

Problem 6.12

```
import tensorflow as tf
import numpy as np
import PIL
import cv2
import os
import sklearn
import pandas as pd
import pickle
import platform
from tqdm.notebook import tqdm
from sklearn.multiclass import OneVsOneClassifier
from sklearn import preprocessing
from sklearn import svm
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler
from scipy import stats as st
```

Computational Environment

```
physical_devices = tf.config.list_physical_devices('GPU')
my_system = platform.uname()
print(physical_devices)
print(f"System: {my_system.system}")
print(f"Node Name: {my_system.node}")
print(f"Release: {my_system.release}")
print(f"Version: {my_system.version}")
print(f"Machine: {my_system.machine}")
print(f"Processor: {my_system.processor}")
```

```
[PhysicalDevice(name='/physical_device:GPU:0', device_type='GPU')]
```

System: Darwin

Node Name: qiushaotings-MacBook-Pro-2.local

Release: 21.5.0

Version: Darwin Kernel Version 21.5.0: Tue Apr 26 21:08:29 PDT 2022; root:xnu-8020.121.3~4/RELEASE_ARM64_T8020

Machine: arm64

Processor: i386

Helper function

```
def load_image(path, width=484, preprocess_input=tf.keras.applications.vgg16.preprocess_in
    """
    Load and Preprocessing image
    """
    img = tf.keras.utils.load_img(path)
    x = tf.keras.utils.img_to_array(img)
    x = x[0:width,:,:]
    x = np.expand_dims(x, axis=0)
    return tf.keras.applications.vgg16.preprocess_input(x)
```

Data inspection

```
dpath = os.path.join("data", "CMU-UHCS_Dataset")
pic_path = os.path.join(dpath, "images")
df_micro = pd.read_csv( os.path.join(dpath, "micrograph.csv"))
df_micro = df_micro[["path", "primary_microconstituent"]]

for i in range(0, len(df_micro)):
    img_ph = os.path.join(pic_path, df_micro.iloc[i][0])
    assert os.path.exists(img_ph)
    df_micro.iloc[i][0] = img_ph
df_micro2 = df_micro.copy()
CLS_rm = ["pearlite+widmanstatten", "martensite", "pearlite+spheroidite"] #(type, sample s

for c in CLS_rm:
    df_micro.drop(df_micro[df_micro["primary_microconstituent"] == c].index, inplace=True)

# labels
name_lbs = df_micro["primary_microconstituent"].unique()
le = preprocessing.LabelEncoder()
le.fit(name_lbs)
list(le.classes_)
```

```
['network', 'pearlite', 'spheroidite', 'spheroidite+widmanstatten']
```

```

dlabel = le.transform(df_micro["primary_microconstituent"])
df_micro.insert(2, "label", dlabel)
df_micro

```

	path	primary_microconstituent	label
0	data/CMU-UHCS_Dataset/images/micrograph1.tif	pearlite	1
1	data/CMU-UHCS_Dataset/images/micrograph2.tif	spheroidite	2
3	data/CMU-UHCS_Dataset/images/micrograph5.tif	pearlite	1
4	data/CMU-UHCS_Dataset/images/micrograph6.tif	spheroidite	2
5	data/CMU-UHCS_Dataset/images/micrograph7.tif	spheroidite+widmanstatten	3
...
955	data/CMU-UHCS_Dataset/images/micrograph1722.tif	spheroidite	2
957	data/CMU-UHCS_Dataset/images/micrograph1726.tif	spheroidite+widmanstatten	3
958	data/CMU-UHCS_Dataset/images/micrograph1730.png	spheroidite	2
959	data/CMU-UHCS_Dataset/images/micrograph1731.tif	pearlite	1
960	data/CMU-UHCS_Dataset/images/micrograph1732.tif	pearlite	1

Data Processing

```

# Train-test split
df_test = df_micro.copy()
df_train = pd.DataFrame(columns = df_micro.keys())

split_info = [("spheroidite", 100),\
               ("network", 100),\
               ("pearlite", 100),\
               ("spheroidite+widmanstatten", 60)] #(type, sample size)

for ln in split_info:
    label, n = ln
    id_train = df_micro[df_micro["primary_microconstituent"] == label][0:n].index
    df_test.drop(id_train, axis=0, inplace=True)
    df_train = pd.concat([df_train, df_micro.loc[id_train]])

df_train

