# CS 241: Systems Programming Lecture 13. Bits and Bytes 2

Fall 2019 Prof. Stephen Checkoway

Data are physically stored in binary (logically)

32 bit unsigned integer values are:

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#### 32 bit unsigned integer values are:

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```
32 bit unsigned integer values are:
```

bitwise AND

```
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```

bitwise OR

- bitwise AND
- bitwise OR
- bitwise XOR

- bitwise AND
- bitwise OR
- bitwise XOR
- << left shift

- bitwise AND
- bitwise OR
- bitwise XOR
- << left shift
- >> right shift

- bitwise AND
- bitwise OR
- bitwise XOR
- << left shift
- >> right shift
- one's complement (unary)

## Review of Boolean logic

A	B	~A	A&B	AB	A^B
0	0	1	0	0	0
0	1	1	0	1	1
1	0	0	0	1	1
1	1	0	1	1	0

#### What is the value of 0x4E & 0x1F?

B. 0x51

C. 0x5F

D. 0xB1

E. 0xE0

Hex	Binary	Hex	Binary
0	0000	8	1000
1	0001	9	1001
2	0010	A	1010
3	0011	В	1011
4	0100	C	1100
5	0101	D	1101
6	0110	E	1110
7	0111	F	1111

Manipulates the position of bits

Left shift fills with 0 bits

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- Right shift of unsigned variable fills with 0 bits

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  - Same as multiplying by 4
- x >> 3; // shifts bits of x three positions right

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- Right shift of unsigned variable fills with 0 bits
- Right shift of signed variable fills with sign bit (Actually implementation defined if negative!)
- x << 2; // shifts bits of x two positions left
  - Same as multiplying by 4
- x >> 3; // shifts bits of x three positions right
  - Same as dividing by 8 (if x is unsigned)

What does the following do?

$$x = ((x >> 2) << 2);$$

- A. Changes x to be positive
- B. Sets the least significant two bits to 0
- C. Sets the most significant two bits to 0
- D. Gives an integer overflow error
- E. Implementation-defined behavior

```
#include <stdbool.h>

// Returns true if the nth bit of x is 1.
bool is_bit_set(unsigned int x, unsigned int n) {
  return x & (lu << n); // lu is an unsigned int with value 1.
}</pre>
```

```
#include <stdbool.h>

// Returns true if the nth bit of x is 1.
bool is_bit_set(unsigned int x, unsigned int n) {
   return x & (lu << n); // lu is an unsigned int with value 1.
}

lu << n gives an integer with only the nth bit set</pre>
```

```
#include <stdbool.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
  return x & (lu << n); // lu is an unsigned int with value 1.
1u << n gives an integer with only the nth bit set
If the nth bit is 1, then x \in (1u << n) is 1u << n which is nonzero.
If the nth bit is 0, then x \in (1u << n) is 0
```

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// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
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If the nth bit is 1, then x \in (1u << n) is 1u << n which is nonzero.
If the nth bit is 0, then x \in (1u << n) is 0
```

What happens if n is too large?

```
#include <stdbool.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
  return x & (lu << n); // lu is an unsigned int with value 1.
1u << n gives an integer with only the nth bit set
If the nth bit is 1, then x \in (1u << n) is 1u << n which is nonzero.
If the nth bit is 0, then x \in (1u << n) is 0
```

What happens if n is too large?

Undefined behavior!

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
  return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
  unsigned int x = atoi(argv[1]);
  unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
  else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad shift 3 0
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
 return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
 return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
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  if (argc != 3)
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 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
 return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
$ ./bad_shift 3 2
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
$ ./bad_shift 3 2
Bit 2 of 3 is 0
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
$ ./bad_shift 3 2
Bit 2 of 3 is 0
$ ./bad_shift 3 32
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
  unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
$ ./bad_shift 3 2
Bit 2 of 3 is 0
$ ./bad_shift 3 32
Bit 32 of 3 is 1
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
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 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad_shift 3 0
Bit 0 of 3 is 1
$ ./bad_shift 3 1
Bit 1 of 3 is 1
$ ./bad_shift 3 2
Bit 2 of 3 is 0
$ ./bad_shift 3 32
Bit 32 of 3 is 1
$ ./bad_shift 3 33
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
#include <stdlib.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
 return x & (1u << n);
int main(int argc, char **argv) {
  if (argc != 3)
    errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad shift 3 0
Bit 0 of 3 is 1
$ ./bad shift 3 1
Bit 1 of 3 is 1
$ ./bad shift 3 2
Bit 2 of 3 is 0
$ ./bad shift 3 32
Bit 32 of 3 is 1
$ ./bad shift 3 33
Bit 33 of 3 is 1
```

