



CS489/698: Intro to ML

Lecture 15: Generative Adversarial Networks



Outline

- Motivation
- Formulation
- Optimization
- Advanced

Generative Models

- Given training data from p_{data}
- Generate new samples from p_{model}
- Want $p_{\text{model}} \sim p_{\text{data}}$



The “Obvious” Approach

- Use training data to estimate density $p_{\text{model}} \sim p_{\text{data}}$
 - Which algorithm?
- Then sample from p_{model}
- What might go wrong?
 - Estimating density is hard, very hard...
 - Sampling from high-d density is hard, very hard...

Why Generative Models?

- If we can generate, we must know the objects so well!
 - Feature extraction; pre-training
- Semi-supervised learning
- Planning
- And the cool applications

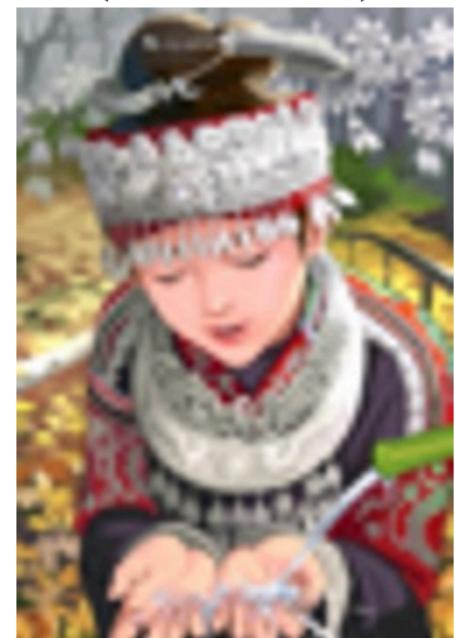
Image Super-Resolution (Ledig et al, CVPR'17)

bicubic
(21.59dB/0.6423)

SRResNet
(23.53dB/0.7832)

SRGAN
(21.15dB/0.6868)

original



Interactive Image Generation

(Zhu et al, ECCV'16)



Neural photo editing (Brock et al, ICLR'17)

Image to Image Translation

(Isola et al, CVPR'17)



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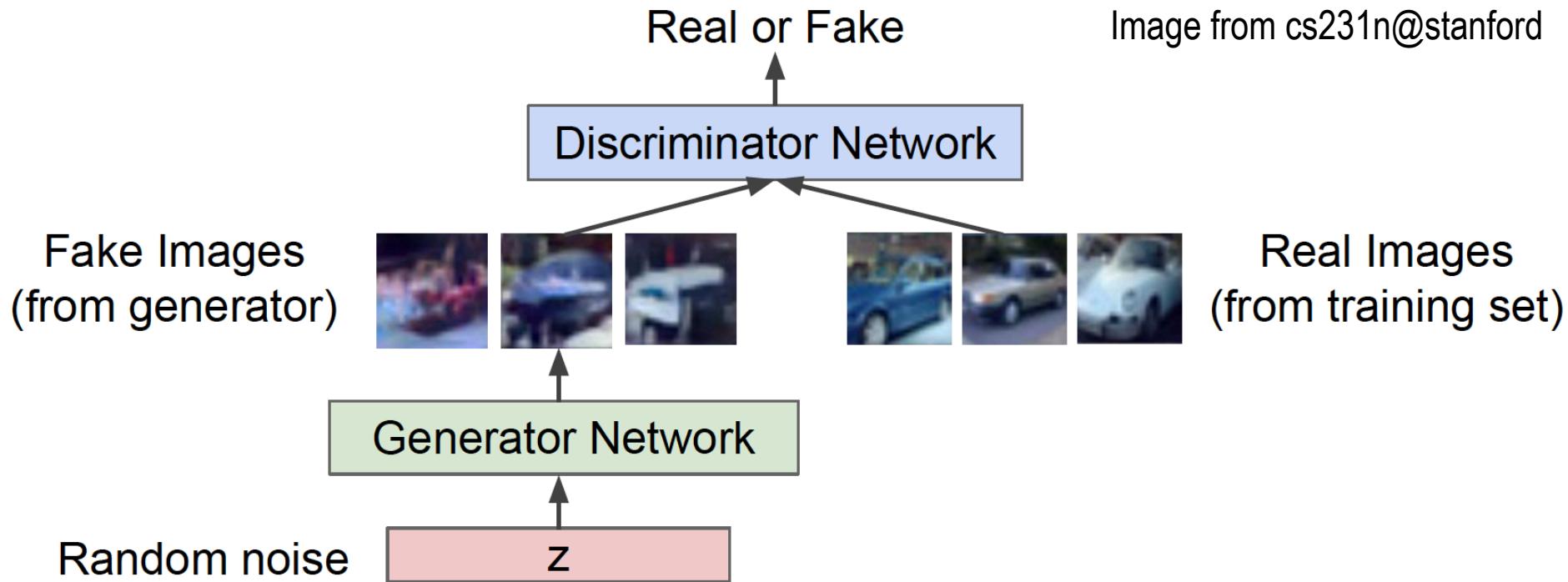
Generative Adversarial Networks

