Lecture F4. MDP without Model - Policy Iteration (Q-learning, double Q-learning)

Sim, Min Kyu, Ph.D., mksim@seoultech.ac.kr



- I. Policy Iteration 3 Q-learning control
- II. Policy iteration 4 Double Q-learning control

• skiier.R is loaded as follows.

```
source("../skiier.R")
## [1] "Skiier's problem is set."
## [1] "Defined are `state`, `P_normal`, `P_speed`, `R_s_a`, `q_s_a_init` (F2, p15)."
## [1] "Defined are `pi_speed`, and `pi_50` (F2, p16)."
## [1] "Defined are `simul_path()` (F2, p17)."
## [1] "Defined are `simul_step()` (F2, p18)."
## [1] "Defined are `pol_eval_MC()` (F2, p19)."
## [1] "Defined are `pol_eval_TD()` (F2, p20)."
## [1] "Defined are `pol_imp()` (F2, p20)."
```

I. Policy Iteration 3 - Q-learning control

Strategy

• (pol_eval_MC()) MC control updates q(s, a):

$$g^{n}(s, a)$$

$$= r_{t} + r_{q} g^{n}(s', a')$$

$$s, a$$

 $q(s,a) \leftarrow q(s,a) + \alpha(G_t - q(s,a)), \ \, \forall s,a$ • (pol_eval_TD()) TD control updates q(s,a):

$$q(s,a) \leftarrow$$

$$q(s,a) \leftarrow q(s,a) + \alpha(r_t + \gamma \underline{q(s',a')} - q(s,a)), \ \, \forall s,a$$
 • (pol_eval_Q()) Q-learning updates $q(s,a)$:

$$q(s,a) \leftarrow q(s,a) + \alpha(r_t + \gamma \underbrace{max_{a' \in \mathcal{A}}q(s',a')}_{\text{Q, tat}}) - q(s,a)), \ \forall s,a$$

- Q-learning is a variation of TD control.
- Q-learning is greedy in a sense by taking maximum among possible future action.
- It is called off-policy learning since it may take action other than the current policy dictates.

Write pol_eval_Q()

```
pol eval TD <- function(sample step, q s a, alpha) {
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
                                                                           sarsá
 a next <- sample step[5]
 q s a[s,a] \leftarrow q s a[s,a] + alpha*(r+q s a[s next,a next]-q s a[s,a])
  return(q s a)
                                         TD-tst
pol eval 0 <- function(sample step, q s a, alpha) {
  s <- sample step[1]
  a <- sample step[2]
                                                                          Sars
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
  a_next <- sample_step[5] # not used here
 q_s_a[s,a] <- q_s_a[s,a] + alpha*(r+max(q_s_a[s_next,])-q_s_a[s,a]) # change here</pre>
  return(q s a)
                                        Q-+8+
```

Q-learning

```
num ep <- 10<sup>5</sup>
                                                    print(end time-beg time)
beg time <- Sys.time()</pre>
                                                    ## Time difference of 10.06 secs
q s a <- q s a init
                                                    t(pi)
pi <- pi 50
exploration rate <- 1
                                                         0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
                                                    ## n 0 0 0
                                                                  1 0
  s now <- "0"
                                                    ## s 1 1 1 0 1 0 0 0
  while (s now != "70") {
    sample step <- simul step(pi, s now, P normal, P speed, R s a)
    q s a <- pol eval Q(sample step, q s a, alpha = max(1/epi i, 0.05)) v
    if (epi i %% 100 == 0) {
      pi <- pol_imp(pi, q_s_a, epsilon = exploration_rate) 	✔
    s now <- sample step[4]
    exploration rate <- max(exploration rate*0.9995, 0.001)
end time <- Sys.time()</pre>
t(q s a)
##
          0
                10
                       20
                               30
                                      40
                                             50
                                                    60 70
## n -5.588 -4.662 -3.961 -2.695 -1.999 -2.000 -1.000 0
## s -5.017 -4.469 -3.362 -3.085 -1.673 -2.026 -1.685 0
```

