

# **MATHEMATICAL SKILLS**

## **GEARS, GEAR TRAINS AND COMPOUND GEARS**

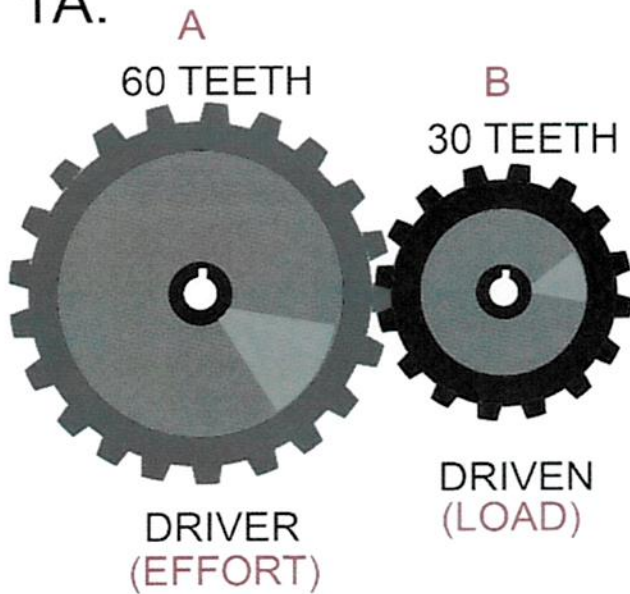
### **ASSOCIATED EXAMINATION QUESTIONS**

#### **DESIGN AND TECHNOLOGY**

# CALCULATING GEAR RATIO (VELOCITY RATIO)

In examinations, one of the first questions will be - to work out the 'gear ratio' (sometimes called velocity ratio). As a guide - always assume that the larger gear revolves one revolution. The number of rotations of the second gear has then to be worked out.

1A.



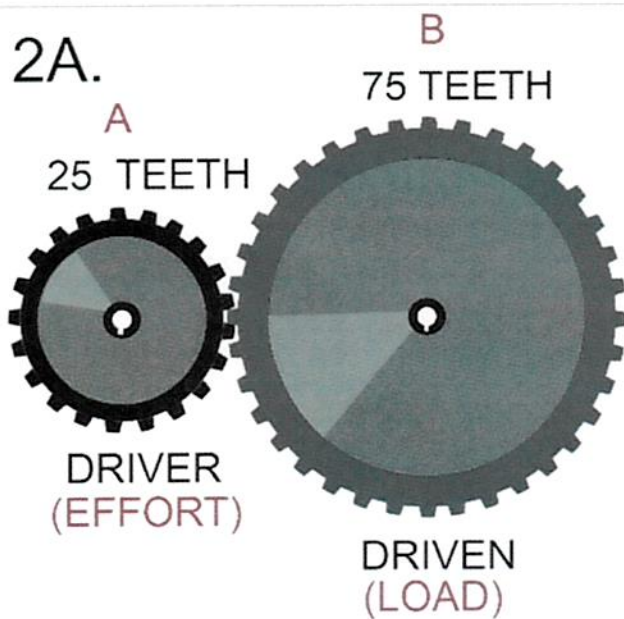
GEAR RATIO / VELOCITY RATIO

$$\frac{\text{Distance moved by Effort}}{\text{Distance moved by Load}} = \underline{\hspace{2cm}}$$

$$= \frac{\text{Input movement}}{\text{Output movement}}$$

$$= \text{Driver : Driven}$$

2A.

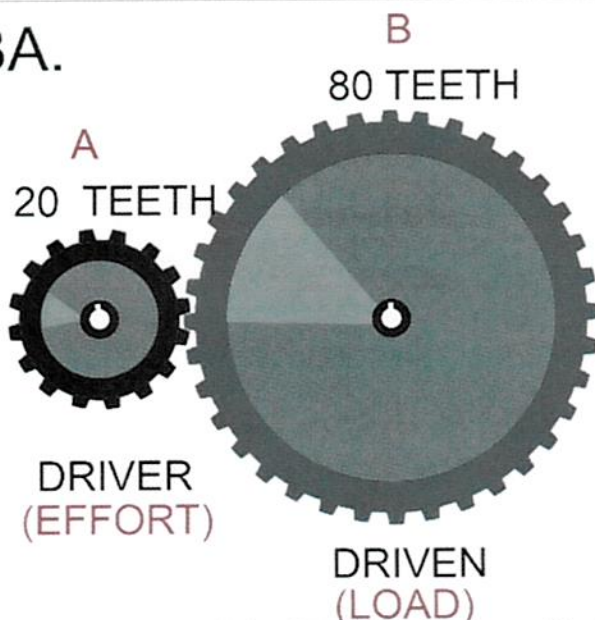


$$\frac{\text{Distance moved by Effort}}{\text{Distance moved by Load}} = \underline{\hspace{2cm}}$$

$$= \frac{\text{Input movement}}{\text{Output movement}}$$

$$= \text{Driver : Driven}$$

3A.



