

ANSWERS

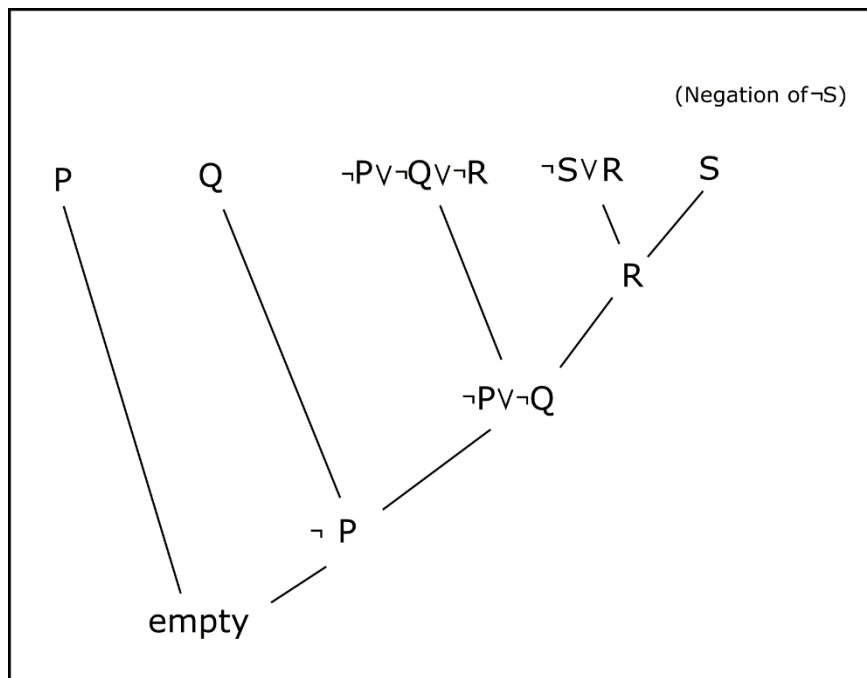
PROBLEM 1 – LOGIC

a)

1. $P \wedge Q$ given (premise)
2. P (from 1, decomposing a conjunction)
3. Q (from 1)
4. $P \rightarrow \neg(Q \wedge R)$ given
5. $\neg(Q \wedge R)$ (from 2,4)
6. $\neg Q \vee \neg R$ (from 5)
7. $\neg R$ (from 3,6)
8. $S \rightarrow R$ given
9. $\neg S$ (from 7,8)

b) Draw the truth table and see there is one row where 1,2, and 3 is true and $\neg S$ is also true there.

c)



d) First, we need to convert the definition of Green into CNF.

- $\forall x : \text{Green}(x) \leftrightarrow \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]$

Break the double-implication into 2 conjoined implications

- $\forall x : [\text{Green}(x) \rightarrow \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \wedge$
 $[[\text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \rightarrow \text{Green}(x)]$

Convert implications to disjunctions

- $\forall x : [\neg \text{Green}(x) \vee \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \wedge$
 $\neg[\text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \vee \text{Green}(x)$

Move negations inward

- $\forall x : [\neg \text{Green}(x) \vee \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \wedge$
 $\neg \text{Bikes}(x) \wedge \neg[\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)] \vee \text{Green}(x)$

Continue moving negations inward

- $\forall x : [\neg \text{Green}(x) \vee \text{Bikes}(x) \vee [\exists y : \text{Drives}(x, y) \wedge \text{Electric}(y)]] \wedge$
 $\neg \text{Bikes}(x) \wedge [\forall y : \neg \text{Drives}(x, y) \vee \neg \text{Electric}(y)] \vee \text{Green}(x)$

Skolemizing produces an $F(x)$ in place of the existential-quantified y :

- $\forall x : [\neg \text{Green}(x) \vee \text{Bikes}(x) \vee [\text{Drives}(x, F(x)) \wedge \text{Electric}(F(x))]] \wedge$
 $\neg \text{Bikes}(x) \wedge [\forall y : \neg \text{Drives}(x, y) \vee \neg \text{Electric}(y)] \vee \text{Green}(x)$

Remove the universal quantifications, since all remaining variables are universally quantified.

