South Africa

```
## [1] "Census Females"
## # A tibble: 86 x 7
        age `1970`
##
                     `1985`
                              `1991`
                                    `1996`
                                              `2001`
                                                      `2011`
##
      <dbl>
              <dbl>
                      <dbl>
                              <dbl>
                                       <dbl>
                                               <dbl>
                                                       <dbl>
          0 347577 265629
##
   1
                            334664 434223. 454482 575028
          1 327004. 260708. 364874. 434296. 440667
          2 325266 271447. 381647. 449406. 442266. 564236.
##
          3 320516. 274451. 377053. 461697. 449032. 556210.
##
##
          4 318140. 273011. 379364. 474658. 459546. 544576.
   5
##
          5 313147. 267934. 375903. 480788. 469845. 526048.
##
   7
          6 309948 265764 368341. 479310. 477704. 502114.
          7 306471. 267165. 360249. 473457. 482862. 478502.
##
##
          8 303223. 272819. 354368. 467138. 492895. 460004.
          9 295460. 275083. 348572. 464657. 503893. 451534.
## # ... with 76 more rows
## [1] "Census Females 5-year"
##
  # A tibble: 18 x 2
        age `1980`
##
##
      <dbl>
              <dbl>
##
   1
          0 1736315
##
   2
          5 1575298
##
    3
         10 1382085
##
   4
         15 1296548
##
   5
         20 1187044
##
   6
         25
            956402
##
   7
         30
             799542
##
   8
         35 680398
##
   9
         40
             576749
## 10
         45
            488030
##
  11
         50
            401384
## 12
         55
            339598
## 13
         60 289582
## 14
         65
             221493
## 15
         70
             160492
## 16
         75
              93129
## 17
         80
              59494
## 18
         85
              52494
## [1] "Census Males"
## # A tibble: 86 x 7
##
        age
            `1970`
                     1985
                             `1991`
                                     `1996`
                                              `2001`
                                                      `2011`
##
      <dbl>
                      <dbl>
                              <dbl>
                                       <dbl>
                                               <dbl>
                                                       <dbl>
              <dbl>
##
          0 353187 266840
                            332158 432514. 453924 584097
          1 328995. 262455
                            371515 433911. 441106. 577574.
##
                    272988. 389101. 448461. 441893
##
          2 322879
##
          3 316004. 276266. 384583. 461203. 448540. 565571.
##
    5
          4 313864. 275394. 387601. 475238. 459394. 553093.
          5 310881. 270720. 383920. 482371. 470590. 534653
##
```

```
## 7
          6 309771. 268497. 375467. 481068. 478769. 510001.
## 8
         7 307354. 269153. 366494. 473935. 482864. 485063.
## 9
          8 304558. 274192. 360549. 465731. 491967. 465714.
          9 296602. 275718. 354626. 461874. 503328. 457150.
## 10
## # ... with 76 more rows
## [1] "Census Males 5-year"
## # A tibble: 18 x 2
##
        age `1980`
##
      <dbl>
              <dbl>
##
   1
          0 1756592
   2
         5 1582313
##
##
   3
        10 1387903
##
   4
        15 1336257
##
   5
         20 1316011
##
   6
         25 1089762
## 7
         30 908968
## 8
         35 754899
## 9
         40 626078
## 10
         45 513247
## 11
         50 416271
## 12
         55 326920
         60 262972
## 13
## 14
         65 189590
## 15
         70 123694
         75
## 16
            68244
## 17
         80
              33990
## 18
         85
              26737
```

$Thiele\ log\text{-}Normal\ Hump\ Spline$

[1] "relative convergence (4)"

##	log_tau2_logpop	log_tau2_logpop	log_tau2_logpop	log_tau2_logpop	log_lambda_fx	log
##	4.958921913	6.833850041	4.940434001	6.621883433	6.552399712	7
##	log_lambda_tp	tp_slope	tp_params_5	tp_params_10	log_lambda_phi	log_
##	5.103757886	-0.004964438	0.119853127	0.182806028	11.314626753	11
##	log_lambda_lambda	log_lambda_delta	log_lambda_epsilon			
##	2.884135789	4.729316870	5.292525158			

