CS 241: Systems Programming Lecture 12. Bits and Bytes 1

Spring 2020 Prof. Stephen Checkoway

Computers use binary

Everything in a computer is stored and manipulated as a collection of bits

The bits mean something only in how they are used, not what they are

Example with 32-bits: 01000011010100110100001101001001

- As a integer: 1129530185
- As a (single-precision) floating point number: 211.262833
- As a sequence of four ASCII characters: CSCI
- As 32-bit x86 instructions:

```
inc ebx
push ebx
inc ebx
dec ecx
```

Given a decimal (base 10) number 1253₁₀

► 3 ones (10°)

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- ► 5 tens (10¹)

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- ► 2 hundreds (10²)

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- ► 5 tens (10¹)
- 2 hundreds (10²)
- ► 1 thousand (10³)

```
10<sup>3</sup> 10<sup>2</sup> 10<sup>1</sup> 10<sup>0</sup>
1 2 5 3
```

Only uses the digits 0-7

In C, literal starts with leading 0

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Given an octal (base 8) number 02345

- ► 5 ones (8°)
- ► 4 eights (8¹)
- 3 sixty-fours (8²)
- 2 five hundred twelves (83)

Only uses the digits 0-7

In C, literal starts with leading 0

Given an octal (base 8) number 02345

- ► 5 ones (8°)
- ► 4 eights (8¹)
- 3 sixty-fours (8²)
- 2 five hundred twelves (83)
 - 83
 82
 81
 80
 3
 4
 5

Single place has values of 0-15

- ► Need digits larger than 9. Use A=10, B=11, ..., F=15
- In C, starts with a leading 0x or 0x

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Given a hexadecimal (base 16) number 0x04E5

- ► 5 ones (16°)
- ► 14 sixteens (16¹)
- 4 two hundred fifty-sixes (16²)
- ► 0 four thousand ninety-sixes (16³)

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```
16<sup>3</sup>
16<sup>2</sup>
16<sup>1</sup>
16<sup>0</sup>
5
```

Only uses the digits 0 and 1

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Given a binary number 0b000010011100101

```
► 1 2<sup>0</sup>, 0 2<sup>1</sup>, 1 2<sup>2</sup>, 0 2<sup>3</sup>
```

- ► 0 2⁴, 1 2⁵, 1 2⁶, 1 2⁷
- ► 0 28, 0 29, 1 2¹⁰, 0 2¹¹
- ► 0 2¹², 0 2¹³, 0 2¹⁴, 0 2¹⁵

Only uses the digits 0 and 1

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```
► 1 2<sup>0</sup>, 0 2<sup>1</sup>, 1 2<sup>2</sup>, 0 2<sup>3</sup>
```

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- ► 0 2⁸, 0 2⁹, 1 2¹⁰, 0 2¹¹
- ► 0 2¹², 0 2¹³, 0 2¹⁴, 0 2¹⁵

Only uses the digits 0 and 1

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- ► 0 2⁸, 0 2⁹, 1 2¹⁰, 0 2¹¹
- ► 0 2¹², 0 2¹³, 0 2¹⁴, 0 2¹⁵

```
2^{15..12} 2^{11..8} 2^{7..4} 2^{3..0} 0000 0100 1110 0101
```

```
\mathbf{1253} = 1*10^3 + 2*10^2 + 5*10^1 + 3*10^0 = 1253
```

```
► 1253 = 1*10^3 + 2*10^2 + 5*10^1 + 3*10^0 = 1253

► 02345 = 2*8^3 + 3*8^2 + 4*8^1 + 5*8^0 = 1253
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► 0x04E5 = 0*16^3 + 4*16^2 + 14*16^1 + 5*16^0 = 1253
```

Multiply and sum up the digit * baseposition value

```
► 1253 = 1*10^3 + 2*10^2 + 5*10^1 + 3*10^0 = 1253

► 02345 = 2*8^3 + 3*8^2 + 4*8^1 + 5*8^0 = 1253

► 0x04E5 = 0*16^3 + 4*16^2 + 14*16^1 + 5*16^0 = 1253
```

 $blue{0}$ 0b0000010011100101 = 1253

Convert the octal value 031 to decimal

- A. 7
- B. 25
- C. 31
- D. 49
- E. 248

Hex	Binary	Hex	Binary
0	0000	8	1000
1	0001	9	1001
2	0010	A	1010
3	0011	В	1011
4	0100	C	1100
5	0101	D	1101
6	0110	E	1110
7	0111	F	1111