- $[\neg \text{Green}(x) \vee \text{Bikes}(x) \vee [\text{Drives}(x, F(x)) \wedge \text{Electric}(F(x))]] \wedge$
 $\neg \text{Bikes}(x) \wedge [\neg \text{Drives}(x, y) \vee \neg \text{Electric}(y)] \vee \text{Green}(x)$

Distribute the disjunction in the first half

- $[\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Drives}(x, F(x))] \wedge$
 $[\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Electric}(F(x))] \wedge$
 $\neg \text{Bikes}(x) \wedge [\neg \text{Drives}(x, y) \vee \neg \text{Electric}(y)] \vee \text{Green}(x)$

Distribute the disjunction in the second half to produce a conjunction of 4 disjuncts (CNF).

- $[\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Drives}(x, F(x))] \wedge$

$[\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Electric}(F(x))] \wedge$

$[\text{Green}(x) \vee \neg \text{Bikes}(x)] \wedge$

$[\neg \text{Drives}(x, y) \vee \neg \text{Electric}(y) \vee \text{Green}(x)]$

Next, combine these 4 clauses with the other givens and add in the negation of the goal sentence: $\text{Green}(\text{Sophie})$. Then keep applying the resolution rule until $\theta = \text{False}$ is derived, indicating the contradiction.

1. $\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Drives}(x, F(x))$ Given
2. $\neg \text{Green}(x) \vee \text{Bikes}(x) \vee \text{Electric}(F(x))$ Given
3. $\text{Green}(x) \vee \neg \text{Bikes}(x)$ Given
4. $\neg \text{Drives}(x, y) \vee \neg \text{Electric}(y) \vee \text{Green}(x)$ Given
5. $\text{Electric}(\text{Tesla})$ Given
6. $\text{Drives}(\text{Sophie}, \text{Tesla})$ Given
7. $\neg \text{Green}(\text{Sophie})$ (Assuming negation of target sentence)
8. $\neg \text{Drives}(x, \text{Tesla}) \vee \text{Green}(x)$ (Resolving 4 and 5 with $\theta = \{y/\text{Tesla}\}$)
9. $\text{Green}(\text{Sophie})$ (Resolving 6 and 8 with $\theta = \{x/\text{Sophie}\}$)
10. (Resolving 7 and 9 with $\theta = \{\}$)

Notice that only 1 of the 4 clauses derived from the definition of Green was used to prove the target sentence.

PROBLEM 2 --INFORMED AND UNINFORMED SEARCH

a) Uniform cost:

Expanded nodes: SADBCE G2

Solution path: S D C G2

Path cost: 13. Optimal path. Uniform cost search is optimal when there are no negative path costs.

b) Breadth first:

Expanded: S A G1. (goal check is when childs are generated)

S. Path: S A G1

Path cost: 14. Not optimal. BFS is cost optimal only when the steps costs are identical

c) Depth first

Expanded nodes: S A B C F D E G3

Solution cost: 45

d) A*

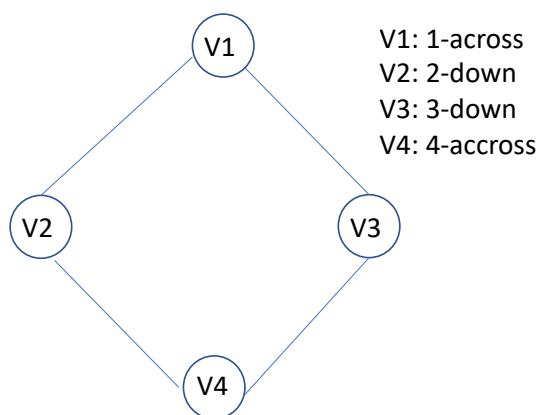
Expanded nodes: S A B D C E G2

Solution path: S D C G2

Path cost: 13. Optimal.

