



I estimated  $J_L$ , using standard inertia formulas for a rod rotating about one end and a satellite (for the weight) and added them together.

Equation for rod:  $J_{\text{arm}} = \frac{1}{3}m_{\text{arm}}L^2$

Equation for weight:  $J_{\text{weight}} = m_{\text{weight}}L^2$

I got the mass of the arm and weight using their measurements and the average density for aluminum and brass.

- Arm Dimensions:  $L = 30$  cm,  $h = 0.7$  cm,  $w = 1.1$  cm

- Volume:

$$V_{\text{arm}} = L \times h \times w = 30 \times 0.7 \times 1.1 = 23.1 \text{ cm}^3 \quad (1)$$

- Density of aluminum:  $\rho_{\text{Al}} \approx 2.7 \text{ g/cm}^3$

- Mass of the arm:

$$m_{\text{arm}} = V_{\text{arm}} \times \rho_{\text{Al}} = 23.1 \times 2.7 = 62.37 \text{ g} = 0.0624 \text{ kg} \quad (2)$$

- Weight Dimensions:  $3.2 \times 2.0 \times 3.4$  cm

- Volume:

$$V_{\text{brass}} = 3.2 \times 2.0 \times 3.4 = 21.76 \text{ cm}^3 \quad (3)$$

- Density of brass:  $\rho_{\text{brass}} \approx 8.5 \text{ g/cm}^3$

- Mass of the brass weight:

$$m_{\text{brass}} = V_{\text{brass}} \times \rho_{\text{brass}} = 21.76 \times 8.5 = 184.96 \text{ g} = 0.185 \text{ kg} \quad (4)$$

Then I used those numbers (including length of arm for L) to calculate the moments of inertia and combine them.

$$J_{\text{arm}} = \frac{1}{3}m_{\text{arm}}L^2 \quad (5)$$

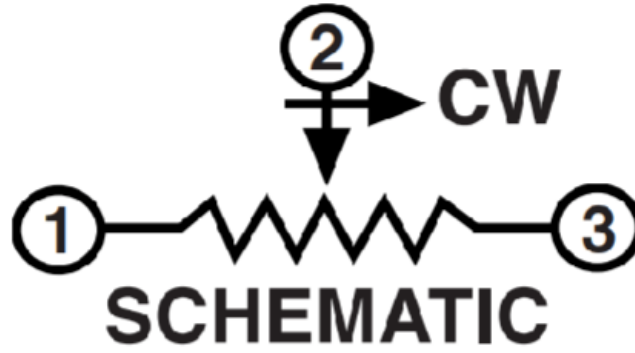
$$J_{\text{arm}} = \frac{1}{3}(0.0624)(0.30)^2 = 0.001872 \text{ kgm}^2 \quad (6)$$

$$J_{\text{weight}} = m_{\text{weight}}L^2 \quad (7)$$

$$J_{\text{weight}} = (0.185)(0.30)^2 = 0.01665 \text{ kgm}^2 \quad (8)$$

$$J_L = J_{\text{arm}} + J_{\text{brass}} \quad (9)$$

$$J_L = 0.00187 + 0.01645 = 0.01832 \text{ kgm}^2 \quad (10)$$



Measurement of port 2, with respect to port 1 (GND)

-90 Deg shows 1.25 V

0 Deg shows 2.488 V

+90 Deg shows 3.76 V

To derive  $K_S$  I used the readings/schematic above. I took the total voltage difference over the total angle difference (converted to radians).

$$K_S = (3.76V - 1.25V) / \left( \frac{\pi}{2} rad + \frac{\pi}{2} rad \right) \quad (11)$$

$$K_S = 0.8 \text{ V/rad} \quad (12)$$