Machine Learning: Programming Exercise 3

Multi-class Classification and Neural Networks

In this exercise, you will implement one-vs-all logistic regression and neural networks to recognize hand-written digits.

Files needed for this exercise

- ex3.mlx MATLAB Live Script that steps you through the exercise
- ex3data1.mat Training set of hand-written digits
- ex3weights.mat Initial weights for the neural network exercise
- submit.m Submission script that sends your solutions to our servers
- displayData.m Function to help visualize the dataset
- fmincg.m Function minimization routine (similar to fminunc)
- sigmoid.m Sigmoid function
- *lrCostFunction.m Logistic regression cost function
- *oneVsAll.m Train a one-vs-all multi-class classifier
- *predictOneVsAll.m Predict using a one-vs-all multi-class classifier
- *predict.m Neural network prediction function

*indicates files you will need to complete

Confirm that your Current Folder is set correctly

Click into this section, then click the 'Run section' button above. This will execute the dir command below to list the files in your Current Folder. The output should contain all of the files listed above and the 'lib' folder. If it does not, right-click the 'ex3' folder and select 'Open' before proceding or see the instructions in README.mlx for more details.

dir					
	displayData.m	ex3_companion.mat	ex3data1.mat	fmincg.m	lrCostFunc
• •	ex3.mlx	ex3_companion.mlx	ex3weights.mat	lib	lrCostFunc

Before you begin

The workflow for completing and submitting the programming exercises in MATLAB Online differs from the original course instructions. Before beginning this exercise, make sure you have read through the instructions in README.mlx which is included with the programming exercise files. README also contains solutions to the many common issues you may encounter while completing and submitting the exercises in MATLAB Online. Make sure you are following instructions in README and have checked for an existing solution before seeking help on the discussion forums.

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1. Multi-class Classification

For this exercise, you will use logistic regression and neural networks to recognize handwritten digits (from 0 to 9). Automated handwritten digit recognition is widely used today - from recognizing zip codes (postal codes) on mail envelopes to recognizing amounts written on bank checks. This exercise will show you how the methods you've learned can be used for this classication task. In the first part of the exercise, you will extend your previous implemention of logistic regression and apply it to one-vs-all classification.

1.1 Dataset

You are given a data set in ex3data1.mat that contains 5000 training examples of handwritten digits*. The .mat format means that that the data has been saved in a native MATLAB matrix format, instead of a text (ASCII) format like a csv-file. These matrices can be read directly into your program by using the load command. After loading, matrices of the correct dimensions and values will appear in your program's memory. The matrix will already be named, so you do not need to assign names to them.

*This is a subset of the MNIST handwritten digit dataset

Run the code below to load the data.

```
% Load saved matrices from file
load('ex3data1.mat');
% The matrices X and y will now be in your MATLAB environment
```

There are 5000 training examples in ex3data1.mat, where each training example is a 20 pixel by 20 pixel grayscale image of the digit. Each pixel is represented by a floating point number indicating the grayscale intensity at that location. The 20 by 20 grid of pixels is 'unrolled' into a 400-dimensional vector. Each of these training examples becomes a single row in our data matrix X. This gives us a 5000 by 400 matrix X where every row is a training example for a handwritten digit image.

$$X = \begin{bmatrix} -(x^{(1)})^T - \\ -(x^{(2)})^T - \\ \vdots \\ -(x^{(m)})^T - \end{bmatrix}$$

The second part of the training set is a 5000-dimensional vector y that contains labels for the training set. To make things more compatible with MATLAB indexing, where there is no zero index, we have mapped the digit zero to the value ten. Therefore, a '0' digit is labeled as '10', while the digits '1' to '9' are labeled as '1' to '9' in their natural order.

1.2 Visualizing the data

You will begin by visualizing a subset of the training set. The code below randomly selects selects 100 rows from X and passes those rows to the displayData function. This function maps each row to a 20 pixel by 20 pixel grayscale image and displays the images together. We have provided the displayData function, and you are encouraged to examine the code to see how it works. After you run this step, you should see an image like Figure 1.

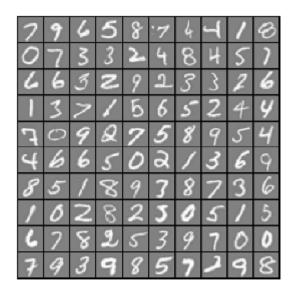
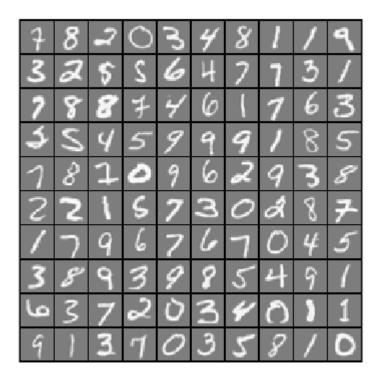


Figure 1: Examples from the dataset



1.3 Vectorizing logistic regression

You will be using multiple one-vs-all logistic regression models to build a multi-class classifier. Since there are 10 classes, you will need to train 10 separate logistic regression classifiers. To make this training efficient, it is important to ensure that your code is well vectorized. In this section, you will implement a vectorized version of logistic regression that does not employ any for loops. You can use your code in the last exercise as a starting point for this exercise.

1.3.1 Vectorizing the cost function

We will begin by writing a vectorized version of the cost function. Recall that in (unregularized) logistic regression, the cost function is

$$J(\theta) = \frac{1}{m} \sum_{i=1}^{m} \left[-y^{(i)} \log(h_{\theta}(x^{(i)})) - (1-y^{(i)}) \log(1-h_{\theta}(x^{(i)})) \right],$$

To compute each element in the summation, we have to compute $h_{\theta}(x^{(i)})$ for every example i, where $h_{\theta}(x^{(i)}) = g(\theta^T x^{(i)})$ and $g(z) = \frac{1}{1 + e^{-z}}$ is the sigmoid function. It turns out that we can compute this quickly for all our examples by using matrix multiplication. Let us define X and θ as

$$X\theta = \begin{bmatrix} -(x^{(1)})^T \theta & - \\ -(x^{(2)})^T \theta & - \\ \vdots \\ -(x^{(m)})^T \theta & - \end{bmatrix} = \begin{bmatrix} -\theta^T(x^{(1)}) - \\ -\theta^T(x^{(2)}) & - \\ \vdots \\ -\theta^T(x^{(m)}) & - \end{bmatrix}$$

In the last equality, we used the fact that $a^Tb = b^Ta$ if a and b are vectors. This allows us to compute the products $\theta^T x^{(i)}$ for all our examples i in one line of code.