```

	path	primary_microconstituent	label
1	data/CMU-UHCS_Dataset/images/micrograph2.tif	spheroidite	2
4	data/CMU-UHCS_Dataset/images/micrograph6.tif	spheroidite	2
8	data/CMU-UHCS_Dataset/images/micrograph10.png	spheroidite	2
9	data/CMU-UHCS_Dataset/images/micrograph11.tif	spheroidite	2
20	data/CMU-UHCS_Dataset/images/micrograph29.tif	spheroidite	2
...
596	data/CMU-UHCS_Dataset/images/micrograph1093.tif	spheroidite+widmanstatten	3
618	data/CMU-UHCS_Dataset/images/micrograph1129.tif	spheroidite+widmanstatten	3
631	data/CMU-UHCS_Dataset/images/micrograph1156.tif	spheroidite+widmanstatten	3
672	data/CMU-UHCS_Dataset/images/micrograph1218.tif	spheroidite+widmanstatten	3
673	data/CMU-UHCS_Dataset/images/micrograph1219.tif	spheroidite+widmanstatten	3

`df_test`

	path	primary_microconstituent	label
237	data/CMU-UHCS_Dataset/images/micrograph436.png	spheroidite	2
238	data/CMU-UHCS_Dataset/images/micrograph437.tif	spheroidite	2
239	data/CMU-UHCS_Dataset/images/micrograph440.png	spheroidite	2
241	data/CMU-UHCS_Dataset/images/micrograph442.tif	spheroidite	2
242	data/CMU-UHCS_Dataset/images/micrograph443.tif	spheroidite	2
...
955	data/CMU-UHCS_Dataset/images/micrograph1722.tif	spheroidite	2
957	data/CMU-UHCS_Dataset/images/micrograph1726.tif	spheroidite+widmanstatten	3
958	data/CMU-UHCS_Dataset/images/micrograph1730.png	spheroidite	2
959	data/CMU-UHCS_Dataset/images/micrograph1731.tif	pearlite	1
960	data/CMU-UHCS_Dataset/images/micrograph1732.tif	pearlite	1

Feature Extraction

VGG16

```
base_model = tf.keras.applications.vgg16.VGG16(
    include_top=False,
    weights='imagenet',
    input_tensor=None,
    input_shape=None,
    pooling=None,
```

```

        classes=1000,
        classifier_activation='softmax'
    )

    base_model.summary()

```

Model: "vgg16"

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	[(None, None, None, 3)]	0
block1_conv1 (Conv2D)	(None, None, None, 64)	1792
block1_conv2 (Conv2D)	(None, None, None, 64)	36928
block1_pool (MaxPooling2D)	(None, None, None, 64)	0
block2_conv1 (Conv2D)	(None, None, None, 128)	73856
block2_conv2 (Conv2D)	(None, None, None, 128)	147584
block2_pool (MaxPooling2D)	(None, None, None, 128)	0
block3_conv1 (Conv2D)	(None, None, None, 256)	295168
block3_conv2 (Conv2D)	(None, None, None, 256)	590080
block3_conv3 (Conv2D)	(None, None, None, 256)	590080
block3_pool (MaxPooling2D)	(None, None, None, 256)	0
block4_conv1 (Conv2D)	(None, None, None, 512)	1180160
block4_conv2 (Conv2D)	(None, None, None, 512)	2359808
block4_conv3 (Conv2D)	(None, None, None, 512)	2359808
block4_pool (MaxPooling2D)	(None, None, None, 512)	0
block5_conv1 (Conv2D)	(None, None, None, 512)	2359808

```

block5_conv2 (Conv2D)          (None, None, None, 512)    2359808
block5_conv3 (Conv2D)          (None, None, None, 512)    2359808
block5_pool (MaxPooling2D)     (None, None, None, 512)    0
=====
Total params: 14,714,688
Trainable params: 14,714,688
Non-trainable params: 0
-----

```

Use five layers

```

out_layer_ns = ["block{}_pool".format(i) for i in range(1,6)]
out_layer_ns

['block1_pool', 'block2_pool', 'block3_pool', 'block4_pool', 'block5_pool']

# Construct 5 models for feature extraction
extmodel = dict(zip(out_layer_ns, [tf.keras.Model(
    inputs= base_model.input,
    outputs=base_model.get_layer(bk_name).output
) for bk_name in out_layer_ns]))

extmodel

{'block1_pool': <keras.engine.functional.Functional at 0x29f411e20>,
'block2_pool': <keras.engine.functional.Functional at 0x2af72ecd0>,
'block3_pool': <keras.engine.functional.Functional at 0x2b06b63d0>,
'block4_pool': <keras.engine.functional.Functional at 0x2b06be5b0>,
'block5_pool': <keras.engine.functional.Functional at 0x2b06bedf0>}}

# Display output dimensions
out_shapes = [extmodel[m].output_shape[-1] for m in extmodel.keys()]
out_shapes

