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# Player Modelling Using NMF In Recommender Systems

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## Abstract

1 Player modelling methods are commonly seen in video games. Such methods  
2 are implemented to improve players' user experience. Other than being popular  
3 in video games, player modelling methods can also be used for recommender  
4 systems. Users are being modelled by such methods so that a corresponding item  
5 can be recommended to the user based on his/her user type.

## 1 Introduction

7 Have you ever wondered, why can't you find the best music on Spotify? Or the most interesting  
8 book on Amazon? Or the finest hotel in the city of New York? In today's world, we want the service  
9 we get from the service providers (no matter online or offline) to be tailored to our interests, which  
10 means the services these days better to be personalized to amaze the customers. This is why recom-  
11 mendation systems are crucial in such business applications.  
12 For this project, I have implemented a player modelling algorithm called *NMF* for a hotel recom-  
13 mendation problem.

## 2 Non-negative Matrix Factorization (NMF)

### • Introduction to NMF

15 *NMF* is a matrix factorization algorithm which factorize a big matrix  $V(m \text{ by } n)$  into two smaller  
16 matrices  $W(m \text{ by } r)$  and  $H(r \text{ by } n)$ .

$$V \approx W \times H$$

18 For each column  $v_i$  in  $V$ , we have

$$v_i \approx W \times h_i$$

20 where  $h_i$  is the corresponding column in  $H$ , in other words, every column in  $V$  is a linear combi-  
21 nation of  $W$  where  $H$  is the coefficient matrix. Geometrically, *NMF* projects the data points in  
22 higher dimensional space to the lower dimensional space formed by the basis vectors in  $W$ , and  $H$   
23 contains the projected coefficients.

24 To integrate the theory with the context, matrices are commonly seen in recommendation problems,  
25 with columns and rows being users and the corresponding items. When *NMF* factorizes such a  
26 matrix into  $W$  and  $H$ , the columns in  $W$  contains the hidden features of the original matrix. Each  
27 basis vector in  $W$  can be viewed as basic user type, every user therefore is represented as a linear  
28 combination of such basic user types which are .

$$u = a_1 w_1 + a_2 w_2 + \dots + a_r w_r$$

29 where  $u$  is a single user and  $a_i$ s are the coefficients. Besides, such user-item matrices are usually

32 sparse (with high percentage of missing values), *NMF* with EM algorithm can reconstruct the orig-  
 33 inal matrix by filling out the missing values.  
 34 Here is an example of how *NMF* works, the number of basis was set to be 100(which might not be  
 35 optimal in this case):



Figure 1: Original face image without any missing values

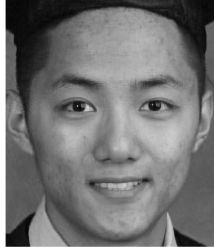


Figure 2: Face reconstruction with 50% missing values in the original image

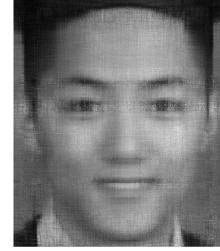


Figure 3: Face reconstruction with 90% missing values in the original image

#### 36 • Related work

37 In 2014, Yu & Riedl from Georgia Tech have published a paper[1] about a recent success of *NMF*  
 38 for interactive narrative recommendation system. The research was to build a drama manager that  
 39 learns a model of the player's storytelling preferences and automatically recommends a narrative  
 40 experience that is predicted to optimize the player's experience while conforming to the human  
 41 designer's storytelling intentions [1, p. 1].

42 In their research, a new method called *Prefix – Based Collaborative Filtering* (PBCF) [1,  
 43 p. 2] has been introduced in which each prefix is a sequence of story plots. Based on *PBCF*, a  
 44 prefix-rating matrix was constructed in which each row represents a prefix, each column represents  
 45 a player, every entry in the matrix is the numerical rating rated by a player for a prefix. Similar to  
 46 most recommendation problems, this matrix is sparse, due to the nature that it is impossible for a  
 47 single player to encounter all the prefixes.