Your job is to write the unregularized cost function in the file 1rCostFunction.m Your implementation should use the strategy we presented above to calculate $\theta^T x^{(i)}$. You should also use a vectorized approach for the rest of the cost function. A fully vectorized version of 1rCostFunction.m should not contain any loops. (Hint: You might want to use the element-wise multiplication operation (.*) and the sum operation sum when writing this function)

1.3.2 Vectorizing the gradient

Recall that the gradient of the (unregularized) logistic regression cost is a vector where the *j*th element is defined as

$$\frac{\partial J(\theta)}{\partial \theta_i} = \frac{1}{m} \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_j^{(i)}$$

To vectorize this operation over the dataset, we start by writing out all the partial derivatives explicitly for all θ_i ,

$$\begin{bmatrix} \frac{\partial J(\theta)}{\partial \theta_{0}} \\ \frac{\partial J(\theta)}{\partial \theta_{1}} \\ \frac{\partial J(\theta)}{\partial \theta_{2}} \\ \vdots \\ \frac{\partial J(\theta)}{\partial \theta_{n}} \end{bmatrix} = \frac{1}{m} \begin{bmatrix} \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_{0}^{(i)} \\ \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_{1}^{(i)} \\ \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_{2}^{(i)} \\ \vdots \\ \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_{n}^{(i)} \end{bmatrix} = \frac{1}{m} \sum_{i=1}^{m} \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_{0}^{(i)} = \frac{1}{m} X^{T} (h_{\theta}(x) - y)$$

$$(1)$$

where

$$h_{\theta}(x) - y = \begin{bmatrix} h_{\theta}(x^{(1)}) - y^{(1)} \\ h_{\theta}(x^{(2)}) - y^{(2)} \\ \vdots \\ h_{\theta}(x^{(m)}) - y^{(m)} \end{bmatrix}$$

Note that $x^{(i)}$ is a vector, while $(h_{\theta}(x^{(i)}) - y^{(i)})$ is a scalar (single number). To understand the last step of the derivation, let $\beta_i = (h_{\theta}(x^{(i)}) - y^{(i)})$ and observe that:

$$\sum_{i} \beta_{i} x^{(i)} = \begin{bmatrix} | & | & | & | \\ x^{(1)} & x^{(2)} & \dots & x^{(m)} \end{bmatrix} \begin{bmatrix} \beta_{1} \\ \beta_{2} \\ \vdots \\ \beta_{m} \end{bmatrix} = X^{T} \beta,$$

The expression above allows us to compute all the partial derivatives without any loops. If you are comfortable with linear algebra, we encourage you to work through the matrix multiplications above to convince yourself that the vectorized version does the same computations. You should now implement Equation (1) to compute the correct vectorized gradient. Once you are done, complete the function 1rCostFunction.m by implementing the gradient.

Debugging Tip: Vectorizing code can sometimes be tricky. One common strategy for debugging is to print out the sizes of the matrices you are working with using the size function. For example, given a data matrix X of size 100 x 20 (100 examples, 20 features) and θ , a vector with dimensions 20 x 1, you can observe that $X\theta$ is a valid multiplication operation, while θX is not. Furthermore, if you have a non-vectorized version of your code, you can compare the output of your vectorized code and non-vectorized code to make sure that they produce the same outputs.

1.3.3 Vectorizing regularized logistic regression

After you have implemented vectorization for logistic regression, you will now add regularization to the cost function. Recall that for regularized logistic regression, the cost function is defined as

$$J(\theta) = \frac{1}{m} \sum_{i=1}^{m} \left[-y^{(i)} \log(h_{\theta}(x^{(i)})) - (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})) \right] + \frac{\lambda}{2m} \sum_{i=1}^{n} \theta_{j}^{2}$$

Note that you should not be regularizing θ_0 which is used for the bias term. Correspondingly, the partial derivative of regularized logistic regression cost for θ_i is defined as

$$\frac{\partial J(\theta)}{\partial \theta_j} = \frac{1}{m} \sum_{i=1}^m \left(h_{\theta}(x^{(i)}) - y^{(i)} \right) x_j^{(i)} \quad \text{for } j = 0,$$

$$\frac{\partial J(\theta)}{\partial \theta_i} = \left(\frac{1}{m} \sum_{i=1}^m \left(h_{\theta}(x^{(i)}) - y^{(i)}\right) x_j^{(i)}\right) + \frac{\lambda}{m} \theta_j \quad \text{for } j \ge 1$$

Now modify your code in 1rCostFunction to account for regularization. Once again, you should not put any loops into your code. When you are finished, run the code below to test your vectorized implementation and compare to expected outputs:

theta
$$t = [-2; -1; 1; 2]$$

theta_t = 4×1 -2

```
X t = [ones(5,1) reshape(1:15,5,3)/10]
X_t = 5 \times 4
   1.0000
             0.1000
                      0.6000
                               1.1000
   1.0000
            0.2000
                      0.7000
                               1,2000
                    0.8000
                               1.3000
   1.0000
            0.3000
             0.4000
                               1.4000
   1.0000
                      0.9000
   1.0000
             0.5000
                    1.0000
                               1.5000
y_t = ([1;0;1;0;1] >= 0.5)
y_t = 5 \times 1 logical array
  1
  0
  1
  0
  1
lambda t = 3;
[J, grad] = lrCostFunction(theta_t, X_t, y_t, lambda_t);
fprintf('Cost: %f | Expected cost: 2.534819\n',J);
Cost: 2.534819 | Expected cost: 2.534819
fprintf('Gradients:\n'); fprintf('%f\n',grad);
Gradients:
0.146561
-0.548558
0.724722
1.398003
fprintf('Expected gradients:\n 0.146561\n -0.548558\n 0.724722\n 1.398003');
Expected gradients:
0.146561
-0.548558
0.724722
1.398003
```