PROBLEM 3 ---CSP CROSS WORD PUZZLE

a)



b) C1: V1 has 5 letters

C2: V2 has 3 letters

C3: V3 has 3 letters

C4: V4 has 4 letters

C5: 3rd letter of V1 is the same letter as the first letter of V2

C6: 5th letter of V1 is the same letter as the first letter of V3

C7: 2nd letter of V4 is the same letter as 3rd letter of V2

....

....

c) Domains, according to node consistency:

V1 ----Domain1={ astar, happy, hello, hoses}

V2 ----Domain2={ live, load, loam, peal, peel, save, talk, anon, nerd, tine }

V3 ----Domain3={ ant, oak, old, run, ten}

V2 ----Domain2={ live, load, loam, peal, peel, save, talk, anon, nerd, tine}

d)

Arc consistency Queue	Set to consider arc consistency	Set domains of the 2 variables of the arc	Domains of the 2 variables after consistency checked
V1V2, V1V3, V2V1, V2V4, V3V1, V3V4, V4V2, V4V3	V1V2	V1 {astar, happy, hello, hoses} V2 {live, load, loom, peal, peel, save, talk, anon, nerd, tine}	V1 {astar, happy, hello, hoses} V2 {live, load, loom, peal, peel, save, talk, anon, nerd, tine}
V1V3, V2V1, V2V4, V3V1, V3V4, V4V2, V4V3	V1V3	V1 {astar, happy, hello, hoses} V3 {ant, oak, old, ten, run}	V1 {astar, hello} V3 {ant, oak, old, ten, run}
V2V1, V2V4, V3V1, V3V4, V4V2, V4V3	V2V1	V2 {live, load, loom, peal, peel, save, talk, anon, nerd, tine} V1 {astar, hello}	V2 {live, load, loom, talk, tine} V1 {astar, hello}
V2V4, V3V1, V3V4, V4V2, V4V3, V1V2	V2V4	V2 {live, load, loom, talk, tine} V4 {live, load, loom, peal, peel, save, talk, anon, nerd, tine}	V2 {load, loom, tine} V4 {live, load, loom, peal, peel, save, talk, anon, nerd, tine}
V3V1, V3V4, V4V2, V4V3, V1V2	V3V1	V3 {ant, oak, old, ten, run} V1 {astar, hello}	V3 {oak, old, run} V1 {astar, hello}

