Time Synchronization in Ad Hoc Networks

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ABSTRACT

Ubiquitous computing environments are typically based upon ad hoc networks of mobile computing devices. These devices may be equipped with sensor hardware to sense the physical environment and may be attached to real world artifacts to form so–called smart things. The data sensed by various smart things can then be combined to derive knowledge about the environment, which in turn enables the smart things to "react" intelligently to their environment. For this so–called sensor fusion, temporal relationships (X happened before Y) and real–time issues (X and Y happened within a certain time interval) play an important role. Thus physical time and clock synchronization are crucial in such environments. However, due to the characteristics of sparse ad hoc networks, classical clock synchronization algorithms are not applicable in this setting. We present a time synchronization scheme that is appropriate for sparse ad hoc networks.

Keywords

time synchronization, clock synchronization, ad hoc networks, spontaneous networking, ubiquitous computing, sensor fusion, smart things

1. INTRODUCTION

Consider ubiquitous computing scenarios where everyday things (such as watches, coffee cups, books) are made "smart" by attaching small computing devices to them that are able to sense the physical environment (e.g., location, illumination, temperature, acceleration) and are able to communicate via short range radio with each other. Such smart things are spontaneously networked: if they are brought into the vicinity of one another, a communication link is established, which is removed again when the smart things are moved away from each other. In general, communication links are rather short lived and the resulting network of smart things is highly dynamic.

In such a setting, one often wants to reason about the "real world" (the environment of the smart things) as sensed by smart artifacts. The idea is to combine the information collected about the environment by the individual smart things into some higher level information or knowledge [4, 7, 8, 11] also known as sensor fusion.

Consider for example environment monitoring systems, which involve the detection of direction and speed of certain phenomena such as fire, oil slicks, water pollution, or animal herds. Mobile computing devices equipped with sensors, clocks, and short range radio are deployed in the environment (e.g., dropped into water, or attached to animals). The devices record the time when they detect or no longer detect the phenomenon and communicate this information to other devices as they pass by. In order to determine the direction of the phenomenon, temporal ordering of these events originating from different devices (and thus different clocks) has to be determined. To estimate the speed of the phenomenon time differences between events originating from different devices have to be calculated.

Time synchronization is also useful for estimating proximity of and distances between smart things by taking into account the points in time when a certain phenomenon in the environment (e.g., sound, light, air pressure) is sensed by different smart things.

These examples indicate that temporal ordering and other real–time[1] issues play an important role in such environments. As we will see later, neither logical time [12, 14] nor classical physical clock synchronization algorithms [3, 13, 16, 17] can be used to solve this problem in general. We will suggest an algorithm that solves the temporal ordering problem and other real–time issues in environments sketched above.

2. AD HOC NETWORKS

Ad hoc networks [2] are networks of mobile wireless computing devices. Due to the limited communication range of wireless technology (about 10 meters for Bluetooth [1]), nodes of the network form spontaneous connections when they are brought within the communication range of each other, providing typically a symmetrical communication link where message exchange is possible in both directions. The limited communication range and the mobility of the nodes lead to frequent reconfiguration of the network topology.

The left hand side of figure 1 shows the configurations (topologies) of an ad hoc network consisting of three nodes at two points in time $t_1 < t_2$. At t_1 nodes 1 and 2 are able to communicate with

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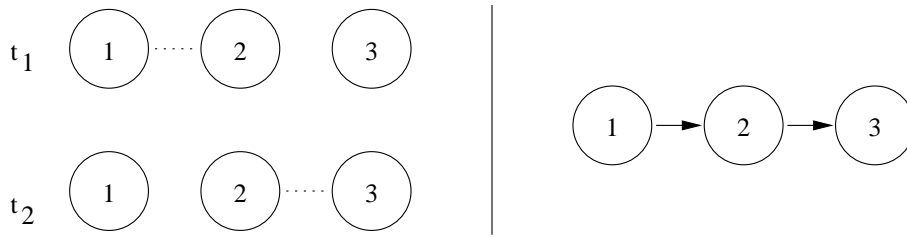[1]Throughout the paper the term real–time refers to UTC.

Figure 1: Connectivity vs. message flow in ad hoc networks

each other, and at t_2 nodes 2 and 3 are able to communicate with each other. This may result from the following physical setting: nodes 1 and 3 are out of the communication range of each other. At t_1 node 2 is within the communication range of node 1, then node 2 is moved out of the communication range of node 1 into the communication range of node 3.

Assuming this setting, there is no point in time $t_1 \le t \le t_2$ where communication between node 1 and 3 (either directly or indirectly via node 2) is possible. This example shows an important property of ad hoc networks: the frequent temporary existence of network partitions, especially in *sparse ad hoc networks* with only a few nodes distributed over a large area (relative to the communication range) in contrast to *dense ad hoc networks*.

Despite this partitioning, it is often possible for two nodes that always reside in different partitions to communicate in an indirect way with each other by using store and forward techniques. In figure 1, node 1 can send a message to node 2 at t_1, which is then stored in node 2 and forwarded to node 3 at t_2, resulting in an *unidirectional delayed message flow* from node 1 to node 2, which is depicted in the right hand side of figure 1. In contrast, an *immediate message flow* is possible if there is no need to store a message on intermediate nodes as in classical networks.