```

```
[64, 128, 256, 512, 512]
```

```

# Initiate feature maps for testing and training
fs_train = [np.zeros((df_train.shape[0], n_f)) for n_f in out_shapes]
fs_test = [np.zeros((df_test.shape[0], n_f)) for n_f in out_shapes]

features_train = dict(zip(out_layer_ns, fs_train))
features_test = dict(zip(out_layer_ns, fs_test))

features_train

{'block1_pool': array([[0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        ...,
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.])),
 'block2_pool': array([[0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        ...,
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.])),
 'block3_pool': array([[0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        ...,
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.])),
 'block4_pool': array([[0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        ...,
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.])),
 'block5_pool': array([[0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        [0., 0., 0., ..., 0., 0., 0.],
                        ...,

```

```
[0., 0., 0., ..., 0., 0., 0.],
[0., 0., 0., ..., 0., 0., 0.],
[0., 0., 0., ..., 0., 0., 0.]]}]}
```

```
# Feature extraction with VGG16
if os.path.exists(os.path.join(dpath, "feature_train.pkl")) == False:
    for m in tqdm(extmodel.keys()):
        for i, df in enumerate([df_train, df_test]):
            for j, ph in tqdm(enumerate(df["path"])):
                x = load_image(ph)
                xb = extmodel[m].predict(x, verbose = 0) # silence output
                F = np.mean(xb,axis=(0,1,2))
                # Save features
                if i ==0:
                    features_train[m][j, :] = F
                else:
                    features_test[m][j, :] = F

#save file
paths = dict(zip(["train", "test"],\
    [os.path.join(dpath, "feature_{}.pkl".format(n))\
    for n in ["train", "test"]]))
## Create new files
f_train = open(paths["train"], "wb")
f_test = open(paths["test"], "wb")
## Write
pickle.dump(features_train, f_train)
pickle.dump(features_test, f_test)
## Close files
f_train.close()
f_test.close()
```

SVM

```
# load data
ftn = open(paths["train"], "rb")
ftt = open(paths["test"], "rb")
featn = pickle.load(ftn) # train feature
featt = pickle.load(ftt) # test feature
ftn.close()
ftt.close()
```



```
# label
ltrain = df_train[["primary_microconstituent", "label"]].reset_index()
ltest = df_test[["primary_microconstituent", "label"]].reset_index()
```

```
ltrain
```

	index	primary_microconstituent	label
0	1	spheroidite	2
1	4	spheroidite	2
2	8	spheroidite	2
3	9	spheroidite	2
4	20	spheroidite	2
...
355	596	spheroidite+widmanstatten	3
356	618	spheroidite+widmanstatten	3
357	631	spheroidite+widmanstatten	3
358	672	spheroidite+widmanstatten	3
359	673	spheroidite+widmanstatten	3

```
ltest["label"].to_numpy()
```

```
array([2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
        2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
        2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
        2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 2,
        0, 2, 2, 0, 2, 0, 2, 0, 2, 2, 2, 2, 2, 2, 0, 2, 2, 0, 2, 2, 2, 0,
        0, 0, 2, 2, 0, 2, 2, 0, 2, 0, 2, 2, 0, 0, 0, 0, 2, 0, 0, 2, 2, 2,
        2, 2, 0, 0, 2, 2, 0, 2, 2, 2, 2, 0, 2, 2, 0, 0, 2, 2, 2, 2, 0, 2,
        0, 2, 0, 2, 2, 2, 2, 2, 2, 0, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 0,
        0, 2, 2, 2, 2, 0, 0, 2, 2, 2, 2, 0, 2, 2, 2, 2, 2, 0, 2, 2, 2, 2,
        2, 2, 0, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 0, 2, 2, 2, 2, 2, 2, 0, 0,
        2, 0, 2, 2, 0, 2, 0, 2, 2, 3, 0, 2, 2, 0, 3, 2, 2, 0, 0, 2, 0, 2,
        0, 2, 2, 2, 2, 0, 2, 3, 0, 2, 0, 2, 0, 3, 2, 0, 2, 0, 2, 2, 2, 3,
        2, 2, 0, 0, 2, 2, 0, 2, 2, 2, 3, 2, 0, 2, 0, 2, 2, 2, 2, 2, 2, 0,
        0, 2, 0, 2, 0, 0, 2, 0, 3, 0, 2, 2, 2, 2, 3, 3, 0, 2, 0, 0, 2, 0,
        0, 2, 2, 2, 0, 2, 1, 2, 0, 2, 2, 0, 0, 0, 3, 1, 3, 1, 0, 2, 2, 1,
        0, 2, 2, 2, 2, 0, 2, 2, 2, 2, 3, 2, 2, 0, 1, 1, 2, 1, 3, 3, 1, 2,
        2, 0, 3, 0, 2, 0, 2, 2, 2, 3, 0, 2, 2, 2, 0, 0, 3, 1, 1, 1, 0, 1,
```

```

3, 0, 1, 2, 2, 3, 2, 2, 0, 2, 2, 0, 2, 0, 2, 2, 2, 1, 1, 2, 1, 2,
2, 2, 1, 1, 0, 0, 2, 1, 2, 3, 2, 2, 2, 0, 2, 2, 2, 2, 1, 1, 0, 2,
2, 0, 2, 2, 0, 0, 2, 1, 2, 3, 2, 1, 1])