(Goodfellow et al, NIPS'14)

- A generator proposes samples
- A discriminator examines samples
 - Accept if sample “resembles” training data
 - Reject otherwise
- How can generator “fool” discriminator?



Key Idea



- No density estimation
- Directly generate image from random noise!

Minimax Game

$$\min_G \max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{z \sim p_z} [\log(1 - D(G(z)))]$$

- $D(x)$: probability of x coming from same distribution as training data
- Discriminator D : max prob of training data and min prob of generated sample
- Generator G : max prob of generated sample (fool discriminator)
- Zero-sum game: your loss is my gain

Why Would It Work?

$$\min_G \max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{z \sim p_z} [\log(1 - D(G(z)))]$$



change of variable

$$\min_G \max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [\log(1 - D(x))]$$

- Fix G , when is D optimal?

- $D(x) = p_{\text{data}}(x) / [p_{\text{data}}(x) + p_{\text{model}}(x)]$



$$\min_G \text{JS}(p_{\text{data}} \| p_{\text{model}})$$

- Plug in optimal D , when is G optimal?
 - $p_{\text{model}} = p_{\text{data}}$

Minimax Theorem

$$\min_G \max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [\log(1 - D(x))]$$



$$\max_D \min_G \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [\log(1 - D(x))]$$

- Fix D, when is G optimal?
 - **collapsing on modes of D**
- Plug in optimal G, when is D optimal?
 - **D(x) = 1/2**

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Representing D and G

- So far assumed D and G can be arbitrarily “smart”
- In practice, $D(x) = D(x; \theta_d)$ and $G(z; \theta_g)$
 - Each is a DCNN, with θ being the weights
[Deep CNN](#)
- Run SGD to find best θ_d and θ_g

Algorithm (Goodfellow et al, NIPS'14)

for number of training iterations **do**

for k steps **do**

- Sample minibatch of m noise samples $\{\mathbf{z}^{(1)}, \dots, \mathbf{z}^{(m)}\}$ from noise prior $p_g(\mathbf{z})$.
- Sample minibatch of m examples $\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(m)}\}$ from data generating distribution $p_{\text{data}}(\mathbf{x})$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D \left(\mathbf{x}^{(i)} \right) + \log \left(1 - D \left(G \left(\mathbf{z}^{(i)} \right) \right) \right) \right].$$