3. TIME IN AD HOC NETWORKS

Ad hoc networks as described in the previous section are important for ubiquitous computing environments, where mobile wireless computing devices equipped with sensor hardware are embedded in real–world artifacts to form so–called smart things.

The information collected by individual smart things about the environment is often combined to form higher level information or knowledge about their environment. This knowledge can in turn be used by these smart things to react intelligently to changes in the environment.

When combining the sensor data, temporal relationships (X happened before Y) and real–time issues (X and Y happened within a certain time interval) play an important role. Logical time cannot be used to determine temporal relationships here, because we consider events and their causal relationships in the real world, which do not manifest themselves in network messages between the event generating entities, which is a basic assumption for algorithms implementing logical time [12, 14].

So we have to use physical time shared by the smart things, requiring some means of clock synchronization. However, the frequent temporary network partitions in sparse ad hoc networks are a serious problem for classical clock synchronization algorithms.

Consider for example figure 2, which models an environment monitoring system ad hoc network as sketched in the introduction. At real–time t_1 device 1 detects the phenomenon. At t_2 device 2 detects the phenomenon. At t_3 device 2 passes by device 3, a communication link is established and E_2 is sent to device 3. At t_4 device 1 passes by device 3, a link is established and E_1 is sent to device 3.

Now device 3 wants to determine speed and direction of the phenomenon and therefore has to determine whether E_1 happened after E_2 and the time difference between E_1 and E_2.

Classical clock synchronization algorithms rely on two important assumptions: first, the ability to periodically exchange messages between nodes that have to be synchronized, and second, the ability to estimate the time it takes for a message to travel between two (not necessarily adjacent) nodes to be synchronized.

The scenario depicted in figure 2 is a serious problem for classical clock synchronization algorithms with the above assumptions, because the clocks of nodes 1 and 2 have already to be synchronized when they sense events E_1 and E_2 (and record the time when they were sensed), in order to compare the time stamps of E_1 and E_2 later when they arrive at node 3. However, as shown in figure 2 there is no way for nodes 1 and 2 to communicate for all $t \le t_3$, which makes clock synchronization of nodes 1 and 2 impossible before E_1 and E_2 are sensed (the first assumption for classical clock synchronization algorithms is violated).

Even at time t_4 where an unidirectional delayed message path from node 2 to node 1 via node 3 exists, clock synchronization of nodes 1 and 2 seems almost impossible, because this path is unidirectional and arbitrarily delayed, ruling out good estimation of message delay (violating assumption two of classical clock synchronization algorithms).

Last but not least the future might probably bring us millions of smart everyday things, which all *potentially* need synchronized clocks because one day they could meet and want to exchange offline sensed data. In fact, only relatively few smart things will ever meet in reality, but one cannot know in advance which ones. This presents an enormous scalability challenge for classical clock synchronization algorithms.

4. COMPUTER CLOCKS

Todays computing devices are equipped with a hardware oscillator assisted computer clock, which implements an approximation $C(t)$ for real–time t. $C(t) = k \int_{t_0}^{t} \omega(\tau)\mathrm{d}\tau + C(t_0)$ is a real valued function over real–time t, which depends on the angular frequency $\omega(t)$ of the hardware oscillator. k is a proportional coefficient.
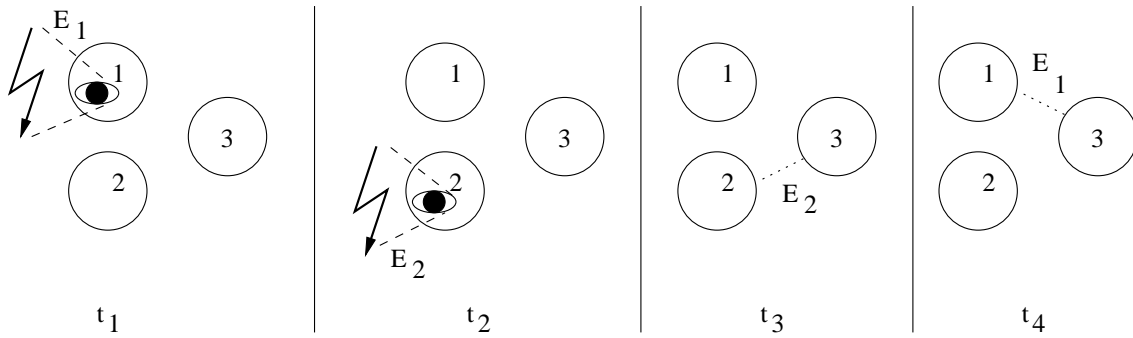
Figure 2: Time synchronization in ad hoc networks

For a perfect hardware clock $\frac{dC}{dt}$ would equal 1. However, all hardware clocks are imperfect, they are subject to *clock drift*. The exact clock drift is hard to predict because it depends on environmental influences (e.g., temperature, pressure, power voltage). One can usually only assume that the clock drift of a computer clock doesn't exceed a maximum value ρ. This means that we assume:

$$1 - \rho \leq \frac{dC}{dt} \leq 1 + \rho \qquad (1)$$

A typical value for ρ achievable with today's hardware is 10^{-6}, which means that the computer clock drifts away from real–time by no more than one second in ten days, which is still a significant value. Note that different computer clocks have different maximum clock drift values ρ_i.

