

<i>subject area and application</i>	<i>vertex attributes and meaning edge/arc attributes and meaning</i>	<i>reference</i>
cartography	regions are countries	§8.6.4
map-coloring	edges are borders	
highway construction	vertices are road intersections	§8.7.1
avoiding overcrossings	edges are roads	
electrical network boards	vertices are circuit components	§8.7.1
avoiding insulation	edges are wires	
VLSI computer chips	vertices are circuit components	§8.7.4
minimizing layering	edges are wires	
information management	vertices are data records	§17.1.4
binary search trees	edges are decisions	
computer operating systems	vertices are prioritized jobs	§17.1.5
priority trees	edges are priority relations	
physical chemistry	vertices are atoms	§9.3.2
counting isomers	edges are molecular bonds	
network optimization	edges are connections	§10.1.1
min-cost spanning trees	edge-labels are costs	
bipartite matching	parts are people and jobs	§10.2.2
personnel assignment	edges are job-capabilities	
network optimization	vertices are locations	§10.3.1
shortest path	edge-labels are distances	
traveling salesman routing	vertices are locations	§10.7.1
shortest complete tour	edge-labels are distances	

The **out-degree** of vertex  $v$ , denoted  $\delta^+(v)$ , is the number of arcs with tail at  $v$ .

The **in-degree** of vertex  $v$ , denoted  $\delta^-(v)$ , is the number of arcs with head at  $v$ .

A digraph  $D$  is **transitive** if whenever it contains an arc from  $u$  to  $v$  and an arc from  $v$  to  $w$ , it also contains an arc from  $u$  to  $w$ .

The **adjacency matrix**  $A_D$  of a digraph  $D$  is

$$A_D = [a_{ij}], \text{ where } a_{ij} = \text{number of arcs from } v_i \text{ to } v_j.$$

The **incidence matrix**  $M_D$  of a digraph  $D$  with no self-loops is  $M_D = [b_{ij}]$ , where

$$b_{ij} = \begin{cases} +1, & \text{if } v_i \text{ is the tail of } e_j \text{ but not the head} \\ -1, & \text{if } v_i \text{ is the head of } e_j \text{ but not the tail} \\ 0, & \text{otherwise.} \end{cases}$$

There is no standard convention for self-loops.

### Facts:

1. **Strict-digraph terminology:** In a context focusing primarily on strict digraphs, there is often a different terminological convention:

- “digraph” refers to a strict digraph;
- a directed graph with multi-arcs is called a *multidigraph*;
- a directed graph with self-loops is called a *pseudodigraph*;
- an arc with tail  $u$  and head  $v$  is designated  $uv$ .