end for

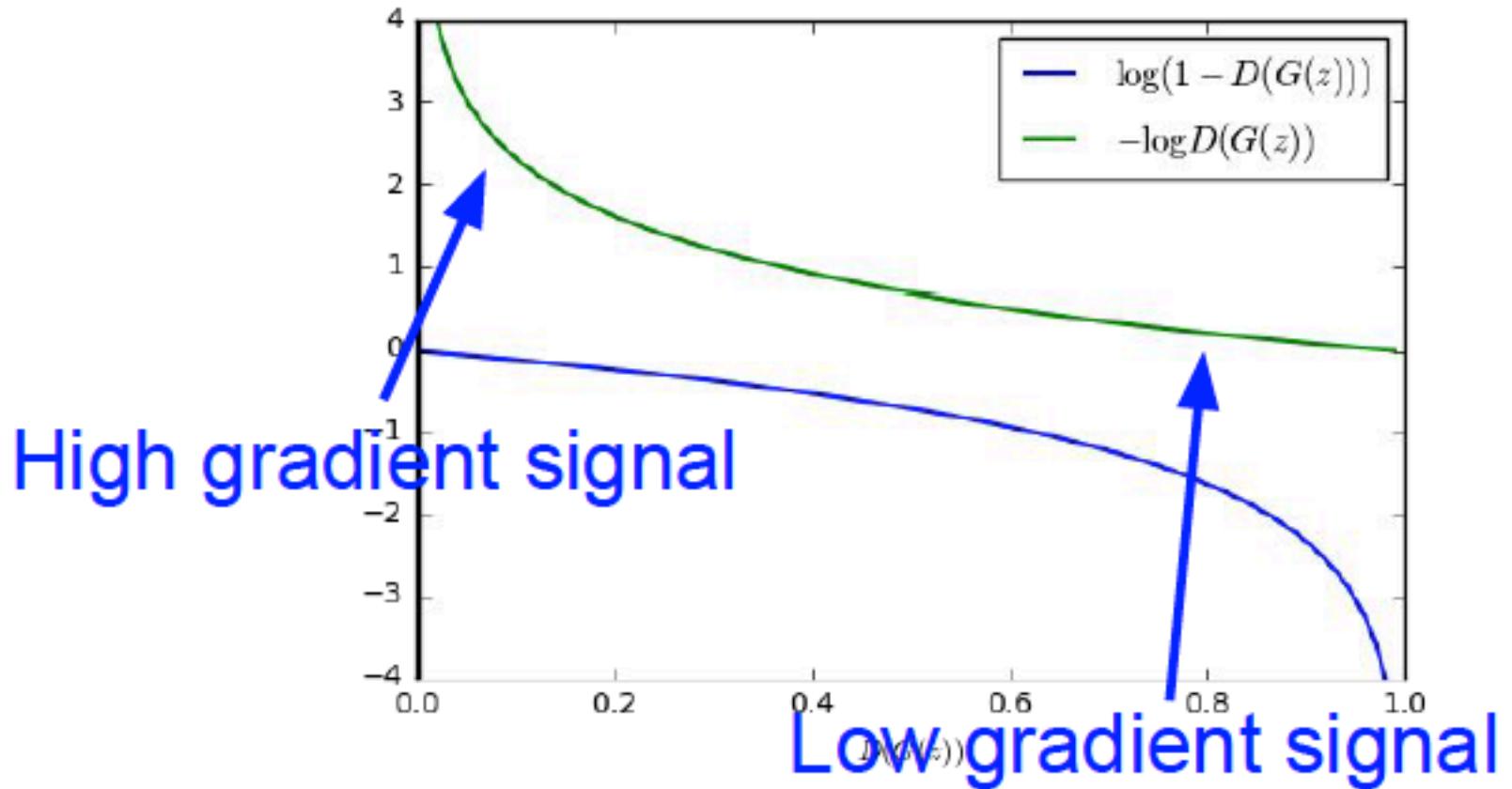
- Sample minibatch of m noise samples $\{\mathbf{z}^{(1)}, \dots, \mathbf{z}^{(m)}\}$ from noise prior $p_g(\mathbf{z})$.
- Update the generator by descending its stochastic gradient:

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log \left(1 - D \left(G \left(\mathbf{z}^{(i)} \right) \right) \right).$$

end for

Trick for Saturating Gradient

Image from cs231n@stanford



In practice

$$\max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [\log(1 - D(x))]$$

$$\min_G \mathbf{E}_{x \sim p_{\text{model}}} [\log(1 - D(x))]$$

$$\min_G \mathbf{E}_{x \sim p_{\text{model}}} [-\log D(x)]$$

$$\min_G \max_D \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [-\log D(x)]$$

Fix G, what is the optimal D?

Plug in optimal D, what is the optimal G?

