

# Practical Identity-Based Encryption for Online Social Networks

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Thesis submitted for the degree of Master of Science in Electrical Engineering, option Embedded Systems and Multimedia

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# **Preface**

An intensive year of programming, writing and reviewing has preceded the submission of this thesis text. I would like to take the opportunity to present my gratitude to those who have made this possible.

First of all, I would like to thank Prof. Bart Preneel and Prof. Vincent Rijmen for supporting this research and giving me this opportunity.

Second of all, I would like to thank my mentor Filipe Beato for the many intensive feedback sessions. I am truly inspired by his enthusiasm and patience while answering all my questions. I can imagine the frustration Filipe must have gone through while reading thesis drafts that lacked every sign of academic English. Thereby neglecting, the even larger frustration Filipe must have felt when I simply did not understand his remarks on my academic English from the beginning.

I would also like to acknowledge my assessors, Prof. Claudia Diaz and Prof. Frank Piessens for giving their insights and taking the time to read this text.

I cannot forget to express my gratefulness to Sofie, for being around and supporting me. No one in my environment has inspired and motivated me more than Sofie during my last year as a master student.

Special gratitude goes to all my friends at Lerkeveld and VTK for distracting me during my leisure time. I am sorry for all the times I shared these little frustrations that come with writing a thesis text.

Finally, special thanks goes to my parents who have always believed in me during my five year study at KU Leuven. Without their financial and emotional support I would not have pursued my dream to become an engineer. Therefore, this work is also partially their realisation.

Stijn Meul

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# **Abstract**

Currently Online Social Networks (OSNs) constitute an important and useful communication channel. However, coarse-grained privacy preferences protect the shared information insufficiently. Although cryptography provides interesting mechanisms to protect privacy, existing solutions face several issues such as, OSN provider acceptance, user adoption, key management and usability.

In this thesis, we propose a practical solution that uses Identity Based Encryption (IBE) to simplify key management and enforce confidentiality of data in OSNs. By translating key generation of traditional IBE schemes to a distributed setting, our scheme prevents key escrow as long as the number of colluding key generators does not exceed a predefined threshold. Moreover, we devise an outsider anonymous broadcast IBE scheme to disseminate information among multiple users, even if they are not using the system. Apart from increased usability, the proposed solution no longer requires complex key management infrastructures keeping track of all keys in the system thereby relaxing users' prior knowledge on cryptographic primitives.

The viability and tolerable overhead of our solution is demonstrated by extending an existing plugin for encryption in OSNs called Scramble. Based on the existing Scramble architecture and the MIRACL multi-precision library, we program an open-source prototype that implements our proposed solution on Facebook but can be generalised for use in any existing OSN infrastructure.

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# List of Abbreviations

ANO-IBE Anonymous IBE

ANO-IND-CCA Anonymity preserving IBE scheme that is indistinguishable

under chosen ciphertext attacks

ANO-IND-CPA Anonymity preserving IBE scheme that is indistinguishable

under chosen plaintext attacks

API Application Programming Interface

CA Certification Authority
DKG Distributed Key Generation
IBE Identity-Based Encryption

IND-CCA Indistinguishability under Chosen Ciphertext Attack IND-CPA Indistinguishability under Chosen Plaintext Attack

OSN Online Social Network
PKG Public Key Generator
PKI Public Key Infrastructure

UI User Interface

# List of Symbols

(G,\*)

G

 $\mathbb{Z}_n$ 

viii

tion \*

Group (G, \*)

Set of integers modulo n

$\lambda$	Security parameter
l	The number of bits required to realise security level $\lambda$
s	Secret
${\mathcal S}$	Set of intended recipients
$sk_i$	Private key corresponding to the public key $pk_i$ or the public verifying key $vk_i$ depending on the application
$pk_i$	Public key with corresponding private key $sk_i$
$vk_i$	Verifying key with corresponding signing key $sk_i$
$sk_{msk}$	Master secret key
$\{0,1\}^{l}$	Binary bit sequence of length $l$
$\{0,1\}^*$	Binary bit sequence of variable length
m	Message
c	Ciphertext
v,w	Binary bit sequences
$\{v \parallel w\}$	Concatenated bit sequences
$\mathtt{id}_{Alice}$	Identity of Alice
$s_{\mathtt{id}_{Alice}}$	IBE private key corresponding to the identifier $\mathtt{id}_{Alice}$
k	Generic symmetric session key
$\mathtt{E}_{k}\left( m ight)$	Symmetric encryption of the message $m$ under session key $k$
$\mathtt{D}_{k}\left( c ight)$	Symmetric decryption of the ciphertext $c$ under session key $k$
*	Binary operation

Algebraic group with respect to the set G and the binary opera-

$H\left(w\right)$	Hash function with bit sequence $w$ as input
$S_A\left(m ight)$	Signature of entity $A$ on message $m$
$S_{sk_A}\left(m\right)$	Signature generated by the signing key $sk_A$ of entity $A$ on
	message $m$
$e:G_1\times G_2\to G_T$	Bilinear map
U, P, Q	Points on an elliptic curve
$e\left(P,Q\right)$	Bilinear map for the points $P \in G_1, Q \in G_2$ such that
	$e\left(P,Q\right)\in G_{T}$
$\{a,\ldots,b\}$	Set of values of the same type
$\langle a, \dots, P \rangle$	Collection of objects of different type
$\mathcal{A}\left(a,b\right)$	Algorithm $\mathcal{A}$ with parameters $a$ and $b$
$\langle a,b,c\rangle \leftarrow \mathcal{A}(d,e)$	Algorithm ${\mathcal A}$ with parameters $d$ and $e,$ returns the collection of values $a,b,c$
$v \oplus w$	Bit by bit XOR operation of $v$ and $w$
$\perp$	Invalid output

1

# Introduction

Online Social Networks (OSNs) represent the most impactful internet trend at the dawn of the 21st century. Words like tweeting, sharing, liking, trending and tagging have found common acceptance in the vocabulary of current internet users, while services like Facebook, Google+, LinkedIn and Twitter have become part of everyday life. OSNs offer millions of users an efficient and reliable channel to distribute and share information. At the same time, OSNs store large amounts of data which prompts several privacy concerns, as it is possible to infer a considerable amount of sensitive information from the shared and stored content. Currently, users are allowed to configure "privacy preferences" in order to limit and select which users or groups can access the shared content. However, these preferences are generally too coarse-grained and difficult to configure [27]. Another problem is that these preferences do not exclude the provider along with the dangers of data leaks [54] nor external governments [100].

