CSCI 210: Computer Architecture Lecture 17: Combinational Logic

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Slides from Cynthia Taylor

Announcements

Problem Set 5 due Friday!

Lab 4 due Sunday

Join circuitverse.org for Lab 5

Digital Logic

Previously: Established rules of Boolean algebra and digital logic

Today: Building stuff!

Sum of Products

- Developed from Truth Table form
 - Each product term contains each input exactly once, complemented or not.
 - Need to OR together set of AND terms to satisfy table
 - One product for each 1 in F column

Х	Υ	F
0	0	0
0	1	1
1	0	1
1	1	0

Programmable Logic Array

 Simple way to create a logical circuit from a truth table, using sum of products

Either programmed during manufacture, or can be reprogrammed

Used in CPUs to generate "control signals"

Programmable Logic Array

- Set of inputs and their complements
- Array of AND gates
 - Form set of product terms
- Array of OR gates
 - Logical sum of product terms
- Multiple outputs

Creating a PLA

- Prepare the truth table
- Write the Boolean expression in sum of products form.
- Decide the input connection of the AND matrix for generating the required product term.
- Then decide the input connections of OR matrix to generate the sum terms.
- Program the PLA.

Size

 Only truth table entries that have a True (1) output are represented

 Each different product term will have only one entry in the PLA, even if the product term is used in multiple outputs

Multiple outputs

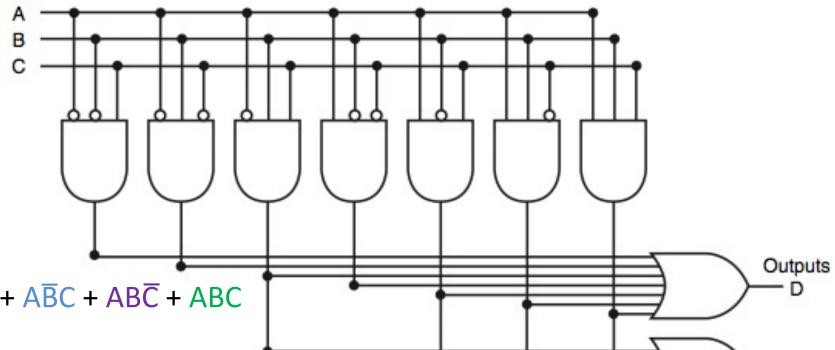
Inputs			Outputs		
A	В	C	D	E	F
0	0	0	0	0	0
0	0	1	1	0	0
0	1	0	1	0	0
0	1	1	1	1	0
1	0	0	1	0	0
1	0	1	1	1	0
1	1	0	1	1	0
1	1	1	1	0	1

Output functions: D(A, B, C), E(A, B, C), F(A, B, C)

Inputs			Outputs		
A	В	C	D	E	F
0	0	0	0	0	0
0	0	1	1	0	0
0	1	0	1	0	0
0	1	1	1	1	0
1	0	0	1	0	0
1	0	1	1	1	0
1	1	0	1	1	0
1	1	1	1	0	1

	Sum of Products for output D
Α	$\overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + \overline{A}BC + A\overline{B}\overline{C} + A\overline{B}C + AB\overline{C} + ABC$
В	$\overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC} + \overline{ABC}$
С	$(A+B+\overline{C})(A+\overline{B}+C)(A+\overline{B}+\overline{C})(\overline{A}+B+C)(\overline{A}+B+\overline{C})(\overline{A}+\overline{B}+C)(\overline{A}+\overline{B}+\overline{C})$
D	$\overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + \overline{A}BC + A\overline{B}\overline{C} + A\overline{B}C + AB\overline{C} + ABC$





Ε

 $D = \overline{A}\overline{B}C + \overline{A}B\overline{C} + \overline{A}\overline{B}C + A\overline{B}\overline{C} + A\overline{B}C + AB\overline{C} + ABC$