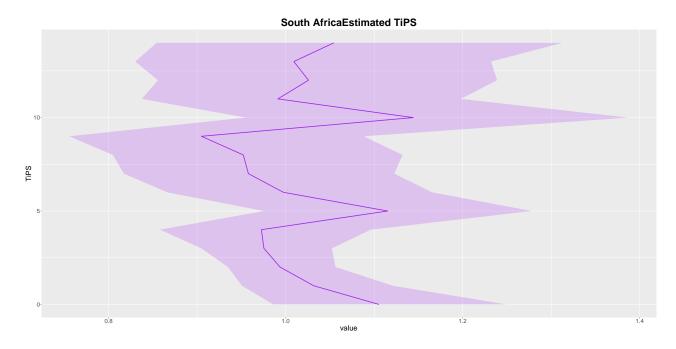


Figure 1: Estimated TiPS

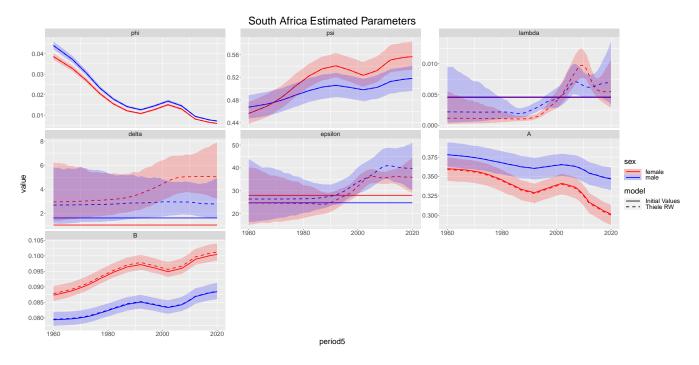


Figure 2: Estimated parameters

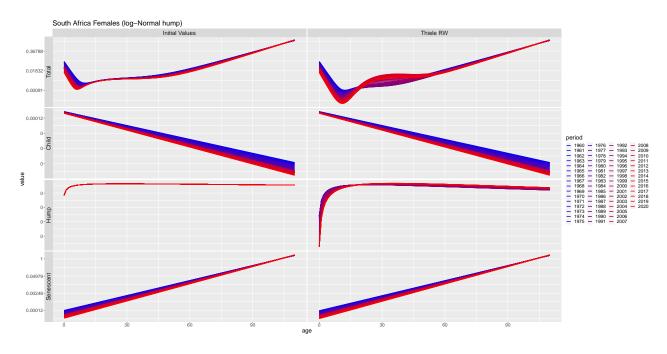


Figure 3: Thiele Decomposed

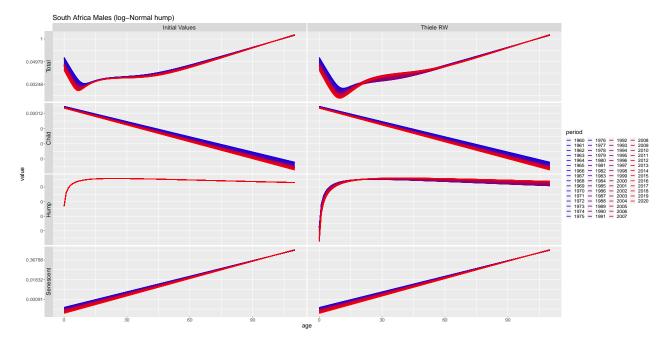


Figure 4: Thiele Decomposed

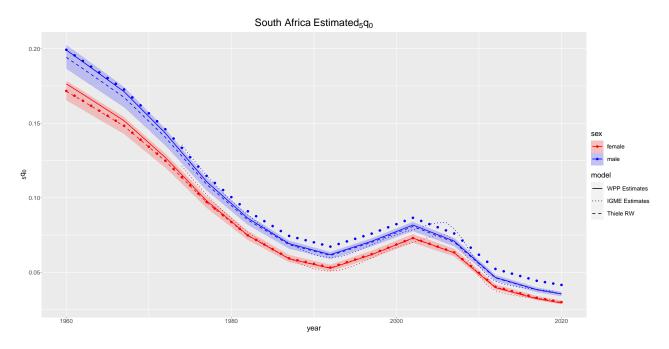