## 1.1 Problem Statement

All these worrisome issues motivate the need for effective techniques to properly protect users' privacy in OSNs. Several solutions have been proposed and advocated to use cryptographic mechanisms in order to address the privacy issues, either by an add-on atop existing OSNs [7, 15, 70, 88], or by complete new privacy-friendly architectures [43, 44, 50]. In general, those solutions suffer from user adoption and key management issues as users are required to register and then share, certify and store public keys [9]. Completely new architectures represent a difficult step for users as the trade off of moving away from the commonly used social ecosystem compared with the risk of losing interactions is agonising. Arguably, current centralised OSNs are here to stay and will continue to be actively used by millions of people. In light of recent events, such as Edward Snowden's whistle-blowing on US surveillance programs [100], OSN providers have all interest to maintain their users and a privacy-friendly image. However, not all OSNs are probably willing to cooperate in a more private infrastructure since an important part of their revenues consists of targeted advertising.

# 1.2 Existing Solutions

Earlier research has proposed peer-to-peer OSNs such as Safebook [44] and Diaspora [50], in which no centralised authority has control over the network. However, these solutions face slow user adoption since users prefer not to face the risk of less social interaction in exchange for increased privacy. Therefore, only solutions to existing centralised OSN infrastructures are considered in the remainder of this text.

FLYBYNIGHT [87] is a Facebook application which protects user data by storing it in encrypted form on Facebook. It relies on Facebook servers for its key management and is thus not secure against active attacks by Facebook itself.

NOYB (None Of Your Business) [70] replaces details of a user with details from other random users thereby making this process only reversible by friends. However, the proposed solution does not apply to user messages or status updates that are the most frequently used features in the OSNs considered in this thesis.

FACECLOAK [88] stores published Facebook data on external servers in encrypted form and replaces the data on Facebook with random text from Wikipedia. This could be a useful mechanism to prevent OSNs from blocking security aware users because they are scared to see their advertising revenues shrink. However, this approach has the disadvantage that other users could take this data as genuine user content which may lead to social issues. Furthermore, FaceCloaks architecture leads to an inefficient key distribution system.

PERSONA [7] is a scheme that can be used as a Firefox extension to let users of an OSN determine their own privacy by supporting the ability to encrypt messages to a group of earlier defined friends based on attribute-based encryption (ABE) [104]. The scheme supports a wide range of meaningful use cases. For instance, sending messages to all friends that are related to a certain attribute or even encrypting messages to friends of friends. However, the major drawback of this system is that, for every new friend a public key is exchanged before he is able to interact in the privacy preserving architecture consequently requiring an infrastructure for broadcasting and storing public keys. Furthermore, to support the encryption of messages to friends of friends, user defined groups should be made available publicly thereby making the public key distribution system even more complicated. Finally the proposed ABE encryption scheme is 100 to 1000 times slower than a standard RSA operation [7].

SCRAMBLE [15] is a Firefox extension that allows users to define groups of friends that are given access to stored content on OSNs. The tool uses public key encryption based on OpenPGP [32] to broadcast encrypted messages on any platform. Furthermore Scramble provides the implementation of a tiny link server such that OSN policies not allowing to post encrypted data are bypassed. However, as indicated by usability studies [114] OpenPGP has a higher usage threshold because an average user does not manage to understand OpenPGP properly. Additionally, Scramble has to rely on the security decisions of the web of thrust. It therefore inherits the unpleasant property of OpenPGP that the user can not be sure that the used PGP key actually belongs to the intended Facebook profile.

However, the most unattractive property of all centralised applications is the need to rely on a rather complex infrastructure. For instance, Persona has to support an extended public key distribution system and Scramble relies on the leap-of-faith OpenPGP web of trust. All proposed solutions require users without background on asymmetric cryptography to make responsible decisions concerning the management of their keys. Furthermore, maintaining such complex key infrastructures becomes more and more complex as more users subscribe.

## 1.3 Goals

The goal of this thesis is to design and implement an architecture that solves the aforementioned issues thereby taking the challenges and pitfalls from earlier solutions into account. Specifically, the architecture should present the following properties:

- User friendly: The average OSN user should be able to use the resulting architecture, i.e. a user with no knowledge on cryptographic primitives.
- Applicable: The original OSN environment should not be altered since some OSN providers are probably not willing to support a more confidential architecture because it could hurt their business model.
- Immediately ready to use: No additional registration or subscription to third party key architectures should be required to enable usage of the system. As soon as a user subscribes to the OSN provider he should be able to start receiving confidential messages.

## 1.4 Main Idea

Identity Based Encryption (IBE) [109] schemes accomplish most of the preceding properties. IBE solutions overcome the key management problem as the public key of the user can be represented by any valid string, such as the email, unique id or username. Therefore, by using an OSN username any savvy and concerned user can share encrypted content with other users who are not using the solution, thereby motivating curious ones to use the system as well. Nevertheless, IBE-based systems require a trusted central Private Key Generator (PKG) to compute the private parameters for each user based on a master secret. Consequently, such an architecture only shifts the trusted party from the OSN to the PKG. However, this problem can be mitigated if the master secret is divided among multiple PKGs following a Distributed Key Generation (DKG) [99] protocol based on Verifiable Secret Sharing (VSS) [39]. A DKG protocol allows n entities to jointly generate a secret requiring that a threshold t out of n entities does not get compromised. In fact, each entity holds only a share of the master secret, that can be reconstructed by at least t shares.

Many OSN users are not only represented on a single OSN but on several, thus, can also hold multiple public keys. Moreover, the multi-PKG setting could be supported and maintained by different organisations, each with their own motivations to reinforce increased privacy in OSNs. In particular, if OSN providers see their advertisement revenues drop due to privacy concerned users deleting their profiles, they have an incentive to support and maintain such a multi-PKG setting. Certainly, in light of recent events, such as Edward Snowden's whistle-blowing on US surveillance programs [100], OSN providers have all interest to maintain their users and a privacy-friendly image. Since collaboration between competing OSNs is assumed to be a difficult task and orthogonal to their business model, the different PKGs do not compromise the security of the protocol. Figure 1.1 overviews an example of a possible model, where a user authenticates to t-PKGs of his choice using, e.g. a similar token as in open id protocols, to retrieve his private key. This action can be performed after the reception of encrypted content. The PKG servers can also be represented by governmental entities or subsidised research institutions from different continents, with no incentives to collaborate nor overcome more powerful adversaries using legal measures [91] among at least t-PKGs.

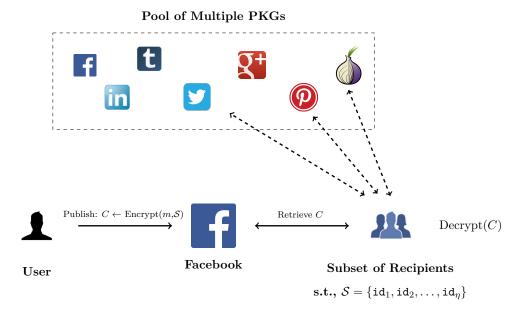


Figure 1.1: Multiple (n, t)-PKG IBE for OSNs overview, for a message m published for the set S for t = 3. The PKG infrastructure can be maintained by virtually any organisation with an incentive to make OSNs more private.