Clock synchronization now tries to equalize $C_i(t)$ for $i = 2, ..., N$ computing devices connected by a network. It is not sufficient to synchronize at one point in real–time t_x, since the clocks will drift away afterwards. So either the precisions of the clocks $\frac{dC_i}{dt}$ have to be adjusted as well, or synchronization of the C_i has to be repeated over and over again. Synchronizing the clocks with UTC is a special case called external synchronization where one or more of the computing devices is equipped with a special hardware clock, like an atomic clock.

Due to unpredictability and imperfect measurability of message delays, physical clock synchronization is always imperfect. Therefore one has to take care to avoid false statements when reasoning about temporal ordering and real–time issues based on synchronized computer clocks.

5. SYNCHRONIZATION ALGORITHM

The algorithm we will present considers message flows in ad hoc networks, which can be depicted by (time independent) message flow graphs, where the nodes of the graph correspond to network nodes, each equipped with its own computer clock. Paths in the graph correspond to possibly delayed message flows between the nodes.

Computing nodes are able to sense events in the real world via sensor hardware. When node i senses an event E at real–time $t(E)$ it generates a time stamp $S_i(E)$ using its local clock, which may later be passed to other nodes inside exchanged messages.

The algorithm enables all participating nodes to reason about sets of time stamps (e.g., determine temporal ordering and time spans) received from arbitrary nodes.

Goals

- Handles all kinds of partitioning in sparse ad hoc networks.

- Does not require a particular network topology beyond the one required already by the application that needs time synchronization.

- Correctness: When the algorithm claims a certain property on a set of time stamps $\{S_i(E_j)\}$ such as $S_1(E_1) < S_2(E_2)$, then this property must also hold on the corresponding set of points in real time $\{t(E_j)\}$, i.e., $t(E_1) < t(E_2)$. However, the algorithm is allowed not to claim such a property on $S_i(E_j)$ although the property holds on the corresponding set $t(E_j)$. For example, if $t(E_1) < t(E_2)$ then the algorithm is allowed to report $S_1(E_1)$ *maybe* $< S_2(E_2)$.

- Usefulness: Minimal number of *maybe* results.

- Scalability.

- Performance: Low message overhead for time synchronization.

Assumptions

- Computer clocks with known maximum clock drift ρ_i.

- When an application message is exchanged between two adjacent nodes, the connection between the nodes remains established long enough to exchange another (synchronization algorithm) message between these two nodes.

5.1 The Idea

The basic idea of the algorithm is *not* to synchronize the local computer clocks of the devices but instead generate time stamps using unsynchronized local clocks. When such locally generated time stamps are passed between devices, they are transformed to the local time of the receiving device.

Due to various reasons such transformations cannot be done with high precision, therefore the algorithm uses time intervals as a lower and upper bound for the exact value. When a message containing a time stamp is transferred between devices, the time stamps are first transformed from the local time to UTC (which is used as a common time transfer format) and then to the local time of the receiver.
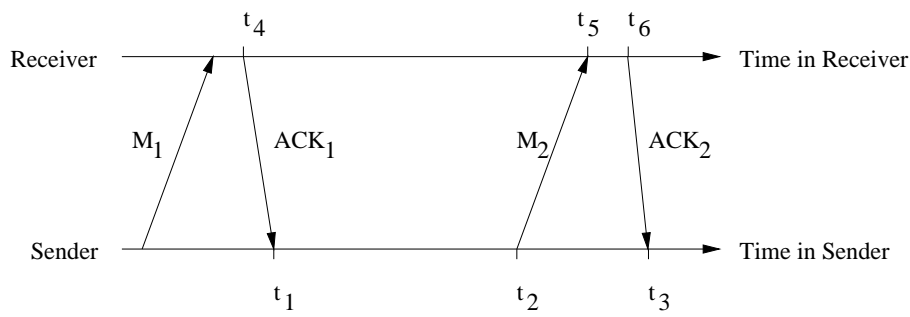
Figure 3: Message delay estimation

Stated in more detail, the algorithm determines lower and upper bounds for the real–time passed from generation of the time stamp in the source node to arrival of the message in the destination node, transforms these bounds to the time of the receiver and subtracts the resulting values from the time of arrival in the destination node. The resulting interval specifies lower and upper bounds for the time stamp relative to the local time of the receiving node.

5.2 Time Transformation

As we will see in the following section, transforming real–time differences Δt into computer clock differences ΔC and vice versa is at the heart of the algorithm. These transformations cannot be done exactly due to the unpredictability of the computer clocks, but will result in estimates (lower and upper bounds). Basis for the transformation is the difference based version of inequality 1:

$$1 - \rho \leq \frac{\Delta C}{\Delta t} \leq 1 + \rho \qquad (2)$$

which can be transformed into $(1 - \rho)\Delta t \leq \Delta C \leq (1 + \rho)\Delta t$ and $\frac{\Delta C}{1+\rho} \leq \Delta t \leq \frac{\Delta C}{1-\rho}$, which means that we can approximate the computer clock difference ΔC that corresponds to the real–time difference Δt by the interval $[(1 - \rho)\Delta t, \ (1 + \rho)\Delta t]$. Vice versa the real–time difference Δt that corresponds to the computer clock difference ΔC can be approximated by the interval $[\frac{\Delta C}{1+\rho}, \ \frac{\Delta C}{1-\rho}]$ accordingly.