Figure 5: Estimated $_5q_0$

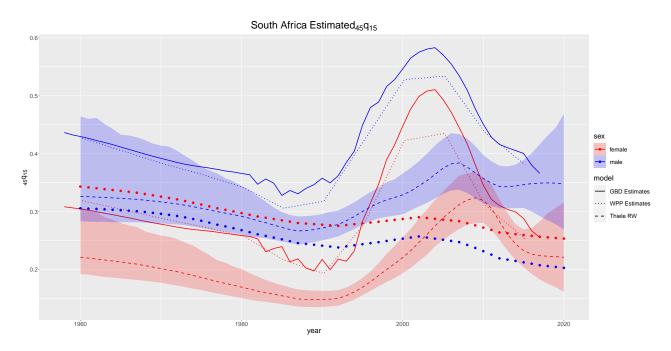


Figure 6: Estimated $_{45}q_{15}$

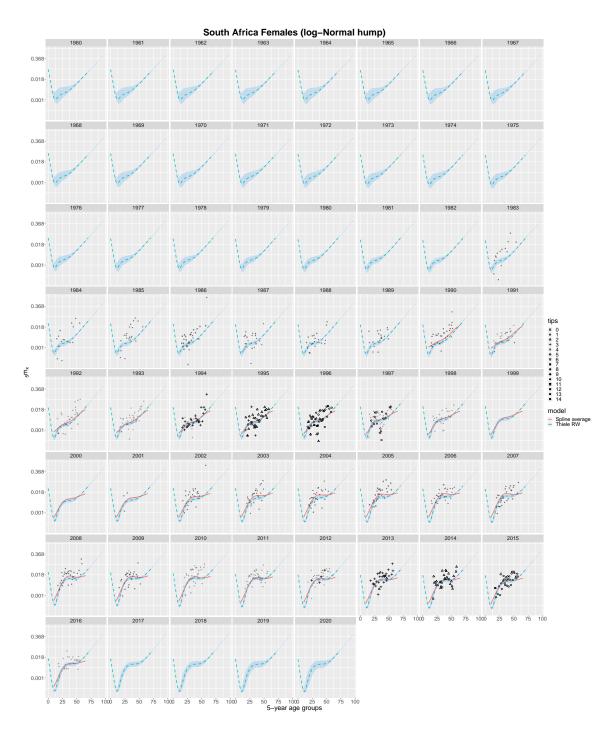


Figure 7: Mortality Schedules

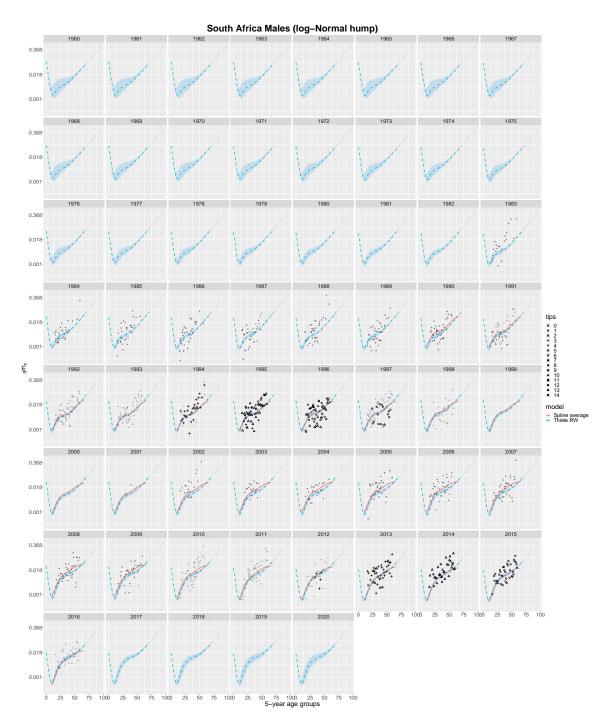


Figure 8: Mortality Schedules

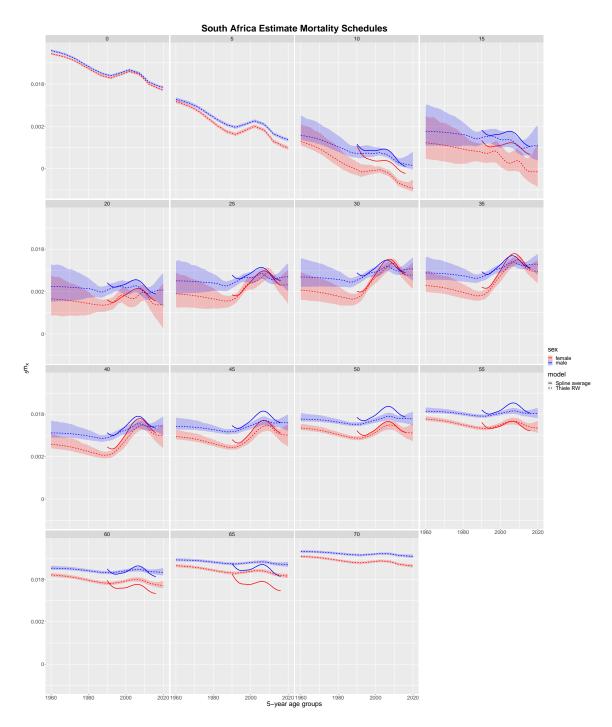