 $E = \overline{A}BC + A\overline{B}C + AB\overline{C}$

F = ABC

Inputs			Outputs		
A	В	C	D	E	F
0	0	0	0	0	0
0	0	1	1	0	0
0	1	0	1	0	0
0	1	1	1	1	0
1	0	0	1	0	0
1	0	1	1	1	0
1	1	0	1	1	0
1	1	1	1	0	1

Programmable PLAs

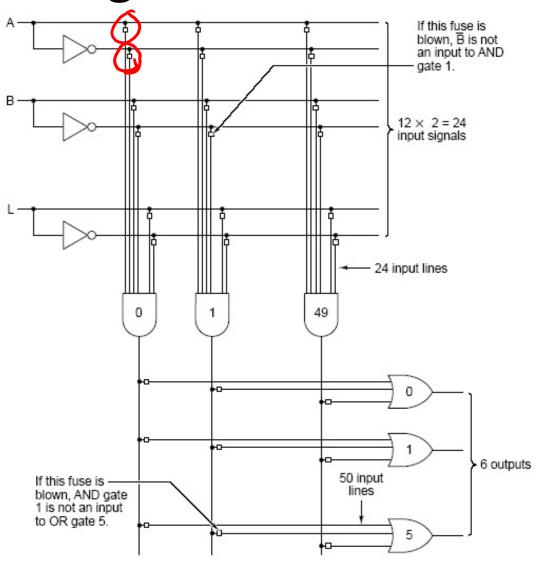


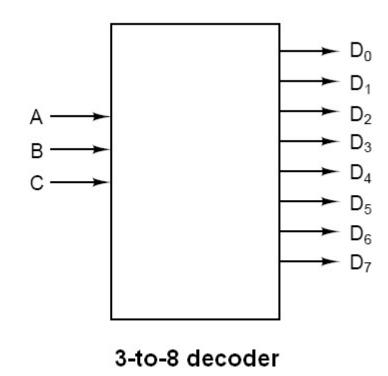
Figure 3-15. A 12-input, 6-output programmable logic array.

Decoder

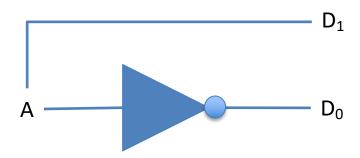
Interprets n inputs (e.g., A, B,
C) as an n-bit binary number

 Sets output D_n to 1, all other outputs to 0

The output is "one hot"

