**BIOS560R Introduction to R Programming**

**2013 Spring Semester Final Exam**

**INSTRUCTIONS:**

Answer all three questions. All work and codes are to be your own. Save all codes into a single text file called YOURNAME\_final.R where YOURNAME should be replaced by your Last and First name. Email the file to [hao.wu@emory.edu](mailto:hao.wu@emory.edu) and [wsp@emory.edu](mailto:wsp@emory.edu).

Total is 100 points. Partial credit will be given.

**QUESTION #1) (40 points)**

In this question you will write functions to compute the variance, covariance and correlation of an input vector. There are a few rules and suggestions:

1. Do not use the built in “var” (variance function), “sd”, or “cov” (covariance) functions.
2. Try to vectorize your computations. Using loops is allowed but to receive full credit you should use vectorization approaches where possible.

**a) Variance (10 points)**

In a [sample](http://stattrek.com/Help/Glossary.aspx?Target=Population), the **variance** is the average squared deviation from the sample mean, as defined by the following formula:

where x is a vector of length "n" and is the mean of the sample vector. Write a function called **sampvar** that implements this formula. As an example:

set.seed(123)

x = rnorm(30,10)

sampvar(x)

[1] 0.962

**b) Covariance (15 points)**

The **covariance** of two variables *x* and *y* in a data sample measures how the two are linearly related. A positive covariance would indicate a positive linear relationship between the variables, and a negative covariance would indicate the opposite. The **sample covariance** is defined in terms of the sample means as:

and represent the mean of x and y, respectively, and are vectors of length "n". Write a function called "**sampcov**" in R that, given vectors x and y, implements the above formula. Thus, it will return the covariance of two vectors x and y. As an example using the following vectors:

set.seed(123)

x = rnorm(1000)

set.seed(456)

y = rnorm(1000)

sampcov(x,y)

[1] 0.0134

**c) Pearson's Correlation Coefficient (15 points)**

We can compute the **Pearson's correlation coefficient** by using the formula where x and y are vectors of length "n". and are the standard deviations of x and y respectively. Note that the standard deviation is the square root of the sample variance.

where and

Write a function called "**mypearson**" that implements the formula for r. Take advantage of the functions you wrote in a and b. As an example:

set.seed(123)

x = rnorm(1000)

set.seed(456)

y = rnorm(1000)

mypearson(x,y)

[1] 0.0137

**QUESTION #2 (30 points)**

Consider the function *f(x)* defined as:

Create a function in R that implements this function definition. The function will take the following inputs:

1. **xvals**: a single number or a vector for *x*.
2. **plot**: optional TRUE/FALSE indicator. (This should be equal to TRUE by default). If plot=TRUE, a scatter plot of *f(x)* versus *x* will be shown.

The output of the function is a number or vector for the *f(x)* values. The length of the output should equal to the length of the input.

As an example, you should get following results given the following inputs:

myfunc(-2:2, plot=FALSE)

[1] 8.000000 1.000000 0.000000 1.000000 1.414214

myfunc(seq(-2,2, by=0.5), plot=TRUE) # Note that this will create a plot

[1] 8.000000 3.375000 1.000000 0.125000 0.000000 0.250000 1.000000 1.224745

[9] 1.414214



**To get the full credit of the question:**

1. Your function has to work with vectors of different lengths and different values.
2. The figure needs to have the same line type, xlab, ylab, and title as shown in the example.
3. Use vectorization.

**QUESTION #3 (30 points)**

Read the following .csv file in

url = "http://steviep42.bitbucket.org/bios560rs2014/DATA.DIR/my.diamonds.csv"

myd = read.csv(url)

Create a function that presents a plot of price (y axis) vs. carat size (x axis) such that the points lying below the average price have the color blue and the points lying above the average price are in red. Use base graphics to create this function.

myplotter(mydf=myd)

To get full credit the figure generated from the function must have similar point type, colors, labels and titles as shown in the example.

