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Problem 1.1. Read chapter 1 of Bird *Introduction to Functional Programming using Haskell*.

If you have not ordered a copy of the book yet – you should. I have copies of chapter 1 available in a box outside my office door – but you’ll need to purchase a copy.

Problem 1.2. Do problem 1.4.1 on pg 16 of Bird and 1.4.5 on page 17.

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In class we discussed the following code.

```
plus :: (Integer, Integer) -> Integer
plus (x,y) = x + y

plusc :: Integer -> Integer -> Integer
plusc x y = x + y
```

The function `plus` takes its arguments all at once packaged in a pair while `plusc` takes its arguments one at a time.

We discussed how Haskell supports a notation for describing a function without forcing you to choose a name for it.

The general form is

$$\backslash x \rightarrow e$$

where x is a variable and e is a Haskell expression.

Note that in Haskell “ \rightarrow ” is used to denote the *type constructor* for functions (e.g. if γ and δ are types, then $\gamma \rightarrow \delta$ is the type of functions from γ to δ). Also, “ \rightarrow ” is used in the expression language to describe an actual function, $(\backslash x \rightarrow e)$ denotes a function whose single argument is referred to in the expression e by the variable x .

This overloading of syntax is similar to that for Cartesian products. If γ and δ are types then (γ, δ) is the type whose elements are the pairs where the first element comes from γ and the second element comes from δ . But also, if $a \in \gamma$ and $b \in \delta$, then the pair $(a, b) \in (\gamma, \delta)$. So the developers of Haskell have used the same notation for the type constructor and to construct the elements of the type in both cases.

Now, consider the following interaction with the Haskell interpreter.

```
Main> :type plusc
:type plusc
plusc :: Integer -> Integer -> Integer
Main> :type plusc 7
:type plusc 7
plusc 7 :: Integer -> Integer
```

Evidently `plusc 7` is a function of type `Integer -> Integer`. But what function is it? It is the function that is expecting an input y and will compute the expression `7 + y`. So, it is the function described by the following expression:

$\backslash y \rightarrow 7 + y$

This form of Haskell expression is called a *lambda-term* (λ -term).

We can write $(\backslash x y \rightarrow e)$ for $(\backslash x \rightarrow (\backslash y \backslash e))$.

Every function can be written in a form where no arguments are declared on the left side of the definition. If e is an arbitrary Haskell expression, then the following examples show how this works.

$f x = e$ is the same as $f = \backslash x \rightarrow e$
 $g x y = e$ is the same as $g x = \backslash y \rightarrow e$ is the same as $g = \backslash x y \rightarrow e$

We say that `plusc` is in *Curried Form*¹; that is, it takes its arguments one at a time.

Consider the following function:

```
curry f x y = f(x,y)
```

In Haskell we have the following.

```
Main> :l test
:l test
Main> :t curry
:t curry
curry :: ((a,b) -> c) -> a -> b -> c
Main>
```

So `curry` takes a function of type $((a,b) \rightarrow c)$ and returns a function of type $(a \rightarrow b \rightarrow c)$.

Problem 2.1. Write the function `uncurry :: (a -> b -> c) -> (a,b) -> c`. You may prove the following, or (if you don't want to do the proofs), run extensive tests to show the following hold.

- i.) $uncurry\ plusc = plus$
- ii.) $curry\ plus = plusc$
- iii.) $curry(uncurry\ plusc) = plusc$
- iv.) $uncurry(curry\ plus) = plus$

¹“Currying” is the verb form of the adjective “Curried”. This form of function definition, where the function takes its arguments one at a time, is named after Haskell Curry (1900-1982), an American mathematician and logician. As you might guess, the Haskell programming language is named after him as well.