Due: 6 September 2011

Prove the following. You may use the methods taught by Cowles & Velleman (Givens and Goals) or use the sequent rules from the handout.

1.
$$\vdash (p \land q) \Rightarrow (p \lor q)$$

2.
$$\vdash (p \land (p \Rightarrow q)) \Rightarrow q$$

3.
$$\vdash ((p \land q) \Rightarrow r) \Rightarrow ((p \Rightarrow r) \lor (q \Rightarrow r))$$

4.
$$\vdash (\exists x. P(x) \lor R(x)) \Rightarrow (\exists x. P(x)) \lor \exists x. R(x)$$

5.
$$\vdash (\forall x. P(x) \land R(x)) \Rightarrow (\forall x. P(x)) \land \forall x. R(x)$$

6.
$$\vdash \neg(\exists x. P(x)) \Rightarrow (\forall x. \neg P(x))$$