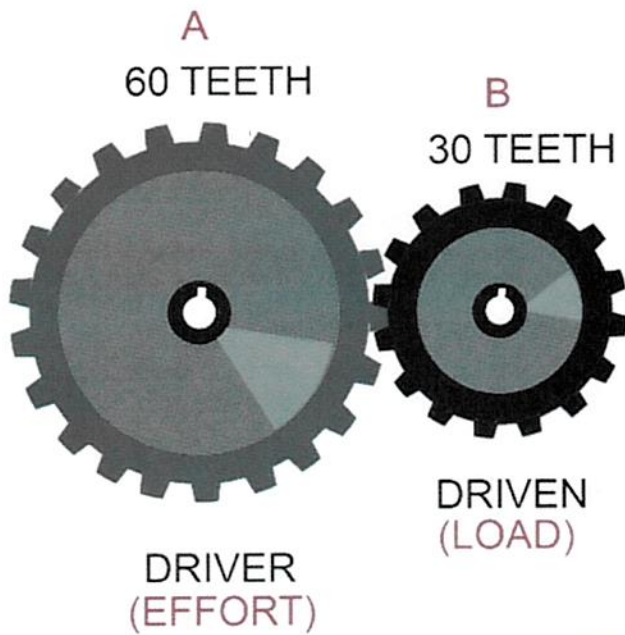
$$\frac{\text{Distance moved by Effort}}{\text{Distance moved by Load}} = \underline{\hspace{2cm}}$$

$$= \frac{\text{Input movement}}{\text{Output movement}}$$

$$= \text{Driver : Driven}$$



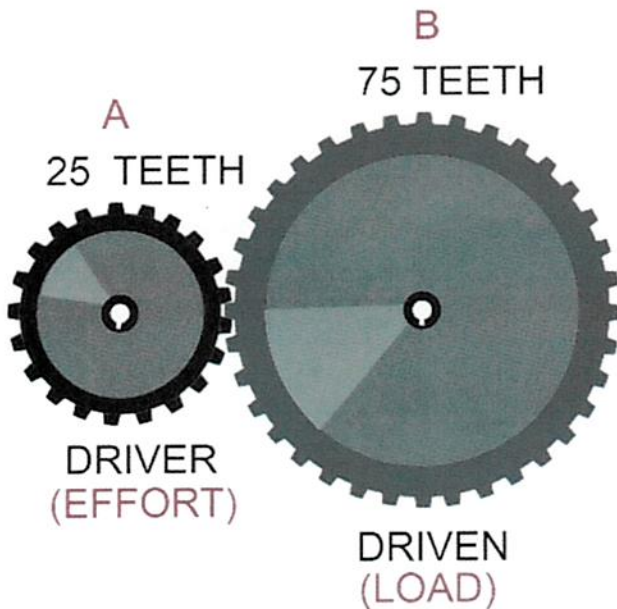
## CALCULATING REVOLUTIONS PER MINUTE (RPM)



GEAR A	GEAR B
60 teeth	30 teeth
120 rpm	

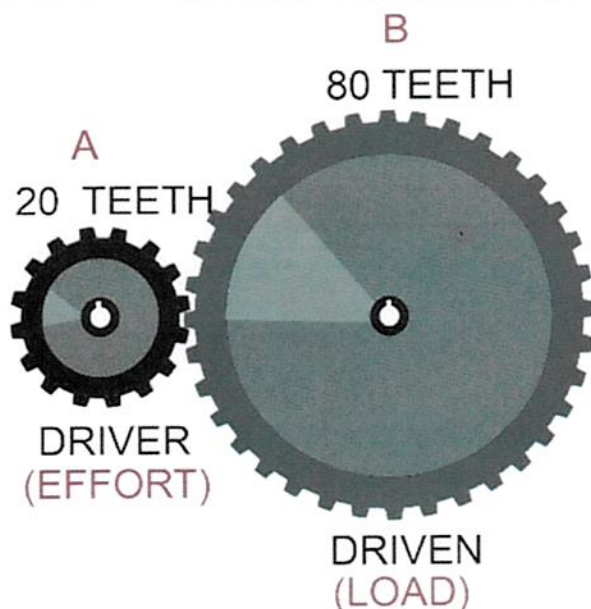
$$\frac{\text{---}}{\text{---}} = \text{---} \text{ revs/min}$$

World Association of Technology Teachers    <https://www.facebook.com/groups/254963448192823/>    V.Ryan © 2025



