CSCI 210: Computer Architecture Lecture 15: Digital Logic

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Slides from Cynthia Taylor

Announcements

Problem Set 4 due today

Lab 3 due Sunday!

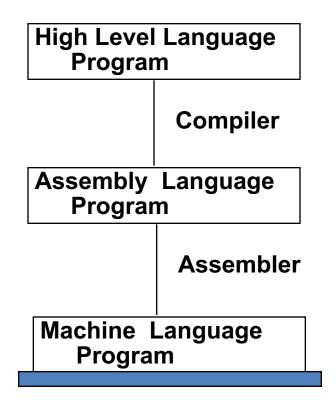
Office Hours today 13:30 – 14:30 pm

Creating the Universe from 1 and 0

We have seen how to build programs from assembly

 Now we'll learn how we build assembly language instructions out of circuits

Machine Interpretation



Machine Interpretation

```
temp = v[k];

v[k] = v[k+1];

v[k+1] = temp;

Iw $15, 0($2)

Iw $16, 4($2)

sw $16, 0($2)

sw $15, 4($2)
```

Machine does something!

A digital circuit is comprised of signals, gates, and wires.

- Signals
 - Voltages applied to lines which generate electric current

- Binary signals are represented by different voltages:
 - -0: 0-1 volts
 - -1: 2-5 volts

A digital circuit is comprised of signals, gates, and wires.

Gates

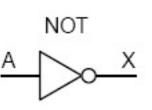
- Devices which perform operations on signals corresponding to basic logic operations: and, or, not, nand, nor, xor
- Made out of transistors

Wires

Lines over which signals are transmitted between gates

Representation of Logic Gates

Symbol

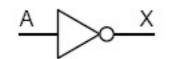


• Truth Table

Α	Χ
0	1
1	0

Algebraic Representation

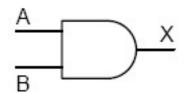
Not



Α	Х
0	1
1	0

- Inverts the input
- Algebraic representation: $ar{A}$

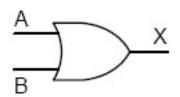
And



A	В	X
0	0	0
0	1	0
1	0	0
1	1	1

• Algebraic representation: AB or $A \cdot B$

Or



A	В	X
0	0	0
0	1	1
1	0	1
1	1	1

• Algebraic representation: A+B

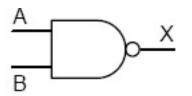
And and Not



A. 0

B. 1

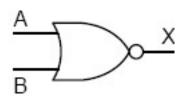
Nand



A	В	Х
0	0	1
0	1	1
1	0	1
1	1	0

• Algebraic representation: $\overline{(A \cdot B)}$

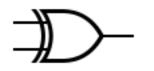
Nor



A	В	Х
0	0	1
0	1	0
1	0	0
1	1	0

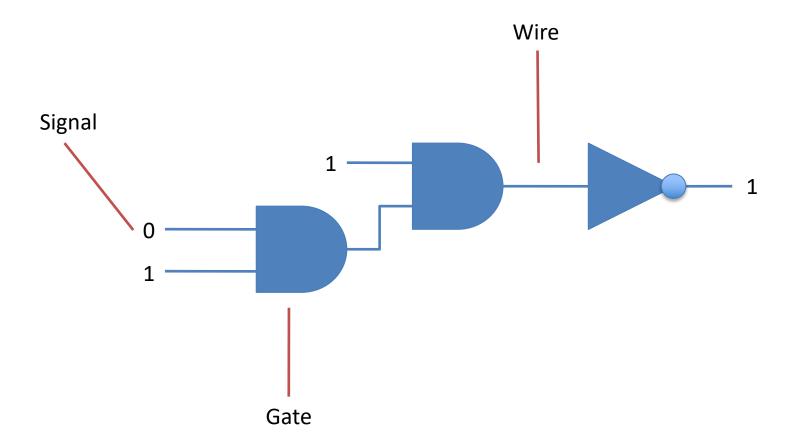
• Algebraic representation: $\overline{(A+B)}$