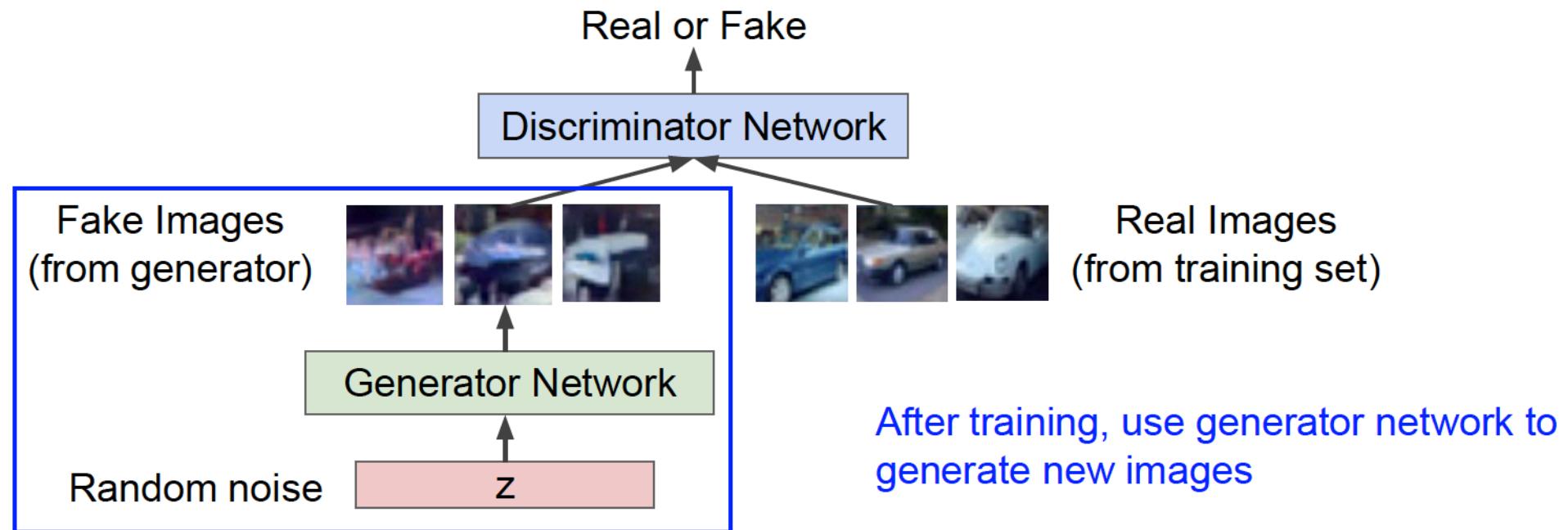
$$\max_D \min_G \mathbf{E}_{x \sim p_{\text{data}}} [\log D(x)] + \mathbf{E}_{x \sim p_{\text{model}}} [-\log D(x)]$$

Fix D, what is the optimal G?

Plug in optimal G, what is the optimal D?

