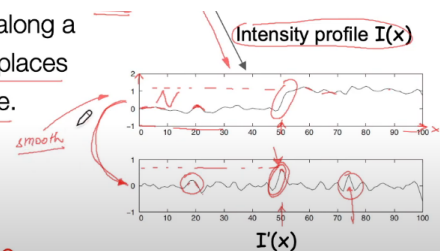


Principle: Build a profile of image brightness $I(x)$ along a dimension, and differentiate the image to look for places where the magnitude of the derivative $I'(x)$ is large.

- There is a peak at around $x = 50$
- There is also another peak at $x = 75$ (noise)

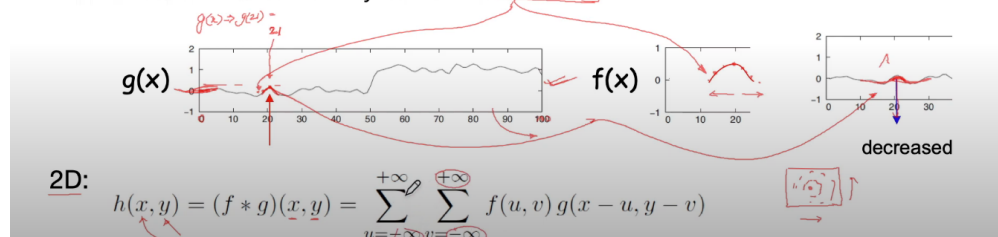


Convolution for edge detection/smoothing - 1D/2D

- A function h is the convolution of two functions f and g (denoted by $f * g$) if we have

$$h(x) = (f * g)(x) = \sum_{u=-\infty}^{+\infty} f(u) g(x-u)$$

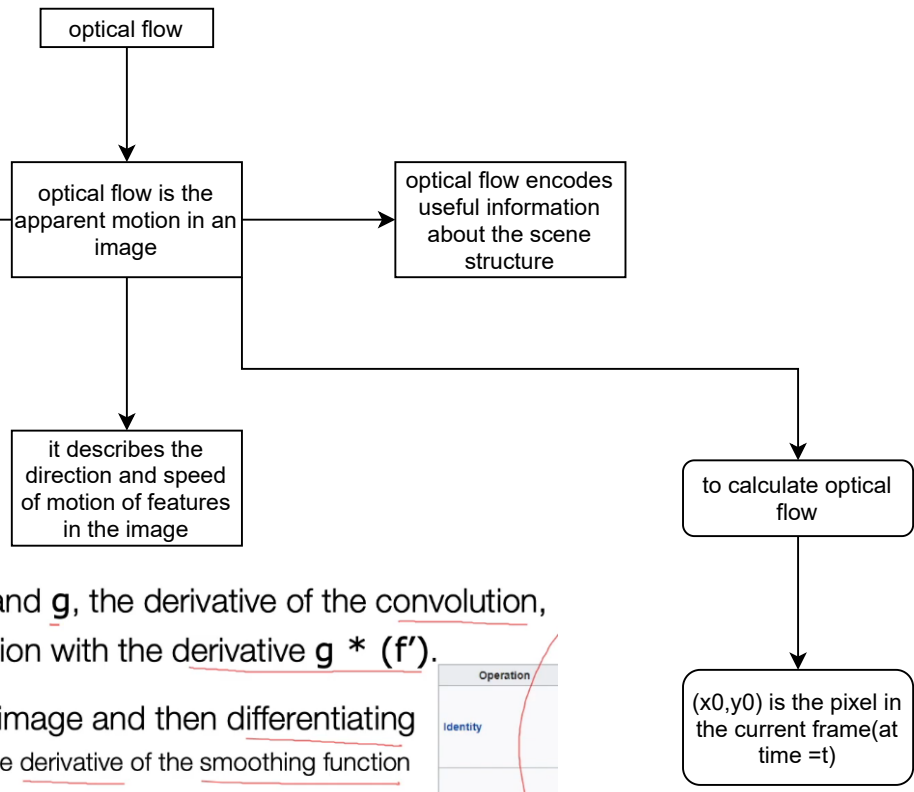
Handwritten notes: 1/p pixel, small, only using 2, 4/p
- Usually $g(x)$ is the image matrix and $f(x)$ is the Gaussian filter. Instead of running u from $-\infty$ to $+\infty$ we usually run it from -3 to $+3$.