In order to transform a time difference ΔC from the local time of one node (with ρ_1) to the local time of a different node (with ρ_2), ΔC is first estimated by the real–time interval $[\frac{\Delta C}{1+\rho_1}, \ \frac{\Delta C}{1-\rho_1}]$, which in turn is estimated by the computer time interval $[\Delta C \frac{1-\rho_2}{1+\rho_1}, \ \Delta C \frac{1+\rho_2}{1-\rho_1}]$ relative to the local time of node 2.

5.3 Message Delay

As pointed out above, the algorithm will determine estimations for the lifetime of a time stamp. For this it has to know estimations for the message delay d of messages sent between adjacent nodes. Since we cannot assume a constant message delay due to the highly dynamic characteristics of ad hoc networks, message delay has to be measured for each transferred message in order to achieve the correctness goal.

One important observation is that a message transfer between two nodes is often accomplished by sending two messages, the message that is to be transferred from the sender to the receiver and an acknowledgment back from the receiver to the sender to inform the

sender of the successful arrival of the message. Thus, it is possible to measure the round trip time rtt (time passed from sending the message in the sender to arrival of the acknowledgment in the sender) using the local clock of the sender. The message delay can then be estimated by the the lower bound 0 and the upper bound rtt. Now the sender knows an estimation for the message delay, but in our algorithm the receiving side has to know this approximation in order to update the received time stamp. Transferring the estimation from the sender to the receiver would take another pair of messages (one for passing the estimation from sender to receiver and an ack back to the sender to inform the sender of the successful arrival of the message), which would result in 100% message overhead.

Now have a look at figure 3, which shows two consecutive acknowledged message exchanges between a pair of sender and receiver. We want to estimate the message delay d for message M_2. Using the technique pointed out above the estimation would be $0 \leq d \leq (t_3 - t_2) - (t_6 - t_5)\frac{1-\rho_s}{1+\rho_r}$ in terms of the sender's clock, where ρ_s and ρ_r are the ρ values for sender and receiver, respectively. A different estimation is

$$0 \leq d \leq (t_5 - t_4) - (t_2 - t_1)\frac{1 - \rho_r}{1 + \rho_s} \qquad (3)$$

in terms of the receiver's clock that makes use of two consecutive message transfers. The big advantage of this second estimation is that the receiver knows an estimation for d without additional message exchanges since $t_2 - t_1$ can be piggybacked on M_2. We will call $t_5 - t_4$ the round trip time rtt for the message, which is measured using the receiver's clock, and $t_2 - t_1$ the idle time $idle$ for the message, which is measured using the sender's clock.

However, the second estimation has two disadvantages. The individual values for $t_2 - t_1$ and $t_5 - t_4$ can become quite large if the nodes communicate rarely, which leads to bad estimations due to the clock drift of the local clocks. This problem can be relaxed by sending a dummy message if the resulting $idle$ value for the message would be to large.

The second disadvantage stems from the fact that t_4, t_1 and t_5, t_2 are associated with different message transfers, forcing both sender and receiver to keep track of state information between message transfers (t_1 and t_4 in figure 3, respectively). This is problematic if a node sends messages to or receives messages from many different nodes over time. However, this problem can be relaxed by deleting state information at the cost of a later dummy message exchange

to reinitialize the clock values, for example in a least recently used manner. Thus, one can trade off space for message overhead.

5.4   Time Stamp Calculation

The algorithm for time synchronization in sparse ad hoc networks consists of two major parts. First, a representation of time stamps and rules for transforming them when they are passed between nodes inside messages, and second, rules for comparing time stamps.

A time stamp $S_i(E)$ for event E is represented in node i by the interval $[C_{i,l}(E), C_{i,r}(E)]$ where the end points of the interval are computer clock values relative to the computer clock in node i, such that the value of the computer clock at real–time $t(E)$ showed a value $C_i(E)$ with $C_{i,l}(E) \leq C_i(E) \leq C_{i,r}(E)$. This means that $S_i(E)$ is an estimation of the unknown value $C_i(E)$.

Now consider figure 4. Device 1 wants to pass a time stamp on to device $2, 3, ..., N$ along the depicted chain of nodes. Each node i has 3 attributes, the local time r_i when the message containing the time stamp interval is received, the local time s_i when the message containing the time stamp interval is sent, and the clock drift ρ_i. All time values are measured using the local clock of the device. Each edge has two attributes rtt_i and $idle_i$, the round trip time for sending the message measured using the clock of the receiving node as described in the previous section, and the idle time elapsed after sending the last message over this edge measured using the clock of the sending node. Separate instances of all attributes (except ρ_i that is a constant attribute of the computer clock) have to be maintained for each message, for simplicity we only consider a single message transfer from node 1 to node N.

The generator of a time–stamped message is a special case, because it does not receive a message. Instead, r_1 is set to the time value it wants to pass along (NOW in figure 4). Now let us consider the time stamp interval as it is being passed along the chain from node 1 to node N.