```

```

clf.predict(featt["block1_pool"])

```

```

array([2, 3, 2, 1, 2, 1, 2, 3, 2, 2, 1, 2, 2, 2, 2, 2, 2, 1, 2, 2, 2, 2,
       2, 3, 0, 2, 2, 2, 2, 0, 2, 2, 2, 3, 2, 2, 1, 2, 1, 2, 3, 2, 3, 2,
       2, 2, 3, 2, 3, 2, 2, 3, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 2, 2, 0,
       3, 2, 2, 0, 1, 1, 1, 2, 3, 2, 0, 0, 3, 0, 2, 2, 0, 0, 0, 0, 2, 2,
       3, 2, 1, 3, 2, 2, 0, 0, 2, 1, 2, 2, 2, 3, 0, 2, 2, 0, 3, 2, 2, 2,
       3, 3, 2, 2, 0, 2, 2, 3, 2, 2, 2, 2, 2, 0, 0, 3, 0, 3, 0, 2, 2, 0,
       2, 1, 2, 0, 2, 2, 3, 2, 1, 2, 2, 0, 2, 2, 0, 2, 2, 2, 2, 2, 2, 2,
       0, 2, 0, 0, 2, 2, 2, 2, 2, 0, 0, 0, 0, 0, 2, 0, 2, 1, 2, 2, 2, 2,
       0, 2, 2, 1, 2, 2, 0, 2, 2, 2, 0, 0, 3, 2, 2, 2, 2, 0, 2, 2, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 0, 2, 2, 1, 3, 2, 2, 2, 2, 1, 2, 0,
       2, 2, 3, 2, 0, 0, 2, 2, 2, 2, 0, 2, 2, 2, 2, 2, 0, 2, 2, 0, 2,
       0, 0, 3, 2, 2, 0, 2, 3, 2, 2, 0, 2, 0, 3, 2, 2, 2, 2, 1, 3, 3, 0,
       1, 2, 2, 0, 0, 2, 0, 2, 3, 2, 2, 2, 0, 2, 0, 2, 2, 1, 2, 2, 2, 0,
       0, 2, 2, 2, 3, 2, 2, 0, 2, 0, 2, 2, 3, 0, 3, 1, 0, 2, 3, 2, 2, 2,
       2, 2, 3, 2, 0, 3, 2, 2, 0, 2, 2, 2, 2, 0, 3, 2, 1, 1, 3, 2, 2, 1,
       0, 1, 2, 2, 2, 0, 2, 2, 1, 0, 0, 1, 0, 0, 1, 1, 1, 0, 1, 3, 2, 2,
       2, 2, 1, 2, 2, 3, 2, 2, 2, 0, 2, 3, 0, 2, 0, 0, 3, 1, 1, 1, 0, 1,
       2, 2, 1, 0, 2, 2, 2, 0, 2, 2, 2, 2, 2, 0, 2, 2, 0, 1, 3, 2, 1, 2,
       2, 2, 2, 1, 2, 3, 2, 0, 2, 2, 2, 2, 0, 0, 1, 3, 0, 2, 1, 2, 3, 1,
       2, 2, 2, 2, 0, 0, 1, 1, 0, 3, 2, 1, 1])

```

One-to-One SVM

```

class One2OneSVM:
    def __init__(self, n_class=4):
        self.n_class = n_class
        self.clfs = [[svm.SVC(kernel="rbf", C=1., gamma="auto")\
                       for i in range(0,self.n_class)]\
                      for j in range(0,self.n_class)]
        self.cv = np.zeros((self.n_class,self.n_class))
    def train(self, ltrain, feature, fold=10):
        # traversal all features
        for i in range(0, self.n_class-1):
            lis = ltrain[ltrain["label"] == i].index.to_numpy()