Figure 9: Mortality Schedules

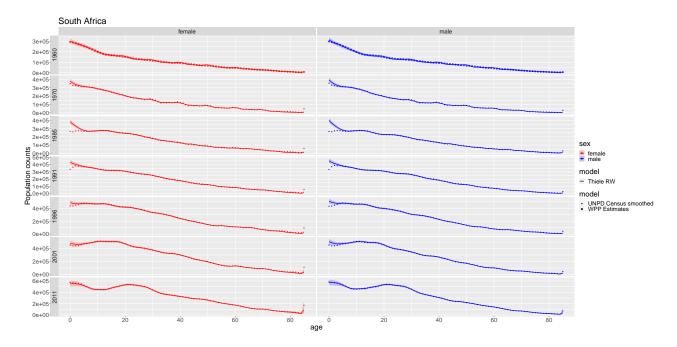


Figure 10: Population

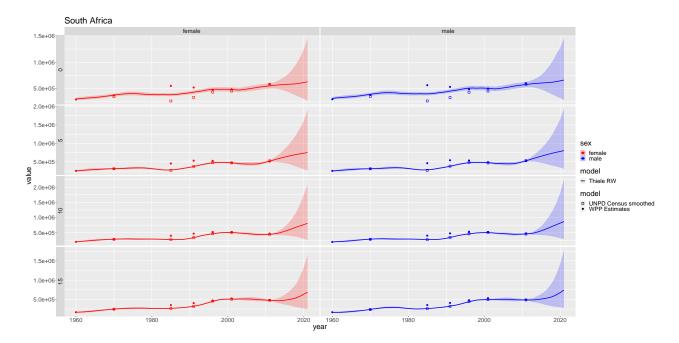


Figure 11: Population

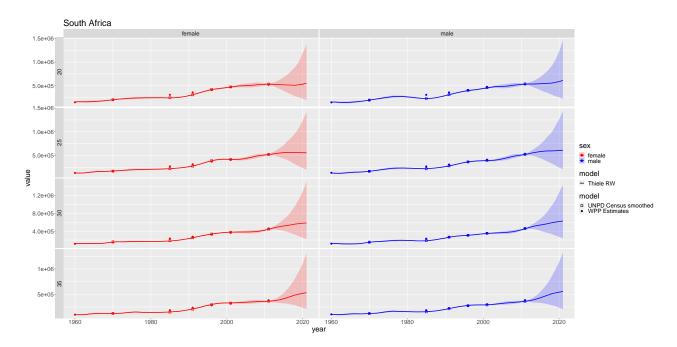


Figure 12: Population

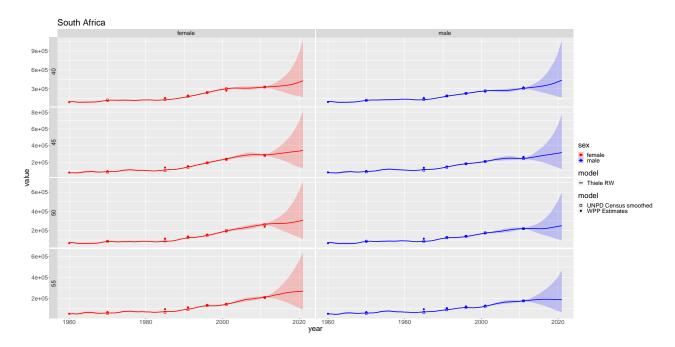
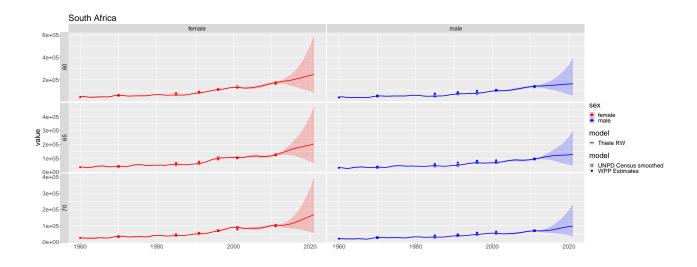


