

# Cambridge International AS & A Level

CANDIDATE NAME					
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MATHEMATICS 9709/61

Paper 6 Probability & Statistics 2

October/November 2023

1 hour 15 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 16 pages. Any blank pages are indicated.

bility that the mean of a random sample of 36 values of $X$ is less than 405.	[3]

	who exercise regularly. The upper bound of the confidence interval was found to be 0.487, corresponding significant figures.
F	Find the value of $\alpha$ correct to the nearest integer.

()	Assu	ume that the owner is correct.
	(i)	Find the probability that there will be at least 4 hits during a 10-minute period.
	(ii)	Use a suitable approximating distribution to find the probability that there will be fewer the 40 hits during a 3-hour period.

A friend agrees that the website receives, on average, 0.3 hits per minute. However, she notices that the number of hits during the day-time (9.00 am to 9.00 pm) is usually about twice the number of hits during the night-time (9.00 pm to 9.00 am).

	follows a Poisson distribution.	[1]
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(ii)	Specify separate Poisson distributions that might be suitable models for the number of during the day-time and during the night-time.	hits [2]
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inde	masses, in kilograms, of chemicals $A$ and $B$ produced per day by a factory are modelled by the ependent random variables $X$ and $Y$ respectively, where $X \sim N(10.3, 5.76)$ and $Y \sim N(11.4, 9.61)$ . income generated by the chemicals is \$2.50 per kilogram for $A$ and \$3.25 per kilogram for $B$ .
(a)	Find the mean and variance of the daily income generated by chemical $A$ . [2]
(b)	Find the probability that, on a randomly chosen day, the income generated by chemical $A$ is greater than the income generated by chemical $B$ .
(b)	

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In the past the number of enquiries per minute at a customer service desk has been modelled by

Given the	at the total	number o	of enquir	ries is 5,	carry o	ut the te	st at the	2.5% s	ignifica	nce lev	el.
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6	A continuous random variable X takes values from 0 to 6 only and has a probability distribution that
	is symmetrical.

Two values, a and b, of X are such that P(a < X < b) = p and  $P(b < X < 3) = \frac{13}{10}p$ , where p is a positive constant.

(a)	Show that $p \leq \frac{5}{23}$ .	[1]
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<b>(b)</b>	Find $P(b < X < 6 - a)$ in terms of $p$ .	[2]

It is now given that the probability density function of X is f, where

$$f(x) = \begin{cases} \frac{1}{36}(6x - x^2) & 0 \le x \le 6, \\ 0 & \text{otherwise.} \end{cases}$$

Given that $b = 2$ and $p = \frac{5}{27}$ , find the value of $a$ .	[5]
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	$n = 50$ $\Sigma x = 23.0$ $\Sigma x^2 = 13.02$
	$n = 50 \qquad \angle x = 25.0 \qquad \angle x = 13.02$
(a)	Carry out a test at the 5% significance level of the null hypothesis $\mu = 0.5$ against the alternative hypothesis $\mu < 0.5$ .

Later, a similar test is carried out at the 5% significance level using another sample of size 50 and the same hypotheses as before. You should assume that the standard deviation is unchanged.

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# **Additional Page**

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