Just group digits by 4s starting with LSB

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Each block of 4 bits is 0–15

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Replace each with a hex digit

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Just group digits by 4s starting with LSB

- ► 0b000010011100101
- ► 0b 0000 0100 1110 0101

Each block of 4 bits is 0–15

- Replace each with a hex digit
- ► 0 4 E 5

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Just group digits by 4s starting with LSB

- b 0b000010011100101
- ► 0b 0000 0100 1110 0101

Each block of 4 bits is 0–15

- Replace each with a hex digit
- ► 0 4 E 5
- ► 0x04E5

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1	0001	9	1001
2	0010	A	1010
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4	0100	C	1100
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6	0110	E	1110
7	0111	F	1111

Octal	Binary
0	000
1	001
2	010
3	011
4	100
5	101
6	110
7	111

Just group digits by 3s starting with LSB

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0	000
1	001
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Just group digits by 3s starting with LSB

► 0b000010011100101

Octal	Binary
0	000
1	001
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Just group digits by 3s starting with LSB

- b 0b000010011100101
- ► 0b 000 000 010 011 100 101

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Just group digits by 3s starting with LSB

- b 0b000010011100101
- ► 0b 000 000 010 011 100 101

Each block of 3 bits is 0–7

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Just group digits by 3s starting with LSB

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Each block of 3 bits is 0–7

Replace each with a octal digit

Octal	Binary
0	000
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Just group digits by 3s starting with LSB

- b 0b000010011100101
- ► 0b 000 000 010 011 100 101

Each block of 3 bits is 0–7

- Replace each with a octal digit
- ► 0 0 2 3 4 5

Octal	Binary
0	000
1	001
2	010
3	011
4	100
5	101
6	110
7	111

Just group digits by 3s starting with LSB

- b 0b0000010011100101
- ► 0b 000 000 010 011 100 101

Each block of 3 bits is 0–7

- Replace each with a octal digit
- ► 0 0 2 3 4 5
- 0002345 (We prepended a 0 to denote octal)

Octal	Binary
0	000
1	001
2	010
3	011
4	100
5	101
6	110
7	111

Convert the 16-bit binary number 0b11001010_11111110 to hex.

(I added an underscore to separate the two groups of 8 bits to improve

readability.)

A.	0xBEE	F

B.		XCAFE
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Alternative view of hex/octal

Binary is a pain to read/work with

Consider a 64-bit number

so long it doesn't fit on one line!

Hex (and much less commonly octal) can be viewed as a more compact way to represent binary numbers

Ox4c40d6b036c547b0

Converting hex/octal to binary

- 1. Take each hexadecimal (or octal) digit
- 2. Convert it into binary
 - 4 places hex (e.g., A becomes 1010)
 - 3 places octal (e.g., 6 becomes 110)
- 3. Group them together from LSB to MSB

Converting between Hex & Octal

- 1. Take hexadecimal number
- 2. Convert to binary
- 3. Regroup in clusters of 3 from LSB
- 4. Generate Octal digits
- 5. Use reverse process for Octal to Hex

Repeatedly divide by 2, recording remainders

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Remainders form the binary number from least to most significant

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$$\rightarrow$$
 39 / 2 = 19 r 1

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Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1

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Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1
- \rightarrow 9 / 2 = 4 r 1

Repeatedly divide by 2, recording remainders

Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1
- \rightarrow 9 / 2 = 4 r 1
- -4 / 2 = 2 r 0

Repeatedly divide by 2, recording remainders

Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1
- \rightarrow 9 / 2 = 4 r 1
- -4 / 2 = 2 r 0
- 2 / 2 = 1 r 0

Repeatedly divide by 2, recording remainders

Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1
- \rightarrow 9 / 2 = 4 r 1
- -4 / 2 = 2 r 0
- 2 / 2 = 1 r 0
- 1 / 2 = 0 r 1

Repeatedly divide by 2, recording remainders

Remainders form the binary number from least to most significant

- \rightarrow 39 / 2 = 19 r 1
- -19 / 2 = 9 r 1
- \rightarrow 9 / 2 = 4 r 1
- -4 / 2 = 2 r 0
- 2 / 2 = 1 r 0
- 1 / 2 = 0 r 1
- \rightarrow 39 = 0b100111

In-class exercise

https://checkoway.net/teaching/cs241/2020-spring/exercises/Lecture-12.html

Grab a laptop and a partner and try to get as much of that done as you can!