Figure 13: Population



vear

Figure 14: Population

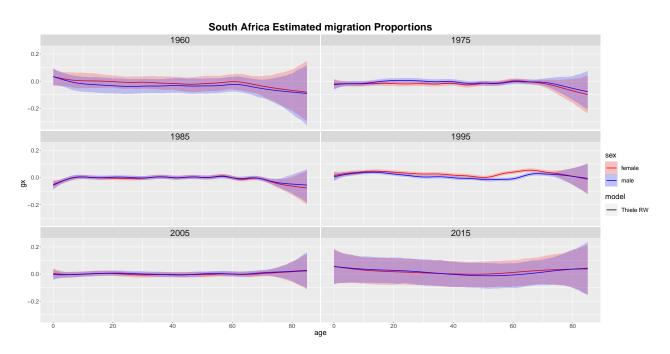


Figure 15: Migration

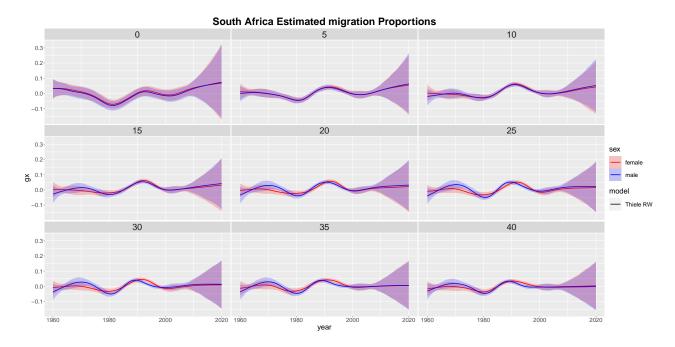


Figure 16: Migration

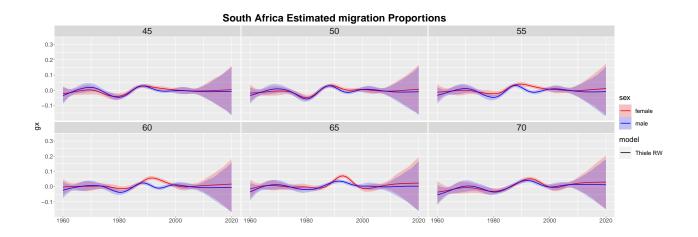


Figure 17: Migration

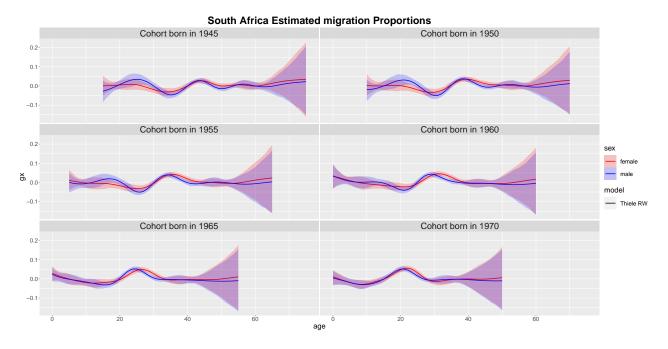