Node 1

$$[r_1 , r_1] = [NOW , NOW]$$

Node 2

$$\left[r_2 - (s_1 - r_1)\frac{1 + \rho_2}{1 - \rho_1} - (rtt_1 - idle_1\frac{1 - \rho_2}{1 + \rho_1}) \, ,\right.$$
$$\left. r_2 - (s_1 - r_1)\frac{1 - \rho_2}{1 + \rho_1} \right]$$

Node 3

$$\left[r_3 - (s_1 - r_1)\frac{1 + \rho_3}{1 - \rho_1} - (s_2 - r_2)\frac{1 + \rho_3}{1 - \rho_2} \right.$$
$$-(rtt_1\frac{1 + \rho_3}{1 - \rho_2} - idle_1\frac{1 - \rho_3}{1 + \rho_1}) - (rtt_2 - idle_2\frac{1 - \rho_3}{1 + \rho_2}),$$
$$\left. r_3 - (s_1 - r_1)\frac{1 - \rho_3}{1 + \rho_1} - (s_2 - r_2)\frac{1 - \rho_3}{1 + \rho_2} \right]$$

Node N

$$\left[r_N - (1 + \rho_N) \sum_{i=1}^{N-1} \frac{s_i - r_i + rtt_{i-1}}{1 - \rho_i} - rtt_{N-1} \right.$$
$$+ (1 - \rho_N) \sum_{i=1}^{N-1} \frac{idle_i}{1 + \rho_i},$$
$$\left. r_N - (1 - \rho_N) \sum_{i=1}^{N-1} \frac{s_i - r_i}{1 + \rho_i} \right]$$

The interval for node 1 is straightforward, it consists just of the single point in time NOW. For node 2 we take the time when the message containing the time interval is received in node 2 (r_2) and subtract the time the message was stored in node 1 after being generated and before being sent ($s_1 - r_1$). The round trip time minus the idle time $rtt_1 - idle_1$ is used as an upper bound for the message delay (0 is used as the lower bound). Transforming time values between the different clocks as described in section 5.2 results in the interval shown for node 2. Continuing this way with subtracting total node storage time from message arrival time and using the sum of round trip minus idle times as the upper bound for the total message delay, and assuming $rtt_0 = 0$, one will end up with the interval shown for node N.

5.5   Implementation

The basic idea for implementing the algorithm is to incrementally calculate the three sums in the formula shown for node N in the previous section as the message is passed along a chain of nodes. The implementation assumes an asynchronous, reliable communication mechanism but can easily be extended to unreliable communication mechanisms.

The timed message can be represented in the following way using C:

```
struct Message {
    Time begin, end, received;
    Time lifetime_min, lifetime_max, idletime_min;
    /* ... */
};
```

where `begin` and `end` are the left and right ends of the interval, `received` is the time of arrival, `lifetime_min` and `lifetime_max` are lower and upper bounds for the real–time passed from generation of the time stamp to the arrival in the current node, `idletime_min` is the accumulated idle time. That is, `lifetime_max`, `idletime_min`, and `lifetime_min` are used to incrementally calculate the three sums in the formula for node N shown in the previous section. `begin`, `end`, and `received` don't need to be transferred between nodes, they are local variables but are included into the message here for simplicity.

`Time` is an appropriate representation for points in time and time differences. Computer clocks are discrete, so an integer type would be appropriate. But care has to be taken because of the clock drift, which may result in fractional values, so either a floating point type must be used or the results have to be rounded such that the resulting integer interval always contains the floating point interval. Here we assume floating point values.

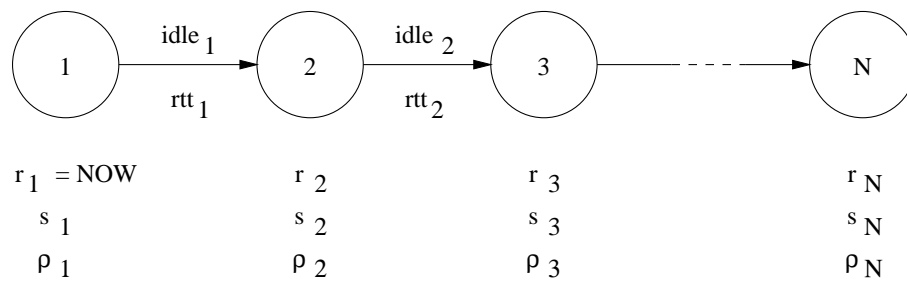The generator of a time–stamped message performs the following actions:

Figure 4: Message flow graph

```
1 Generator:
2   Message M;
3   M.begin = M.end = M.received = NOW;
4   M.lifetime_min = M.lifetime_max = 0;
5   M.idletime_min = 0;
```

where NOW refers to the current value of the local clock. As explained in the previous section the interval is initialized to [NOW, NOW]. All other fields are set to zero.