```

```

        for j in range(i+1, self.n_class):
            ljs = ltrain[ltrain["label"] == j].index.to_numpy()
            # Data
            X = np.concatenate(\
                (feature[lis,:],\
                 feature[ljs,:]), axis=0)
            Y = np.concatenate((np.ones(len(lis))*i,np.ones(len(ljs))*j))
            # Train SVM
            scores = sklearn.model_selection.cross_val_score(self.clfs[i][j], X, Y, cv=5)
            self.clfs[i][j].fit(X,Y)
            self.cv[i][j] = np.max(scores)

def test_1v1_error(self, ltest, feature):
    # traversal all features
    errM = np.zeros((self.n_class, self.n_class))
    for i in range(0, self.n_class-1):
        lis = ltest[ltest["label"] == i].index.to_numpy()
        for j in range(i+1, self.n_class):
            ljs = ltest[ltest["label"] == j].index.to_numpy()
            # Data
            X = np.concatenate(\
                (feature[lis,:],\
                 feature[ljs,:]), axis=0)
            Y = np.concatenate((np.ones(len(lis))*i,np.ones(len(ljs))*j))
            # Train SVM
            y_pred = self.clfs[i][j].predict(X)
            errM[i,j] = error(Y, y_pred)
    return errM

def predict(self, feature):
    predM = np.zeros((int(self.n_class * (self.n_class -1)/2), feature.shape[0]))
    c = 0
    for i in range(0, self.n_class-1):
        for j in range(i+1, self.n_class):
            predM[c,:] = self.clfs[i][j].predict(feature)
            c += 1
    return st.mode(predM, axis=0, keepdims=True).mode[0,:] #majority voting

def error(ans, pred):
    assert len(ans) == len(pred)
    return (ans != pred).sum()/float(ans.size)

```

(a)

The convolution layer used and the cross-validated error estimate for each of the six pairwise two-label classifiers

(b)

Separate test error rates on the unused micrographs of each of the four categories, for the pairwise two-label classifiers and the multilabel one-vs-one voting classifier described previously. For the pairwise classifiers use only the test micrographs with the two labels used to train the classifier. For the multilabel classifier, use the test micrographs with the corresponding four labels.

```
def df_cv(m, clf, info=""):
    var1 = []
    var2 = []
    cvs = []
    errs = []
    for i in range(0, m.shape[0]-1):
        for j in range(i+1, m.shape[0]):
            var1.append(i)
            var2.append(j)
            cvs.append(clf.cv[i,j])
            errs.append(m[i,j])
    infos = [info] * len(errs)
    return pd.DataFrame({"Info": infos, "Label 1": var1, "Label 2": var2, "Test error": errs})
```

Pair-wise classifier

```
df_errors = []
for b in out_layer_ns:
    clf1 = One2OneSVM()
    clf1.train(ltrain, features_train[b])
    errs = clf1.test_1v1_error(ltest, features_test[b])
    df_errors.append(df_cv(errs, clf1, b))

res_error = pd.concat(df_errors)
res_error
```

	Info	Label 1	Label 2	Test error	Cross Validation Score
0	block1_pool	0	1	0.823529	0.500
1	block1_pool	0	2	0.290155	0.550
2	block1_pool	0	3	0.157895	0.625
3	block1_pool	1	2	0.906040	0.500
4	block1_pool	1	3	0.466667	0.625
5	block1_pool	2	3	0.071186	0.625
0	block2_pool	0	1	0.823529	0.650
1	block2_pool	0	2	0.709845	0.650
2	block2_pool	0	3	0.157895	0.625
3	block2_pool	1	2	0.919463	0.500
4	block2_pool	1	3	0.466667	0.625
5	block2_pool	2	3	0.071186	0.625
0	block3_pool	0	1	0.823529	0.600
1	block3_pool	0	2	0.290155	0.600
2	block3_pool	0	3	0.157895	0.625
3	block3_pool	1	2	0.080537	0.550
4	block3_pool	1	3	0.466667	0.625
5	block3_pool	2	3	0.071186	0.625
0	block4_pool	0	1	0.823529	0.500
1	block4_pool	0	2	0.290155	0.550
2	block4_pool	0	3	0.157895	0.625
3	block4_pool	1	2	0.080537	0.500
4	block4_pool	1	3	0.466667	0.625
5	block4_pool	2	3	0.071186	0.625
0	block5_pool	0	1	0.073529	1.000
1	block5_pool	0	2	0.033679	1.000
2	block5_pool	0	3	0.060150	1.000
3	block5_pool	1	2	0.000000	1.000
4	block5_pool	1	3	0.088889	1.000
5	block5_pool	2	3	0.061017	0.875

