

# Applied Static Analysis

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## An Introduction to Points-to and Alias Analysis

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Some of the images on the following slides are inspired by slides created by Eric Bodden.

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# Points-to analysis vs. alias analysis

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- Points-to analysis computes for each variable the allocation sites whose objects the variable *may/must* point to:  $\text{points-to}(v) = \{a1, a2, \dots\}$
- Alias analysis determines which variables *may* or *must* alias, i.e., point to the same objects:
  - $\text{may-alias}(v1, v2) = \text{true/false}$
  - $\text{must-alias}(v1, v2) = \text{true/false}$

In case of a *may* analysis **true** means **maybe**. I.e., if two variables may alias then they may point to the same object, but they don't have to. If the answer is **false**, they definitively never alias.

In case of a *must* analysis **false** (only) means *maybe not*.

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# May vs. must alias analysis

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```
a = new A();  
if(..) {  
    b = a;  
}  
c = new C();  
d = c;
```

$\text{may-alias}(a, b) = \text{true}$

$\text{must-alias}(a, b) = \text{false}$

$\text{may-alias}(a, c) = \text{false}$

$\text{must-alias}(c, d) = \text{true}$

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# May vs. must alias analysis

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```
a = new A();  
if(..) {  
    b = a;  
}  
c = new C();  
d = c;  
d = a;    // <= NEW
```

**may-alias**( $a, b$ ) = *true*

**must-alias**( $a, b$ ) = *false*

**may-alias**( $a, c$ ) = *false*

**must-alias**( $c, d$ ) = *false*

Over the lifetime of an entire execution, two variables (practically) never always alias. Thus must-alias analysis typically needs to take control flow into account (they have to be flow-sensitive).

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# Flow-sensitive must analysis

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```
    b = null;  
    d = null;  
s1:  a = new A();  
    if(..) {  
        b = a;  
    }  
s2:  c = new C();  
    b = c;  
s3:  d = a;
```

$\text{must-alias}(\text{variable } v1, \text{variable } v2; \text{after execution of } s_x) \rightarrow \{true, false\}$

$\text{must-alias}(a, d; s2) = false$

$\text{must-alias}(a, d; s3) = true$

$\text{must-alias}(b, c; s2) = false$

$\text{must-alias}(b, c; s3) = true$

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# Flow-insensitive must analysis

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In a flow-insensitive analysis the order in which the instructions will be evaluated is ignored.

```
    b = null;  
    d = null;  
s1:  a = new A();  
    if(..) {  
        b = a;  
    }  
s2:  c = new C();  
    b = c;  
s3:  d = a;
```

$\text{must-alias}(\text{variable } v1, \text{variable } v2) \rightarrow \{true, false\}$

$\text{must-alias}(a, d) = false$

$\text{must-alias}(a, d) = false$

$\text{must-alias}(b, c) = false$

$\text{must-alias}(b, c) = false$

Here, we always have to choose the same default answer: *false*. However, this observation is generally true: most program properties don't always hold and **therefore most must-analyses have to be flow sensitive**.

The above observation does not hold for may-analyses. They only determine whether a property may (if at all) hold somewhere in the program.

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# Points-to and alias analysis

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Points-to analysis can answer alias-analysis queries:

$$\text{alias}(v1, v2) = (\text{points-to}(v1) \cap \text{points-to}(v2) \neq \emptyset)$$

This leads us to the question: *Is points-to analysis always more expressive than alias analysis?*

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# Points-to vs. alias analysis

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- Points-to analysis requires a notion of allocation sites:  $\text{points-to}(v) = \{a1, a2, \dots\}$
- Alias analysis only talks about variables:  $\text{may-alias}(v1, v2) = \text{true/false}$  or  $\text{must-alias}(v1, v2) = \text{true/false}$

Important in real world: What if we have *incomplete knowledge about allocation sites*?

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# Points-to and alias analysis for incomplete programs

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```
void readProp(String id, String default) {  
    String s = Properties.read(id);  
    if(s==null) s = default;  
    return s;  
}
```

Assume that `Properties.read` is a native method or that for some other reason we don't know its definition.

A may alias analysis will be able to derive:  $\text{may-alias}(s, \text{default}) = \text{true}$ .

We cannot compute the information by using **points-to** information:

$\text{may-alias}(s, \text{default}) = (\text{points-to}(s) \cap \text{points-to}(\text{default}) \neq \emptyset)$ .

The underlying issue is that **points-to**(s) cannot be computed. Choosing either the empty set ( $\emptyset$ ) or `any object` will both render the analysis practically unusable. Using the empty set is (potentially grossly) unsound and using `any object` is (grossly) imprecise.

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# Problem of points-to analysis for incomplete programs

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## *Summary*

- Points-to analysis associates variables with allocation sites.
  - If allocation sites are unknown then this association is necessarily either unsound or imprecise, depending on the analysis design.
  - In comparison, alias analysis can recover precision by analyzing the relationship between variables without caring which objects they point to.
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# A direct alias analysis

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(We are not using points-to information!)

```
b = a  
c = b
```

**may-alias**(*b*, *a*) = *true*

**may-alias**(*c*, *b*) = *true*

What happens if `a = null` ?

In this case ( `a = null` ) the variables do not alias. Hence, returning `true` is imprecise (but still sound).

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# When to prefer points-to analyses?

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```
l = new LinkedList(); // Allocation site a1
l.clear();
```

In the above case, points-to information ( $\text{points-to}(l) = \{a1\}$ ) can be used to devirtualize the ( `clear` ) method call; it can only invoke `LinkedList.clear()` . Alias information (  $\text{type-of}(\text{points-to}(l)) = \{LinkedList\}$  ) is (in general) of no use in this case.

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# Weak Updates

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So-called weak updates are generally required if *only may-alias information is available*. **For aliases, information before the statement is retained, only new information is added.**

*We cannot kill information; otherwise we would be unsound!*

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# Weak Updates - example

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We only know:

- $x.f \mapsto 0$  ,  $y.f \mapsto 0$  (the fields  $f$  are initialized to  $0$  )
- **may-alias**( $x, y$ )

We see an update:

```
x.f = 3
```

Given that we only have may-alias information, we must retain the old value for field  $f$  of alias  $y$ :

- $x.f \mapsto 3$  ,  $y.f \mapsto 3$  ,  $y.f \mapsto 0$
- **may-alias**( $x, y$ )

A weak update is necessary, because **may-alias**( $x, y$ ) tells us that there is a path along which  $x$  and  $y$  do alias and there may be a path along which they don't. But the value  $y.f$  must represent both possible truths at the same time; hence both  $y.f \mapsto 3$  ,  $y.f \mapsto 0$  must be included!

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# Strong Updates

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So-called strong updates require must-alias information and can *kill* analysis information associated with an alias.

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# Strong Updates - example

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We (only) know:

- $x.f \mapsto 0$  ,  $y.f \mapsto 0$  (the fields `f` are initialized to `0` )
- **must-alias**( $x, y$ )

We see an update:

```
x.f = 3
```

Given that we have must-alias information, we can safely kill  $y.f \mapsto 0$  .

- $x.f \mapsto 3$  ,  $y.f \mapsto 3$
- **must-alias**( $x, y$ )

Generally, we can never kill information on aliases without must-alias information.