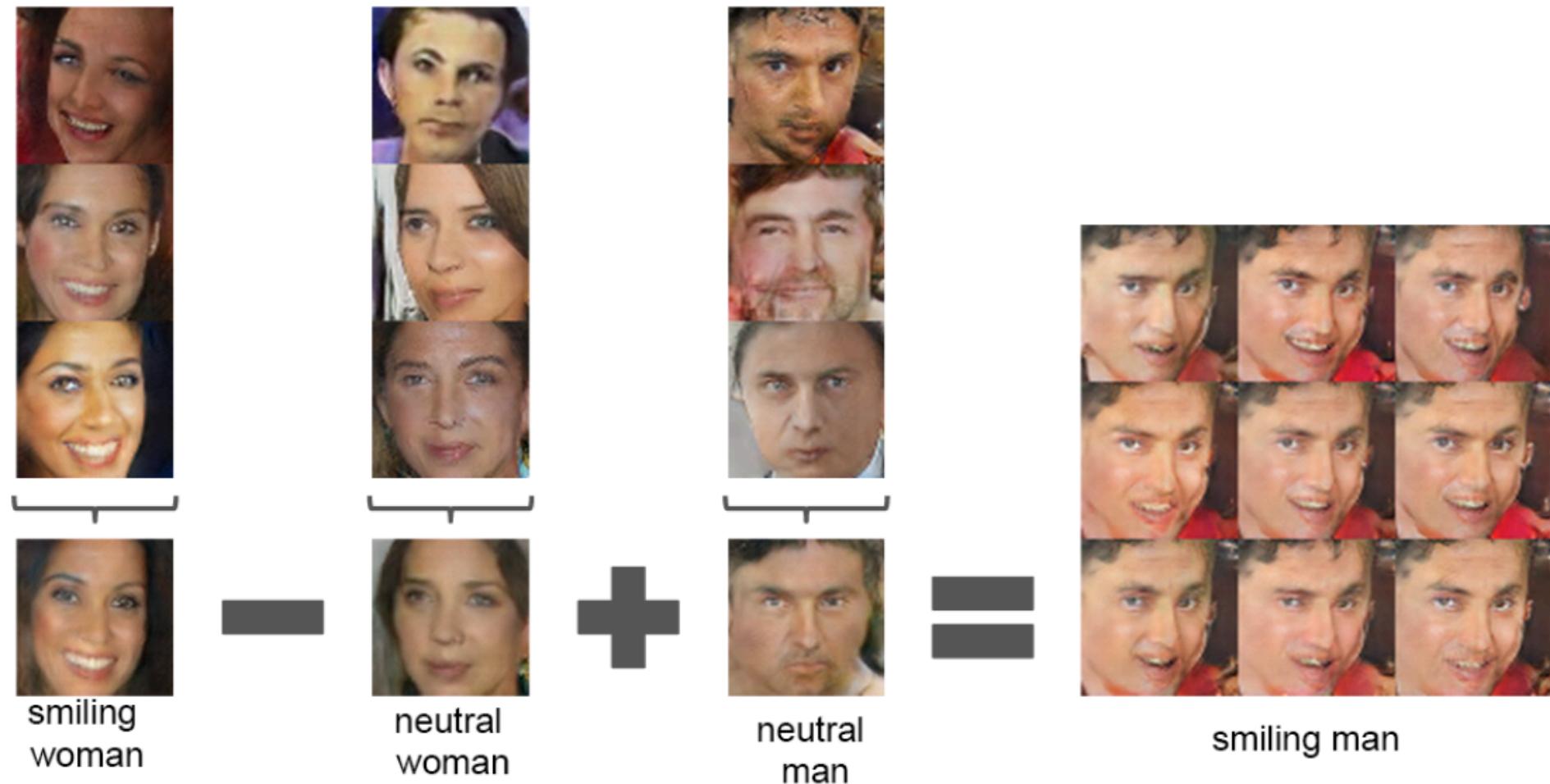
Testing

Image from cs231n@stanford



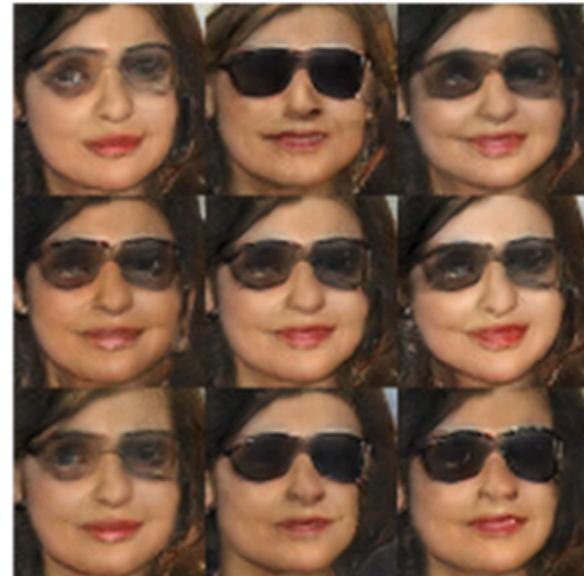
More Intriguing Examples

(Radford et al, ICLR'16)



More Intriguing Examples cont'

