Lecture F3. MDP without Model - Policy Iteration (MC, TD)

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- I. Policy Iteration 1 MC Control
- II. Policy Iteration 2 TD Control (a.k.a. sarsa)

• skiier.R is loaded as follows.

```
source("../skiier.R")

## [1] "Skiier's problem is set."

## [1] "Defined are `state`, `P_normal`, `P_speed`, `R_s_a`, `q_s_a_init` (F2, p15)."

## [1] "Defined are `pi_speed`, and `pi_50` (F2, p16)."

## [1] "Defined are `simul_path()` (F2, p17)."

## [1] "Defined are `simul_step()` (F2, p18)."

## [1] "Defined are `pol_eval_MC()` (F2, p19)."

## [1] "Defined are `pol_eval_TD()` (F2, p20)."

## [1] "Defined are `pol_imp()` (F2, p20)."
```

I. Policy Iteration 1 - MC Control

Process

- The MC policy iteration process is summarized as follows:
 - 0. Initialize q(s, a)
 - 1. Begin with a policy π
 - 2. Generate a sample path using the current π (simul_path())
 - 3. Evaluate the current policy π and update q(s,a) (pol_eval_MC())

$$q(s,a) \leftarrow q(s,a) + \alpha(G_t - q(s,a)), \ \forall s,a$$

4. Improve the policy into a ϵ -greedy policy using q(s,a) (pol_imp())

$$\pi(s, a) \leftarrow argmax_{a \in \mathcal{A}} \pi(s, a)$$

5. Repeat 2-4 many times

 \bullet We will let num_ep to grow from 10^3 , 10^4 , and $5\cdot 10^4$.

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```
num ep <- 10<sup>3</sup>
beg time <- Sys.time()</pre>
q s a <- q s a init
pi <- pi 50
for (epi i in 1:num ep) {
  sample path i <- simul path(pi, P normal, P speed, R s a)</pre>
  q s a <- pol eval MC(sample path i, q s a, alpha = 1/epi i)
  pi <- pol_imp(pi, q_s_a, epsilon = 1/epi i)</pre>
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 0.2078 secs
t(pi)
     0 10 20 30 40 50 60 70
## n 0 1 0 1 1
## s 1 0 1 0 0 1 0 0
t(q s a)
##
          0
                10
                        20
                               30
                                       40
                                              50
                                                       60 70
## n -5.358 -4.004 -3.859 -2.650 -1.646 -1.608 -0.9929 0
## s -5.081 -4.006 -3.340 -3.004 -1.654 -1.606 -1.0003 0
```

```
num ep <- 10<sup>4</sup>
beg time <- Sys.time()</pre>
q s a <- q s a init
pi <- pi 50
for (epi i in 1:num ep) {
  sample path i <- simul path(pi, P normal, P speed, R s a)</pre>
  q s a <- pol eval MC(sample path i, q s a, alpha = 1/epi i)
  pi <- pol_imp(pi, q_s_a, epsilon = 1/epi i)</pre>
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 1.811 secs
t(pi)
     0 10 20 30 40 50 60 70
## n 0 0 1 1 1
## s 1 1 0 0 0 1 0 0
t(q s a)
##
          0
                10
                        20
                               30
                                       40
                                              50
                                                       60 70
## n -5.734 -4.500 -3.679 -2.677 -1.675 -1.678 -0.9206 0
## s -5.338 -2.969 -4.005 -2.726 -2.018 -1.670 -1.7399 0
```

```
num ep <- 5*10^4
beg time <- Sys.time()</pre>
q s a <- q s a init
pi <- pi 50
exploration rate <- 1
for (epi i in 1:num ep) {
  sample path i <- simul path(pi, P normal, P speed, R s a)
  q s a <- pol eval MC(sample path i, q s a, alpha = 1/epi i)
  pi <- pol imp(pi, q s a, exploration rate)</pre>
  exploration rate <- max(exploration rate*0.9997, 0.001) # exponential decay # 0.9997^10000=0.050
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 8.18 secs
t(pi)
     0 10 20 30 40 50 60 70
##
## n 0 1 0
## s 1 0 1 0 1 1 0 0
t(q s a)
##
          0
                10
                       20
                              30
                                     40
                                            50
                                                    60 70
## n -6.044 -4.768 -4.176 -2.781 -1.92 -2.131 -0.9983 0
## s -5.146 -5.795 -3.474 -3.568 -1.69 -1.710 -1.5800 0
```

II. Policy Iteration 2 - TD Control (a.k.a. sarsa)

Process

- The TD policy iteration process is summarized as follows:
 - 0. Initialize q(s, a)
 - 1. Begin with a policy π
 - 2. Begin a new sample path from the state s
 - 3. Proceed a time step to generate subsequent a, r, s', a' (simul_step())
 - 4. Evaluate the current policy π and update q(s,a) (pol_eval_TD())

$$q(s, a) \leftarrow q(s, a) + \alpha(r_t + \gamma q(s', a') - q(s, a)), \ \forall s, a$$

- 5. Improve the policy into a ϵ -greedy policy using q(s,a) (pol_imp())
- 6. Repeat 3-5 until the episode ends.
- 7. Repeat 2-6 many times (why not until policy converges?)
- \bullet Likewise, We will let num_ep to grow from 10^3 , 10^4 , and $5\cdot 10^4$.