## 1.5 Structure of this Thesis

The structure of this thesis is organised as follows:

- Chapter 2 introduces required mathematical background such as definitions on complexity theory, probability theory, algebraic groups, finite fields and number theoretic assumptions. Bilinear maps are introduced as a response to different variants of the Diffie-Hellman assumption. The notion of bilinear maps then allows to derive the Bilinear Diffie-Hellman problem (BDH) which guarantees the security of our future constructions. The chapter concludes with basic definitions and notations on cryptography along with hash functions and the random oracle assumption.
- Chapter 3 highlights all cryptographic building blocks for the design of our solution. The chapter starts with a review on traditional public key infrastructures (PKI). An elaborate discussion on identity-based encryption (IBE) follows, describing a comparison of IBE with PKI, security notions of IBE, a summary of literature on IBE and the most attractive IBE schemes proposed in literature. Consequently, the reader is introduced to broadcast encryption and secret sharing. Chapter 3 concludes with distributed key generation as an anonymous generalisation of secret sharing.
- Chapter 4 describes the design of a practical encryption scheme for OSNs. We start by defining a model which describes the current OSN situation. With the help of this model, the current security threats are uncovered along with possible adversaries and realistic assumptions on these adversaries. Consecutively, different cryptographic design goals are defined to resolve the earlier described security threats. The design goals serve as a guideline to construct a practical algorithm based on the cryptographic building blocks from Chapter 3. The end of Chapter 4 proposes a mathematical Algorithm that is the result of our earlier design decisions.
- Chapter 5 discusses the practical details of implementing the algorithm derived in Chapter 4 as a proof-of-concept. First, an introduction is given on Scramble, an existing tool for broadcast encryption in OSNs. This is followed by adaptations to the existing architecture in order to implement our proposed algorithm. Chapter 5 further discusses the practical implementation decisions along with the structure of our code. This is followed by a performance analysis of the implementation. The last section of Chapter 5 presents the current limitations of our proof-of-concept.
- Chapter 6 concludes this thesis with a summary of earlier research results along with the limitations of our current solution. Finally, we close this thesis by highlighting topics that might be subject of future work along with the wide plethora of applications our construction might enable.

2

# Required Background

This chapter briefly covers the required background to understand cryptographic algorithms presented later in this text. The mathematical details of this chapter represent a fundament of exciting cryptographic concepts like identity-based encryption. If the reader feels he has sufficient background of the topics covered in this chapter, the chapter can be skipped without loss of comprehension.

Note that this chapter only overviews the cryptographic fundamentals required to understand the remainder of the thesis. Definitions and theorems are always provided without proof. For a more in depth discussion on algebraic topics in this chapter, the reader is referred to [95] and [19]. More information on elliptic curves, Diffie-Hellman assumptions and pairing based cryptography can be found in [1].

For the remainder of this chapter, complexity theoretic notions are introduced, followed by an introduction to statistical indistinguishability and an overview of algebraic structures and their properties. Then, a number of theoretic assumptions fundamental for cryptographic security are presented. Moreover, the introduction of gap groups and bilinear maps naturally follows by exploring these variants of the Diffie-Hellman assumption. Finally, hash functions are defined as well as their relation to the random oracle assumption.

# 2.1 Complexity Theory

Complexity theory classifies mathematical problems according to their inherent difficulty. The inherent difficulty of a mathematical problem is expressed in terms of the required resources to solve the problem independent of the algorithm used [95].

**Definition 2.1 (Asymptotic upper bound).** A function f(n) which is non-negative for all integers  $n \geq 0$ , has an asymptotic upper bound g(n) denoted f(n) = O(g(n)), if there exists an integer  $n_0$  and a constant c > 0 such that for all integers  $n \geq n_0$ ,  $f(n) \leq cg(n)$ 

**Definition 2.2 (Polynomial-time algorithm [95]).** A polynomial-time algorithm is an algorithm whose worst-case running time function is of the form  $O(n^c)$  where n is an input parameter and c is a constant.

**Definition 2.3 (Exponential-time algorithm [95]).** Any algorithm whose running time is not computationally bounded like a polynomial-time algorithm, is called an *exponential-time algorithm*.

Exponential-time algorithms are inefficient since they can take a long time to complete. Security of cryptographic algorithms is guaranteed if no polynomial-time algorithm exists to reverse the cryptographic operation without additional information.

An algorithm is considered secure against computationally bounded adversaries if the probability of success is smaller than the reciprocal of any polynomial function. The negligible function can be used to exactly describe this notion in a formal way.

**Definition 2.4 (Negligible function).** A negligible function in  $\lambda$  is a function  $\mu(\lambda): \mathbb{N} \to \mathbb{R}$  if for every polynomial  $p(\cdot)$  there exists an N such that for all  $\lambda > N$  [63]

$$\mu(\lambda) < \frac{1}{p(\lambda)}$$

The negligible function is used along this chapter to formally describe computationally infeasible problems. In such a context  $\lambda$  often represents the security parameter. The larger  $\lambda$  will be chosen, the smaller  $\mu(\lambda)$  will be.

# 2.2 Probability Theory

We introduce basic terminology on probability theory that allows to introduce statistical indistinguishability and computational indistinguishability.

**Definition 2.5 (Experiment).** An *experiment* is a procedure that yields one of a set of given outcomes. The set of all possible outcomes is called the *sample space* S. [95]

This thesis only considers discrete sample spaces, i.e. sample spaces with only a finite number n of possible outcomes such that  $S = \{s_1, \dots, s_n\}$ .

**Definition 2.6 (Probability distribution).** A probability distribution P on S is a sequence of numbers  $p_1, p_2, \dots, p_n$ , that are all non-negative and sum to one. The number  $p_i$  is interpreted as the probability of  $s_i$  being the outcome of the experiment, such that  $\Pr[s_i] = p_i$ . [95]

**Definition 2.7 (Random variable [95]).** A random variable X is a function from the sample space S to the set of real numbers; to each simple event  $s_i \in S$ , X assigns a real number  $X(s_i)$ 

**Definition 2.8 (Distribution ensemble).** An ensemble of random variables is a set of indexed random variables  $E_X = \{X_1, \dots, X_n\}, n \in \mathbb{N}$ .

**Definition 2.9 (Perfect randomness).** A bit sequence w contains perfect randomness or is said to be chosen uniformly random if every bit b in w could have been the result of the toss of a fair coin. That is, the probability that b=1 equals the probability of b=0 or more formally,  $\Pr[b=1] = \Pr[b=0] = \frac{1}{2}$ . Such that, a bit sequence is an ensemble of random variables where each random variable represents one bit.