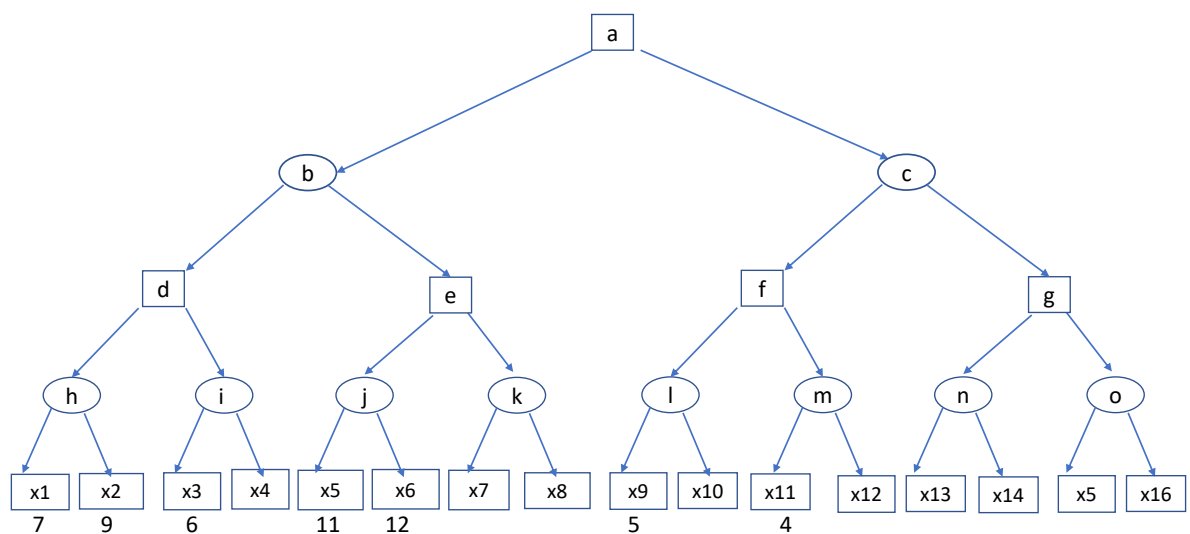
V3V4, V4V2, V4V3, V1V2, V1V3	V3V4	V3{oak, old, run} V4{live, load, loom, peal, peel, save, talk, anon, nerd, tine}	V3{oak, old, run} V4{live, load, loom, peal, peel, save, talk, anon, nerd, tine}
V4V2, V4V3, V1V2, V1V3	V4V2	V4{live, load, loom, peal, peel, save, talk, anon, nerd, tine} V2{load, loom, tine}	V4{load, loom, save, talk, anon} V2{load, loom, tine}
V4V3, V1V2, V1V3, V2V4, V3V4	V4V3	V4{load, loom, save, talk, anon} V3{oak, old, run}	V4{load, talk, anon} V3{oak, old, run}
V1V2, V1V3, V2V4, V3V4	V1V2	V1{astar, hello} V2{load, loom, tine}	V1{astar, hello} V2{load, loom, tine}
V1V3, V2V4, V3V4	V1V3	V1{astar, hello} V3{oak, old, run}	V1{astar, hello} V3{oak, old, run}
V2V4, V3V4	V2V4	V2{load, loom, tine} V4{load, talk, anon}	V2{load, loom, tine} V4{load, talk, anon}
V3V4	V3V4	V3{oak, old, run} V4{load, talk, anon}	V3{oak, old, run} V4{load, talk, anon}

e) One of the possible solutions is:

A	S	T	A	R
		I		U
	A	N	O	N
		E		

PROBLEM 4 ---- ADVERSARIAL SEARCH

- a) $H=7, i \leq 6, d=7, j=11, e \geq 11, b=7, c \leq 5, f \leq 5, l \leq 5, m \leq 4$. solution=7
b) x4, k, x10, x12, and g are pruned



PROBLEM 5--- GAME THEORY

- a) $N=\{A1, A2\}$, Domains of $A1=A2=\{0,10,20,30,40,50\}$, and the payoff fns are specified by the following matrix

A1, Agent2	0	10	20	30	40	50
0	40, 0	0, 30	0, 30	0, 30	0, 30	0, 30
10	40, 0	30, 0	0, 20	0, 20	0, 20	0, 20
20	40, 0	30, 0	20, 0	0, 10	0, 10	0, 10
30	40, 0	30, 0	20, 0	10, 0	0, 0	0, 0
40	40, 0	30, 0	20, 0	10, 0	0, 0	0, -10
50	40, 0	30, 0	20, 0	10, 0	0, 0	-10, 0

- b) There is no weakly dominant strategy eq. as neither player has a weakly dominant action. Notice that for both players, actions 30 and 40 weakly dominate every other action. But not each other.
- c) D) There is no strictly dominated action for either player and hence all the action profiles survive IESD actions
- d) We can eliminate the weakly dominated actions in the following order:
- A:0
A2:0
A1: 50
A2: 50
A1:10
A2: 10
A1: 20
- Which leads to the following set of outcomes $\{30,40\} \times \{20,30,40\}$. However, there are other orders of elimination which lead to different outcomes.
- e) The game is not dominance solvable.