d1);
    f=round(d_diff);
    D=f*u*UR(1)+fak*d1+(d_diff-f)/2; %주기 d1기준 위상차
    D=mod(D,prod(UR))/fak;
end
```

d_{diff} : 0→3→-1→2→-2→1→0
 $\text{mod}(d_{\text{diff}}, 4)$: 0→3→3→2→2→1→0
 k_0*d_{diff} : 0→-3→1→-2→2→-1→0
 $\text{mod}(k_0 d_{\text{diff}}, 4)$: 0→1→1→2→2→3→0

마이너스 위상차 보상