**Definition 2.10 (Statistical indistinguishability).** Two ensembles of random variables  $E_X = \{X_1, \ldots, X_n\}$  and  $E_Y = \{Y_1, \ldots, Y_n\}$  with a common discrete sample space  $S_n$  for all n, are said to be *statistically indistinguishable* if for every polynomial  $p(\cdot)$  and sufficiently large n

$$\sum_{s \in S_n} \left| \Pr \left[ X_n(s) \right] - \Pr \left[ Y_n(s) \right] \right| \le \frac{1}{p(n)}$$

**Definition 2.11 (Computational indistinguishability).** Two ensembles of random variables  $E_X = \{X_1, \ldots, X_n\}$  and  $E_Y = \{Y_1, \ldots, Y_n\}$  with a common discrete sample space  $S_n$  for all n, are said to be *computationally indistinguishable* if for every polynomial  $p(\cdot)$ , sufficiently large n and every polynomial time algorithm  $\mathcal{A}$ 

$$\sum_{s \in S_n} \left| \Pr \left[ \mathcal{A} \left( X_n \right) = 1 \right] - \Pr \left[ \mathcal{A} \left( Y_n \right) = 1 \right] \right| \leq \frac{1}{p \left( n \right)}$$

where the probability is over the relevant distribution of  $X_n$  or  $Y_n$  and the random bits of the algorithm  $\mathcal{A}$ . [64]

More intuitively, statistical indistinguishable distributions resemble each other to that level that no one can determine their difference statistically. On the contrary, computational indistinguishable distributions can be statistically different but no existing algorithm with reasonable execution time can determine their difference [81].

# 2.3 Abstract Algebra

Abstract algebra is a field of mathematics that studies algebraic structures such as groups, rings and vector spaces. These algebraic structures define a collection of requirements on mathematical sets such as e.g., the natural numbers  $\mathbb{N}$  or matrices of dimension  $2 \times 2 \mathbb{R}^{2x^2}$ . If these requirements hold, abstract properties can be derived. Once a mathematical set is then categorised as the correct algebraic structure, properties derived for the algebraic structure will hold for the set as a whole.

In the light of our further discussion, especially additive and multiplicative groups prove to be essential concepts. However, algebraic groups come with a specific vocabulary such as binary operation, group order and cyclic group that are defined in this section as well.

**Definition 2.12 (Binary operation).** A binary operation \* on a set S is a mapping  $S \times S \to S$ . That is, a binary operation is a rule which assigns to each ordered pair of elements a and b from S a uniquely defined third element c = a \* b in the same set S. [19, 95]

**Definition 2.13 (Group).** A group (G, \*) consists of a set G with a binary operation \* on G satisfying the following three axioms:

- 1. Associativity  $\forall a, b, c \in G : a * (b * c) = (a * b) * c$
- 2. Identity element  $\forall a \in G, \exists e \in G : a * e = e * a = a$  where e denotes the identity element of G
- 3. Inverse element  $\forall a \in G, \exists \ a^{-1}: a*a^{-1}=a^{-1}*a=1$  where  $a^{-1}$  denotes the inverse element of a

**Definition 2.14 (Commutative group).** A group (G,\*) is called a *commutative group* or an *abelian group* if in addition to the properties in Definition 2.13, also commutativity holds.

#### 4. Commutativity $\forall a, b \in G : a * b = b * a$

Depending on the group operation \*, (G,\*) is either called a *multiplicative group* or an *additive group*. In Definition 2.13 the multiplicative notation is used. For an additive group the inverse of a is often denoted -a [95].

A group (G, \*) is often represented by the more concise symbol G although groups are always defined with respect to a binary group operation \*. Despite of a more concise notation, any group G still obeys all axioms from Definition 2.13 with respect to an implicitly known group operation \*.

A perfect example of a commutative group is the set of integers with the addition operation  $(\mathbb{Z}, +)$  since the addition is both associative and commutative in  $\mathbb{Z}$ . Furthermore, the identity element e = 0 and the inverse element  $\forall a \in \mathbb{Z}$  is  $-a \in \mathbb{Z}$ . Note that the set of natural numbers with the addition operation  $(\mathbb{N}, +)$  is not a commutative group as not every element of  $\mathbb{N}$  has an inverse element.

**Definition 2.15 (Cyclic group).** A group G is *cyclic* if and only if  $\forall b \in G, \exists g \in G, \exists n \in \mathbb{Z} : g^n = b$ . Such an element g is called a *generator* of  $\mathbb{G}$ .

Definition 2.15 implies that in a cyclic group every element can be written as a power of one of the group's generators.

**Definition 2.16 (Finite group).** A group G is *finite* if the number of elements in G denoted |G| is finite. The number of elements |G| in a finite group is called the *group order*.

The set  $\mathbb{Z}_n$  denotes the set of integers modulo n. The set  $\mathbb{Z}_5$  with the addition operation is a cyclic finite group of order 5. The set  $\mathbb{Z}_5 \setminus \{0\}$  with the multiplication operation, often denoted  $\mathbb{Z}_5^*$ , is a cyclic finite group of order 4 where the neutral element e = 1. For example, 2 is a generator in  $\mathbb{Z}_5^*$  since every element in  $\mathbb{Z}_5^*$  can be written as  $\{2^n | n \in \mathbb{Z}\}$ .

**Definition 2.17 (Order of an element).** Let G be a group. The *order of an element*  $a \in G$  is defined as the least positive integer t such that  $a^t = e$ . If there exists no such t, t is defined as  $\infty$ .

**Theorem 2.18.** If the group order of G equals a prime p, G is cyclic and commutative.

**Definition 2.19 (Subgroup).** Given a group (G, \*), any H that is a non-empty subset  $H \subseteq G$  and satisfies the axioms of a group with respect to the group operation \* in H, is a *subgroup of* G.

**Definition 2.20 (Ring).** A ring(R, +, \*) consists of a set R with two binary operations + and \* on R satisfying the following axioms:

- 1. (R, +) is an abelian group with identity denoted e
- 2. Associativity  $\forall a, b, c \in R : a * (b * c) = (a * b) * c$
- 3. Multiplicative identity element  $\forall a \in R, \exists 1 \in R : a * 1 = 1 * a = a$  where 1 denotes the multiplicative identity element of R
- 4. Left distributivity  $\forall a, b, c \in R : a * (b + c) = (a * b) + (a * c)$
- 5. Right distributivity  $\forall a, b, c \in R : (b+c) * a = (b*a) + (c*a)$

**Definition 2.21 (Commutative ring).** A ring (R, +, \*) is called a *commutative ring* or an *abelian ring* if in addition to the properties in Definition 2.20, also commutativity holds.