Xor

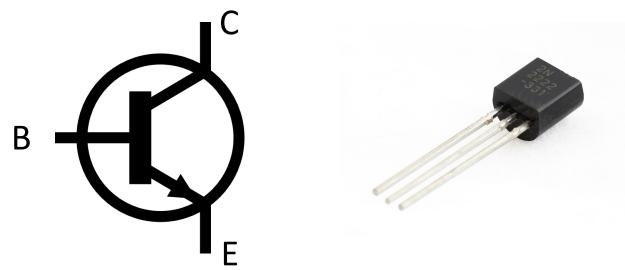


A	В	X
0	0	0
0	1	1
1	0	1
1	1	0

• Algebraic representation: A^B or $A \oplus B$



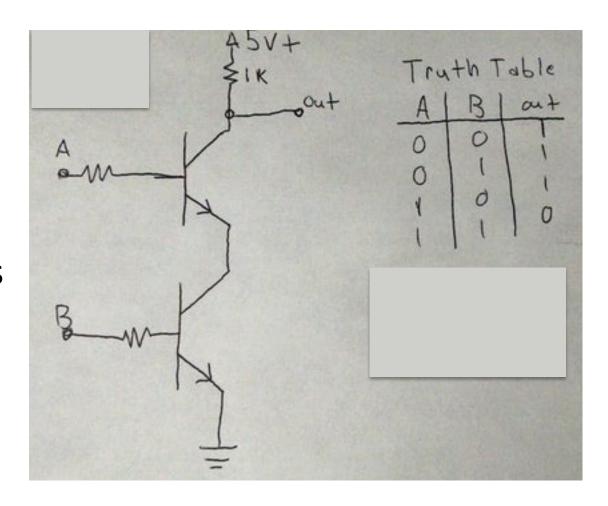
Our Friend the Transistor



- The basic electronic component from which all gates are created; there are many types, this is an NPN transistor
- When the base (B) has a high voltage, current can flow from the collector (C) to the emitter (E)
- This creates an on/off switch

Building gates out of switches

- Two inputs A and B
- One output out
- When A or B are 1, the other two electrodes (collector and emitter) are connected
- When A and B are both 1, out is connected to ground (logic value 0)
- When either A or B is 0, out is not connected to ground and current can flow from 5V to out

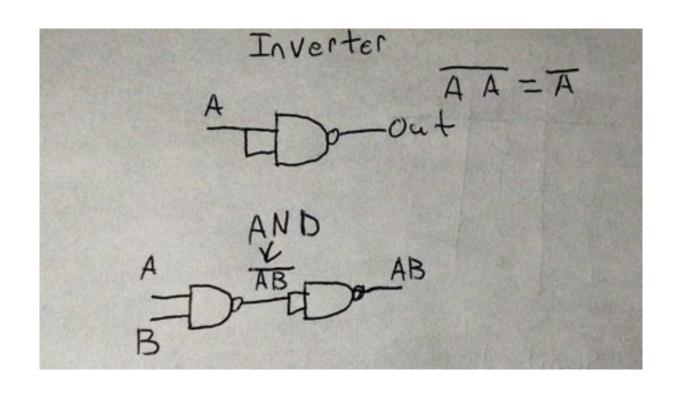


What Gate Does This Match?

- If A and B are high voltage (logical 1), C will be low voltage (logical 0)
- Otherwise, C is high voltage

- A. AND
- B. OR
- C. NAND
- D. NOR

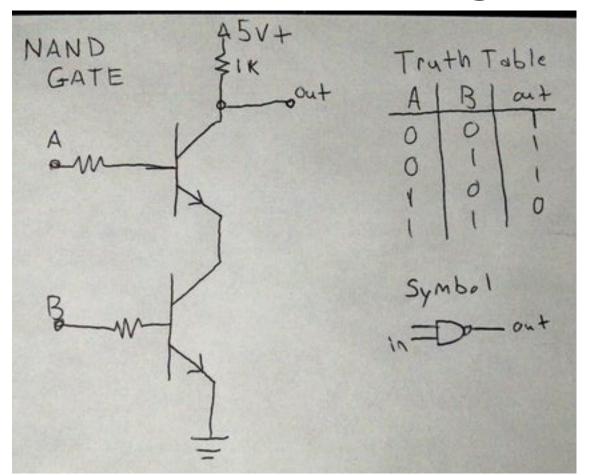
All Other Gates Can Be Created From NAND

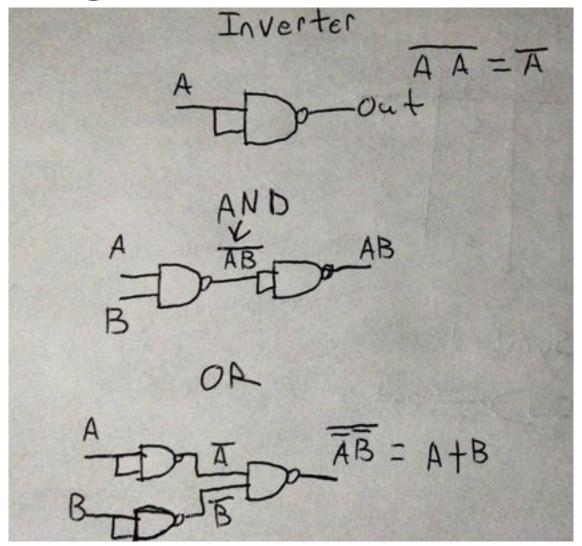


Which is equivalent to A OR B?