Multiple one-vs-one classifier

```
# Multiclass one-vs-one
dfm_errors = []
for b in out_layer_ns:
    clf = OneVsOneClassifier(svm.SVC(kernel="rbf", C=1., gamma="auto").fit(features_train[
        ltrain["label"].to_numpy(int)))
    clf.fit(features_train[b],\
```

```

        ltrain["label"].to_numpy(int))
    y_predm = clf.predict(features_test[b])
    dfm_errors.append(1 - error(y_predm, ltest["label"].to_numpy()))

# Display result
res_multi1v1 = pd.DataFrame({"Info": out_layer_ns, "Score": dfm_errors})
res_multi1v1

```

	Info	Score
0	block1_pool	0.064965
1	block2_pool	0.055684
2	block3_pool	0.635731
3	block4_pool	0.635731
4	block5_pool	0.928074

(c)

For the mixed pearlite + spheroidite test micrographs, apply the trained pairwise classifier for pearlite vs. spheroidite and the multilabel voting classifier. Print the predicted labels by these two classifiers side by side (one row for each test micrograph). Comment your results

The pairwise SVM classifier performs better than Multiclass one-to-one classifier. Because the pairwise SVM is specialized for the binary problem and not be interfered with other classification setting.

```

ltestm = ltest[(ltest["primary_microconstituent"] == "pearlite") | \
               (ltest["primary_microconstituent"] == "spheroidite")]
feature_m = features_test["block5_pool"][ltestm.index.to_numpy(), :]
l = le.transform(["pearlite", "spheroidite"])

pred_pairs = clf1.clfs[l[0]][l[1]].predict(feature_m)
pred_multi = clf.predict(feature_m)

res_ps = pd.DataFrame({"Test Label": le.inverse_transform(ltestm["label"]), \
                      "Pairwise (pearlite vs. spheroidite)": le.inverse_transform(pred_pairs.astype(int)), \
                      "Multi-OnevsOne": le.inverse_transform(pred_multi)})

print(res_ps.to_string())

```

	Test Label	Pairwise (pearlite vs. spheroidite)	Multi-OnevsOne
0	spheroidite	spheroidite	spheroidite
1	spheroidite	spheroidite	spheroidite
2	spheroidite	spheroidite	spheroidite
3	spheroidite	spheroidite	spheroidite
4	spheroidite	spheroidite	spheroidite
5	spheroidite	spheroidite	spheroidite
6	spheroidite	spheroidite	spheroidite
7	spheroidite	spheroidite	spheroidite
8	spheroidite	spheroidite	spheroidite
9	spheroidite	spheroidite	spheroidite
10	spheroidite	spheroidite	spheroidite
11	spheroidite	spheroidite	spheroidite
12	spheroidite	spheroidite	spheroidite
13	spheroidite	spheroidite	spheroidite
14	spheroidite	spheroidite	spheroidite
15	spheroidite	spheroidite	spheroidite
16	spheroidite	spheroidite	spheroidite
17	spheroidite	spheroidite	spheroidite
18	spheroidite	spheroidite	spheroidite
19	spheroidite	spheroidite	spheroidite
20	spheroidite	spheroidite	spheroidite
21	spheroidite	spheroidite	spheroidite
22	spheroidite	spheroidite	spheroidite
23	spheroidite	spheroidite	spheroidite+widmanstatten
24	spheroidite	spheroidite	spheroidite
25	spheroidite	spheroidite	spheroidite
26	spheroidite	spheroidite	spheroidite
27	spheroidite	spheroidite	spheroidite+widmanstatten
28	spheroidite	spheroidite	spheroidite
29	spheroidite	spheroidite	spheroidite
30	spheroidite	spheroidite	spheroidite
31	spheroidite	spheroidite	spheroidite
32	spheroidite	spheroidite	spheroidite
33	spheroidite	spheroidite	spheroidite
34	spheroidite	spheroidite	spheroidite
35	spheroidite	spheroidite	spheroidite
36	spheroidite	spheroidite	spheroidite
37	spheroidite	spheroidite	spheroidite
38	spheroidite	spheroidite	spheroidite
39	spheroidite	spheroidite	spheroidite
40	spheroidite	spheroidite	spheroidite+widmanstatten
41	spheroidite	spheroidite	spheroidite