6. Commutativity  $\forall a, b \in R : a * b = b * a$ 

**Definition 2.22 (Field).** A commutative ring (R, +, \*) is called a *field* if in addition to the properties in Definition 2.21 and Definition 2.20 all elements of R have a multiplicative inverse.

7. Multiplicative inverse  $\forall a \in R, \exists a^{-1} : a * a^{-1} = a^{-1} * a = 1$  where  $a^{-1}$  denotes the inverse element of a

**Definition 2.23 (Finite field).** A finite field or a Galois Field is a field F with a finite number of elements. The number of elements |F| of a finite field F is called its order.

**Definition 2.24 (Ring homomorphism).** Given rings R and S, a *ring homomorphism* is a function  $f: R \to S$  such that the following axioms hold:

- 1.  $\forall a, b \in R : f(a+b) = f(a) + f(b)$
- 2.  $\forall a, b \in R : f(ab) = f(a) f(b)$
- 3.  $f(e_R) = f(e_S)$  where  $e_S$  and  $e_R$  denote the identity element of respectively S and R

**Definition 2.25 (Bijective function).** Any function  $f: R \to S$  is bijective if it satisfies the following axioms

- 1. Injective Each element in S is the image of at most one element in R. Hence,  $\forall a_1, a_2 \in R$  if  $f(a_1) = f(a_2)$  then  $a_1 = a_2$  naturally follows.
- 2. Surjective Each  $s \in S$  is the image of at least one  $r \in R$ .

**Definition 2.26 (Ring isomorphism).** A ring isomorphism is a bijective homomorphism.

Informally speaking, a ring isomorphism  $f: R \to S$  is a mapping between rings that are structurally the same such that any element of R has exactly one image in S.

Note that  $(\mathbb{Z}_n, +, \cdot)$  is a finite field if and only if n is a prime number. Furthermore, if F is a finite field, then F contains  $p^m$  elements for some prime p and integer  $m \geq 1$ . For every prime power order  $p^m$ , there is a unique finite field of order  $p^m$ . This field is denoted by  $\mathbb{F}_{p^m}$  or  $GF(p^m)$ . The finite field  $\mathbb{F}_{p^m}$  is unique up to an isomorphism.

# 2.4 Number Theoretic Assumptions

This section presents a collection of number theoretic assumptions. The cryptographic security of our future constructions falls or stands on these assumptions [22, 95].

In the definitions that follow  $\langle G, n, g \rangle \leftarrow \mathcal{G}\left(1^{\lambda}\right)$  is defined as the setup algorithm that generates a group G of order n and a generator  $g \in G$  on input of the security parameter  $\lambda$ .

**Definition 2.27 (DL).** The discrete logarithm problem is defined as follows. Given a finite cyclic group G of order n, a generator  $g \in G$  and an element  $a \in G$ , find the integer  $x, 0 \le x \le n-1$  such that  $g^x = a$ .

The discrete logarithm assumption holds if for any algorithm  $\mathcal{A}(g, g^x)$  trying to solve the DL problem there exists a negligible function  $\mu(\lambda)$  such that

$$\Pr\left[\mathcal{A}\left(g,g^{x}\right)=a\mid\left\langle G,n,g\right\rangle \leftarrow\mathcal{G}\left(1^{\lambda}\right)\right]\leq\mu\left(\lambda\right)$$

where the probability is over the random choice of n, g in G according to the distribution induced by  $\mathcal{G}\left(1^{\lambda}\right)$ , the random choice of a in G and the random bits of the algorithm  $\mathcal{A}$ .

**Definition 2.28 (CDH).** The Computational Diffie-Hellman problem is defined as follows. Given a finite cyclic group G of order n, a generator  $g \in G$  and  $g^a, g^b$  with uniformly chosen random independent elements  $a, b \in \{1, \ldots, |G|\}$ , find the value  $g^{ab}$ .

The Computational Diffie-Hellman assumption holds if for any algorithm  $\mathcal{A}\left(g,g^{a},g^{b}\right)$  trying to solve the CDH problem there exists a negligible function  $\mu\left(\lambda\right)$  such that

$$\Pr\left[\mathcal{A}\left(g,g^{a},g^{b}\right)=g^{ab}\mid\left\langle G,n,g\right\rangle \leftarrow\mathcal{G}\left(1^{\lambda}\right)\right]\leq\mu\left(\lambda\right)$$

where the probability is over the random choice of n, g in G according to the distribution induced by  $\mathcal{G}\left(1^{\lambda}\right)$ , the random choice of a, b in  $\{1, \ldots, |G|\}$  and the random bits of the algorithm  $\mathcal{A}$ .

**Definition 2.29 (DDH).** The *Decisional Diffie-Hellman problem* is defined as follows. Given a finite cyclic group G of order n, a generator  $g \in G$  and  $g^a, g^b, g^{ab}, g^c$  with uniformly chosen random independent elements  $a, b, c \in \{1, \ldots, |G|\}$ , distinguish  $\langle g, g^a, g^b, g^{ab} \rangle$  from  $\langle g, g^a, g^b, g^c \rangle$ .

Define  $\mathcal{A}(x)$  as an algorithm returning true if  $x = \langle g, g^a, g^b, g^{ab} \rangle$  and false if  $x = \langle g, g^a, g^b, g^c \rangle$  for  $c \neq ab$ . The *Decisional Diffie-Hellman assumption* holds if for any such algorithm  $\mathcal{A}(x)$  there exists a negligible function  $\mu(k)$  such that

$$\left|\Pr\left[\mathcal{A}\left(\left\langle g,g^{a},g^{b},g^{ab}\right\rangle\right)=\mathtt{true}\right]-\Pr\left[\mathcal{A}\left(\left\langle g,g^{a},g^{b},g^{c}\right\rangle\right)=\mathtt{true}\right]\right|\leq\mu\left(\lambda\right)$$

where the probability is over the random choice of n, g in G according to the distribution induced by  $\mathcal{G}\left(1^{\lambda}\right)$ , the random choice of a, b, c in  $\{1, \ldots, |G|\}$  and the random bits of the algorithm  $\mathcal{A}$ .

Definition 2.29 states that  $\langle g, g^a, g^b, g^{ab} \rangle$  and  $\langle g, g^a, g^b, g^c \rangle$  are computationally indistinguishable.

Someone with the ability to calculate discrete logarithms could trivially solve the CDH problem. That is, if a and b can be derived from  $\langle g^a, g^b \rangle$ , it becomes easy to calculate  $g^{ab}$ . Therefore, a group structure where the CDH assumption holds, immediately implies a group where the DL assumption is valid as well. There is no mathematical proof that supports the inverse relation. Thus, a group where the DL problem is hard not necessarily implies the CDH problem. For specific group structures the CDH assumption immediately follows from the DL assumption as shown in [92, 93]. However, their proof can not be generalised to just any group.