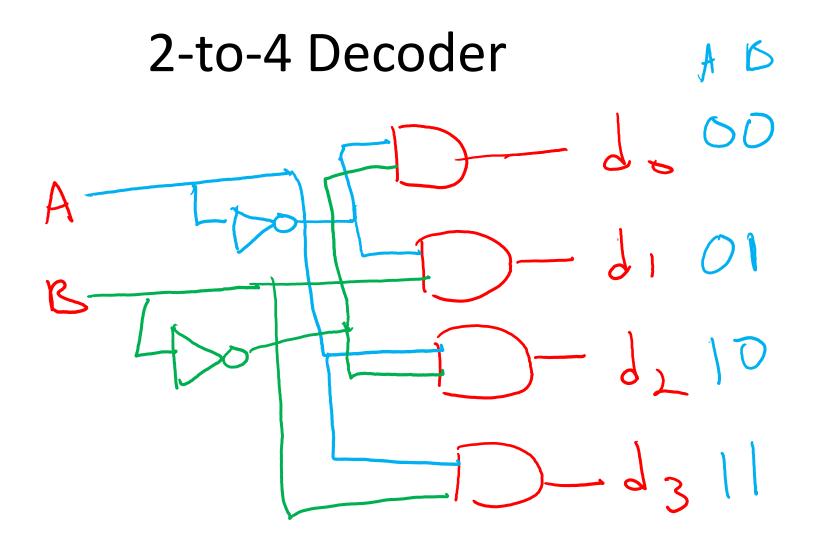


Creating a Decoder

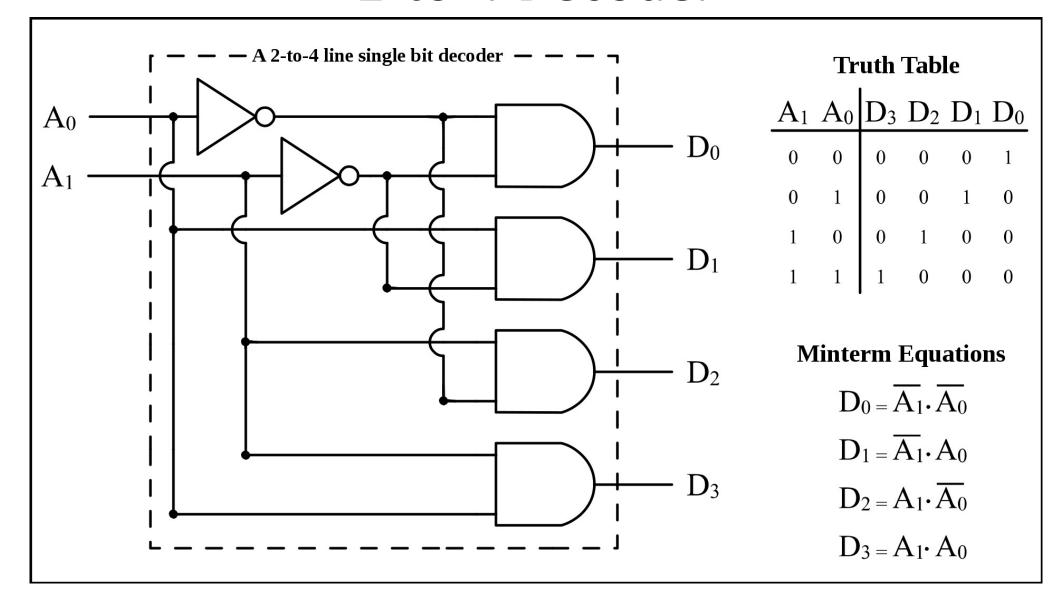


For each input signal, we need the signal and its complement

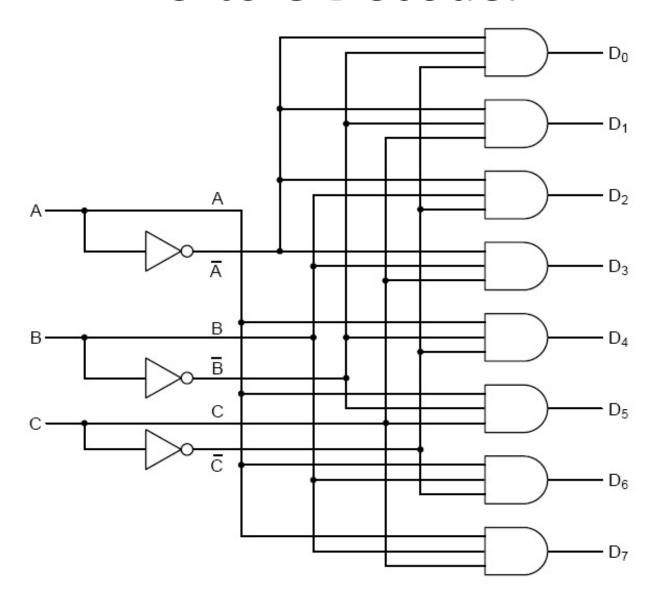
 Signals are connected to outputs via AND gates so that inputs turn on output that the digit they represent is present in