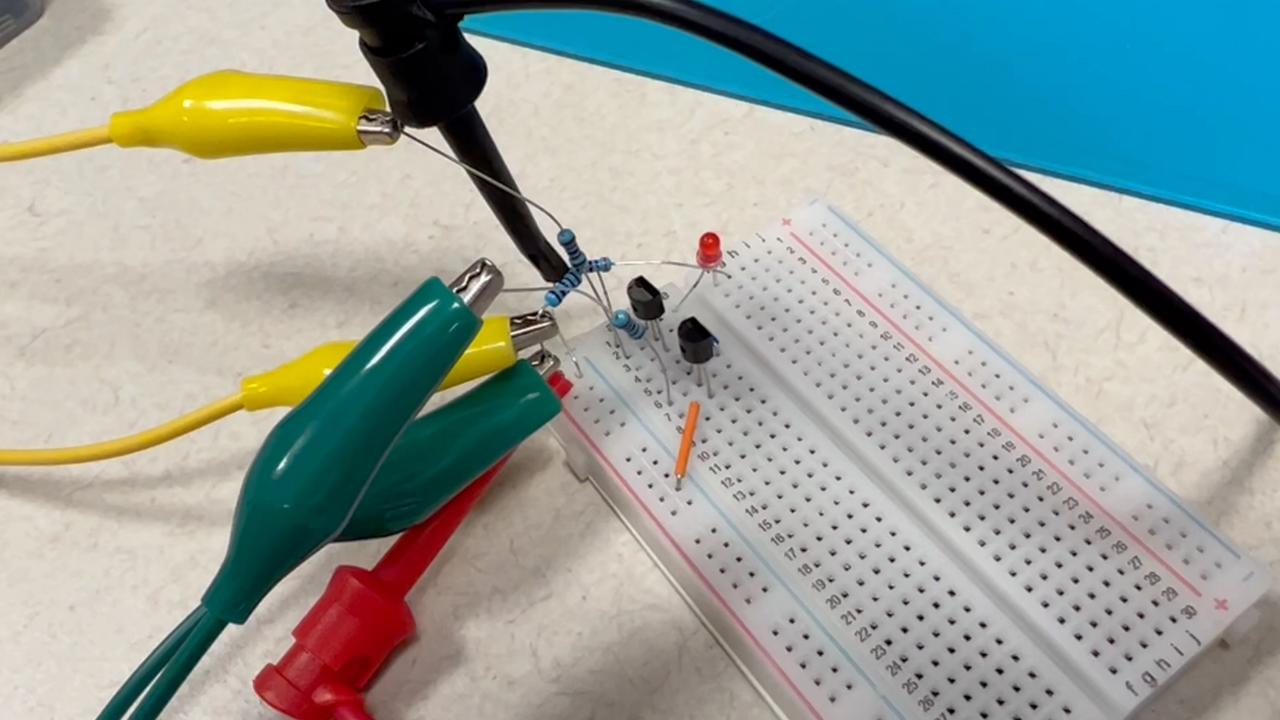
- A. A NAND B
- B. NOT (A NAND B)
- C. (NOT A) NAND (NOT B)
- D. NOT ((NOT A) NAND (NOT B))
- E. None of the above

Putting them together





Images from: https://www.instructables.com/Build-a-NAND-gate-from-transistors/



All Other Gates Can Be Created from NOR

You will show this in Problem Set 5

Which column completes the truth table for

$$F = \overline{X} \cdot (Y + Z)$$
?

```
X Y Z A B C D
0 0 0 0 0 1 1
0 0 1 1 1 1 1
0 1 0 1 1 1 1
0 1 1 1 1 1 1
1 0 0 0 0 0
1 0 1 0 1 0 1
1 1 0 0 1 0 1
```

Diagram:
$$F = \overline{X} \cdot (Y + Z)$$

$$F = \overline{A} + (B(AC + \overline{AB}))$$

Truth Table

A B C
$$AC$$
 \overline{AB} $B(AC + \overline{AB})$ F

Reading

• Next lecture: Boolean Algebra

-3.3

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