South Africa

```
[1] "Census Females"
##
   # A tibble: 18 x 8
##
                           `1980`
                                              1991
                                                        1996
                                                                 2001
                                                                          `2011`
                  `1970`
                                    1985
      aggr.age
##
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                   <dbl>
                            <dbl>
                                     <dbl>
                                               <dbl>
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                                                                           <dbl>
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                                                                         2817868
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    2
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                          1575298 1332389 1782993.
                                                     2336693. 2406137. 2394570
                                                     2314907. 2510579. 2250611
    3
             10 1348764. 1382085 1399441 1642750
##
                1142882. 1296548 1265211 1571097
                                                     2192147. 2448870. 2504906
##
    4
                                                     2035716. 2238729. 2679896
##
    5
                 952966. 1187044 1196891 1472589
             20
##
    6
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                           956402 1000419 1323364
                                                     1835591. 2003318. 2516635
##
    7
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                           799542
                                   833799 1175631
                                                     1613717. 1789725. 1992804
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                                                     1379470. 1598192. 1758421
##
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                 603029
                                   704174
##
    9
             40
                 515926
                           576749
                                   587718
                                            816986
                                                     1124687. 1380426
                                                                         1546290
##
  10
             45
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                           488030
                                   489247
                                            671648
                                                      885848. 1123476. 1424543
##
  11
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                 362600.
                           401384
                                   398974
                                            565948.
                                                      704560.
                                                                877440
                                                                         1206940
##
  12
             55
                 297728.
                           339598
                                   318212
                                            458901
                                                      601565.
                                                                698798.
                                                                          985458
##
  13
             60
                 247674.
                           289582
                                   308936
                                            369214
                                                      535498.
                                                                594419.
                                                                          773404
##
  14
             65
                 193298.
                           221493
                                   244633
                                            274265
                                                      438712.
                                                                496508.
                                                                          556257
##
  15
             70
                 133027.
                           160492
                                    170841
                                            234870
                                                      319702.
                                                                378027.
                                                                          454833
## 16
             75
                  84691.
                            93129
                                    106760
                                                      221228.
                                                                260309.
                                                                          315984
                                            126677
## 17
             80
                  53949
                            59494
                                     66852
                                             86159
                                                      118149.
                                                                164176.
                                                                          222222
                            52494
                                     57501
                                                                135317
## 18
             85
                  48644
                                             57829.
                                                       95115.
                                                                          180126
##
  [1] "Census Males"
   # A tibble: 18 x 8
##
##
                  `1970`
                           `1980`
                                    `1985`
                                              `1991`
                                                        1996
                                                                 `2001`
                                                                          `2011`
      aggr.age
##
          <dbl>
                            <dbl>
                                     <dbl>
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    1
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                                                     2246133. 2223731
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                          1582313 1343319 1813819.
##
    2
              5 1511795
                                                     2328610. 2398574.
                                                                        2425181
             10 1336716. 1387903 1397197 1663472
##
    3
                                                     2280138. 2479199.
                                                                        2344276
##
    4
             15 1109962. 1336257 1203645 1587893
                                                     2109358. 2381102
                                                                         2498573
##
    5
                 919115. 1316011 1135300 1494166
                                                     1912284. 2137698
                                                                         2694646
##
    6
             25
                 782368
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                                                     1699104. 1873008.
                                                                        2542680
##
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                           908968
                                   848049 1234243
                                                     1488215. 1632402.
                                                                         2036206
##
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             35
                 591159.
                           754899
                                   726751 1020908. 1282776. 1427784
                                                                         1709346
##
    9
                                   595215
                                                     1053771. 1219094
             40
                 516576.
                           626078
                                            843271
                                                                         1402327
## 10
             45
                 442546.
                           513247
                                   505889
                                            674435
                                                      825470.
                                                                984585. 1195740
##
  11
             50
                 363686.
                           416271
                                   389010
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                                                      632887.
                                                                764732. 1011349
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##
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                                            432148
                                                                579664.
                                                                          811949
##
  13
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                           262972
                                   243118
                                            313535
                                                      377891.
                                                                436526.
                                                                          612364
                           189590
                                   194598
                                                      292626.
                                                                321646.
                                                                          401548
##
  14
             65
                 160633.
                                            219243
##
  15
             70
                 103104
                           123694
                                    128751
                                            171275
                                                      211793.
                                                                226574.
                                                                          293497
##
  16
             75
                  59768.
                            68244
                                     72518
                                                      137011.
                                                                149064
                                                                          165282
                                             84373
## 17
             80
                  32982
                            33990
                                     39123
                                             49036
                                                       62894.
                                                                 86738.
                                                                          100693
                                                       43803.
## 18
             85
                  29792
                            26737
                                     28949
                                                                 59628.
                                                                           75542
                                             27177.
```