Figure 18: Migration

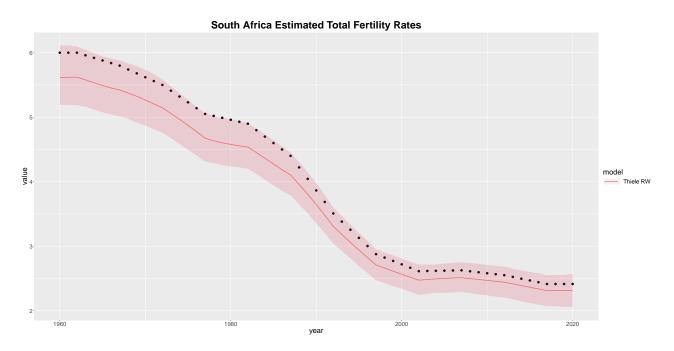


Figure 19: Total Fertility

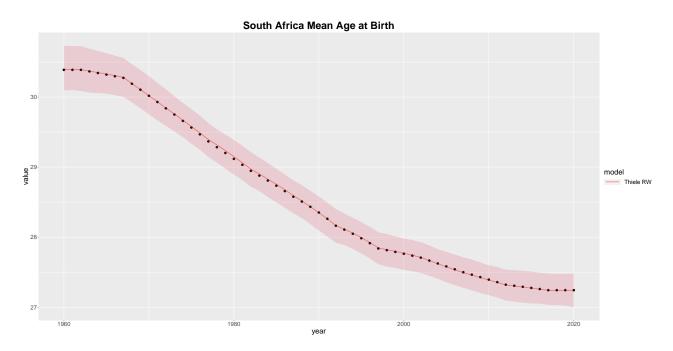


Figure 20: Mean age at births

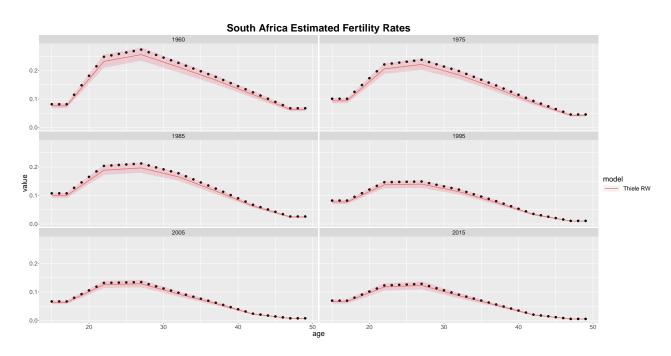


Figure 21: Fertility

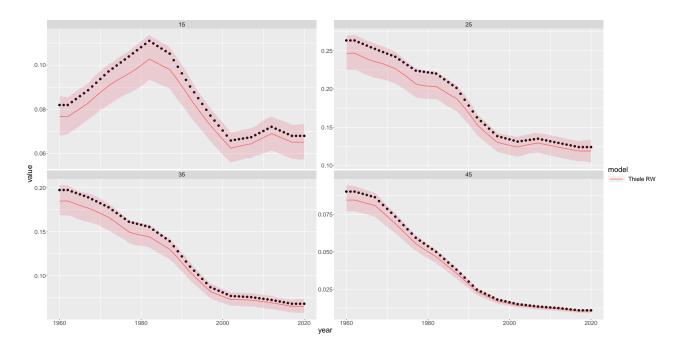


Figure 22: Fertility