Theorem: For any functions f and g , the derivative of the convolution, $(g*f)'$ is equal to the convolution with the derivative $g * (f')$.

- Instead of smoothing the image and then differentiating
 - Convolve the image with the derivative of the smoothing function

Operation
Identity



and \mathbf{g} , the derivative of the convolution, operation with the derivative $\mathbf{g} * (\mathbf{f}')$.

the image and then differentiating the derivative of the smoothing function

Operation
Identity

image patches and corresponding points have similar intensity patterns

Consider a block of pixels centered at pixel p , (x_0, y_0) , at time t

Step 1: We compare this block of pixels with many pixel blocks centered at various candidate pixels $(x_0 + D_x, y_0 + D_y)$ at time $t + D_t$

$(x_0 + D_x, y_0 + D_y)$ is the center of a candidate block at time D_t

$D_x = 5, 2$
 $D_y = 5, 5$

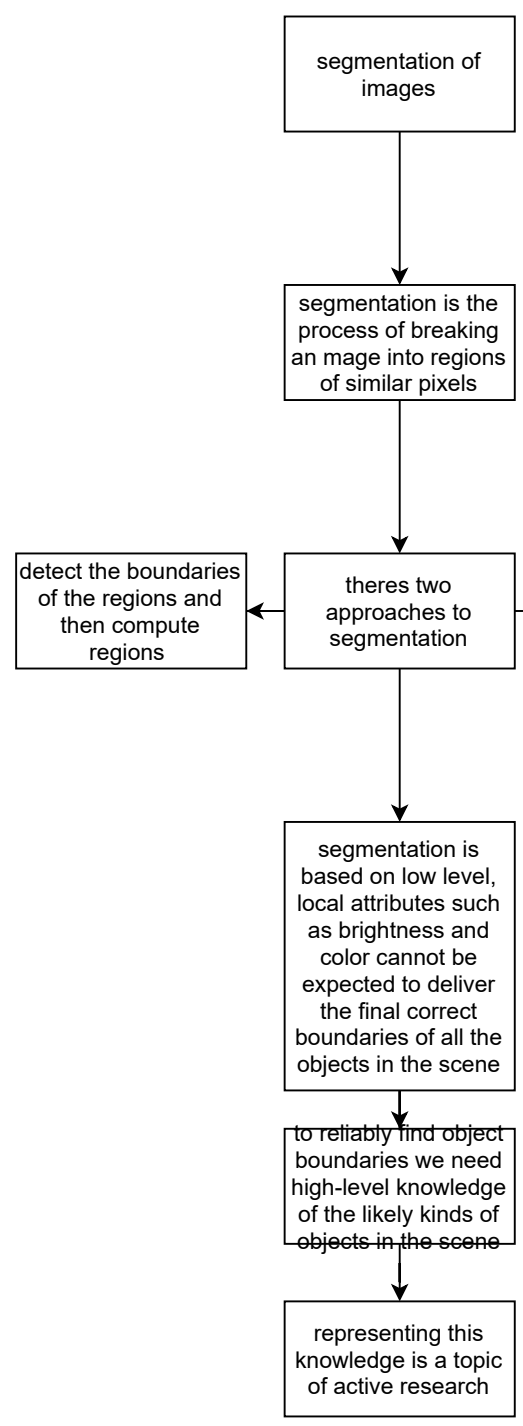
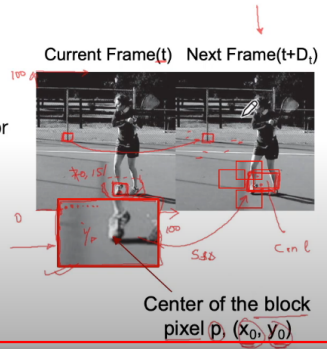
Step 2: Calculate Sum of Squared Differences (SSD) of intensities for each of the many blocks

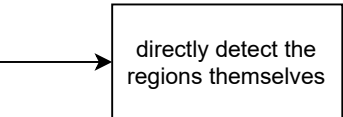
$$SSD(D_x, D_y) = \sum_{(x,y)} (I(x, y, t) - I(x + D_x, y + D_y, t + D_t))^2$$

(x, y) ranges over pixels in the block centered at (x_0, y_0)

Step 3: Find the (D_x, D_y) that minimizes SSD

$-10 \quad +10$





directly detect the
regions themselves