There exists a similar relation between the CDH and the DDH problem. If a powerful algorithm could solve CDH, i.e. derive  $g^{ab}$  from  $\langle g, g^a, g^b \rangle$  alone, it would become trivial to distinguish  $\langle g, g^a, g^b, g^{ab} \rangle$  from  $\langle g, g^a, g^b, g^c \rangle$ . Again, an inverse relation can not be proven. As a matter of fact, concrete examples of groups exist where CDH is hard although DDH is not.

Therefore, the relation between DL, CDH and DDH is often written as follows

$$DDH \Rightarrow CDH \Rightarrow DL$$

The  $\Rightarrow$  notation is then translated into "immediately implies". In a group where DDH is hard both CDH and DL will be hard. Contrarily, there exist group structures where the CDH and the DL assumption hold while DDH can be found easily. Such groups are called *gap Diffie-Hellman groups* or simply *gap groups*.

**Definition 2.30 (GDH).** The *Gap Diffie-Hellman problem* is defined as follows. Solve the CDH problem with the help of a DDH oracle. Given a finite cyclic group G of order n, a generator  $g \in G$  and  $g^a, g^b$  with uniformly chosen random independent elements  $a, b \in \{1, \ldots, |G|\}$ , find the value  $g^{ab}$  with the help of a DDH oracle  $\mathcal{DDH}\left(g, g^a, g^b, z\right)$ . Where the DDH oracle  $\mathcal{DDH}\left(g, g^a, g^b, z\right)$  is defined to return true if  $z = g^{ab}$  and false if  $z \neq g^{ab}$ .

The Gap Diffie-Hellman assumption holds if for any algorithm  $\mathcal{A}\left(g,g^{a},g^{b}\right)$  trying to solve the CDH problem with the help of a DDH oracle  $\mathcal{DDH}\left(g,g^{a},g^{b},z\right)$  there exists a negligible function  $\mu\left(k\right)$  such that

$$\Pr\left[\mathcal{A}\left(g,g^{a},g^{b}\right)=g^{ab}\mid\left\langle G,n,g\right\rangle \leftarrow\mathcal{G}\left(1^{\lambda}\right)\right]\leq\mu\left(\lambda\right)$$

where the probability is over the random choice of n, g in G according to the distribution induced by  $\mathcal{G}\left(1^{\lambda}\right)$ , the random choice of a, b in  $\{1, \ldots, |G|\}$  and the random bits of the algorithm  $\mathcal{A}$ .

# 2.5 Bilinear Maps

Joux and Nguyen [77] show that bilinear pairings are an example of a practical usable DDH oracle.

#### 2.5.1 Definition

**Definition 2.31 (Admissible bilinear map).** Let  $G_1, G_2$  and  $G_T$  be three groups of order q for some large prime q. An admissible bilinear map  $e: G_1 \times G_2 \to G_T$  is defined as a map from the gap groups  $G_1$  and  $G_2$  to the target group  $G_T$  that satisfies the following properties:

- 1. Bilinearity  $\forall a, b \in \mathbb{Z}, \forall P \in G_1, \forall Q \in G_2 : e(aP, bQ) = e(P, Q)^{ab}$
- 2. Non-degeneracy If P is a generator of  $G_1$  and Q is a generator of  $G_2$ , e(P,Q) is a generator of  $G_T$
- 3. Computability There is an efficient algorithm to compute  $e\left(P,Q\right)$  for all  $P\in G_1$  and  $Q\in G_2$

In literature, authors distinguish two types of admissible bilinear maps: symmetric and asymmetric bilinear maps. A symmetric bilinear map is an admissible bilinear map where the gap groups are the same, i.e.  $G_1 = G_2$ . Definition 2.31 describes the more general asymmetric bilinear map where  $G_1 \neq G_2$ . Schemes relying on symmetric bilinear maps are easier to construct information theoretic security proofs although asymmetric bilinear maps are more efficient and suitable for implementation thanks to their flexible embedding degree [26, 117].

In practice, bilinear maps are constructed using pairings. The most popular pairings implementing admissible bilinear maps are the Weil pairing [26] and the Tate

pairing [58]. Both the Tate and the Weil pairing rely on abelian varieties for their implementation.  $G_1$  is mostly an additive elliptic curve group,  $G_2$  a multiplicative elliptic curve group while  $G_T$  is a finite field. For instance, the asymmetric Weil pairing is often implemented with a cyclic subgroup of  $E(\mathbb{F}_p)$  of order q for  $G_2$  and a different cyclic subgroup of  $E(\mathbb{F}_{p^6})$  of the same order q for  $G_1$  where  $E(\mathbb{F}_{p^6})$  denotes the group of points on an elliptic curve E over the finite field  $\mathbb{F}_{p^6}$ . The interested reader is referred to [1] for more information concerning elliptic curves and their use in pairing based cryptography. Details on Elliptic Curve Cryptography fall out of the scope of this thesis as it suffices to make abstraction of these concepts for the remainder of the text.

The only correct notation would be to use additive notation in  $G_1$  and multiplicative notation in  $G_2$  to denote operations in the gap groups. However, authors in literature often use one notation in both gap groups to emphasise the symmetric properties of bilinear maps. In the remainder of this text the additive notation is used for operations in both  $G_1$  and  $G_2$ .

Recent research [6, 11, 76] has shown that the discrete logarithm problem is easier in the symmetric setting because symmetric pairings rely on more structured supersingular (hyper)elliptic curves. Therefore, it is discouraged to rely on symmetric pairings in practical implementations [117].

### 2.5.2 Bilinear Diffie-Hellman Assumption

A bilinear map allows to solve the Decisional Diffie-Hellman problem in  $G_1$  and  $G_2$ . The DDH problem in  $G_1$  consists of distinguishing  $\langle P, aP, bP, abP \rangle$  from  $\langle P, aP, bP, cP \rangle$  where  $P \in G_1$ , P is a generator of  $G_1$  and a, b, c chosen uniformly random in  $\{1, \ldots, |G_1|\}$ . Given a symmetric bilinear map  $e: G_1 \times G_1 \to G_T$  a solution to this problem is found by relying on the bilinearity of the pairing as follows:

$$e(aP, bP) = e(P, P)^{ab} \stackrel{?}{=} e(P, cP) = e(P, P)^{c}$$

Such that the second equality will hold only if ab = c. A similar statement can be made concerning  $G_2$  with the help of the map  $e: G_2 \times G_2 \to G_T$ . Consequently,  $G_1$  and  $G_2$  are both GDH groups. Since DDH (Definition 2.29) is a stronger assumption than CDH (Definition 2.28), CDH can still be hard in GDH groups [26].