II. Policy iteration 4 - Double Q-learning control

Method

• (pol_eval_Q()) Q-learning updates q(s,a):

$$q(s, a) \leftarrow q(s, a) + \alpha(r_t + \gamma \max_{a' \in \mathcal{A}} q(s', a') - q(s, a)), \ \forall s, a \in \mathcal{A}$$

- (pol_eval_dbl_Q()) Double Q-learning uses a pair of q-functions, $q_1()$ and $q_2()$. It updates
 - with probability 0.5 (wpdate 3, (s.a))
 - $\mathbf{V} \quad q_1(s,a) \leftarrow q_1(s,a) + \alpha(r_t + \gamma q_2(s', \underbrace{argmax_{a' \in \mathcal{A}} \ q_1(s',a')}) q_1(s,a)), \ \forall s,a \in \mathcal{A}$
 - with probability 0.5
 - - Policy is improved using $q_1(\cdot, \cdot) + q_2(\cdot, \cdot)$.
- By using multiple Q-functions, it is known to have less variance.

Write pol_eval_dbl_Q()

```
pol eval Q <- function(sample_step, q_s_a, alpha) {</pre>
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample_step[3] %>% as.numeric()
  s next <- sample step[4]
  q_sa[s,a] \leftarrow q_sa[s,a] + alpha*(r+max(q_sa[s_next,])-q_sa[s,a]) # change here
  return(q s a)
                                           Q tost
pol_eval_dbl_Q <- function(sample_step, q_s_a_1, q s a 2, alpha) {</pre>
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
                                                ひちいと れんら、のこと かち
  s next <- sample step[4]
  if (runif(1) < 0.5) { # update q 5 a 1
    q s a 1[s,a] <- q s a 1[s,a] +
      alpha*(r+q_s_a_2[s_next, which.max(q_s_a_1[s_next,])]-q_s_a_1[s,a]) # change here
  } else { # update a s a 2
                                              actions 9(5.0) = 0183mm ldey
    q s a 2[s,a] \leftarrow q s a 2[s,a] +
      alpha*(r+q s a 1[s next, which.max(q s a 2[s next,])]-q s a 2[s,a]) # change here
  return(list(q_s_a_1, q_s_a_2))
```

Double Q-learning

```
num ep <- 10^5
                                                    print(Sys.time()-beg time)
beg time <- Sys.time() # change below
                                                    ## Time difference of 10.58 secs
qsa1 <- qsainit; qsa2 <- qsainit
                                                    t(pi)
pi <- pi 50
exploration rate <- 1
                                                         0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
  s now <- "0"
                                                    ## s 1
  while (s now != "70") {
    sample step <- simul step(pi, s now, P normal, P speed, R s a)</pre>

√ q s a <- pol eval dbl Q(sample step, q s a 1, q s a 2, alpha = max(1/epi i, 0.05)) # change here
</p>

√ q_s_a_1 <- q_s_a[[1]]; q_s_a_2 <- q_s_a[[2]] # change here
</p>
    if (epi i %% 100 == 0) {
      pi <- pol imp(pi, q s a 1+q s a 2, epsilon = exploration rate) # change here
    s now <- sample step[4]
                                                                   0
    exploration rate <- max(exploration rate*0.9995, 0.001)
                                                                    10
t((q s a 1 + q s a 2)/2)
                                                                   20
##
                10
                       20
                              30
                                     40
                                            50
                                                   60 70
## n -5.492 -4.539 -3.843 -2.778 -1.703 -1.891 -1.000 0
                                                                    70
## s -5.071 -4.839 -3.410 -3.284 -1.840 -1.627 -1.695 0
```

Exercise 1

Implement double-Q learning, and feel free to try different schemes for the number of iterations and exploration decaying scenarios.

"It's not that I'm so smart, it's just that I stay with problems longer. - A. Einstein"