

cs430 9-28-2017

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1 Intro

TA: Alex duff

Provides fundamentals of 2d and 3d graphics * Representations (lines, curves, polygons) * Drawing, clipping, transformations, viewing * Implementations of basic graphics systems.

Assignments will build upon each other.

You can use any lang.

7 Programming assignments

Drops lowest assignment

1 point off for every hour late

1.1 Topics

- MATH
- Primitive reps of simple figures.
- Drawing algorithms
- Clipping algorithms
- 2d/3d viewing
- Hidden surface removal.
- color and lighting (wrap up)

2 Lecture

What we want to accomplish is a software service pipeline

2.1 Raster Image

Specify objects via geometry and then produce a 2D image

Fast

But vector allows for better scaling

2.2 Pipeline

How something goes from primitive to graphics on screen.

Vertices -> vertex processor -> Clipper and primitive -> Rasterize -> Fragment Processor -> Pixels

2.3 Math you will need

2.3.1 Geometry

2.3.1.1 Affine

Scalars ,points, vectors, and their operators

2.3.1.2 Euclidean

- affine lacks angles and distance
- inner/dot product * Length Distance normalization

2.3.1.3 Projector

- How to display
- warping?

2.4 Points

Points will be the base for everything we use

2.5 Vectors

- Directed line segment
- Magnitude

Note: No actual position in space

Can be defined by two points via subtraction

$$v = P - Q$$

This means: Vector from Q to P

2.5.1 Arrive at a new point

$$v = P + Q$$

2.5.2 Operations

Every vector has an inverse

Can be multiplied by a scalar

Sum of two vectors is a vector

2.5.3 Parametric form of lines

Given an initial point and a vector we can find any point. $P(\alpha)$ on the line α units from P_0 in the direction of d .

$$P(\alpha) = P_0 + \alpha(d)$$

2.6 Dot Product

$$u \cdot v = \sum_{k=1}^N u_k v_k = u_1 v_1 + u_2 v_2 + \dots$$

To compute the distance from the origin to a point.

Euclidean distance from (x,y) to $(0,0)$ $\sqrt{x^2 + y^2}$

Or the n direction continue the formula.

$$\sqrt{p_1^2 + p_2^2 + \dots + p_n^2}$$

2.7 Unit Vector

Has length 1. $|v|$ Also called normalizing.

2.7.1 Helpful for angles

$$u \cdot v = |u||v|\cos(\text{angle})$$

2.7.2 Projection

We can use this to project one vector onto another. we can project u onto v as $u \cdot v / |v|$ as $\cos(\text{angle}) |v|$ where angle is the angle between u and v .

2.8 Matrix Operations

2.8.1 Determinants

- single real number
- Computed recursively * for a fixed row i

$$\det(A) = \sum_{j=1}^n A_{ij}(-1)^{i+j}\det(M_{ij})$$

2.8.2 Cross product

Given two non-parallel vectors, a and b $a \times b$ calculates a third vector n that is orthogonal to both a and b

Right hand rule - explains the direction. of the normal vector $n = a \times b$

$a \times b$ is not $b \times a$

It is the thing with crossing one direction minus cross in other direction This is a not in depth explanation

2.8.2.1 Example

Look at powerpoint online

2.8.3 Matrix Transpose and inverse

$$(A^t)^t = A \quad (A + B)^t = A^t + B^t \quad \text{Fill in rest from slide}$$

3 Second half of lecture

3.1 Motivation

User specifies the shape type

In this lecture We will talk about how to create an object with endpoints

3.2 Scan-Conversion Algorithms

compute pixel coords for ideal line on 2D raster grid

3.3 Drawing a line

given two end points

we can compute the slope with simple math

$$\text{delta}(y)/\text{delta}(x) = m$$

It will not form a perfect line with pixels. We need to start making assumptions of which pixel to fill in.

If we want to draw a line we can:

Ineffecient way

- compute the next x position
- then compute the next y going back to the slope formula * may not be in a strict pixel location so we need to round to an interger location

Ineffecient way

Less mutiplication Makes $m = \text{delta}(y)/1$ $x_{i+1} = x_i + 1$ $y_{i+1} = y_i + m$

3.3.1 Digital Differential Analyzer (DDA)

if $|m| < 1$ * $\text{Deltax} = 1$ and $\text{delta}(y) = m$ * Start left must point * End right most point else * $\text{Delta}(y) = 1$ and $\text{delta}(x) = 1/m$ * start at bottom most point * end top most point

check for vertical line case $m = \text{inf}$

With this we still have floating point operations

3.3.2 Bresenham's algorithm

No floating point operations

Based on implicit equation of a line: $(x, y) = x + y = 0$

Zoned out for this part. Look at powerpoint

$$= 2 - 2 + (2 - + 2(- x))$$

** 5 Diffderent cases ** 1. Vertical line 2. $0 \leq m \leq 1$ * if $q > r$ swap points 3. $m > 1$ 4. $-1 \leq m < 0$ * if $q > r$ swap points 5. $m < -1$

3.3.2.1 Example

$m < -1$ (P_x, P_y) $(P_x + 1/2, P_y - 1)$

4 Assigiment details

- read in post script. (.ps)
- Simulate writing to a frame buffer by creating XPM image
- Draw lines

** It will all build off of each other so make it modular when designing.**

- All black and white.
- Create data structures to hold points

5 Glossary

Orthogonal - Perpendicular