42	spheroidite	spheroidite	spheroidite
43	spheroidite	spheroidite	spheroidite
44	spheroidite	spheroidite	spheroidite
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88	spheroidite	spheroidite	spheroidite
89	spheroidite	spheroidite	spheroidite
90	spheroidite	spheroidite	spheroidite+widmanstatten
91	spheroidite	spheroidite	spheroidite
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112	spheroidite	spheroidite	spheroidite+widmanstatten
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166	spheroidite	spheroidite	network
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178	spheroidite	spheroidite	spheroidite+widmanstatten
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190	spheroidite	spheroidite	spheroidite+widmanstatten
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215	spheroidite	spheroidite	spheroidite
216	spheroidite	spheroidite	spheroidite
217	spheroidite	spheroidite	spheroidite
218	spheroidite	spheroidite	spheroidite+widmanstatten
219	pearlite	pearlite	pearlite
220	spheroidite	spheroidite	spheroidite
221	spheroidite	spheroidite	spheroidite
222	spheroidite	spheroidite	spheroidite
223	pearlite	pearlite	pearlite
224	pearlite	pearlite	pearlite
225	spheroidite	spheroidite	spheroidite
226	spheroidite	spheroidite	spheroidite
227	pearlite	pearlite	pearlite
228	spheroidite	spheroidite	spheroidite
229	spheroidite	spheroidite	spheroidite
230	spheroidite	spheroidite	spheroidite
231	spheroidite	spheroidite	spheroidite
232	spheroidite	spheroidite	spheroidite
233	spheroidite	spheroidite	network
234	spheroidite	spheroidite	spheroidite
235	spheroidite	spheroidite	spheroidite+widmanstatten
236	spheroidite	spheroidite	spheroidite
237	spheroidite	spheroidite	spheroidite
238	pearlite	pearlite	pearlite
239	pearlite	pearlite	pearlite
240	spheroidite	spheroidite	spheroidite
241	pearlite	pearlite	pearlite
242	pearlite	pearlite	pearlite
243	spheroidite	spheroidite	spheroidite
244	spheroidite	spheroidite	spheroidite
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246	spheroidite	spheroidite	spheroidite
247	spheroidite	spheroidite	spheroidite
248	spheroidite	spheroidite	spheroidite
249	spheroidite	spheroidite	spheroidite
250	spheroidite	spheroidite	spheroidite
251	spheroidite	spheroidite	spheroidite
252	pearlite	pearlite	pearlite
253	pearlite	pearlite	pearlite
254	pearlite	pearlite	pearlite
255	pearlite	pearlite	pearlite
256	pearlite	pearlite	pearlite

257	spheroidite	spheroidite	spheroidite
258	spheroidite	spheroidite	spheroidite
259	spheroidite	spheroidite	spheroidite
260	spheroidite	spheroidite	spheroidite
261	spheroidite	spheroidite	spheroidite
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263	spheroidite	spheroidite	spheroidite
264	spheroidite	spheroidite	spheroidite
265	spheroidite	spheroidite	spheroidite
266	spheroidite	spheroidite	spheroidite
267	pearlite	pearlite	pearlite
268	pearlite	pearlite	pearlite
269	spheroidite	spheroidite	spheroidite
270	pearlite	pearlite	pearlite
271	spheroidite	spheroidite	spheroidite
272	spheroidite	spheroidite	spheroidite
273	spheroidite	spheroidite	spheroidite
274	pearlite	pearlite	pearlite
275	pearlite	pearlite	pearlite
276	spheroidite	spheroidite	spheroidite
277	pearlite	pearlite	pearlite
278	spheroidite	spheroidite	spheroidite
279	spheroidite	spheroidite	spheroidite
280	spheroidite	spheroidite	spheroidite
281	spheroidite	spheroidite	spheroidite
282	spheroidite	spheroidite	spheroidite
283	spheroidite	spheroidite	spheroidite
284	spheroidite	spheroidite	spheroidite
285	spheroidite	spheroidite	spheroidite
286	pearlite	pearlite	pearlite
287	pearlite	pearlite	pearlite
288	spheroidite	spheroidite	spheroidite
289	spheroidite	spheroidite	spheroidite
290	spheroidite	spheroidite	spheroidite
291	spheroidite	spheroidite	spheroidite
292	spheroidite	spheroidite	spheroidite
293	pearlite	pearlite	pearlite
294	spheroidite	spheroidite	spheroidite
295	spheroidite	spheroidite	spheroidite
296	pearlite	pearlite	pearlite
297	pearlite	pearlite	pearlite

(d)

Now apply the multilabel classifier on the pearlite + Widmanstatten and martensite micrographs and print the predicted labels. Compare to the results in part (c)