MATLAB Tip: When implementing the vectorization for regularized logistic regression, you might often want to only sum and update certain elements of θ . In MATLAB, you can index into the matrices to access and update only certain elements. For example, A(:,3:5)=B(:,1:3) will replace columns 3 to 5 of A with the columns 1 to 3 from B. One special keyword you can use in indexing is the end keyword in indexing. This allows us to select columns (or rows) until the end of the matrix. For example, A(:,2:end) will only return elements from the 2nd to last column of A. Thus, you could use this together with the sum and .^ operations to compute the sum of only the elements you are interested in (e.g. $sum(z(2:end).^2)$). In the starter code, lrCostFunction.m, we have also provided hints on yet another possible method computing the regularized gradient.

You should now submit your solutions. Enter **submit** at the command prompt, then enter or confirm your login and token when prompted.

1.4 One-vs-all classication

In this part of the exercise, you will implement one-vs-all classification by training multiple regularized logistic regression classifiers, one for each of the K classes in our dataset (Figure 1). In the handwritten digits dataset, K = 10, but your code should work for any value of K.

You should now complete the code in oneVsAll.m to train one classifier for each class. In particular, your code should return all the classifier parameters in a matrix $\Theta \in \mathbb{R}^{K \times (N+1)}$, where each row of Θ corresponds to the learned logistic regression parameters for one class. You can do this with a for loop from 1 to K, training each classifier independently.

Note that the y argument to this function is a vector of labels from 1 to 10, where we have mapped the digit '0' to the label 10 (to avoid confusions with indexing). When training the classifier for class $k \in \{1, ..., K\}$, you will want a m-dimensional vector of labels y, where $y_j \in \{0, 1\}$ indicates whether the j-th training instance belongs to class k ($y_j = 1$), or if it belongs to a different class ($y_j = 0$). You may find logical arrays helpful for this task.

MATLAB Tip: Logical arrays in MATLAB are arrays which contain binary (0 or 1) elements. In MATLAB, evaluating the expression a == b for a vector a (of size $m \times 1$) and scalar b will return a vector of the same size as a with ones at positions where the elements of a are equal to b and zeroes where they are different. To see how this works for yourself, run the following code:

```
% a = 1:10; % Create a and b
% b = 3;
% disp(a == b) % You should try different values of b here
```

Furthermore, you will be using fmincg for this exercise (instead of fminunc). fmincg works similarly to fminunc, but is more more efficient for dealing with a large number of parameters. After you have correctly completed the code for oneVsAll.m, run the code below to use your oneVsAll function to train a multi-class classifier.

```
num_labels = 10; % 10 labels, from 1 to 10
lambda = 0.1;
[all_theta] = oneVsAll(X, y, num_labels, lambda);
```

```
Iteration
            1 | Cost: 2.802128e-01
            2 | Cost: 9.454389e-02
Iteration
Iteration
           3 | Cost: 5.704641e-02
Iteration
            4 | Cost: 4.688190e-02
Iteration 5 | Cost: 3.759021e-02
Iteration
           6 | Cost: 3.522008e-02
Iteration
           7 | Cost: 3.234531e-02
Iteration
           8 | Cost: 3.145034e-02
Iteration
           9 | Cost: 3.008919e-02
Iteration 10 | Cost: 2.994639e-02
Iteration 11 | Cost: 2.678528e-02
Iteration 12 | Cost: 2.660323e-02
Iteration 13 | Cost: 2.493301e-02
           14 | Cost: 2.475211e-02
Iteration
          15 | Cost: 2.318421e-02
Iteration
          16 | Cost: 2.287050e-02
Iteration
Iteration
           17 | Cost: 2.160258e-02
```

Iteration	18	Cost:	2.120371e-02
Iteration	19	Cost:	2.064125e-02
Iteration	20		2.055695e-02
Iteration	21		2.045466e-02
Iteration	22	Cost:	2.029177e-02
Iteration	23	Cost:	2.005296e-02
Iteration	24	Cost:	1.995949e-02
Iteration	25		1.982849e-02
Iteration	26		1.975129e-02
Iteration	27	Cost:	1.897815e-02
Iteration	28	Cost:	1.887065e-02
Iteration	29	Cost:	1.869107e-02
Iteration	30		1.863223e-02
Iteration	31		1.837394e-02
Iteration	32	Cost:	1.816951e-02
Iteration	33	Cost:	1.781689e-02
Iteration	34	Cost:	1.774665e-02
Iteration	35		1.767439e-02
Iteration	36		1.758469e-02
Iteration	37	Cost:	1.756847e-02
Iteration	38	Cost:	1.753344e-02
Iteration	39	Cost:	1.727931e-02
Iteration	40		1.701833e-02
Iteration	41		1.621657e-02
Iteration	42	Cost:	1.536256e-02
Iteration	43	Cost:	1.488688e-02
Iteration	44	Cost:	1.449606e-02
Iteration	45	Cost:	1.428764e-02
Iteration	46		1.419170e-02
Iteration	47		1.386705e-02
Iteration	48		1.382786e-02
Iteration	49	Cost:	1.374235e-02
Iteration	50	Cost:	1.369533e-02
Iteration	1	Cost:	3.448901e-01
Iteration	2	Cost:	3.150694e-01
Iteration	3		1.846843e-01
Iteration	4		1.699017e-01
Iteration	5		1.529566e-01
Iteration	6		1.317377e-01
Iteration	7	Cost:	1.171533e-01
Iteration	8	Cost:	1.074286e-01
Iteration	9	Cost:	9.531806e-02
Iteration	10		9.301912e-02
Iteration			8.418356e-02
Iteration	12		8.186322e-02
Iteration	13		7.743126e-02
Iteration	14	Cost:	7.645181e-02
Iteration	15	Cost:	7.209877e-02
Iteration	16	Cost:	7.195896e-02
Iteration	17		7.106302e-02
Iteration			
	18		7.081516e-02
Iteration	19		6.984782e-02
Iteration	20	Cost:	6.908892e-02
Iteration	21	Cost:	6.818820e-02
Iteration	22	Cost:	6.804182e-02
Iteration	23	Cost:	6.788125e-02
Iteration	24		6.779397e-02
Iteration	25		6.767277e-02
Iteration	26		6.760372e-02
Iteration	27		6.740638e-02
Iteration	28	Cost:	6.731728e-02
Iteration	29	Cost:	6.698888e-02
Iteration	30		6.692984e-02
Iteration	31		6.630404e-02
Iteration			6.606809e-02
Trei.qr10U	32	Cost:	0.0000096-02