Thiele log-Normal Hump RW

user system elapsed ## 25.32 0.39 25.77 ## [1] "relative convergence (4)"

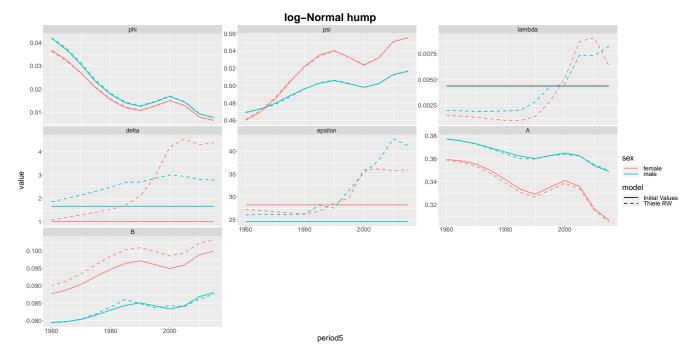


Figure 1: Estimated parameters

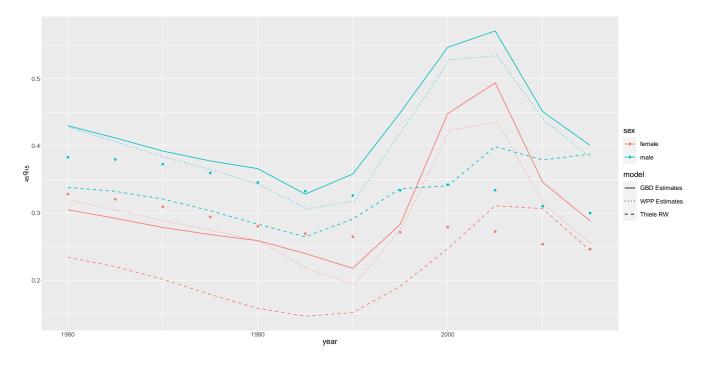


Figure 2: Estimated $_{45}q_{15}$

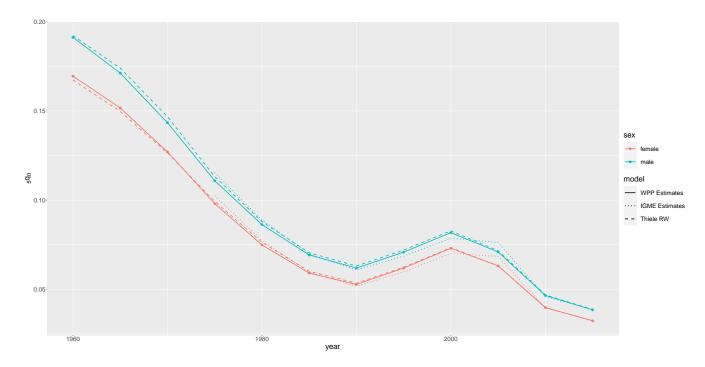


Figure 3: Estimated $_5q_0$