Figure 4: Prefix rating matrix [1, p. 4]

Prefix	User 1	User 2	User 3	...
A (1)	*	*	2	...
B (1, 2)	1	*	2	...
C (1, 2, 6)	*	*	*	...
D (1, 2, 3)	4	3	*	...
...	...	...	...	...

48 *NMF* was applied to this matrix to learn the player types so that the prefix that has the highest  
 49 rating is recommended to the reader.

#### 50 • NMF algorithm

51 In *Algorithms for Non – negative Matrix Factorization* published by Daniel F. Lee and H.  
 52 Sebastian Seung in 2001, several *NMF* updating rules have been introduced. One of which is

$$54 H_{\alpha\mu} = H_{\alpha\mu} \frac{(W^T R)_{\alpha\mu}}{(W^T W H)_{\alpha\mu}}, W_{i\alpha} = W_{i\alpha} \frac{(R H^T)_{i\alpha}}{(W H H^T)_{i\alpha}} \quad [2, p. 3]$$

56 For predicting the new user, we use the algorithm introduced in

## 57 3 Experiment

### 58 3.1 Dataset

59 The dataset we use for experiment is the Expedia hotel recommendation dataset from Kaggle com-  
60 petition in 2016. This dataset contains the hotel booking information of more than 2,000,000 users,  
61 of which the training set is obtained from 2013 and 2014 user data and the test set is obtained from  
62 2015 user data.

63 In the data set, each column represent a user, each column contains a feature of the user. All of  
64 the feature variable are non-negative numerical variable except for date variable. For the purpose  
65 of simplifying of the data set, I have removed the date columns. Then the user types will only be  
66 represented by numerical values.

67 For privacy purpose, *Expedia* has encoded some of the feature values, which makes the problem  
68 harder since the original values have changed. Moreover, some of the features contain missing  
69 values. This might also create some challenge to the problem.

### 70 3.2 User modeling and Feature selection

71 When using *NMF* for building the user model, each basis user type is represented by the com-  
72 bination of different features. For example, assume we have  $W$  as a user model which has 4  
73 columns  $(w_1, w_2, w_3, w_4)$ ,  $w_1$  represent users who love luxurious hotels,  $w_2$  represent users who  
74 prefer cheaper hotels,  $w_3$  represent users who want to live in downtown,  $w_4$  represent users who  
75 desire great hotel service. Then a new user maybe of 10% of type 1, 30% of type 2, 20% of type 3  
76 and 40% of type 4.

77 For feature selection, in some cases, we may also be able to select the number of basis based on  
78 some prior or domain knowledge. However, in our case, no proven knowledge is available. *NMF*  
79 is capable of selecting the number basis user type by running cross validations. The number of basis  
80 that generates the smallest cross validation error is selected.

81 When running cross validation, 10 – fold cross validation is selected. The loss metric is set to the  
82 rmse value between two matrices.

83 
$$rmse_{A,B} = \sqrt{avg((A - B)^2)}$$

#### 84 • Algorithm

85 For this method, *KNN* has been implemented as a complementary algorithm to *NMF* for predict-  
86 ing the hotel clusters. We build the user model only using the general information of Expedia users  
87 without the latent description of search regions. Each user type is simply defined by the numerical  
88 features in the training set, such as search location, etc.

89 In the beginning of the training process, we apply *NMF* on the training set to compute the user  
90 model  $W$ . Then we apply the computed model  $W$  on the testing set to obtain the coefficients ( $H$ ) of  
91 the testing users. Once we have the coefficients of a testing users, we know what types of users they  
92 are. Then we go back to the training set and use *KNN* to find what hotel cluster users that have the  
93 similar coefficients choose, then we use that hotel cluster as a prediction for the unknown users.