Iteration	33	Cost:	6.466816e-02
Iteration	34	Cost:	6.426962e-02
Iteration	35	Cost:	6.267791e-02
Iteration	36	Cost:	6.251576e-02
Iteration	37	Cost:	6.202834e-02
Iteration	38	Cost:	6.188522e-02
	:		
Iteration	39	Cost:	6.013896e-02
Iteration	40	Cost:	5.937078e-02
Iteration	41	Cost:	5.888593e-02
Iteration	42	Cost:	5.862828e-02
Iteration	43	Cost:	5.854428e-02
Iteration	44	Cost:	5.847598e-02
Iteration	45	Cost:	5.840091e-02
Iteration	46	Cost:	5.812346e-02
Iteration	47	Cost:	5.803256e-02
Iteration	48	Cost:	5.773514e-02
Iteration	49	Cost:	5.763077e-02
Iteration	50	Cost:	5.725256e-02
Iteration	1	Cost:	3.456557e-01
Iteration	2	Cost:	2.179164e-01
			1.784174e-01
Iteration	3	Cost:	
Iteration	4	Cost:	1.678808e-01
Iteration	5	Cost:	1.427129e-01
Iteration	6	Cost:	1.150393e-01
Iteration	7	Cost:	1.063718e-01
Iteration	8	Cost:	9.707803e-02
Iteration	9	Cost:	9.518367e-02
Iteration	10	Cost:	9.035733e-02
Iteration	11	Cost:	8.928846e-02
Iteration	12	Cost:	8.531186e-02
Iteration	13	Cost:	8.333526e-02
Iteration	14	Cost:	8.052683e-02
Iteration	15	Cost:	7.932857e-02
Iteration	16	Cost:	7.672637e-02
Iteration	:		7.530942e-02
	:	Cost:	7.500108e-02
Iteration	18	Cost:	
Iteration	19	Cost:	7.445295e-02
Iteration	20	Cost:	7.391453e-02
Iteration	21	Cost:	7.349869e-02
Iteration	22	Cost:	7.307295e-02
Iteration	23	Cost:	7.296937e-02
Iteration	24	Cost:	7.262398e-02
Iteration	25	Cost:	7.129794e-02
Iteration	26	Cost:	7.118480e-02
Iteration	27	Cost:	7.089717e-02
Iteration	28	Cost:	6.963444e-02
Iteration	29	Cost:	6.959800e-02
Iteration	30	Cost:	6.916223e-02
Iteration	31	Cost:	6.893777e-02
Iteration	32	Cost:	6.891915e-02
Iteration	33		6.872550e-02
Iteration	:		6.853716e-02
	34	Cost:	
Iteration	35	Cost:	6.849787e-02
Iteration	36	Cost:	6.754823e-02
Iteration	37	Cost:	6.715262e-02
Iteration	38	Cost:	6.581809e-02
Iteration	39	Cost:	6.573059e-02
Iteration	40	Cost:	6.556100e-02
Iteration	41	Cost:	6.516186e-02
Iteration	42	Cost:	6.465431e-02
Iteration	43		6.445447e-02
Iteration	44		6.444886e-02
Iteration	45	Cost:	6.438075e-02
Iteration	46	Cost:	6.425987e-02
Iteration	47	Cost:	6.422551e-02
TCC: acton	→/	COSC.	0.422316-02

