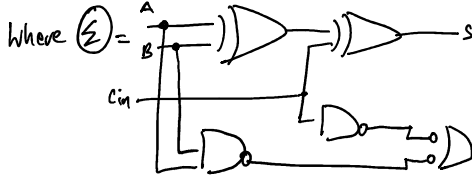
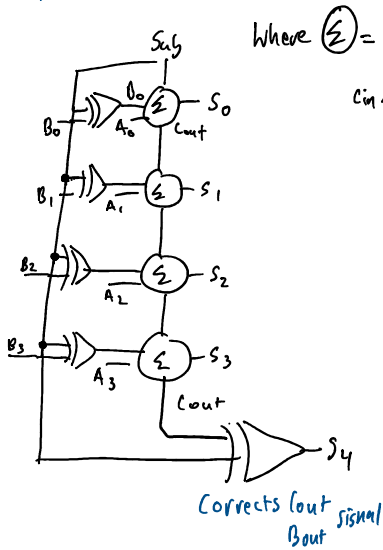


## 4bit Adder:



### Add/Sub Equation

$$\begin{aligned}
 S_0 &= (B_0 \oplus \text{Sub}) \oplus A_0 \oplus (\text{Sub}) & \text{Cout}_0 &= A_0 (B_0 \oplus \text{Sub}) + (A_0 \oplus (B_0 \oplus \text{Sub})) \text{Sub} \\
 S_1 &= ((B_0 \oplus \text{Sub}) \oplus A_1) \oplus \text{Cout}_0 & \text{Cout}_1 &= A_1 (B_1 \oplus \text{Sub}) + (A_1 \oplus (B_1 \oplus \text{Sub})) \text{Cout}_0 \\
 S_2 &= ((B_1 \oplus \text{Sub}) \oplus A_2) \oplus \text{Cout}_1 & \text{Cout}_2 &= A_2 (B_2 \oplus \text{Sub}) + (A_2 \oplus (B_2 \oplus \text{Sub})) \text{Cout}_1 \\
 S_3 &= ((B_2 \oplus \text{Sub}) \oplus A_3) \oplus \text{Cout}_2 \\
 S_4 &= (A_3 (B_3 \oplus \text{Sub}) + A_3 \oplus (B_3 \oplus \text{Sub})) \text{Cout}_2 & \text{Cout}_3 &= (S_4 \oplus \text{Sub})
 \end{aligned}$$

$$\text{Zero} = \overline{S_3} \overline{S_2} \overline{S_1} \overline{S_0}$$

Overflow: Only for signed

$$\text{Sign} = S_3$$

$$\text{Carry} = S_4$$

Subtraction can be treated as addition:

Case 1:		Case 2:	
+ Positive	0 1 1 1 +7	+ Negative	0 1 0 1 -5
+ Positive	0 0 1 1 +7	+ Negative	1 1 0 1 -5
- Negative	0 1 1 0 -2	- Positive	1 0 1 0 -6

$$\text{Cout}_2 S_4 + \text{Cout}_2 S_4 = \boxed{\text{Cout}_2 \oplus S_4}$$

2's complement

$$0 \rightarrow \text{min} \rightarrow \text{max} \rightarrow -8 \rightarrow \text{min} \rightarrow -1$$

## Unsigned Comparisons

$$1010 = 1010 \rightarrow \text{Zero} = \text{UnSign } E_4$$

$$\begin{aligned}
 1010 &> 1001 & C: 0 \\
 10 &- 9 & S: X \text{ - shouldn't matter} \\
 \text{cannot overflow} & & Z: 0 \\
 1010 &> 0001 & C: 0 \\
 & & S: X \\
 & & Z: 0 \\
 & & O: X
 \end{aligned}$$

$$\text{UnSign LT} = (\text{UnSign } E_4 + \text{UnSign } S_4)$$

$$\boxed{\overline{Z} = \text{UnSigned GT}}$$

Since  $|A| < |B|$ , then  $-A < -B$

$$-A > -B$$

$$\begin{aligned}
 C: 0 \\
 S: 0 \\
 Z: 0 \\
 O: 0
 \end{aligned}$$

A > B	A < B
-5 : 1 0 1 1	10 1 1 -5
-6 : 1 0 1 0	01 0 0 -(-4)
Cout = 1 0 0 1	1 1 1 1
Cout = 0	Cout = 0
Cout = 0	Bout = 1

Carry for subtraction: Bout

$$Z (\overline{C} \overline{O} \overline{S} + C(O \oplus \overline{S})) = \text{Signed GT}$$

$$\boxed{Z (\overline{C} \overline{O} \overline{S} + C(O \oplus \overline{S})) = \text{Signed GT}}$$

$$\begin{array}{ccc}
 1 & 1 & 1 \\
 1 & 0 & 0 \\
 0 & 1 & 0 \\
 0 & 0 & 1
 \end{array} = \text{XOR}$$

Similar to:

Carry  
for subtraction: Borrow

0 0 1

$$\text{Signed LT} = \overline{(\text{Signed GT}) + \text{Zero}}$$