GEAR A	GEAR B
25 teeth	75 teeth
60 rpm	

$$\frac{\text{---}}{\text{---}} = \text{---} \text{ revs/min}$$

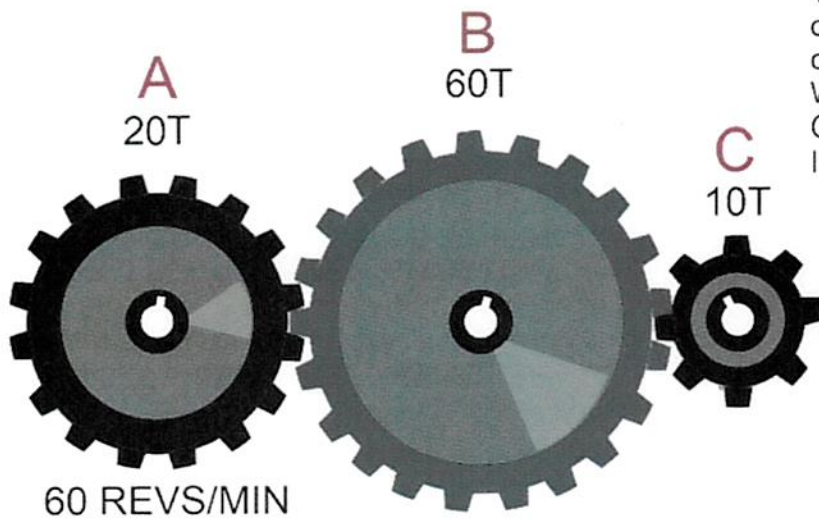


GEAR A	GEAR B
20 teeth	80 teeth
100 rpm	

$$\frac{\text{---}}{\text{---}} = \text{---} \text{ revs/min}$$

## GEAR TRAINS - EXAMPLE QUESTIONS

When faced with three gears the question can be broken down into two parts. First work on Gears A and B. When this has been solved work on gears B and C.



The diagram above shows a gear train composed of three gears. Gear A revolves at 60 revs/min in a clockwise direction.

What is the output in revolutions per minute at Gear C?

In what direction does Gear C revolve ?

GEAR A	GEAR B	GEAR C
20 teeth	60 teeth	10 teeth
60 rpm		

World Association of Technology Teachers    <https://www.facebook.com/groups/254963448192823/>    V.Ryan © 2025

First work out the speed at Gear B.

$$\begin{aligned}
 & \frac{\text{teeth}}{\text{teeth}} \frac{B}{A} = \\
 & = \frac{60_{\text{rpm}}}{\text{}} = \text{ } \text{revs/min at 'B'}
 \end{aligned}$$

(Remember B is larger than A therefore, B outputs less revs/min and is slower)

Next, take B and C. C is smaller, therefore, revs/minute will increase and rotation will be faster.

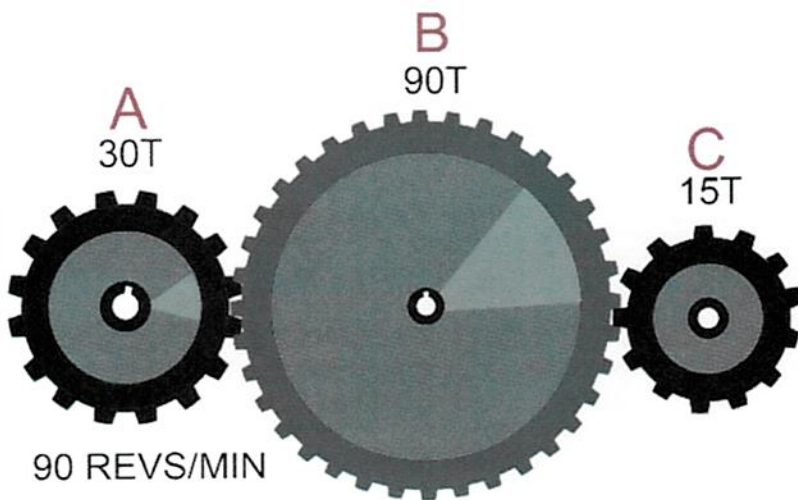
$$\begin{aligned}
 & \frac{\text{teeth}}{\text{teeth}} \frac{B}{C} = \\
 & \text{ } \text{REVS X } \text{ } = \text{ } \text{revs/min at 'C'}
 \end{aligned}$$

What direction does C revolve ?

A is clockwise, B consequently is anti-clockwise and C is therefore \_\_\_\_\_

## GEAR TRAINS - EXAMPLE QUESTIONS AND ANSWERS

When faced with three gears the question can be broken down into two parts. First work on Gears A and B. When this has been solved work on gears B and C.



