

```

; This subroutine computes GCD value of two unsigned 8-bit integers.
; The algorithm implemented is Euclid's subtraction algorithm, and is given
; by the pseudo code below:
;   gcd(a,b):
;       while(b!=0):
;           if a >= b: a = a-b
;           else: swap a and b (will need a temporary variable)
;       return a
;
; The values of a and b are 8-bit values stored in memory in the variables a and b
; respectively. At the end of the program, the GCD of (a,b) is stored in the variable
; a as an unsigned 8 bit integer and the value of variable b will always be 0.
; The value of a is then returned to the accumulator. For error handling,
; faulty inputs (e.g. gcd(0,0)) will return 0.

```

; Revision History

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; 10 Feb 23 Steven Lei      Created pseudo code with comments
; 10 Feb 23 Steven Lei      Converted pseudo code to assembly
; 11 Feb 23 Steven Lei      Hand compiled .asm to .obj
; 11 Feb 23 Steven Lei      Debugged program and ran test cases
; 11 Feb 23 Steven Lei      Successfully tested program

```

```

;0000      EuclidLoop:      ;loop until b is 0
0000 8001;      LDD    b      ;load the value of b
0001 3033;      CMPI   0      ;compare b to 0
0002 9F14;      JZ     Done    ;if b is now 0, we're done
0003 1F80;      NOP
;JNZ      EuclidCheck    ;otherwise compute the gcd by decrementing a

;0004      EuclidCheck:     ;first check if a>=b
0004 8000;      LDD    a      ;load the value of a in the accumulator
0005 3001;      CMP    b      ;compare a to b
0006 8C04;      JAE    Sub     ;if a>=b then go to subtract branch
0007 1F80;      NOP
0008 8F06;      JB     Swap    ;else a<b, so go to swap branch
0009 1F80;      NOP

;000A      Sub:             ;subtract b from a
000A 8000;      LDD    a      ;load the value of a in accumulator
000B 1001;      SUB    b      ;subtract the value of b from accumulator
000C A000;      STD    a      ;and store it to a
000D C000;      JMP    EuclidLoop ;jump back to the start of EuclidLoop
000E 1F80;      NOP

;000F      Swap:           ;swap a and b using register X as a temporary variable
000F 8000;      LDD    a      ;load the value of a in the accumulator
0010 0780;      TAX                ;store it in register X
0011 8001;      LDD    b      ;load the value of b in the accumulator
0012 A000;      STD    a      ;store it in a
0013 6701;      TXA                ;load the value of register X in the accumulator
0014 A001;      STD    b      ;store it in b
0015 C000;      JMP    EuclidLoop ;go back to the start of the EuclidLoop
0016 1F80;

;0017      Done:           ;done with the calculation
0017 8000;      LDD    a      ;load the value of a (the gcd value) into the accumulator

```

```
0018 1F00;          RTS          ;and return
```

```
;Variables
```

```
;00 ?? a          DB    ?          ;the first number for GCD comparison  
;01 ?? b          DB    ?          ;the second number for GCD comparison
```

Caltech10 Simulator v1.5.6

L

filename: gcd.obj

Done.

00/ 00 0

01/ 00 0

S

RETURN A:00 F:01 X:00 S:00 P:0000

00/ 00 32

01/ 00 0

S

RETURN A:32 F:01 X:00 S:00 P:0000

00/ 32 0

01/ 00 32

S

RETURN A:32 F:01 X:00 S:00 P:0000

Edge case 0 and 0:

(should return 0 as defined in the comments)

$\text{GCD}(0,0) = 0$

Edge case: 0 and random number

$\text{GCD}(32,0) = 32$

Edge case: random number and 0

$\text{GCD}(0,32) = 32$

00/ 32 FF

01/ 00 FF

S

RETURN A:FF F:01 X:00 S:00 P:0000

00/ FF FF

01/ 00 0

S

RETURN A:FF F:01 X:00 S:00 P:0000

00/ FF 0

01/ 00 FF

S

RETURN A:FF F:01 X:00 S:00 P:0000

Edge case largest number (FF)

$\text{GCD}(\text{FF},\text{FF}) = \text{FF}$

Edge case: largest number and 0

$\text{GCD}(\text{FF},0) = \text{FF}$

Edge case: 0 and largest number

$\text{GCD}(0,\text{FF}) = \text{FF}$

```
00/ FF 5
01/ 00 FF
S
```

Edge case: random number and largest number

```
RETURN A:05 F:01 X:00 S:00 P:0000
```

$\text{GCD}(5, \text{FF}) = 5$

```
00/ 05 FF
01/ 00 5
S
```

Edge case: largest number and random number

```
RETURN A:05 F:01 X:00 S:00 P:0000
```

$\text{GCD}(\text{FF}, 5) = 5$

```
00/ 09
01/ 00 3
S
```

General case: $\text{GCD}(a, b) = \text{GCD}(b, a)$

```
RETURN A:03 F:01 X:00 S:00 P:0000
```

$\text{GCD}(9, 3) = 3$

```
00/ 03 3
?
01/ 00 9
S
```

```
RETURN A:03 F:01 X:00 S:00 P:0000
```

$\text{GCD}(3, 9) = 3$

```
00/ 02 25
01/ 00 3
S
```

General case: prime numbers

25 is 37 in hex

$\text{GCD}(25, 3) = 1$

```
RETURN A:01 F:01 X:00 S:00 P:0000
```

```
00/ 01 25
01/ 00 9
S
```

General case: prime and composite number

25 is 37 in hex

$\text{GCD}(25, 9) = 1$

```
RETURN A:01 F:01 X:00 S:00 P:0000
```

```
00/ 00 1
01/ 00 1
S
```

```
RETURN  A:01 F:01 X:00 S:00 P:0000
```

```
00/ 01 30
01/ 00 90
S
```

```
RETURN  A:30 F:01 X:00 S:00 P:0000
```

General cases

$\text{GCD}(1,1) = 1$

30 is 48 in hex, 90 is 144

$\text{GCD}(30,90) = 30$

```
00/ 01 8
01/ 00 10
S
```

```
RETURN  A:08 F:01 X:00 S:00 P:0000
```

```
00/ 08 2
01/ 00 6
S
```

```
RETURN  A:02 F:01 X:00 S:00 P:0000
```

```
00/ 02 F
01/ 00 3
S
```

```
RETURN  A:03 F:01 X:00 S:00 P:0000
```

10 is 16 in hex

$\text{GCD}(8,10) = 2$

$\text{GCD}(2,6) = 2$

F is 15 in hex

$\text{GCD}(15, 3) = 3$