User Modelling Using NMF for Expedia Hotel Recommendation

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Abstract

1 Introduction

Have you ever wondered, why can't you find the best music on Spotify? Or the most interesting book on Amazon? Or the finest hotel in the city of New York? In today's world, we want the service we get from the service providers (no matter online or offline) to be tailored to our interests, which means the services these days better to be personalized to amaze the customers. This is why recommendation systems are crucial in such business applications.

2 Non-negative Matrix Factorization (NMF)

• Introduction to NMF

NMF is a matrix factorization algorithm which factorize a big matrix $V(m$ by $n)$ into two smaller matrices $W(m$ by $r)$ and $H(r$ by $n)$.

$$V \approx W \times H$$

For each column v_i in V, we have

$$v_i \approx W \times h_i$$

where h_i is the corresponding column in H, in other words, every column in V is a linear combination of W where H is the coefficient matrix. Geometrically, NMF projects the data points in higher dimensional space to the lower dimensional space formed by the basis vectors in W, and H contains the projected coefficients.

To integrate the theory with the context, matrices are commonly seen in recommendation problems, with columns and rows being users and the corresponding items. When NMF factorizes such a matrix into W and H, the columns in W contains the hidden features of the original matrix. Each basis vector in W can be viewed as basic user type, every user therefore is represented as a linear combination of such basic user typrs which are .

$$u = a_1 w_1 + a_2 w_2 + ... + a_r w_r$$

where u is a single user and $a_i s$ are the coefficients. Besides, such user-item matrices are usually sparse (with high percentage of missing values), NMF with EM algorithm can reconstruct the original matrix by filling out the missing values.
Here is an example of how NMF works, the number of basis was set to be 100(which might not be optimal in this case):

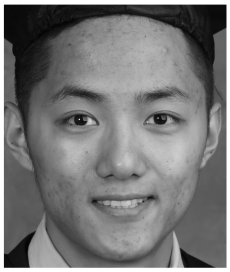

Figure 1: Original face image without any missing values

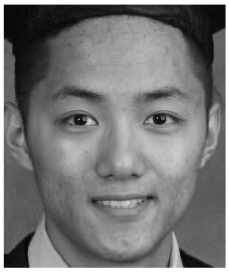

Figure 2: Face reconstruction with 50% missing values in the original image

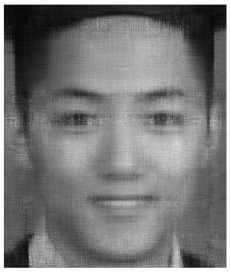

Figure 3: Face reconstruction with 90% missing values in the original image

• Related work

In 2014 Yu & Riedl from Georgia Tech have published a paper[1] about a recent success of NMF for interactive narrative recommendation system. The research was to build a drama manager that learns a model of the player's storytelling preferences and automatically recommends a narrative experience that is predicted to optimize the player's experience while conforming to the human designer's storytelling intentions [1, p. 1].
In their research, a new method called $Prefix-Based\ Collaborative\ Filtering$ (PBCF) [1, p. 2] has been introduced in which each prefix is a sequence of story plots. Based on $PBCF$, a prefix-rating matrix was constructed in which each row represents a prefix, each column represents a player, every entry in the matrix is the numerical rating rated by a player for a prefix. Similar to most recommendation problems, this matrix is sparse, due to the nature that it is impossible for a single player to encounter all the prefixes. NMF was applied to this matrix to learn the player types

Figure 4: Prefix rating matrix $[1, p.\ 4]$

Prefix	User 1	User 2	User 3	...
A (1)	*	*	2	...
B (1, 2)	1	*	2	....
C (1, 2, 6)	*	*	*	...
D (1, 2, 3)	4	3	*	...
...	...	...	...	...

• NMF algorithm
In $Algorithms\ for\ Non-negative\ Matrix\ Factorization$ published by Daniel F. Lee and H. Sebastian Seung, several NMF algorithms have been introduced. One of which is

$$H_{\alpha\mu} = H_{\alpha\mu}\frac{(W^TR)_{\alpha\mu}}{(W^TWH)_{\alpha\mu}},\ W_{i\alpha} = W_{i\alpha}\frac{(RH^T)_{i\alpha}}{(WHH^T)_{i\alpha}}\ [2,\ p.\ 3]$$

For predicting the new user

3 Experiment

3.1 Dataset

The dataset we use for experiment is the Expedia hotel recommendation dataset from Kaggle competition in 2016. This dataset contains the hotel booking information of more than 2,000,000 users, of which the training set is obtained from 2013 and 2014 user data and the test set is obtained from 2015 user data.
In the data set, each column represent a user, each column contains the hotel booking information of the user. Such columns are date_time. site_name, posa_continent, user_location_country, user_location_region, user_location_city, orig_destination_dista, user_id, is_mobile, is_package, channel, srch_ci, srch_co, srch_adults_cnt, srch_rm_cnt, srch_destination_id, srch_destination_type_id, hotel_continent, hotel_country, hotel_market, is_booking, cnt, and hotel_cluster is what to be predicted. Moreover, for each hotel cluster, there are 149 numerical latent descriptions.

