Programming Abstractions

Lecture 26: MiniScheme H

Review: What is the value of this expression?

```
(let ([f add1])

(let ([f (\lambda (x)

(if (= x 0)

10

(* 2 (f 0))))])

(f 3)))
```

A. 2

D. 20

B. 4

E. An error

C. 10

What is the result of this expression?

E. An error

Implementing recursion in MiniScheme H

```
(letrec ([f exp1] [g exp2] ...) body)
```

We'll have the parser parse a letrec expression into something equivalent that uses only things we have implemented

We won't need to change eval-exp at all!

Two options

We can use the Y combinator (technically the Z combinator)

We can use set!/begin

Which would you prefer?

Z combinator it is!

$$Z = \lambda f.(\lambda x.f(\lambda v.xxv))(\lambda x.f(\lambda v.xxv))$$

Translated from λ -calculus to Scheme, we have

Just kidding, let's use set!/begin

To what does this evaluate?

- A. 0
- B. 34
- C. An error

To what does this evaluate?

A. 0

D. 6

B. 1

E. An error

C. 5

To what does this evaluate?

A. 0

D. It runs forever

B. 5

E. An error

C. 10

Let's draw the environments

Write factorial without letrec

Mutual recursion

Mutual recursion without letrec

```
(let ([even? 0]
      [odd? 0])
  (let ([f (lambda (x)
             (cond [(= 0 x) #t]
                    [ (= 1 x) #f]
                    [else (odd? (- x 1))]))
        [g (lambda (x)
             (cond [(= 0 x) \#f]
                    [ (= 1 x) #t]
                    [else (even? (- x 1))])))
    (begin
     (set! even? f)
     (set! odd? g)
     (odd? 23))))
```

General transformation

```
Replace
(letrec ([f1 exp1] ... [fn expn])
  body)
with
(let ([f1 0] ... [fn 0])
  (let ([g1 exp1] ... [gn expn])
    (begin
     (set! f1 g1)
     (set! fn gn)
     body)))
```

General transformation

```
Replace
(letrec ([f1 exp1] ... [fn expn])
  body)
                                   We need some new symbols!
with
(let ([f1 0] ... [fn 0])
  (let ([g1 exp1] ... [gn expn])
     (begin
      (set! f1 g1)
      (set! fn gn)
     body)))
```

Generating symbols

```
(gensym)
```

We can use (gensym) to generate new, unused symbols

```
> (gensym)
'g75075
> (gensym)
'g75106
```

A common mistake with gensym

your code will fail to work because the two symbols will be different!

Final MiniScheme grammar

PARAMS → symbol*

```
EXP → number
                                        parse into lit-exp
                                        parse into var-exp
      symbol
     ( if EXP EXP EXP)
                                        parse into ite-exp
     (let (LET-BINDINGS) EXP)
                                       parse into let-exp
      (letrec (LET-BINDINGS)EXP)
                                       transform into equivalent let-exp
     (lambda (PARAMS) EXP)
                                        parse into lambda-exp
     ( set! symbol EXP )
                                        parse into set-exp
      (begin EXP*)
                                        parse into begin-exp
      (EXP EXP^*)
                                        parse into app-exp
LET-BINDINGS → LET-BINDING*
LET-BINDING \rightarrow [ symbol EXP ]*
```

Parsing letrec expressions

```
(letrec ([f1 exp1] ... [fn expn]) body)
We have three parts
> syms = (f1 ... fn) = (map first (second input))
> exps = (exp1 ... expn) = (map second (second input))
> body = (third input)
```

We need to construct several parts from these

- The outer let: (let ([f1 0] ... [fn 0]) ...)
- The inner let: (let ([g1 exp1] ... [gn expn]) ...)
- The set!s: (begin (set! f1 g1) ... (set! fn gn) ...)

The outer let

```
(let ([f1 0] ... [fn 0]) ...)
```

Recall that our let-exp has a list of symbols, a list of parsed expressions, and a parsed body

We already got the symbols: (f1 ... fn) = syms

For the parsed expressions: $(map (\lambda (s) (lit-exp 0)) syms)$

The parsed body is going to be another let-exp

The inner let

The parsed body is a begin expression

```
(let ([g1 exp1] ... [gn expn]) ...) For the symbols: new-syms = (map (\lambda (s) (gensym)) syms) For the parsed expressions: (map parse exps)
```

The begin expression

```
(begin (set! fl gl) ... (set! fn gn) body)
```

Recall that begin-exp takes a list of parsed expressions

Three reasonable options

- Generate the set!s via (map (λ (s new-s) ...) syms new-syms)
 Append (list (parse body))
- Write your own recursive procedure to build the list

A (mostly) complete example

```
(letrec ([length (lambda (lst)
                    (if (null? lst)
                        (add1 (length (cdr lst)))))))
  (length (list 10 20 30)))
parses to
(let-exp (length)
         (list (lit-exp 0))
         (let-exp'(g75784))
                   (list (lambda-exp (lst) (ite-exp ...)))
                   (begin-exp
                    (list (set-exp length (var-exp 'g75784))
                          (app-exp (var-exp 'length) (...))))
```

And that's it!

We don't need to change eval-exp at all because we already know how to evaluate let-, set-, and begin-expressions.