Iteration	48	Cost:	6.407566e-02
Iteration	49	Cost:	6.385062e-02
	!		
Iteration	50	Cost:	6.373928e-02
Iteration	1	Cost:	3.205301e-01
Iteration	2	Cost:	3.040759e-01
	:		
Iteration	3	Cost:	1.649080e-01
Iteration	4 İ	Cost:	1.438784e-01
Iteration	5	Cost:	9.416994e-02
Iteration	6	Cost:	9.044270e-02
Iteration	7 İ	Cost:	7.499076e-02
	:		
Iteration	8	Cost:	7.202465e-02
Iteration	9	Cost:	6.313221e-02
Iteration	10 İ	Cost:	6.168143e-02
	:		
Iteration	11	Cost:	5.762801e-02
Iteration	12	Cost:	5.638036e-02
Iteration	13	Cost:	5.517793e-02
	:		
Iteration	14	Cost:	5.405985e-02
Iteration	15	Cost:	5.332997e-02
Iteration	16	Cost:	5.177817e-02
	:		
Iteration	17	Cost:	5.019780e-02
Iteration	18	Cost:	5.009061e-02
Iteration	19	Cost:	4.933097e-02
	:		
Iteration	20	Cost:	4.906466e-02
Iteration	21	Cost:	4.795494e-02
Iteration	22	Cost:	4.787525e-02
	:		
Iteration	23	Cost:	4.736362e-02
Iteration	24 l	Cost:	4.703862e-02
Iteration	25	Cost:	4.594096e-02
	:		
Iteration	26	Cost:	4.581042e-02
Iteration	27	Cost:	4.439905e-02
Iteration	28	Cost:	4.419352e-02
	:		
Iteration	29	Cost:	4.354885e-02
Iteration	30	Cost:	4.267120e-02
Iteration	31	Cost:	4.260390e-02
	:		
Iteration	32	Cost:	4.239241e-02
Iteration	33	Cost:	4.229369e-02
Iteration	34 İ	Cost:	4.216082e-02
Iteration	- !		
	35	Cost:	4.196210e-02
Iteration	36	Cost:	4.190518e-02
Iteration	37 l	Cost:	4.041238e-02
Iteration	- !		4.017334e-02
	38	Cost:	
Iteration	39	Cost:	3.858316e-02
Iteration	40	Cost:	3.730013e-02
Iteration	41	Cost:	3.673546e-02
	:		
Iteration	42	Cost:	3.646203e-02
Iteration	43	Cost:	3.628894e-02
Iteration	44	Cost:	3.622490e-02
	!		
Iteration	45	Cost:	3.616266e-02
Iteration	46	Cost:	3.612177e-02
Iteration	47		3.608586e-02
	!		
Iteration	48	Cost:	3.604895e-02
Iteration	49	Cost:	3.599253e-02
Iteration	50	Cost:	3.595885e-02
	:		
Iteration	1		3.314410e-01
Iteration	2	Cost:	2.217377e-01
Iteration	3	Cost:	1.929205e-01
Iteration	:		
			1.568866e-01
Iteration	5	Cost:	1.318005e-01
Iteration	6	Cost:	1.147878e-01
Iteration	7		1.124131e-01
	:		
Iteration	8	Cost:	1.083564e-01
Iteration	9	Cost:	1.069107e-01
Iteration	10	Cost:	1.022962e-01
	:		
Iteration	11	Cost:	1.017049e-01
Iteration	12	Cost:	9.879326e-02
	-		

Iteration	13	Cost:	9.731696e-02
Iteration	14	Cost:	9.216899e-02
Iteration	15	Cost:	9.032623e-02
	:		
Iteration	16	Cost:	8.409627e-02
Iteration	17	Cost:	8.140204e-02
Iteration	18	Cost:	7.863906e-02
Iteration	19	Cost:	7.835122e-02
Iteration	:		7.711350e-02
	:	Cost:	
Iteration	21	Cost:	7.671192e-02
Iteration	22	Cost:	7.538515e-02
Iteration	23	Cost:	7.517315e-02
Iteration	24	Cost:	7.352966e-02
Iteration			
	25	Cost:	7.269690e-02
Iteration	26	Cost:	7.167827e-02
Iteration	27	Cost:	7.156798e-02
Iteration	28	Cost:	7.107344e-02
Iteration	29	Cost:	7.057249e-02
Iteration	30	Cost:	7.054742e-02
Iteration	31	Cost:	7.051131e-02
Iteration	32	Cost:	7.027145e-02
Iteration	33	Cost:	7.015020e-02
Iteration	34	Cost:	6.963282e-02
Iteration	35	Cost:	6.921892e-02
Iteration	36	Cost:	6.867102e-02
Iteration	37	Cost:	6.864035e-02
Iteration	38	Cost:	6.838629e-02
Iteration	:		6.832040e-02
	39	Cost:	
Iteration	40	Cost:	6.803653e-02
Iteration	41	Cost:	6.775374e-02
Iteration	42	Cost:	6.726342e-02
Iteration	43	Cost:	6.682669e-02
	:		
Iteration	44	Cost:	6.474023e-02
Iteration	45	Cost:	6.414481e-02
Iteration	46	Cost:	6.344927e-02
Iteration	47	Cost:	6.291332e-02
Iteration	48	Cost:	6.234600e-02
Iteration	:		6.197231e-02
	49	Cost:	
Iteration	50	Cost:	6.186690e-02
Iteration	1	Cost:	3.354875e-01
Iteration	2	Cost:	2.188639e-01
Iteration	3 İ	Cost:	9.772130e-02
Iteration	4		8.460314e-02
	!		
Iteration	5	Cost:	5.991024e-02
Iteration	6	Cost:	5.318810e-02
Iteration	7	Cost:	4.521935e-02
Iteration	8	Cost:	4.117442e-02
Iteration	9		3.978801e-02
	:		
Iteration	10		3.874084e-02
Iteration	11	Cost:	3.814846e-02
Iteration	12	Cost:	3.812015e-02
Iteration	13	Cost:	3.791387e-02
Iteration	14		3.720946e-02
	:		
Iteration	15	Cost:	3.578365e-02
Iteration	16	Cost:	3.474696e-02
Iteration	17	Cost:	3.395842e-02
Iteration	18	Cost:	3.351052e-02
Iteration	:		3.326145e-02
	19		
Iteration	20		3.314033e-02
Iteration	21	Cost:	3.180976e-02
Iteration	22	Cost:	3.138624e-02
Iteration	23		3.012590e-02
Iteration	:		2.930241e-02
	24		
Iteration	25	Cost:	2.893186e-02
Iteration	26	Cost:	2.802475e-02
	-0 1		
Iteration	27	Cost:	2.666013e-02