A time stamped message is sent using the following actions:

```
1 Sender:
2   Message M; /* locally generated or received */
3   Time idleend = NOW;
4
5   IF (idlebegin[receiver] == 0 OR
6       idleend - idlebegin[receiver] > max_idle)
7   THEN
8       send <sync> to receiver;
9       receive <ack> from receiver;
10      idleend = NOW;
11      idlebegin[receiver] = idleend;
12  ENDIF
13
14  send <xmit(M, idleend - M.received,
15          idleend - idlebegin[receiver],
16          local_rho)> to receiver;
17  receive <ack(resend)> from receiver;
18  idlebegin[receiver] = NOW;
19
20  IF (resend == TRUE) THEN
21      idleend = NOW;
22      send <xmit(M, idleend - M.received,
23              idleend - idlebegin[receiver],
24              local_rho)> to receiver;
25      receive <ack> from receiver;
26      idlebegin[receiver] = NOW;
27  ENDIF
```

The sender first checks if it does not know the time when the last message was sent to the receiver (line 5) or if the idle time is too large (line 6) to avoid large time stamp intervals as described in section 5.3. If so, it sends a sync message and waits for an ack to initialize idlebegin[receiver]. Then the sender transmits the message to the destination node along with the time the message was stored in the current node (line 22) and the idle time (line 23) according to its local time with maximum clock drift local_rho and waits for an acknowledgment containing a parameter resend. If resend is true then the message is sent again in order to enable the receiver to measure round trip time.

The receiver of a message performs the following actions:

```
1 Receiver:
2   IF (receive <sync> from sender) THEN
3       rttbegin[sender] = NOW;
4       send <ack> to sender;
5   ELSEIF (receive <xmit(M, lifetime, idletime,
6                   rho)> from sender)
7   THEN
8       Time rttend = NOW;
9       IF (rttbegin[sender] == 0) THEN
10          rttbegin[sender] = NOW;
11          send <ack(TRUE)> to sender;
12      ELSE
13          M.lifetime_max += lifetime/(1 - rho);
14          M.lifetime_min += lifetime/(1 + rho);
15          M.idletime_min += idletime/(1 + rho);
16          M.begin = rttend
17              - M.lifetime_max*(1 + local_rho)
18              + M.idletime_min*(1 - local_rho)
19              - (rttend - rttbegin[sender]);
20          M.end = rttend
21              - M.lifetime_min*(1 - local_rho);
22          M.lifetime_max += (rttend
23              - rttbegin[sender])*(1 - local_rho);
24          rttbegin[sender] = NOW;
25          send <ack(FALSE)> to sender;
26      ENDIF
27  ENDIF
```

The receiver waits for a sync or xmit message from a sender. If it receives a sync, it just initializes rttbegin[sender] and returns an ack to the sender.

If it receives an xmit message the receiver first checks if it does not know the time when the last message arrived from this sender (line 9) and just initializes rttbegin[sender] and returns an ack(TRUE) to the sender asking it to resend the message in this case.

If the sender knows rttbegin[sender] it can update the fields of the message according to the formula in the previous section and can calculate M.begin and M.end. Note that the received M.lifetime_max does not yet include the last *rtt* value, so it has to be explicitly subtracted (line 19) without time transformation, since it has been measured using local time of the receiver. Only afterwards M.lifetime_max is updated to include the last *rtt* value (line 23) transformed to UTC. Finally the receiver sends an ack back to the sender.

The checks for idlebegin[receiver] and rttbegin[sender] in sender and receiver respectively enable both the sender and receiver to independently run garbage collection algorithms to keep the sets idlebegin and rttbegin small as described in section 5.3.
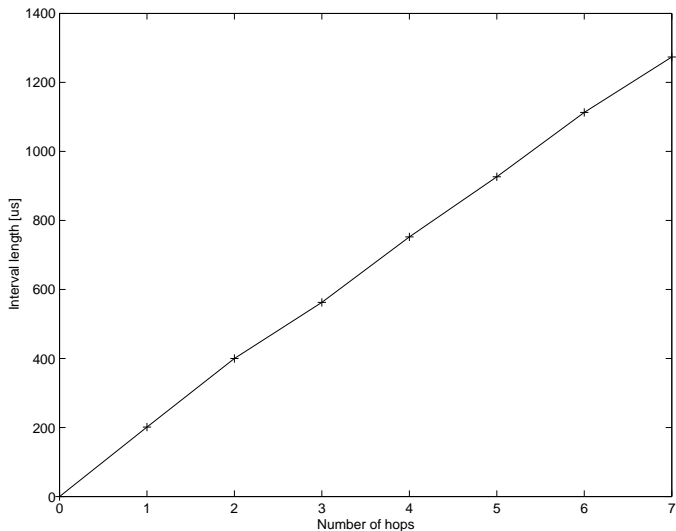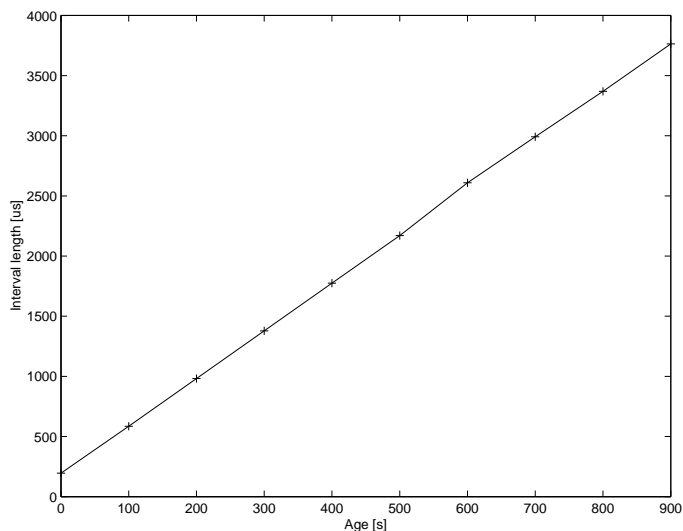
Figure 5: Accuracy depending on age and number of hops