3.2 Modification on dataset

Among all the columns, the date data is string data instead of numerical. The date in the testing set is one or two years later that the date in the training set, moreover, different user ids in this dataset may represent the same user. For the purpose of simplifying of the data set, I have removed the date coulumns. Then the user types will only be represented by numerical values.

3.3 User modeling and Feature selection

When using NMF for building the user model, each basis user type is represented by the combination of different features. For example, assume we have W as a user model which has 4 columns (w_1, w_2, w_3, w_4), w_1 represent users who love luxurious hotels, w_2 represent users who prefer cheaper hotels, w_3 represent users who want to live in downtown, w_4 represent users who dersire great hotel service. Then a new user maybe of 10% of type 1, 30% of type 2, 20% of type 3 and 40% of type 3.
For feature selection, in some cases, we may also be able to select the number of basis based on some prior or domain knowledge. However, in our case, no proven knowledge is available. NMF is capable of selecting the number basis user type by running cross validations. The number of basis that generates the smallest cross validation error is selected.

When running cross validation, $10 - fold$ cross validation is selected. The loss metric is set to the rmse value between two matrices.

$$rmse_{A,B} = \sqrt{avg_{ij}((A_{ij} - B_{ij})^2)}$$

• Method 1

For method 1, KNN has been implemented as a complementary algorithm to NMF for predicting the hotel clusters. In this method, we build the user model only using the general information of Expedia users without the latent description of search regions. Each user type is simply defined by user actions and other information in the training set, such as search location, is mobile, etc.

In the beginning of the training process, we apply NMF on the training set to compute the user model W. Then we apply the computed model W on the testing set to compute the coefficients(H) of the testing users. Once we have the coefficients of a testing user, we go back to the training set and use KNN to find what hotel cluster users that have the similar coefficients choose, then we use that hotel cluster as a prediction for the unknown user.

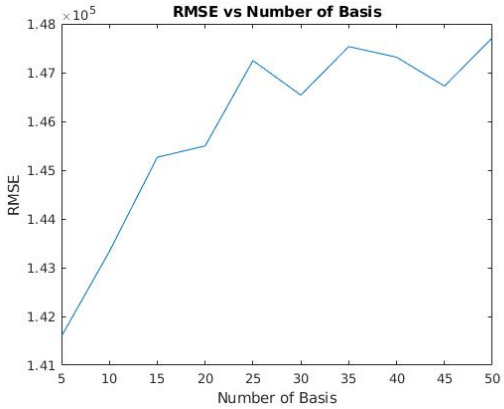

Figure 5: Cross validation with number of basis 5, 10, 15, .., 50

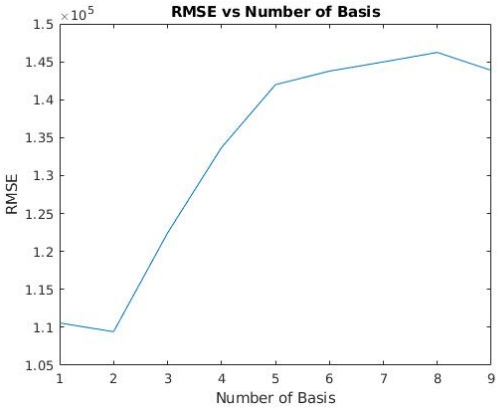

Figure 6: Cross validation with number of basis 1, 2, 3, ...9

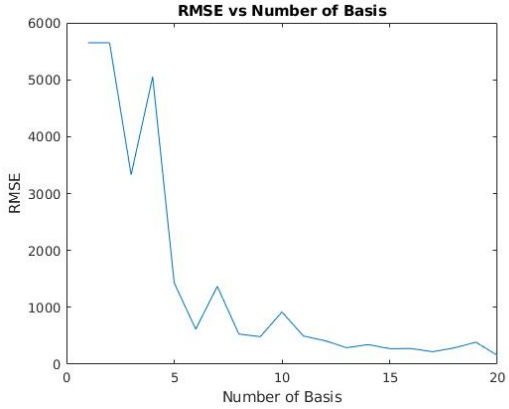

Figure 7: Testing basis without using cross validation

The table below shows the accuracy of the first method, r is the number of basis in the user model, k is the knn parameter.