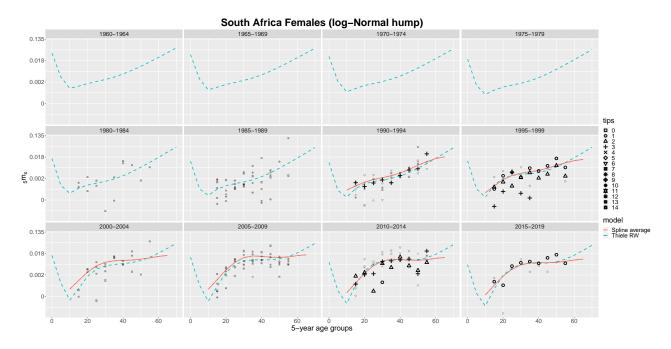


Figure 4: Mortality Schedules

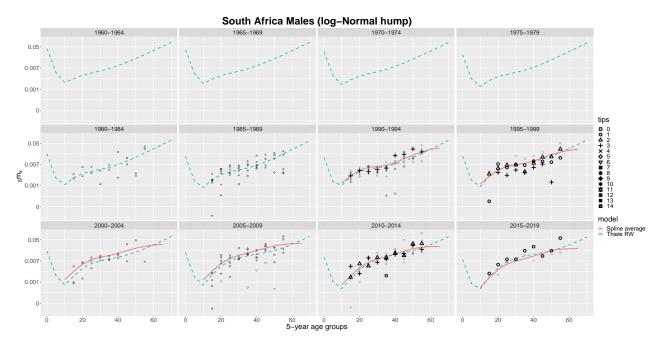


Figure 5: Mortality Schedules

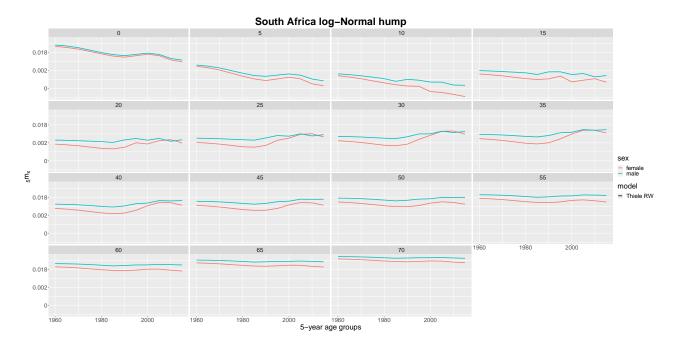


Figure 6: Mortality Schedules

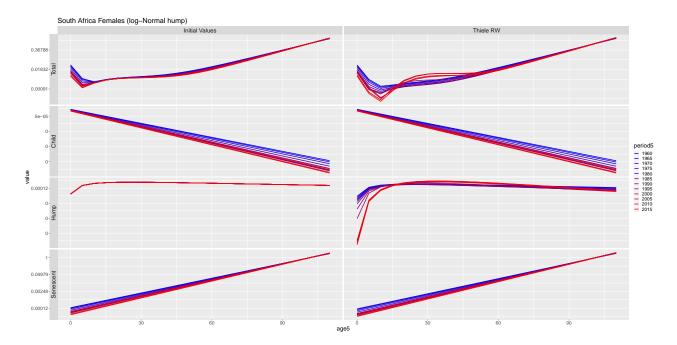


Figure 7: Thiele Decomposed

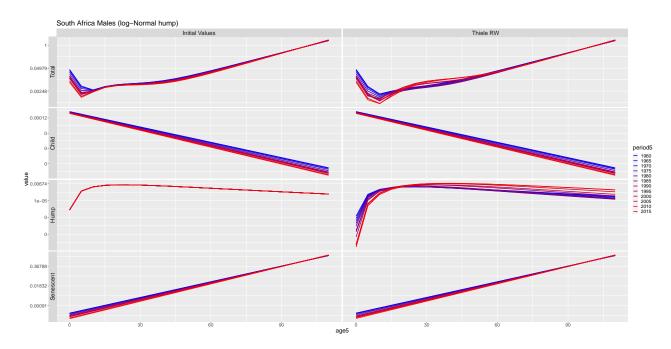