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#include <stdbool.h>
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    printf("Bit u of u is 0 n, n, x);
  return 0;
```

```
$ ./bad shift 3 0
Bit 0 of 3 is 1
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Bit 1 of 3 is 1
$ ./bad shift 3 2
Bit 2 of 3 is 0
$ ./bad shift 3 32
Bit 32 of 3 is 1
$ ./bad shift 3 33
Bit 33 of 3 is 1
$ ./bad shift 3 34
```

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$ ./bad shift 3 2
Bit 2 of 3 is 0
$ ./bad shift 3 32
Bit 32 of 3 is 1
$ ./bad shift 3 33
Bit 33 of 3 is 1
$ ./bad shift 3 34
Bit 34 of 3 is 0
```

```
#include <err.h>
#include <stdbool.h>
#include <stdio.h>
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bool is bit set(unsigned int x, unsigned int n) {
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int main(int argc, char **argv) {
  if (argc != 3)
   errx(1, "Usage: %s integer bit", argv[0]);
 unsigned int x = atoi(argv[1]);
 unsigned int n = atoi(argv[2]);
  if (is bit set(x, n))
   printf("Bit %u of %u is 1\n", n, x);
 else
   printf("Bit u of u is 0 n, n, x);
  return 0;
```

# Testing if a bit is set (i.e., is 1)

```
#include <assert.h>
#include <liimits.h>
#include <stdbool.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
  // assert(cond) will abort at runtime if cond is false.
  assert(n < CHAR BIT * sizeof x);
  return x & (1u << n); // lu is an unsigned int with value 1.
```

# Testing if a bit is set (i.e., is 1)

```
#include <assert.h>
#include <liimits.h>
#include <stdbool.h>
// Returns true if the nth bit of x is 1.
bool is bit set(unsigned int x, unsigned int n) {
  // assert(cond) will abort at runtime if cond is false.
  assert(n < CHAR BIT * sizeof x);
  return x & (1u << n); // lu is an unsigned int with value 1.
E.g., if CHAR_BIT is 8 and size of x is 4, then n must be less than 32 or the
```

program aborts

# Setting a bit (to 1)

```
// Returns the value of x with the nth bit set to 1.
unsigned int set_bit(unsigned int x, unsigned int n) {
   assert(n < CHAR_BIT * sizeof x);
   return x | (lu << n);
}</pre>
```

# Clearing a bit (setting it to 0)

```
// Returns the value of x with the nth bit set to 0.
unsigned int clear_bit(unsigned int x, unsigned int n) {
  assert(n < CHAR_BIT * sizeof x);
  return x & ~(lu << n);
}</pre>
```

# Clearing a bit (setting it to 0)

1u << n gives an integer with just the nth bit set

```
// Returns the value of x with the nth bit set to 0.
unsigned int clear_bit(unsigned int x, unsigned int n) {
  assert(n < CHAR_BIT * sizeof x);
  return x & ~(1u << n);
}</pre>
```

# Clearing a bit (setting it to 0)

```
// Returns the value of x with the nth bit set to 0.
unsigned int clear_bit(unsigned int x, unsigned int n) {
   assert(n < CHAR_BIT * sizeof x);
   return x & ~(1u << n);
}

lu << n gives an integer with just the nth bit set
   ~(1u << n) gives an integer with all bits set except the nth bit</pre>
```