(Radford et al, ICLR'16)



man
with glasses

man
without glasses

woman
without glasses

woman with glasses

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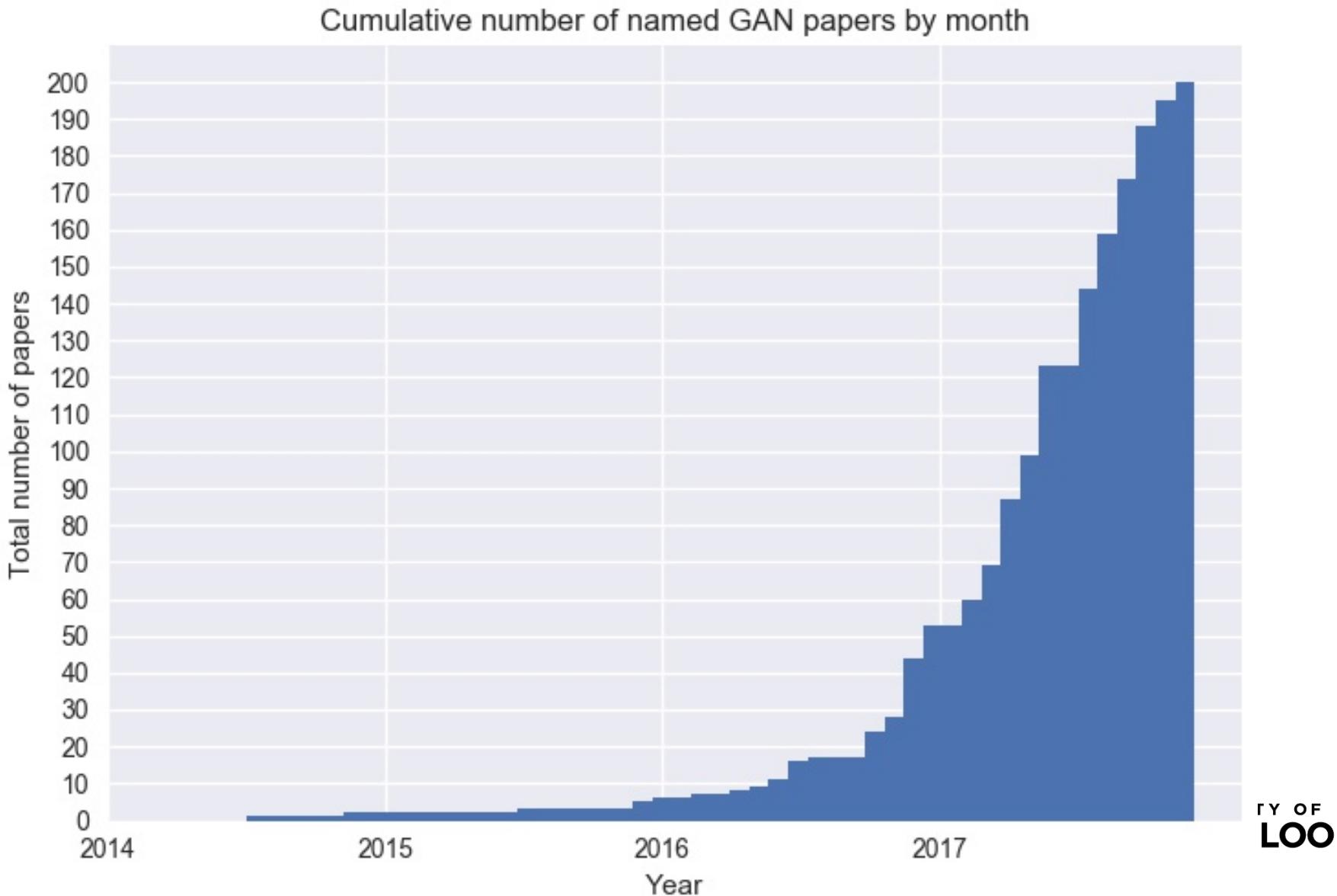
Wasserstein GAN (Arjovsky et al, ICML'17)

- GAN objective
 - Could be discontinuous
- Better objective
 - Much better behaved
 - Connection to kernels

$$\min_G \text{JS}(p_{\text{data}} \| p_{\text{model}})$$

$$\min_G \mathbb{W}(p_{\text{data}}, p_{\text{model}})$$

The GAN Zoo (<https://github.com/hindupuravinash/the-gan-zoo>)



Questions?