Figure 8: Thiele Decomposed

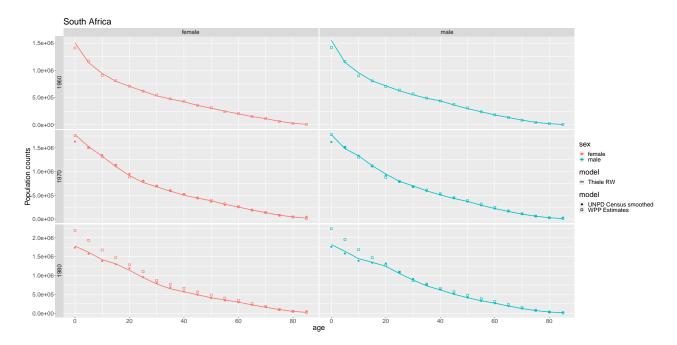


Figure 9: Population

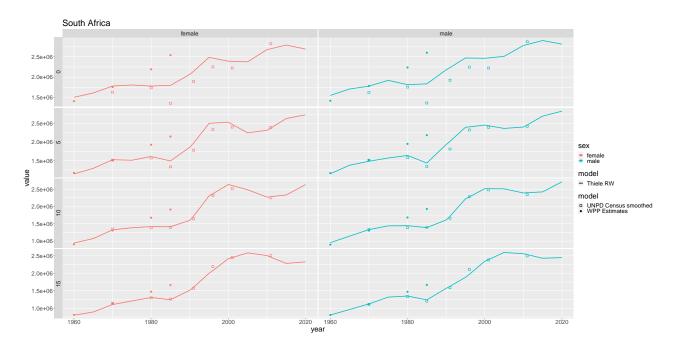


Figure 10: Population

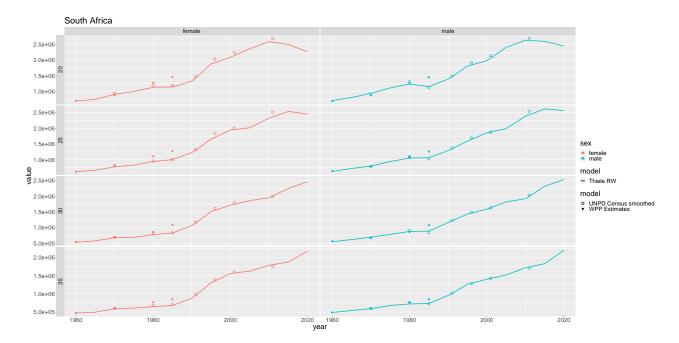


Figure 11: Population

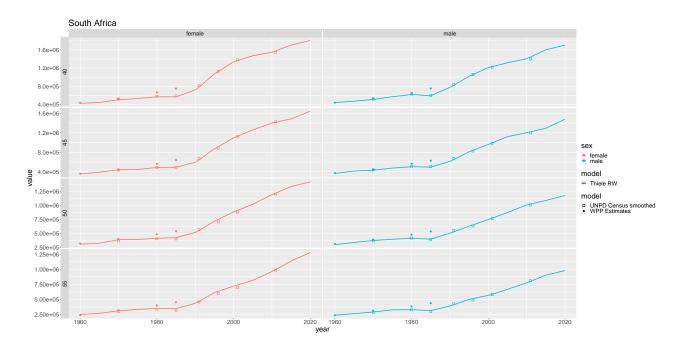


Figure 12: Population

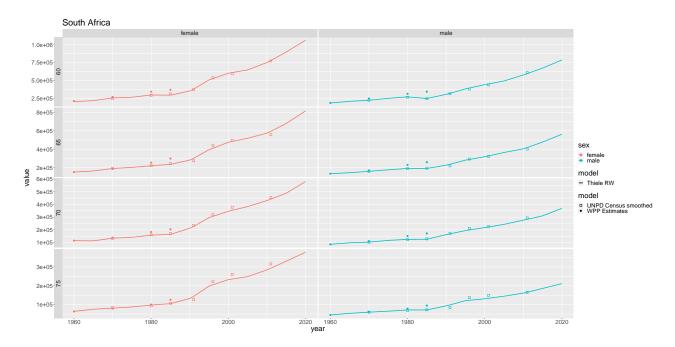