5.6 Interval Arithmetic

Using the algorithm described in the previous sections, we are now able to answer the questions posed in the introduction using a special interval arithmetic, which is based upon [5]. For instance to determine if $[t_1, t_2]$ happened before $[t_3, t_4]$ the following formula can be used:

$$[t_1, t_2] < [t_3, t_4] = \begin{cases} \text{YES} & : & t_2 < t_3 \\ \text{NO} & : & t_4 < t_1 \\ \text{MAYBE} & : & \text{otherwise} \end{cases}$$

To determine whether $[t_1, t_2]$ and $[t_3, t_4]$ happened within a certain real–time span X the following formula is used:

$$\begin{aligned} & \|[t_1, t_2] - [t_3, t_4]\| < X \\ & = \begin{cases} \text{YES} & : & \max(t_4, t_2) - \min(t_3, t_1) < X(1 - \rho) \\ \text{NO} & : & \max(t_3, t_1) - \min(t_4, t_2) \geq X(1 + \rho) \\ \text{MAYBE} & : & \text{otherwise} \end{cases} \end{aligned}$$

Note that the real–time interval X has to be transformed to local time first by multiplying by $1 \pm \rho$, since the time stamp intervals are relative to local time.

The real–time "distance" between two time stamp intervals can be estimated using the following formula:

$$\|[t_1, t_2] - [t_3, t_4]\| \leq (\max(t_4, t_2) - \min(t_3, t_1))/(1 - \rho)$$

Again the calculated local time difference has to be transformed to real–time by dividing by $1 - \rho$.

When comparing points in time (for example a locally generated t_x) against time stamp intervals received from other devices, the time stamp t_x is transformed into the interval $[t_x, t_x]$ and used with the above formulas.

6. ACCURACY

In order to get an impression of the accuracy of the synchronization algorithm we did some measurements on a cluster of 800 MHz Pentium III Linux PCs connected by 100 Mbit/s Ethernet using TCP and assuming $\rho = 10^{-6}$. This has to be considered as a best case scenario, since sensor networks typically use a networking technology providing a bandwidth well below 1 Mbit/s and embedded processors with no more than 10 MIPS. However, since the algorithm is neither especially CPU intensive nor network bandwidth intensive, the measurements should give a good impression of the algorithm's possible accuracy.

Synchronization inaccuracies show up as (increasing) time stamp intervals and stem from two different sources: first, the age of a time stamp (due to the clock drift), and second, the number of hops a time stamp has been passed along (due to using round trip time as an estimation for message delay).

Therefore we did two measurements, the first of which measures time stamp interval length depending on the age of a time stamp. Since the error resulting from age is additive over the nodes, we generate a zero length time stamp interval in node 1, store it for X seconds and send it to node 2, which prints out the length of the received time stamp interval. We repeat this 1000 times and calculate the average. Figure 5 shows the results[2], indicating a linear increase of inaccuracy with age.

The second measurement determines time stamp interval length depending on the number of hops a time stamp has been passed along. We generate a zero length time stamp interval in node 1 and pass it on to node 2, 3, ..., 7, which all print out the length of the received time stamp interval. We repeat this 1000 times and calculate the averages. Figure 5 shows the results[3], indicating a linear increase

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[2]The exact interval lengths are 195, 585, 982, 1378, 1775, 2170, 2609, 2992, 3369, 3764μs.
[3]The exact interval lengths are 0, 201, 400, 562, 752, 926, 1113,

of inaccuracy with the number of hops.

Since the two types of inaccuracies are additive one can interpret the measurements as follows: Passing a time stamp along no more than 5 hops with an age of no more than 500 seconds one can expect an inaccuracy of no more than 3ms in the examined setting, which is a reasonable value compared to existing clock synchronization algorithms. What this means is that the algorithm will be able to give an exact answer (as opposed to MAYBE) when comparing time stamps representing points in time with more than 6ms in between, since then the resulting time stamp intervals (3ms each) cannot overlap. With less than 6ms in between the algorithm might still give an exact answer, but MAYBE answers are likely.

7. IMPROVEMENTS

There are several ways to improve the accuracy of the algorithm (i.e., reduce the probability of MAYBE results), which are worth further investigation.

One idea to avoid MAYBE results when comparing time stamps originating from the same node is to keep a history of time stamps instead of only one time stamp. Instead of *updating* the single time stamp upon receipt, the receiving node *appends* the updated time stamp together with a unique node identification i and its ρ_i value to the time stamp history or *reuses* a time stamp from the history if there already is an entry for this node in the history. If comparing time stamps results in MAYBE then the histories of the compared stamps are searched for common nodes and the comparison is repeated using the time stamps of these common nodes, transforming time values if necessary, using the ρ values stored in the history. This is likely to give a "better" answer, since inaccuracy increases with age and hop count of the time stamps. For the same reason the accuracy of calculated real–time spans can be improved by using "younger" time stamps from the history in the same way whenever possible.

