

Homework 1

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"Due: Monday, February 3, 2025 at 11:59 pm on Canvas. Please assemble a single PDF file for submission that includes your Matlab/Simulink code/diagrams, plots, and explanations of your work and the results. Label sections to correspond with those in the assignment. Don't make it difficult to locate the text/code/plots for each section."

1.

"[10pts] Find the parameters R_M , L_M , K_τ , J_M , and K_B from the motor specification sheet, noting units. Also, find the total gear ratio N from the motor shaft to the load shaft, and estimate the load shaft moment of inertia J_L . Use these to quantify the parameters in the transfer function relating V_P to Θ_L . Also, estimate the potentiometer scale factor K_S from the data file posted on Canvas."

<div><div></div>Stock program</div>	Part Numbers												
<div><div></div>Standard program</div>													
<div><div></div>Special program (on request)</div>													
with terminals			I10181	I10182	I10183	I10184	I10185	I10186	I10187	I10188	I10189	I10190	I10191
with cables			353078	353079	353080	353081	329757	353082	332818	353083	353084	353085	353086
Motor Data													
Values at nominal voltage													
1 Nominal voltage	V	4.5	6	9	12	15	18	24	30	36	42	48	
2 No load speed	rpm	7320	8670	6160	6780	6720	6690	5670	6090	6780	6570	6050	
3 No load current	mA	78.9	77.7	30.2	26.3	20.7	171	9.97	8.9	8.76	7.15	5.5	
4 Nominal speed	rpm	6900	8130	5000	5340	5060	5010	3940	4370	5060	4820	4280	
5 Nominal torque (max. continuous torque)	mNm	4.46	5.02	11.3	13.7	15.8	15.6	15.3	15.3	15.2	15	15	
6 Nominal current (max. continuous current)	A	0.84	0.84	0.84	0.84	0.766	0.627	0.391	0.336	0.31	0.254	0.204	
7 Stall torque	mNm	673	73.5	58.8	63.5	63.6	62.1	50.3	54.2	60.2	56.4	51.4	
8 Stall current	A	11.5	11.2	4.25	3.78	3.01	2.43	1.25	1.16	1.2	0.93	0.683	
9 Max. efficiency	%	84	84	84	84	84	84	83	84	84	84	83	
Characteristics													
10 Terminal resistance	Ω	0.39	0.536	0.22	3.17	4.99	7.41	19.2	25.8	30.1	45.1	70.2	
11 Terminal inductance	mH	0.04	0.051	0.227	0.333	0.529	0.77	1.9	2.58	2.99	4.34	6.68	
12 Torque constant	mNm/A	5.84	6.57	13.9	16.8	21.2	25.5	40.1	46.7	50.3	60.6	75.2	
13 Speed constant	rpm/V	1640	1450	689	569	451	374	238	205	190	158	127	
14 Speed /torque gradient	rpm/mNm	109	119	105	108	106	108	114	113	114	117	119	
15 Mechanical time constant	ms	16.5	16	15	14.9	14.8	14.8	14.9	14.9	14.9	15	15	
16 Rotor inertia	gcm ²	14.4	12.9	13.6	13.2	13.3	13.1	12.5	12.6	12.5	12.2	12.1	

I took the parameters from the motor specification table above using part number 110187.

$$R_M = 19.2 \, \Omega$$

$$L_M = 1.9\text{mH} = 0.0019 \text{ H}$$

$$K_{\tau} = 40.1 \text{mNm/A} = 0.0401 \text{ Nm/A}$$

$$J_M = 12.5 \text{gcm}^2 = 0.00000125 \text{ kgm}^2$$

$$K_B = 238\text{rpm/V} = 0.04 \text{ Vs/rad}$$

$$N = 3.3$$

$$J_L = 0.018522 \text{ kgm}^2$$

$K_S = 0.8$

I estimated J_L , using standard inertia formulas for a rod rotating about one end and a satellite (for the weight) and added them together.

Equation for rod: $J_{\text{arm}} = \frac{1}{3}m_{\text{arm}}L^2$

Equation for weight: $J_{\text{weight}} = m_{\text{weight}} L^2$

I got the mass of the arm and weight using their measurements and the average density for aluminum and brass.

- Arm Dimensions: $L = 30$ cm, $h = 0.7$ cm, $w = 1.1$ cm

- Volume:

$$V_{\text{arm}} = L \times h \times w = 30 \times 0.7 \times 1.1 = 23.1 \text{ cm}^3 \quad (1)$$

- Density of aluminum: $\rho_{\text{Al}} \approx 2.7 \text{ g/cm}^3$

- Mass of the arm:

$$m_{\text{arm}} = V_{\text{arm}} \times \rho_{\text{Al}} = 23.1 \times 2.7 = 62.37 \text{ g} = 0.0624 \text{ kg} \quad (2)$$

- Weight Dimensions: $3.2 \times 2.0 \times 3.4$ cm

- Volume:

$$V_{\text{brass}} = 3.2 \times 2.0 \times 3.4 = 21.76 \text{ cm}^3 \quad (3)$$

- Density of brass: $\rho_{\text{brass}} \approx 8.5 \text{ g/cm}^3$

- Mass of the brass weight:

$$m_{\text{brass}} = V_{\text{brass}} \times \rho_{\text{brass}} = 21.76 \times 8.5 = 184.96 \text{ g} = 0.185 \text{ kg} \quad (4)$$

Then I used those numbers (including length of arm for L) to calculate the moments of inertia and combine them.

$$J_{\text{arm}} = \frac{1}{3} m_{\text{arm}} L^2 \quad (5)$$

$$J_{\text{arm}} = \frac{1}{3} (0.0624) (0.30)^2 = 0.001872 \text{ kgm}^2 \quad (6)$$

$$J_{\text{weight}} = m_{\text{weight}} L^2 \quad (7)$$

$$J_{\text{weight}} = (0.185) (0.30)^2 = 0.01665 \text{ kgm}^2 \quad (8)$$

$$J_L = J_{\text{arm}} + J_{\text{brass}} \quad (9)$$

$$J_L = 0.00187 + 0.01645 = 0.018522 \text{ kgm}^2 \quad (10)$$