Given an unsigned integer x with some value, what value should we use for mask to clear all of the bits of x except for the least significant 5 bits?

```
unsigned int x = /* ... */;  // Given some value here,
unsigned int mask = /* ... */;  // what value goes here
x = x & mask;  // to clear the required bits?
A. 0x5u
```

- $B. \sim 0 \times 5 u$
- C. 0x1Fu
- $D. \sim 0 \times 1 Fu$
- E. sizeof x 5

Given an unsigned integer x with some value, what value should we use for mask to clear the 5 least significant bits of x?

```
unsigned int x = /* ... */;  // Given some value here,
unsigned int mask = /* ... */;  // what value goes here
x = x & mask;  // to clear the required bits?
A. 0x5u
```

 $B. \sim 0 \times 5 u$ 

C. 0x1Fu

 $D. \sim 0 \times 1 Fu$ 

E. sizeof x - 5

# Combining flags via

```
Specify flags via individual bits #define S_IRWXU 0000700
                                                          /* RWX mask for owner */
                               #define S IRUSR 0000400
                                                           /* R for owner */
                               #define S IWUSR 0000200
                                                          /* W for owner */
Combine flags with |
                               #define S IXUSR 0000100
                                                           /* X for owner */
                               #define S IRWXG 0000070
                                                           /* RWX mask for group */
E.g., set file system
                               #define S_IRGRP 0000040
                                                           /* R for group */
permissions via the flags
                               #define S IWGRP 0000020
                                                           /* W for group */
S_I{R,W,X}{USR,GRP,OTH}**define S_IXGRP 0000010
                                                           /* X for group */
                                                             RWX mask for other */
                               #define S IRWXO 0000007
                                                           /* R for other */
                               #define S IROTH 0000004
                               #define S IWOTH 0000002
                                                          /* W for other */
                               #define S IXOTH 0000001
                                                           /* X for other */
                               int chmod(char const *path, mode t mode);
```

## Negative numbers

Usually stored using two's complement

- Take the magnitude of the number
- Invert all of the bits
- Add 1

Converting back uses the same operation

Most significant bit indicates the sign

1 indicates a negative number

### Signed numbers in two's complement

```
10000000 00000000 00000000 000000000 = -231
10000000 00000000 00000000 00000001 = -2^{31}+1
\bullet \bullet \bullet
\bullet \bullet \bullet
01111111 111111111 111111111 1111111 = 2^{31}-1
```

#### Sign and magnitude

- Most significant bit represents the sign, remaining bits are the same
- ► Range -(2<sup>n-1</sup> 1) to 2<sup>n-1</sup> 1
- Two different bit patterns for zero: 0 and 0x8000000 (assuming 32-bits)

#### Sign and magnitude

- Most significant bit represents the sign, remaining bits are the same
- ► Range -(2<sup>n-1</sup> 1) to 2<sup>n-1</sup> 1
- Two different bit patterns for zero: 0 and 0x8000000 (assuming 32-bits)

### Ones' complement

- ► Negative numbers are the bitwise inverse of positive numbers (-x = -x)
- ► Range -(2<sup>n-1</sup> 1) to 2<sup>n-1</sup> 1
- Two different bit patterns for zero: 0 and 0xFFFFFFF (assuming 32-bits)

#### Sign and magnitude

- Most significant bit represents the sign, remaining bits are the same
- ► Range -(2<sup>n-1</sup> 1) to 2<sup>n-1</sup> 1
- Two different bit patterns for zero: 0 and 0x8000000 (assuming 32-bits)

### Ones' complement

- Negative numbers are the bitwise inverse of positive numbers (-x = -x)
- ► Range -(2<sup>n-1</sup> 1) to 2<sup>n-1</sup> 1
- Two different bit patterns for zero: 0 and 0xFFFFFFF (assuming 32-bits)

### Two's complement

- ► Negative numbers are ones' complement plus one (-x = ~x + 1)
- ► Range -2<sup>n-1</sup> to 2<sup>n-1</sup> 1
- Only one zero

## In-class exercise

https://checkoway.net/teaching/cs241/2019-fall/exercises/Lecture-13.html

Grab a laptop and a partner and try to get as much of that done as you can!