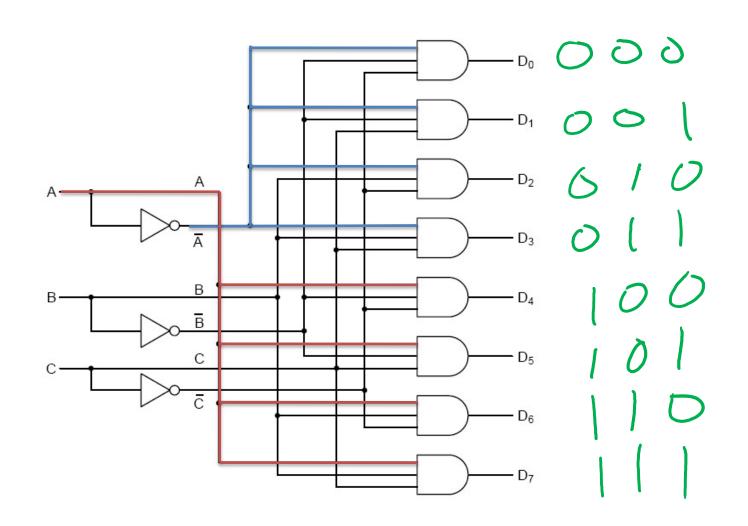
2-to-4 Decoder



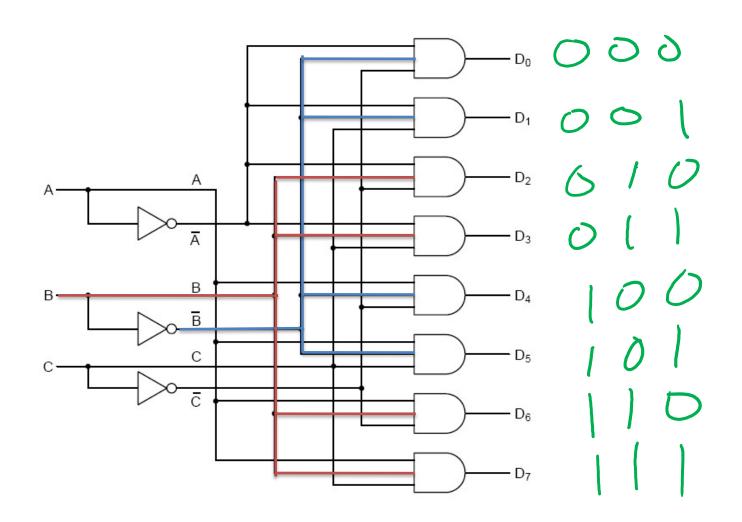
3-to-8 Decoder



3-to-8 Decoder, A is our MSB

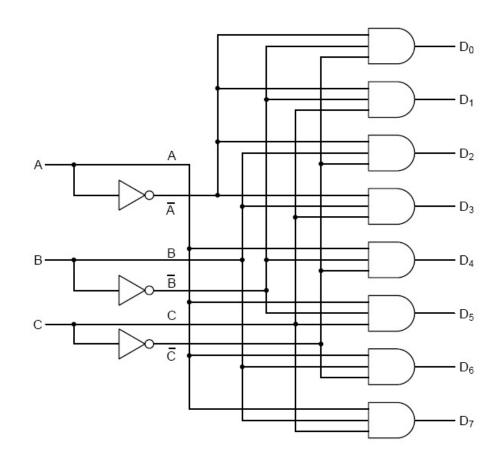


3-to-8 Decoder, B

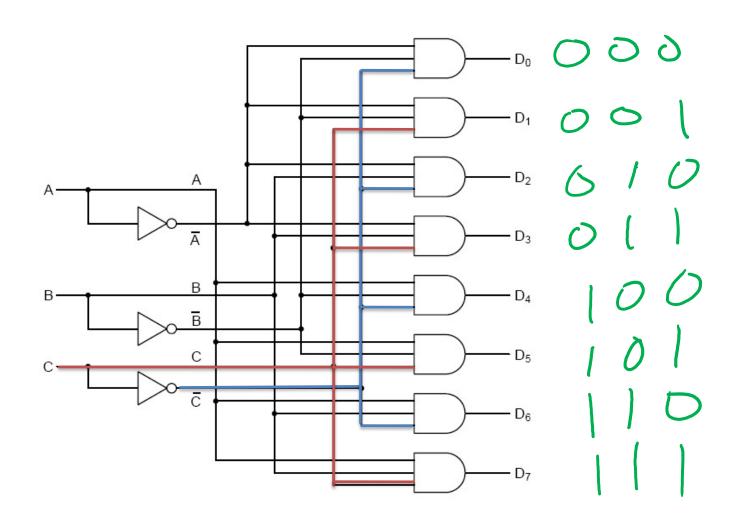


C corresponds to the lowest order bit for the input. In our 3-bit decoder, if C is 1, we should send 0 to _ and 1 to _