```
num ep <- 10<sup>3</sup>
                                                     t(pi)
beg time <- Sys.time()</pre>
                                                           0 10 20 30 40 50 60 70
qsa<-qsainit
                                                                 0
                                                                    1
                                                                      1
pi <- pi 50
                                                                 1
                                                                       a
                                                                             a a
                                                              a
                                                                    a
for (epi i in 1:num ep) {
  s now <- "0"
  while (s now != "70") {
    sample step <- simul step(pi, s now, P normal, P speed, R s a)</pre>
    q s a <- pol eval TD(sample step, q s a, alpha = 1/epi i)
    pi <- pol imp(pi, q s a, epsilon = 1/epi i)
    s now <- sample step[4]
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 0.2954 secs
t(q s a)
##
          0
                10
                        20
                               30
                                      40
                                              50
                                                      69 79
## n -3.511 -2.946 -2.533 -2.028 -1.335 -1.536 -0.9711 0
## s -3.511 -2.947 -2.533 -2.028 -1.335 -1.535 -1.5441 0
```

```
num ep <- 10<sup>4</sup>
                                                      t(pi)
beg time <- Sys.time()</pre>
                                                           0 10 20 30 40 50 60 70
qsa<-qsainit
                                                                     0
                                                                       1
pi <- pi 50
                                                                        a
                                                                              a a
                                                              a
for (epi i in 1:num ep) {
  s now <- "0"
  while (s now != "70") {
     sample step <- simul step(pi, s now, P normal, P speed, R s a)</pre>
     q s a <- pol eval TD(sample step, q s a, alpha = 1/epi i)
     pi <- pol_imp(pi, q_s_a, epsilon = 1/epi_i)</pre>
     s now <- sample step[4]
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 2.655 secs
t(q s a)
##
          0
                 10
                        20
                                30
                                       40
                                              50
                                                       69 79
## n -3.943 -3.359 -2.937 -2.412 -1.566 -1.631 -0.9951 0
## s -3.943 -3.359 -2.937 -2.412 -1.566 -1.630 -0.9952 0
```

```
num ep <- 10<sup>5</sup>
                                                      t(pi)
beg time <- Sys.time()</pre>
                                                            0 10 20 30 40 50 60 70
qsa<-qsainit
pi <- pi 50
                                                                        a
                                                              a
                                                                  1
                                                                     a
exploration rate <- 1
for (epi i in 1:num ep) {
  s now <- "0"
  while (s now != "70") {
     sample step <- simul step(pi, s now, P normal, P speed, R s a)</pre>
     q s a <- pol eval TD(sample step, q s a, alpha = max(1/epi i, 0.01))
     pi <- pol imp(pi, q s a, epsilon = exploration rate)</pre>
     s now <- sample step[4]
     exploration rate <- exploration rate*0.9995
end time <- Sys.time()</pre>
print(end time-beg time)
## Time difference of 21.93 secs
t(q_s_a)
##
          a
                 10
                        20
                                30
                                       40
                                               50
                                                       69 79
## n -5.382 -4.478 -3.687 -2.692 -1.653 -1.887 -0.9996 0
```

s -5.054 -4.561 -3.401 -2.801 -1.769 -1.660 -1.4229 0

Exercise 1

Write the python code for this lecture note (both MC and TD control)

Exercise 2

The previous Part E provides us the correct solution. In your python code for MC and TD control, you have freedom to modify 1) number of iteration and 2) the exploration decaying scheme. Modify the two and see if you can match the results we obtained in Part E.

"It's not that I'm so smart, it's just that I stay with problems longer. - A. Einstein"