Since DDH in the Gap groups  $G_1$  and  $G_2$  is easy, DDH can not serve as a basis for cryptographic systems in these groups. Therefore, an alternative to the CDH problem is defined called the Bilinear Diffie-Hellman problem.

In the definition that follows  $\mathcal{G}\left(1^{\lambda}\right)$  is defined to be a BDH parameter generator as in [26], i.e.  $\mathcal{G}$  takes as input a security parameter  $\lambda$ ,  $\mathcal{G}$  runs in polynomial time in  $\lambda$  and  $\mathcal{G}$  outputs a prime number q, the description of two groups  $G_1, G_2$  of order q and the description of an admissible bilinear map  $e: G_1 \times G_2 \to G_T$ .

**Definition 2.32 (BDH).** The *Bilinear Diffie-Hellman problem* is defined as follows. Given any admissible bilinear pairing  $e: G_1 \times G_2 \to G_T$  with random  $P, aP, bP \in G_1$  and random  $Q, aQ, bQ \in G_2$  with uniformly chosen random independent elements  $a, b, c \in \{1, \ldots, |G|\}$ , find  $e(P, Q)^{abc}$ 

The Bilinear Diffie-Hellman assumption holds if for any algorithm  $\mathcal{A}(P,aP,bP,Q,aQ,bQ)$  trying to solve the BDH problem there exists a negligible function  $\mu(\lambda)$  such that

$$\Pr\left[\mathcal{A}\left(P,aP,bP,Q,aQ,bQ\right)=e\left(P,Q\right)^{abc}\mid\left\langle q,G_{1},G_{2},e\right\rangle\leftarrow\mathcal{G}\left(1^{\lambda}\right)\right]\leq\mu\left(\lambda\right)$$

where the probability is over the random choice of  $q, G_1, G_2, e$  according to the distribution induced by  $\mathcal{G}\left(1^{\lambda}\right)$ , the random choice of a, b in  $\{1, \ldots, |G|\}$  and the random bits of the algorithm  $\mathcal{A}$ .

# 2.6 Cryptographic Definitions

This section defines basic cryptographic notions and the corresponding notation that is applied consistently throughout the remainder of this thesis.

## 2.6.1 Terminology

**Definition 2.33 (Confidentiality).** Confidentiality is the assurance to an entity information is protected from disclosure to unauthorised entities.

**Definition 2.34 (Integrity).** *Integrity* is the assurance to an entity information was not modified by unauthorised entities.

**Definition 2.35 (Authentication).** Authentication is the assurance to an entity that another entity effectively has a claimed identity.

**Definition 2.36 (Authenticity).** Authenticity is the assurance to an entity information comes from the claimed entity.

**Definition 2.37 (Non-repudiation).** *Non-repudiation* is the assurance to an entity of authenticity and integrity of information which undeniably links the originating entity as the source of information.

### 2.6.2 Symmetric Cryptography

Symmetric cryptographic algorithms require a shared secret between different entities to achieve confidentiality. Practically, this translates to the same symmetric key k being used for encryption and decryption.

**Definition 2.38 (Encryption scheme).** An encryption scheme consists of two polynomial time algorithms which achieve confidentiality:

- 1. An encryption algorithm  $c \leftarrow \mathbb{E}_k(m)$  that encodes the plaintext m to a ciphertext c under symmetric key k such that only parties in possession of k can derive m from c.
- 2. A decryption algorithm  $m \leftarrow D_k(c)$  that decodes the ciphertext c back to the plaintext message m on input of the same symmetric key k.

**Definition 2.39 (Authenticated encryption).** An authenticated encryption scheme consists of two polynomial time algorithms which achieve confidentiality and authenticity:

- 1. An encryption algorithm  $\langle c, t \rangle \leftarrow \mathbb{E}_k(m, a)$  that encrypts the plaintext m to a ciphertext c under symmetric key k, thereby generating an authentication tag t that provides integrity and authenticity on both m and authenticated data a.
- 2. A decryption algorithm  $\langle m, t' \rangle \leftarrow D_k(c, a)$  that decrypts the ciphertext c back to the plaintext message m under the same symmetric key k as used for encryption, thereby generating an authentication tag t' that provides integrity and authenticity on both m and authenticated data a.

The difference in notation between an encryption scheme and an authenticated encryption scheme can be derived from the different number of arguments required by their polynomial time algorithms.

### 2.6.3 Asymmetric Cryptography

Asymmetric cryptography assigns a key pair  $\langle sk_A, pk_A \rangle$  to every entity A in the system. The private key is denoted  $sk_A$  and only known by A, while  $pk_A$  represents the public key which is made available to every entity in the system. A private key  $sk_A$  is mathematically related to the corresponding public key  $pk_A$  since  $pk_A$  is derived from  $sk_A$  by applying a one-way function. The one-way property of the function implies that there exists no polynomial time algorithm to derive  $sk_A$  from  $pk_A$ , e.g. in the ElGamal encryption scheme [59] the public key is calculated as  $pk = g^{sk}$  in a group  $\mathbb{Z}_p$  for some large prime p. As long as the DL assumption from Definition 2.27 holds it is infeasible to derive sk from pk.

The concept of each entity possessing an asymmetric key pair enables secure communication between entities who have never met by encrypting under the correct public keys.

**Definition 2.40 (PKI).** A public key infrastructure (PKI) is an infrastructure authenticating key pairs  $\langle sk_A, pk_A \rangle$  effectively belong to the claimed user A.

**Definition 2.41 (Digital signature).** A digital signature  $S_A(m)$  achieves non-repudiation on a message m from a known sender A. m is signed with A's private signing key  $sk_A$  and verified with A's public verifying key  $vk_A$ .

**Definition 2.42 (Commitment scheme).** A commitment scheme allows an entity to commit to a chosen value while keeping it hidden to others, with the ability to reveal the committed value later [63]. After revealing the committed value, any other entity can verify the value has not changed between commitment and revelation. This is achieved by two polynomial time algorithms:

- 1. CS.Commit(m,r): Returns a commitment  $c_{m,r}$  to a message m and a random binary sequence r.
- 2. CS. Verify  $(c_{m,r}, m', r')$ : On input of a commitment  $c_{m,r}$ , a message m' and a random binary sequence r' it returns true if  $c_{m,r} \leftarrow \text{CS.Commit}(params, m, r)$  with m = m' and r = r' and false otherwise.

For a more elaborate discussion on commitment schemes the reader is referred to the original paper from Brassard et al. [31].

#### 2.6.4 Hash Functions

The concept of hash functions is required to further explain random oracles. Random oracles are a useful assumption when proving the security of certain cryptographic algorithms.