T	20		2 654574 02
Iteration	28	Cost:	2.654574e-02
Iteration	29	Cost:	2.573053e-02
Iteration	30	Cost:	2.537200e-02
Iteration	!		2.517240e-02
	31	Cost:	
Iteration	32	Cost:	2.513433e-02
Iteration	33	Cost:	2.503069e-02
Iteration	34	Cost:	2.494552e-02
	- !		
Iteration	35	Cost:	2.493218e-02
Iteration	36	Cost:	2.480207e-02
Iteration	37	Cost:	2.433124e-02
	- !		
Iteration	38	Cost:	2.390550e-02
Iteration	39	Cost:	2.342345e-02
Iteration	40	Cost:	2.341153e-02
	:		
Iteration	41	Cost:	2.329556e-02
Iteration	42	Cost:	2.283882e-02
Iteration	43	Cost:	2.269961e-02
Iteration	44	Cost:	2.261465e-02
	!		
Iteration	45	Cost:	2.241371e-02
Iteration	46	Cost:	2.236912e-02
Iteration	47	Cost:	2.206820e-02
	:		
Iteration	48	Cost:	2.203693e-02
Iteration	49	Cost:	2.177578e-02
Iteration	50	Cost:	2.166675e-02
Iteration	1	Cost:	3.142799e-01
	:		
Iteration	2	Cost:	1.938915e-01
Iteration	3	Cost:	9.858322e-02
Iteration	4 İ	Cost:	8.666461e-02
Iteration	5	Cost:	6.518233e-02
Iteration	6	Cost:	6.163782e-02
Iteration	7	Cost:	5.886007e-02
Iteration	8	Cost:	5.773973e-02
	:		
Iteration	9	Cost:	5.334455e-02
Iteration	10	Cost:	5.036396e-02
Iteration	11	Cost:	4.994868e-02
Iteration	12	Cost:	4.964157e-02
	:		
Iteration	13	Cost:	4.945483e-02
Iteration	14	Cost:	4.920530e-02
Iteration	15	Cost:	4.880147e-02
Iteration	- !		4.766125e-02
	16	Cost:	
Iteration	17	Cost:	4.683578e-02
Iteration	18	Cost:	4.573370e-02
Iteration			
	19	Cost:	4.507942e-02
Iteration	20	Cost:	4.501869e-02
Iteration	21	Cost:	4.433528e-02
Iteration	22	Cost:	4.271154e-02
Iteration	:	Cost:	
	:		4.251498e-02
Iteration	24	Cost:	4.191880e-02
Iteration	25	Cost:	4.178635e-02
Iteration	26	Cost:	4.147292e-02
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Iteration	27	Cost:	4.139877e-02
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Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36	Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.804683e-02 3.769264e-02 3.759701e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.804683e-02 3.769264e-02 3.759701e-02 3.745942e-02
Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36	Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.804683e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37 38	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.804683e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37 38 39	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.804683e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02 3.716713e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37 38 39	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02 3.716713e-02 3.698634e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37 38 39 40	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02 3.716713e-02 3.698634e-02 3.688084e-02
Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration Iteration	30 31 32 33 34 35 36 37 38 39	Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost: Cost:	4.039230e-02 3.980260e-02 3.956674e-02 3.884208e-02 3.769264e-02 3.759701e-02 3.745942e-02 3.722658e-02 3.716713e-02 3.698634e-02

Iteration	43	Cost:	3.604521e-02
Iteration	44	Cost:	3.589366e-02
Iteration	45		3.542274e-02
Iteration	46		3.505539e-02
Iteration	47		3.440294e-02
Iteration	48		3.402448e-02
	:		
Iteration	49		3.383476e-02
Iteration	50		3.356453e-02
Iteration	1		3.693354e-01
Iteration	2		2.565067e-01
Iteration	3	Cost:	2.370476e-01
Iteration	4	Cost:	2.341589e-01
Iteration	5	Cost:	2.103654e-01
Iteration	6	Cost:	1.781526e-01
Iteration	7	Cost:	1.659830e-01
Iteration	8	Cost:	1.523508e-01
Iteration	9		1.506519e-01
Iteration	10		1.400809e-01
Iteration	11		1.383318e-01
Iteration	12		1.229135e-01
Iteration	:		1.205599e-01
	- !		
Iteration	14		1.123879e-01
Iteration	15		1.110733e-01
Iteration	16	Cost:	1.073286e-01
Iteration	17	Cost:	1.068798e-01
Iteration	18	Cost:	1.058981e-01
Iteration	19	Cost:	1.056835e-01
Iteration	20	Cost:	1.019768e-01
Iteration	21	Cost:	1.010370e-01
Iteration	22	Cost:	9.828022e-02
Iteration	23	Cost:	9.812436e-02
Iteration	24		9.792314e-02
Iteration	25		9.689705e-02
Iteration	26		9.686948e-02
Iteration	:		9.630516e-02
	:		9.595524e-02
Iteration	28		
Iteration	29		9.439663e-02
Iteration	30		9.385266e-02
Iteration	31		9.343079e-02
Iteration	32	Cost:	9.268394e-02
Iteration	33	Cost:	9.194399e-02
Iteration	34	Cost:	9.122537e-02
Iteration	35	Cost:	9.091223e-02
Iteration	36	Cost:	9.075900e-02
Iteration	37	Cost:	9.055130e-02
Iteration	38	Cost:	8.988151e-02
Iteration	39		8.962542e-02
Iteration	40		8.948788e-02
Iteration	41		8.933879e-02
Iteration	42		8.918813e-02
Iteration	43		8.916967e-02
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	!		8.849012e-02
Iteration	45		
Iteration	46		8.717888e-02
Iteration	47		8.701134e-02
Iteration	48		8.602666e-02
Iteration	49		8.520386e-02
Iteration	50		8.465920e-02
Iteration	1	Cost:	3.369306e-01
Iteration	2	Cost:	2.513191e-01
Iteration	3	Cost:	2.358271e-01
Iteration	4		2.352523e-01
Iteration	5		1.867055e-01
Iteration	6		1.526791e-01
Iteration	7		1.488460e-01
	, ,	2030.	