Clicker	0	1
А	D0, D1, D2, D3	D4, D5, D6, D7
В	D4, D5, D6, D7	D0, D1, D2, D3
С	D0, D2, D4, D6	D1, D3, D5, D7
D	D1, D3, D5, D7	D0, D2, D4, D6

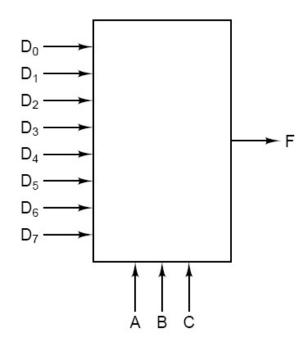


3-8 Decoder, C



Multiplexer

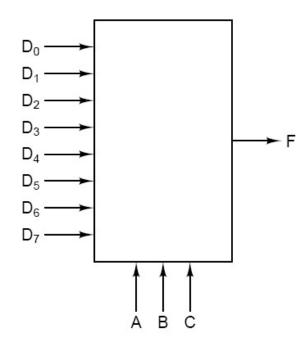
 Select one signal from a group of 2ⁿ inputs, to be output on a single output line.



Multiplexer

• Lines $D_0,...,D_7$ are the data input lines and F is the output line.

• Lines A, B, and C are called the select lines. They are interpreted as a three-bit binary number, which is used to choose one of the D lines to be output on line F.

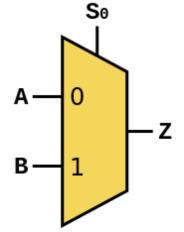


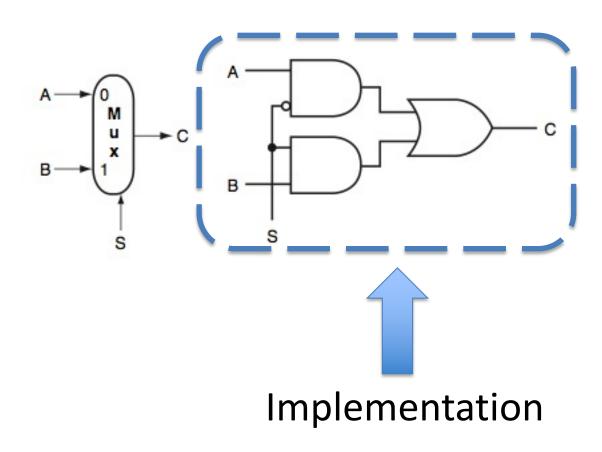
2-to-1 Multiplexer

• S is the selector

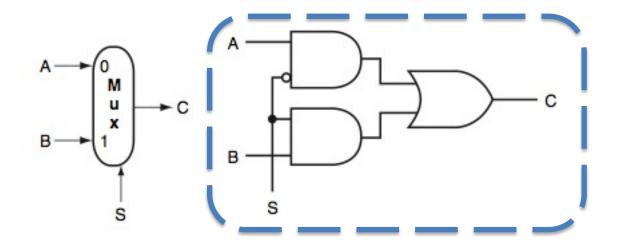
• 0 selects A; 1 selects B

Common circuit symbol





A = 1, B = 0, and S is 1. C will be



- A. 0
- B. 1
- C. Unclear

Arbitrarily Large Multiplexer

If there are n data inputs, there will need to be [log₂n] selector inputs.

- The multiplexer consists of
 - A decoder that generates n signals, each indicating a different control value
 - An array of n AND gates, each combining one of the inputs with a signal from the decoder
 - A single large OR gate that incorporates the outputs of the AND gates

Reading

- Next lecture: ALU
 - Read Section 3.4

- Problem Set 5
 - Due Friday

- Lab 4
 - Due Sunday