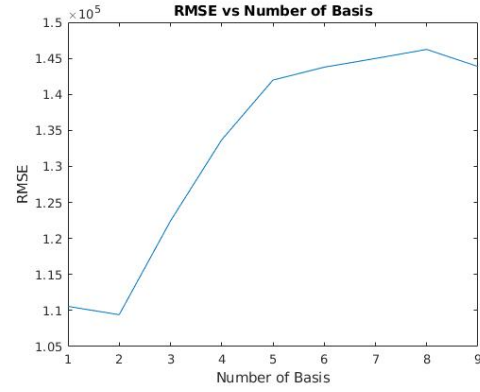
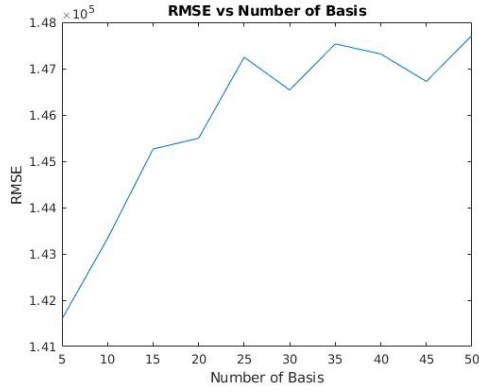


Figure 5: Cross validation with number of basis 5, Figure 6: Cross validation with number of basis 1, 10, 15, ..., 50, 2, 3, ..., 9

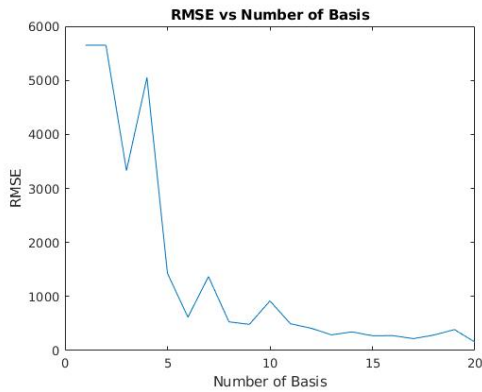


Figure 7: Testing basis without using cross validation

The table below shows the accuracy of the first method,  $r$  is the number of basis in the user model,  $k$  is the knn parameter.

Results using method 1					
	$r=2$	$r=5$	$r=10$	$r=15$	$r=20$
$k = 1$	2.18%	2.20%	2.36%	2.31%	2.39%
$k = 3$	2.11%	2.17%	2.25%	2.20%	2.22%
$k = 5$	2.14%	2.18%	2.24%	2.28%	2.24%
$k = 7$	2.14%	2.29%	2.22%	2.36%	2.26%
$k = 9$	2.19%	2.21%	2.29%	2.25%	2.34%

As we can see, the results are disappointing. There are 100 hotel clusters in the dataset, random guessing gives around 1% accuracy. The accuracy reached by NMF algorithm is just slightly better than random guessing. This phenomenon might come from different factors. Look into some details of the dataset,

### 3.3 Comparison with other algorithms

As in the papers and reports regarding the Expedia hotel recommendation competition, *NMF* has never been implemented.

## 105 4 Extra Experiments

106 To have deeper insights of  $NMF$  and analyse what factors may affect the performance of  $NMF$ . I  
107 have also performed several experiments on  $NMF$  and applied the algorithm on a different dataset.

108 • Number of Basis

109 • Percentage of Missing Values

110 • Percentage of Missing Values

111 • NMF on Movie Dataset

## 112 5 Conclusion

## 113 6 Discussion

114 As we have stated earlier in the introduction to NMF section, one of the most important assump-  
115 tions of  $NMF$  is linearity in the dataset, which assumes that a user can be represented as a linear  
116 combination of basis user types.

## 117 7 Note

118 All the algorithms used for this project, including  $NMF$ ,  $KNN$  have been written by myself, no  
119 libraries have been used. Source code is available upon request.

## 120 8 Acknowledgement

121 I greatly acknowledge Dr. Yaoliang Yu for the amazing knowledge he shared with us and his support  
122 through out the term.

## 123 References

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