Iteration	8	Cost:	1.385401e-01
Iteration	9	Cost:	1.363013e-01
Iteration	10	Cost:	1.276495e-01
	:		
Iteration	11	Cost:	1.258539e-01
Iteration	12	Cost:	1.193549e-01
Iteration	13	Cost:	1.139919e-01
Iteration	14	Cost:	1.070966e-01
Iteration	15	Cost:	1.037065e-01
Iteration	16	Cost:	9.936582e-02
	:		
Iteration	17	Cost:	9.883916e-02
Iteration	18	Cost:	9.734415e-02
Iteration	19	Cost:	9.705827e-02
Iteration	20	Cost:	9.578377e-02
Iteration	21	Cost:	9.569713e-02
Iteration	22	Cost:	9.483495e-02
Iteration	23	Cost:	9.439928e-02
	:		
Iteration	24	Cost:	9.143805e-02
Iteration	25	Cost:	9.082974e-02
Iteration	26	Cost:	8.992841e-02
Iteration	27	Cost:	8.982376e-02
Iteration	28	Cost:	8.939125e-02
Iteration	29	Cost:	8.917813e-02
	:	Cost:	
Iteration	30		8.913997e-02
Iteration	31	Cost:	8.878267e-02
Iteration	32	Cost:	8.832439e-02
Iteration	33	Cost:	8.816155e-02
Iteration	34	Cost:	8.757955e-02
Iteration	35	Cost:	8.739034e-02
Iteration	36	Cost:	8.699316e-02
	!		
Iteration	37	Cost:	8.693601e-02
Iteration	38	Cost:	8.623920e-02
Iteration	39	Cost:	8.616870e-02
Iteration	40	Cost:	8.587702e-02
Iteration	41	Cost:	8.572448e-02
Iteration	42	Cost:	8.569615e-02
Iteration	43	Cost:	8.539339e-02
	:		
Iteration	44	Cost:	8.503547e-02
Iteration	45	Cost:	8.495636e-02
Iteration	46	Cost:	8.488640e-02
Iteration	47	Cost:	8.423525e-02
Iteration	48	Cost:	8.334126e-02
Iteration	49	Cost:	8.255598e-02
Iteration	50	Cost:	8.224558e-02
	:		
Iteration	1	Cost:	3.478011e-01
Iteration	2		2.074559e-01
Iteration	3	Cost:	1.108108e-01
Iteration	4	Cost:	9.723535e-02
Iteration	5	Cost:	4.845901e-02
Iteration	6 İ	Cost:	4.571820e-02
Iteration	7		3.405605e-02
Iteration	:		
	8		3.350113e-02
Iteration	9		2.829574e-02
Iteration	10	Cost:	2.671193e-02
Iteration	11	Cost:	2.288809e-02
Iteration	12	Cost:	2.267282e-02
Iteration	13	Cost:	2.048262e-02
Iteration	14	Cost:	2.001572e-02
	:		
Iteration	15	Cost:	1.815609e-02
Iteration	16	Cost:	1.791330e-02
Iteration	17	Cost:	1.723808e-02
Iteration	18	Cost:	1.702208e-02
Iteration	19	Cost:	1.633115e-02
Iteration	20	Cost:	1.586407e-02
Iteration	21	Cost:	1.557474e-02
Iteration	:		1.528102e-02
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Iteration
            23 | Cost: 1.500042e-02
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            24 | Cost: 1.495532e-02
Iteration
            25 | Cost: 1.464703e-02
Iteration
            26 | Cost: 1.450265e-02
Iteration
            27 | Cost: 1.399742e-02
Iteration
            28 | Cost: 1.345917e-02
Iteration
            29 | Cost: 1.321219e-02
Iteration
            30 | Cost: 1.320100e-02
Iteration
            31 | Cost: 1.294498e-02
Iteration
            32 | Cost: 1.260010e-02
            33 | Cost: 1.256812e-02
Iteration
            34 | Cost: 1.243740e-02
Iteration
            35 | Cost: 1.236272e-02
Iteration
            36 | Cost: 1.230297e-02
Iteration
            37 | Cost: 1.223894e-02
Iteration
Iteration
            38 | Cost: 1.217598e-02
Iteration
            39 | Cost: 1.214852e-02
Iteration
           40 | Cost: 1.208405e-02
Iteration
           41 | Cost: 1.149902e-02
Iteration 42 | Cost: 1.073513e-02
Iteration 43 | Cost: 1.018111e-02
Iteration 44 | Cost: 1.015454e-02
Iteration 45 | Cost: 1.004770e-02
Iteration 46 | Cost: 9.987752e-03
Iteration 47 | Cost: 9.959895e-03
Iteration 48 | Cost: 9.931783e-03
Iteration 49 | Cost: 9.900593e-03
Iteration
           50 | Cost: 9.893971e-03
```

You should now submit your solutions. Enter **submit** at the command prompt, then enter or confirm your login and token when prompted.

1.4.1 One-vs-all prediction

After training your one-vs-all classifier, you can now use it to predict the digit contained in a given image. For each input, you should compute the 'probability' that it belongs to each class using the trained logistic regression classifiers. Your one-vs-all prediction function will pick the class for which the corresponding logistic regression classifier outputs the highest probability and return the class label (1, 2, ..., or K) as the prediction for the input example.

You should now complete the code in predictOneVsAll.m to use the one-vs-all classifier to make predictions. Once you are done, run the code below to call your predictOneVsAll function using the learned value of Θ . You should see that the training set accuracy is about 94.9% (i.e., it classifies 94.9% of the examples in the training set correctly).

```
pred = predictOneVsAll(all_theta, X);
all percentage = 5000×10
    0.0000
              0.0004
                        0.0001
                                  0.0000
                                             0.0010
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              0.0003
                        0.0006
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                                             0.0008
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                                                                            0.0135
    0.0000
              0.0005
                        0.0001
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                                                       0.0006
                                                                  0.0000
                                                                            0.0001
    0.0000
              0.0000
                        0.0001
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                                                       0.0000
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    0.0000
              0.0003
                        0.0000
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                                                       0.0000
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                                                                            0.0220
    0.0000
              0.0000
                        0.0735
                                  0.0000
                                             0.0000
                                                       0.0000
                                                                  0.0000
                                                                            0.0008
    0.0000
              0.4990
                        0.0008
                                  0.0000
                                             0.1309
                                                       0.0000
                                                                  0.0000
                                                                            0.0038
    0.0000
              0.0002
                        0.0012
                                  0.0000
                                             0.0008
                                                       0.0000
                                                                  0.0000
                                                                            0.0233
```