A different and more general idea is to replace MAYBE results with a probability depending on the layout of the compared time stamp intervals, i.e., the algorithm would then answer $X < Y$ with probability p instead of $X maybe < Y$. To implement this we have to find out probability distributions for the time instants over the time stamp intervals.

Consider for example the two overlapping time stamp intervals S_1 and S_2 with $t_1 \leq t_3 \leq t_2 \leq t_4$ shown in figure 6, for which the algorithm would answer MAYBE when asked whether $S_1 < S_2$. If we know probability distributions $p_1(t)$ and $p_2(t)$, such that $p_i(C_i)$ is the probability that the exact point in time represented by S_i is C_i, we can calculate the probability p for $S_1 < S_2$ by "iterating" over the possible C_1 values and summing up the probabilities for $C_1 < C_2$:

$$\int_{t_1}^{t_2} p_1(t) \left(\int_{t}^{t_4} p_2(q) \mathrm{d}q \right) \mathrm{d}t \qquad (4)$$

For uniform distributions $p_i(t)$[4] this evaluates to

1273μs.

[4] $p_1(t) = 1/(t_2 - t_1)$ for $t \in [t_1, t_2]$ and 0 otherwise; $p_2(t)$ likewise
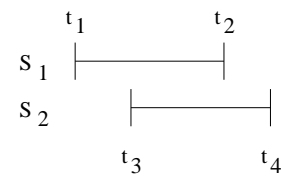

Figure 6: Overlapping time stamp intervals

$$\frac{t_3 - t_1}{t_2 - t_1} + \frac{t_4(t_2 - t_3) - (t_2^2 - t_3^2)/2}{(t_2 - t_1)(t_4 - t_3)} \qquad (5)$$

Assuming for example $t_1 = 0$, $t_2 = t_4 = 2$, and $t_3 = 1$ we can calculate the probability for $S_1 < S_2$ as 0.75. However, assuming a uniform distribution usually is an oversimplification, since due to the characteristics of the algorithm[5] the probability in the middle of the interval is much larger than at the ends. It remains an open task to determine good probability distributions. Furthermore it has to be investigated for which cases knowing a probability instead of MAYBE is advantageous for applications.

8. RELATED WORK

There has been much work on physical clock synchronization in the past [3, 13, 16, 17]. However, most of the proposed synchronization algorithms, including the well known Network Time Protocol [15], rely on a network that is not partitioned and where it is always possible to produce good estimations for the message delay. As pointed out in section 3, this is not the case for sparse ad hoc networks. Furthermore, some of the algorithms do not have the correctness property pointed out in section 5, possibly resulting in claiming false properties on a set of time stamps.

The offline algorithms presented in [6, 9] allow offline time synchronization, i.e., after the distributed computation is finished or after a certain amount of data has been collected. However, these offline algorithms assume a constant message delay and that the actual clock drift is a linear function in time and therefore only produce approximations.

Elson and Estrin present a technique called *post–facto synchronization* [10], which is also based upon unsynchronized local clocks but limits synchronization to the transmit range of the mobile computing nodes and is (as the authors claim) "inappropriate for applications that need to communicate a time stamp over long distances or time", which is the focus of our algorithm.

Global infrastructures like GPS provide an accurate time base. However, GPS is not suitable for use in a large class of smart devices due to its high power consumption and the required line of sight to the GPS satellites.

Logical time algorithms such as [12, 14] provide a solution for causal ordering of events, but they require that causal dependencies between event generating entities manifest themselves in a network message exchange between these entities. This assumption does not hold here, since we are talking about causal relationships in the real world.

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[5] We use 0 and rtt as lower and upper bounds for the message delay. It is much more likely that the actual message delay is about $rtt/2$ than 0 or rtt.

9. CONCLUSION AND OUTLOOK

We pointed out the problem of physical time synchronization in sparse ad hoc networks giving two reasons why classical clock synchronization algorithms fail in this environment.

We then presented a synchronization algorithm suitable for a certain class of applications of sparse ad hoc networks, which transforms time stamps exchanged between nodes inside messages to the local time of the receiver instead of adjusting the clocks. The algorithm has a low resource and message overhead and therefore is well suited for resource restricted distributed sensor networks.

There are several prototype implementations of the algorithm. We are currently working on an event distribution service with temporal delivery order of time stamped events for ad hoc networks, which is based on the presented algorithm. We intend to use this service for time dependent sensor fusion in the Smart–Its project[4].

Further research will focus on working out the improvements sketched in section 7. Another interesting point is how to select the initial time stamp interval that represents the point in time when an external event has been sensed. In the description of the algorithm we assumed that the event we want to time stamp happens "inside" the computing device and therefore we started with a zero length interval $[NOW, NOW]$. However, often a "real world" event is sensed by an external sensor, which itself is connected to the computing device. Furthermore, the detection of the event in the computing device might be indeterministically delayed due to software. In such cases one should already start with a non–zero time interval that contains the point in time the event was sensed. There is no obvious way to determine this interval except calculating it from the properties of the technology that is used. Last but not least, we will have to examine and evaluate different strategies for handling connections to large numbers of peers as pointed out at the end of section 5.3.

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