Figure 13: Population

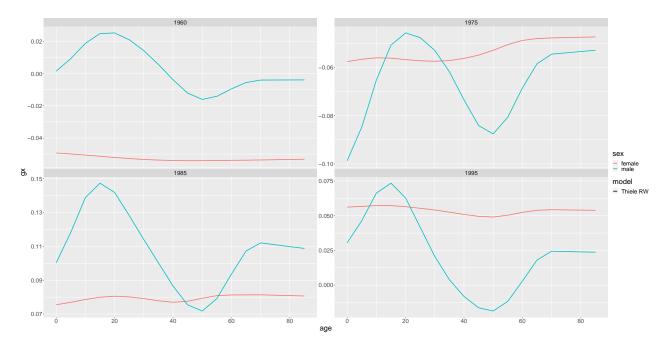


Figure 14: Migration

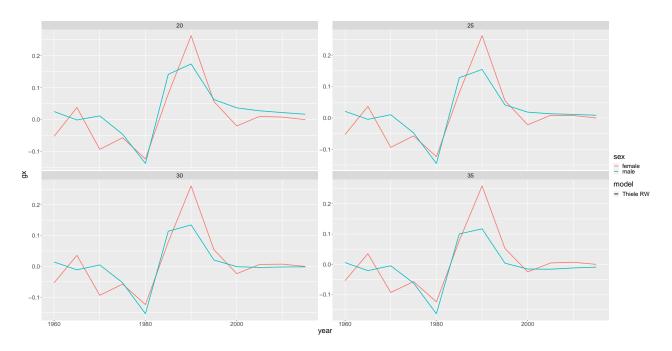


Figure 15: Migration

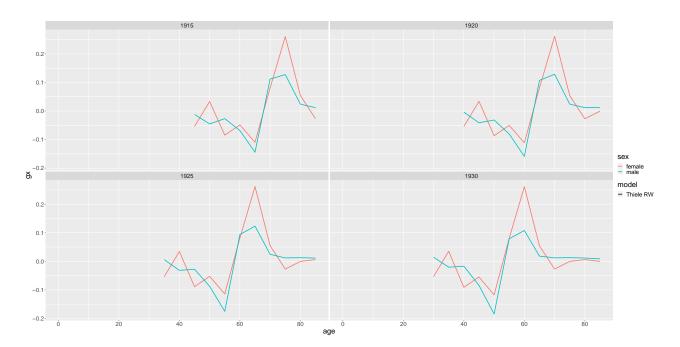


Figure 16: Migration

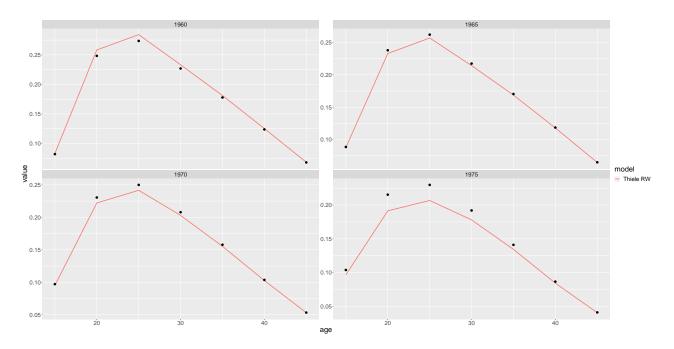


Figure 17: Fertility

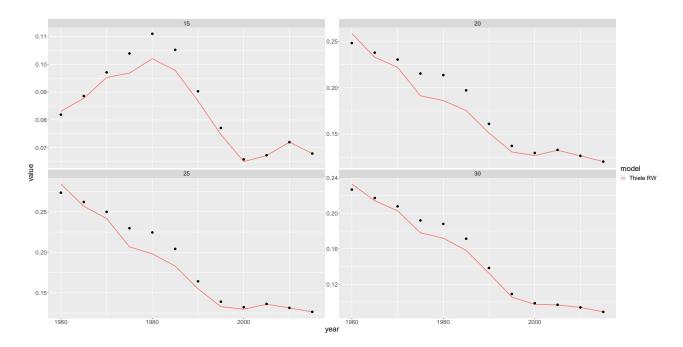


Figure 18: Fertility