```
0.0000
                9.9999
                            0.3211
                                       0.0000
                                                   0.0021
                                                               0.0000
                                                                           0.0000
                                                                                       0.0000
maxValue = 5000 \times 1
    0.9996
    0.9999
    0.9997
    0.9999
    0.9993
    1.0000
    0.9994
    0.9601
    0.9997
    0.9994
p = 5000 \times 1
    10
    10
    10
    10
    10
    10
    10
    10
    10
    10
```

fprintf('\nTraining Set Accuracy: %f\n', mean(double(pred == y)) * 100);

Training Set Accuracy: 95.060000

You should now submit your solutions. Enter submit at the command prompt, then enter or confirm your login and token when prompted.

2. Neural Networks

In the previous part of this exercise, you implemented multi-class logistic regression to recognize handwritten digits. However, logistic regression cannot form more complex hypotheses as it is only a linear classier. (You could add more features such as polynomial features to logistic regression, but that can be very expensive to train.) In this part of the exercise, you will implement a neural network to recognize handwritten digits using the same training set as before. The neural network will be able to represent complex models that form non-linear hypotheses.

For this week, you will be using parameters from a neural network that we have already trained. Your goal is to implement the feedforward propagation algorithm to use our weights for prediction. In next week's exercise, you will write the backpropagation algorithm for learning the neural network parameters.

2.1 Model representation

Our neural network is shown in Figure 2. It has 3 layers- an input layer, a hidden layer and an output layer. Recall that our inputs are pixel values of digit images. Since the images are of size 20 x 20, this gives us 400 input layer units (excluding the extra bias unit which always outputs +1). As before, the training data will be loaded into the variables X and y.

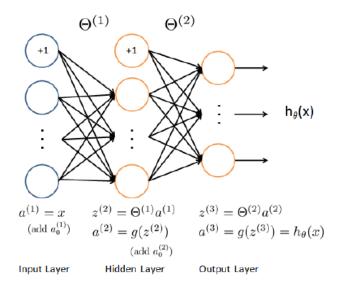
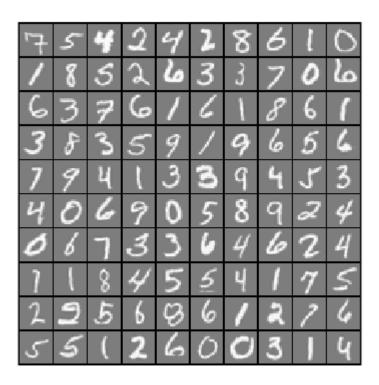


Figure 2: Neural network model.

You have been provided with a set of network parameters $(\Theta^{(1)}, \Theta^{(2)})$ already trained by us. These are stored in ex3weights.mat and are loaded into Theta1 and Thet a2 by running the code below. The parameters have dimensions that are sized for a neural network with 25 units in the second layer and 10 output units (corresponding to the 10 digit classes).

```
load('ex3data1.mat');
m = size(X, 1);
% Randomly select 100 data points to display
sel = randperm(size(X, 1))
sel = 1 \times 5000
                                                      2027
                                                                 1416 ...
       3719
                   2536
                              2141
                                          1487
sel = sel(1:100)
sel = 1 \times 100
                   2536
                              2141
                                          1487
                                                      2027
                                                                 1416 ...
displayData(X(sel, :));
```



```
% Load saved matrices from file
load('ex3weights.mat');
% Theta1 has size 25 x 401
% Theta2 has size 10 x 26
```

2.2 Feedforward propagation and prediction

Now you will implement feedforward propagation for the neural network. You will need to complete the code in predict.m to return the neural network's prediction. You should implement the feedforward computation that computes $h_{\theta}(x^{(i)})$ for every example i and returns the associated predictions. Similar to the one-vs-all classication strategy, the prediction from the neural network will be the label that has the largest output $(h_{\theta}(x))_k$.

Implementation Note: The matrix X contains the examples in rows. When you complete the code in predict.m, you will need to add the column of 1's to the matrix. The matrices Theta1 and Theta2 contain the parameters for each unit in rows. Specically, the first row of Theta1 corresponds to the first hidden unit in the second layer. In MATLAB, when you compute $z^{(2)} = \Theta^{(1)}a^{(1)}$, be sure that you index (and if necessary, transpose) X correctly so that you get $a^{(1)}$ as a column vector.

Once you are done, run the code below to call your predict function using the loaded set of parameters for Theta1 and Theta2. You should see that the accuracy is about 97.5%.

```
pred = predict(Theta1, Theta2, X);
fprintf('\nTraining Set Accuracy: %f\n', mean(double(pred == y)) * 100);
```

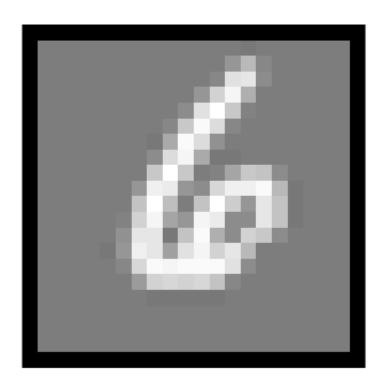
Training Set Accuracy: 97.520000

The code below will displaying images from the training set one at a time, while the console prints out the predicted label for the displayed image. Rerun to repeat with another image.

```
% Randomly permute examples
rp = randi(m);
% Predict
pred = predict(Theta1, Theta2, X(rp,:));
fprintf('\nNeural Network Prediction: %d (digit %d)\n', pred, mod(pred, 10));
```

```
Neural Network Prediction: 6 (digit 6)
```

```
% Display
displayData(X(rp, :));
```



You should now submit your solutions. Enter **submit** at the command prompt, then enter or confirm your login and token when prompted.

Submission and Grading

After completing this assignment, be sure to use the submit function to submit your solutions to our servers. The following is a breakdown of how each part of this exercise is scored.

Part	Submitted File	Points
Regularized Logisic Regression	lrCostFunction.m	30 points
One-vs-all classifier training	oneVsAll.m	20 points
One-vs-all classifier prediction	predictOneVsAll.m	20 points
Neural Network Prediction Function	predict.m	30 points
Total Points		100 points

You are allowed to submit your solutions multiple times, and we will take only the highest score into consideration.