

## 1 Current State

### 1.1 General First-Order Encoding Template

### 1.2 Natural Numbers Program

$$\text{Zero}(x. \epsilon) \quad (1)$$

$$\text{Succ}(x. x.p :: \text{Nat}) \quad (2)$$

$$\forall x. x :: \text{Zero} \Rightarrow x :: \text{Nat} \quad (3)$$

$$\forall x. x :: \text{Succ}, x.p :: \text{Nat} \Rightarrow x :: \text{Nat} \quad (4)$$

$$\text{prev}(x. x :: \text{Nat}) : [y. y :: \text{Nat}] \quad (5)$$

$$\text{prev}(x. x :: \text{Zero}) : [y. y :: \text{Nat}] := \text{new Zero}() \quad (6)$$

$$\text{prev}(x. x :: \text{Succ}, x.p :: \text{Nat}) : [y. y :: \text{Nat}] := x.p \quad (7)$$

### 1.3 First-Order Encoding for Natural Numbers Program