Results using method 1					
	r=2	r=5	r=10	r=15	r=20
k = 1	1.18%	1.20%	1.36%	1.31%	1.39%
k = 3	1.11%	1.17%	1.25%	1.20%	1.22%
k = 5	1.14%	1.18%	1.24%	1.28%	1.24%
k = 7	1.14%	1.29%	1.22%	1.36%	1.26%
k = 9	1.19%	1.21%	1.29%	1.25%	1.34%

• Method 2

For method 2, KNN has also been implemented as a complementary algorithm to NMF for predicting the hotel clusters. However, the exact method is different. In this method, the latent description of search regions has been used when building the user model. Compared to method 1, now each basis user type is also described by the latent variables.

In the beginning of the training process, we apply NMF on the training set to compute the user model W. Then we use the computed model W to computed the associated latent hotel descriptions of the user's potential hotel cluster. At the end, we apply KNN algorithm on the computed latent hotel descriptions to compute the actual hotel cluster.

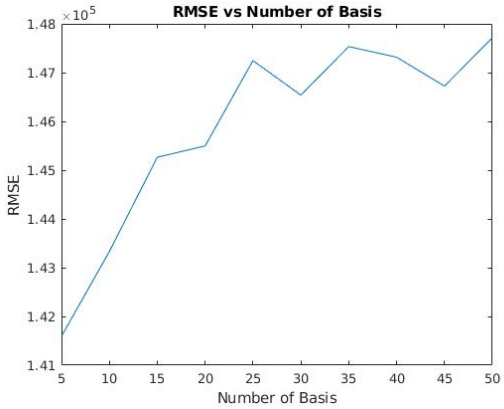

Figure 8: Cross validation with number of basis 5, 10, 15, .., 50

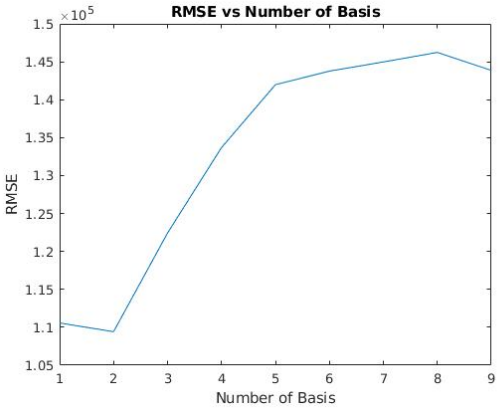

Figure 9: Cross validation with number of basis 1, 2, 3, ...9

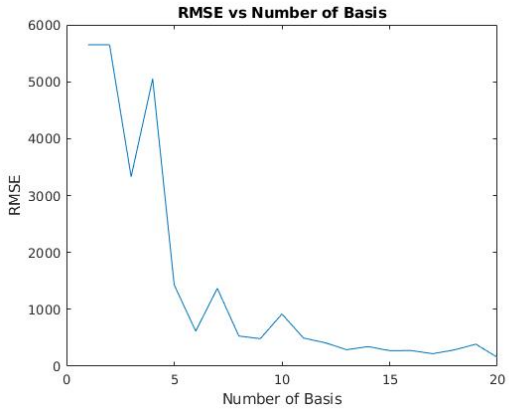

Figure 10: Testing basis without using cross validation

Results using method 1					
	m=2	m=5	m=10	m=15	m=20
k = 1	AF	AFG	004	005	hello
k = 3	AF	AFG	004	005	hello
k = 5	AF	AFG	004	005	hello
k = 7	AF	AFG	004	005	hello
k = 9	AF	AFG	004	005	hello

- Method 3

Results using method 1					
	m=2	m=5	m=10	m=15	m=20
k = 1	AF	AFG	004	005	hello
k = 3	AF	AFG	004	005	hello
k = 5	AF	AFG	004	005	hello
k = 7	AF	AFG	004	005	hello
k = 9	AF	AFG	004	005	hello

3.4 Results

3.5 Comparision with other algorithms

As in the papers and reports regarding the Expedia hotel recommendation competition, NMF has never been implemented.

4 Extra Experiment

5 Conclusion

6 Discussion

7 Note

All the algorithms used for this project, including NMF, KNN have been implemented by myself, no libraries have been used. Source code is available upon request.

8 Acknowledgement

I greatly acknowledge Dr.Yaoliang Yu for the amazing knowledge he shared with us and his support through out the term.

References

[1] Hong Yu and Mark O. Riedl. *Personalized Interactive Narratives via Sequential Recommendation of Plot Points* IEEE Transactions on Computational Intelligence and AI in Games, 6(2):174–187, 2014.

[2] Daniel D. Lee and Seung, H. Sebastian. *Algorithms for Non-negative Matrix Factorization* Advances in Neural Information Processing Systems 13, 556–562, 2001

[3] Daniel D. Lee and Seung, H. Sebastian. *Algorithms for Non-negative Matrix Factorization* Advances in Neural Information Processing Systems 13, 556–562, 2001