There is no specific relation for these unseen datasets. The prediction can not extrapolate, and (c) has preferred prediction accuracy and consistency.

```
df_micro2 = df_micro2[(df_micro2["primary_microconstituent"] == "pearlite+widmanstatten")
(df_micro2["primary_microconstituent"] == "martensite")]

# Encode labels
le2 = preprocessing.LabelEncoder()
le2.fit(df_micro2["primary_microconstituent"].unique())
list(le2.classes_)
```

```
['martensite', 'pearlite+widmanstatten']
```

```
dlabel2 = le2.transform(df_micro2["primary_microconstituent"])
df_micro2.insert(2, "label", dlabel2)
```

```
df_micro2
```

	path	primary_microconstituent	label
15	data/CMU-UHCS_Dataset/images/micrograph20.tif	martensite	0
29	data/CMU-UHCS_Dataset/images/micrograph41.tif	martensite	0
31	data/CMU-UHCS_Dataset/images/micrograph44.tif	martensite	0
63	data/CMU-UHCS_Dataset/images/micrograph99.tif	martensite	0
71	data/CMU-UHCS_Dataset/images/micrograph114.tif	martensite	0
...
892	data/CMU-UHCS_Dataset/images/micrograph1599.tif	martensite	0
936	data/CMU-UHCS_Dataset/images/micrograph1684.tif	pearlite+widmanstatten	1
942	data/CMU-UHCS_Dataset/images/micrograph1697.tif	martensite	0
944	data/CMU-UHCS_Dataset/images/micrograph1700.tif	martensite	0
956	data/CMU-UHCS_Dataset/images/micrograph1723.tif	martensite	0

```

# Feature extraction with VGG16
if os.path.exists(os.path.join(dpath, "feature_test2.pkl")) == False:
    fs_test2 = np.zeros((df_micro2.shape[0], out_shapes[-1]))
    m = "block5_pool"
    for j, ph in tqdm(enumerate(df_micro2["path"])):
        x = load_image(ph)
        xb = extmodel[m].predict(x, verbose = 0) # silence output
        F = np.mean(xb,axis=(0,1,2))
        # Save features
        fs_test2[j, :] = F

    # Save data
    ## Create new files
    fs_test2_p = open(os.path.join(dpath, "feature_test2.pkl"), "wb")
    ## Write
    pickle.dump(fs_test2, fs_test2_p)
    ## Close files
    fs_test2_p.close()

#load data
fs_test2_p = open(os.path.join(dpath, "feature_test2.pkl"), "rb")
fs_test2 = pickle.load(fs_test2_p) # train feature
fs_test2_p.close()

pred_multi2 = clf.predict(fs_test2)

res_ps2 = pd.DataFrame({"Test Label": le2.inverse_transform(df_micro2["label"]),\
                        "Multi-OnevsOne": le.inverse_transform(pred_multi2)})

print(res_ps2.to_string())

```

	Test Label	Multi-OnevsOne
0	martensite	spheroidite
1	martensite	network
2	martensite	pearlite
3	martensite	spheroidite
4	martensite	spheroidite
5	martensite	network
6	martensite	spheroidite
7	pearlite+widmanstatten	pearlite

8	martensite	pearlite
9	martensite	spheroidite
10	martensite	spheroidite
11	pearlite+widmanstatten	pearlite
12	martensite	pearlite
13	pearlite+widmanstatten	pearlite
14	martensite	pearlite
15	pearlite+widmanstatten	spheroidite
16	pearlite+widmanstatten	spheroidite+widmanstatten
17	pearlite+widmanstatten	pearlite
18	martensite	pearlite
19	pearlite+widmanstatten	spheroidite
20	pearlite+widmanstatten	pearlite
21	pearlite+widmanstatten	spheroidite
22	pearlite+widmanstatten	spheroidite
23	pearlite+widmanstatten	pearlite
24	pearlite+widmanstatten	pearlite
25	martensite	pearlite
26	martensite	spheroidite
27	martensite	pearlite
28	martensite	spheroidite
29	martensite	pearlite
30	martensite	spheroidite
31	martensite	pearlite
32	pearlite+widmanstatten	pearlite
33	martensite	pearlite
34	martensite	spheroidite
35	pearlite+widmanstatten	spheroidite
36	martensite	spheroidite
37	pearlite+widmanstatten	spheroidite
38	pearlite+widmanstatten	pearlite
39	pearlite+widmanstatten	pearlite
40	martensite	pearlite
41	martensite	spheroidite
42	pearlite+widmanstatten	pearlite
43	pearlite+widmanstatten	spheroidite
44	pearlite+widmanstatten	spheroidite+widmanstatten
45	pearlite+widmanstatten	pearlite
46	pearlite+widmanstatten	pearlite
47	martensite	pearlite
48	pearlite+widmanstatten	pearlite
49	martensite	pearlite
50	pearlite+widmanstatten	spheroidite+widmanstatten

51	pearlite+widmanstatten	pearlite
52	martensite	pearlite
53	pearlite+widmanstatten	spheroidite
54	martensite	spheroidite
55	martensite	spheroidite
56	martensite	pearlite
57	martensite	network
58	martensite	spheroidite
59	pearlite+widmanstatten	pearlite
60	martensite	spheroidite
61	martensite	pearlite
62	martensite	spheroidite