The diagram opposite shows a gear train composed of three gears. Gear A revolves at 90 revs/min in a clockwise direction.

What is the output in revolutions per minute at Gear C?

In what direction does Gear C revolve?

GEAR A	GEAR B	GEAR C
30 teeth	90 teeth	15 teeth
90 rpm		

World Association of Technology Teachers <https://www.facebook.com/groups/254963448192823/> V.Ryan © 2025

First work out the speed at Gear B.

$$\frac{\text{teeth A}}{\text{teeth B}} = \frac{90 \text{ rpm}}{\text{revs/min at 'B'}}$$

(Remember B is larger than A therefore, B outputs less revs/min and is slower)

Next, take B and C. C is smaller, therefore, revs/minute will increase and rotation will be faster.

$$\frac{\text{teeth B}}{\text{teeth C}} = \frac{\text{revs/min at 'B'}}{\text{revs/min at 'C'}}$$

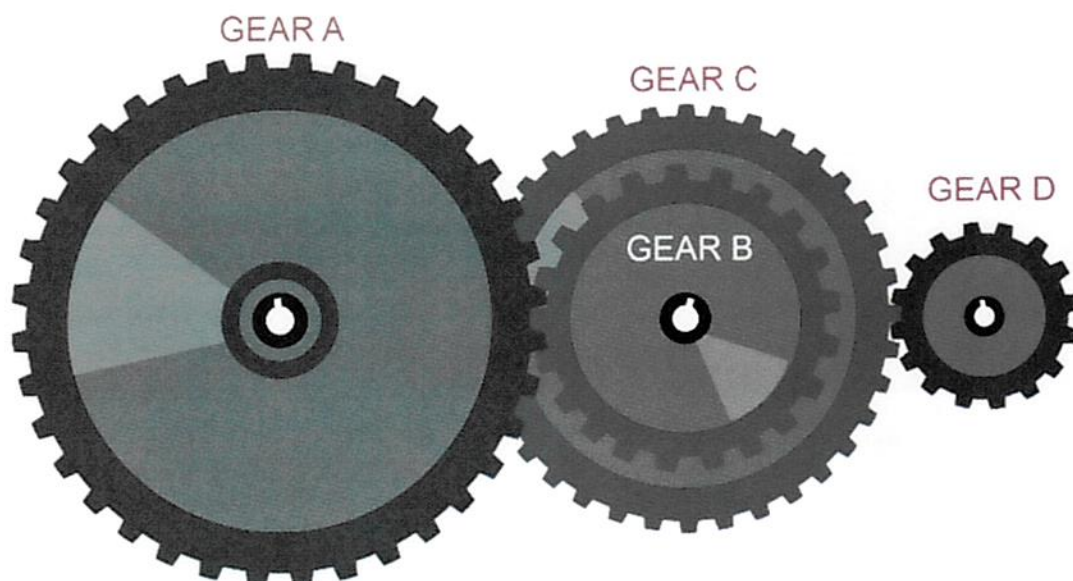
What direction does C revolve?

A is clockwise, B consequently is anti-clockwise and C is therefore \_\_\_\_\_



## COMPOUND GEARS - EXAMPLE QUESTIONS AND ANSWERS

Below is a question regarding 'compound gears'. Gears C and B represent a compound gear as they appear 'fixed' together. When drawn with a compass they have the same centre. Two gears 'fixed' together in this way rotate together and at the same RPM. When answering a question like this split it into two parts. Treat gears A and B as one question AND C and D as the second part.



This is an example of a "compound gear train". Gear A rotates in a clockwise direction at 30 revs/min. What is the output in revs/min at D and what is the direction of rotation?

GEAR A	GEAR B	GEAR C	GEAR D
120 teeth	40 teeth	80 teeth	20 teeth

First find revs/min at Gear B.

$$\frac{\text{teeth}}{\text{teeth}} \frac{B}{A} =$$

$$\underline{\hspace{1cm}} \text{ rpm} \times \underline{\hspace{1cm}} = \underline{\hspace{1cm}} \text{ rpm / min}$$

B is smaller therefore it rotates faster and revs/min increase.

C is fixed to B and therefore, rotates at the same speed.

$$\underline{\hspace{1cm}} \text{ REVS/MIN at C}$$

Next find revs/min at Gear D.

$$\frac{\text{teeth}}{\text{teeth}} \frac{C}{D} =$$

$$\underline{\hspace{1cm}} \text{ rpm (at C)} \times \underline{\hspace{1cm}} = \underline{\hspace{1cm}} \text{ rpm / min}$$

D is smaller than C, therefore rotates faster (increased revs/min).

A revolves in a clockwise direction, B is therefore anti-clockwise, C is fixed to B and is also anti-clockwise, which means D revolves in a \_\_\_\_\_ direction.