#### Definition

A hash function is a computationally efficient deterministic function mapping binary strings of arbitrary length to binary strings of some fixed length, called hash-values. Cryptographic hash functions have the following desirable properties:

- Computability: Given a binary string m, the hash value h can be calculated efficiently h = H(m)
- Pre-image resistance: Given a hash value h, it is infeasible to calculate a corresponding binary string m such that h = H(m)
- Second pre-image resistance: Given a binary string  $m_1$ , it is hard to find a different binary string  $m_2$  such that  $H(m_1) = H(m_2)$
- Strong collision resistance: Given a hash function  $H(\cdot)$ , it is hard to find two different binary strings  $m_1$  and  $m_2$  such that  $H(m_1) = H(m_2)$

Hash functions are useful for a wide variety of practical applications. For instance, hash functions serve as one way functions in password databases to relax sensitivity of the stored content. In addition, hash functions represent a valuable tool for data authentication and integrity checking. Another use of hash functions is in protocols involving a priori commitments. If the reader is new to the concept of hash functions, he is referred to [95] for an in depth discussion on the topic.

#### Random Oracles

A random oracle is a theoretical black box that returns for each unique query a uniformly random chosen result from its output domain. A random oracle is deterministic, i.e. given a particular input it will always produce the same output.

In a perfect world hash functions can be considered random oracles. That is, if hash functions were perfect, their output would look like perfect random bit sequences. Therefore, hash functions are often considered random oracles in security proofs. Such security proofs are said to be proven secure in the random oracle model. Proofs in the random oracle model first show that an algorithm is secure if a theoretical random oracle would be used. A next step of these security proofs is replacing the random oracle accesses by the computation of an appropriately chosen (hash) function h [17]. Algorithms not requiring such a construction in their security proof are said to be proven secure in the standard model.

Although theoretical definitions of random oracles and hash functions are quite similar, some practical implementations of hash functions do not behave like random oracles. Canetti at al. [33] show that there exist signature and encryption schemes that are secure in the random oracle model, although any implementation of the random oracle results in insecure schemes [33]. Coron et al. [41] counter these findings with indifferentiability, i.e. if a hash function is indifferentiable from a random oracle the random oracle can be replaced by the hash function while maintaining a valid security proof. Therefore, it is a common belief that proofs in the random oracle model provide some evidence that a system is secure. Although research results from Coron et al. are debated by Fleishmann et al. [55] and Ristenpart et al. [103]. In fact, indifferentiability from random oracles certainly contributed to the victory of Keccak in the NIST hash function competition for a new SHA-3 hashing standard as all final round hashing algorithms supported this property [14].

# 2.7 Summary

This chapter overviewed the fundamental mathematics required to understand the more advanced concepts described in Chapter 3.

The first part of this chapter introduced basic on complexity theory, probability theory and algebraic structures. These basic notions were used further on to define number theoretic hard problems that serve as a basis for security. From the discrete logarithm assumption, several variants of the Diffie-Hellman problem were introduced, eventually leading to the Gap Diffie-Hellman assumption. The notion of the Gap Diffie-Hellman assumption allowed to uncover gap groups and their use in admissible bilinear maps. The Bilinear Diffie-Hellman assumption was defined as a computationally infeasible problem for the construction of cryptographic protocols relying on bilinear maps. Finally, this chapter concluded with differences between security under random oracle assumptions and security in the standard model.

3

# Cryptographic Building Blocks

This chapter overviews the cryptographic building blocks used to design the encryption mechanism for online social networks proposed in this thesis.

The structure of this chapter is the following. An introduction is given to public key infrastructures and their drawbacks. Then, *Identity-Based Encryption* (IBE) is overviewed as an alternative to existing public key infrastructures along with its drawbacks and advantages, the different security definitions and the evolution of IBE in literature. This is followed by an elaborate discussion on *Broadcast Encryption* (BE) and secret sharing. Finally, *Distributed Key Generation* (DKG) is described as a possible solution to the inherent key escrow problem of IBE.

# 3.1 Public Key Infrastructures

Asymmetric cryptography assigns users a key pair  $\langle sk_i, pk_i \rangle$  to allow secure communication between parties who never met. However, a trusted party is required which verifies the binding of an identity to a public key to prevent impersonation. The infrastructure authenticating all public key values is called the *Public Key Infrastructure* (PKI) as defined by Definition 2.40. However, PKI systems only shift the problem from trusting the users to trusting their keys. For example, if Eve could make the PKI system believe that her own public key  $pk_{Eve}$  actually represents the public key of Alice  $pk_{Alice}$ , Eve would be able to read all Alice's confidential communication as she obviously has the private key  $sk_{Eve}$  corresponding to  $pk_{Eve}$ . Therefore, it is important that public key systems rely on an architecture that authenticates whether key pairs belong to the claimed owner. In practice this is mostly achieved with the help of certification authorities or a web of trust.

## 3.1.1 Certification Authorities

In a traditional PKI system, all entities in the system trust a central party called the *Certification Authority* (CA). It is the CA that guarantees public keys belong to the claimed owner. CA infrastructures are standardised in X.509 [40].

Suppose Alice wants to start using a key pair  $\langle pk_A, sk_A \rangle$ , she has to authenticate herself with the CA by following correctly a protocol that confirms Alice's identity,

usually over offline channels. Once Alice is authenticated with the CA, Alice sends the public key  $pk_A$  to the CA along with a proof showing that Alice also owns the corresponding private key  $sk_A$ . This "proof of correct possession" often takes the form of a signature  $S_{sk_A}(pk_A)$  generated by the private key  $sk_A$  on the public key  $pk_A$ .

Once the CA is convinced of the authenticity of Alice's public key, it distributes a certificate approving that  $pk_A$  effectively belongs to Alice. To avoid forged certificates, the CA signs Alice's certificate with its private key  $sk_{CA}$ . Anyone doubting the authenticity of the public key  $pk_A$  can get convinced  $pk_A$  effectively belongs to Alice by checking the signature of the CA with the CA's public key  $pk_{CA}$ .

In practice, CAs often approve the trustworthiness of other CAs by issuing certificates on their signing keys. In this way, often highly complex hierarchical architectures are achieved that boil down to the trust in one signing key of the highest authority. This puts heavy requirements on the CA's infrastructure as a compromised CA signing key can break the system completely. Indeed, a compromised signing key would allow to sign certificates of unauthenticated public keys or even certificates of public keys that belong to malicious entities.

If an entity's private key is lost or leaked to a third party, it can be revoked by the CA. CAs achieve this by periodic publication of *revocation lists*. These revocation lists contain all compromised public keys. Consequently, users relying on a PKI should always verify these continuously growing lists before trusting a keypair. Thereby, revocation lists not only make the system less transparent, they also impose high demands on the infrastructure of entities relying on the PKI.

Suppose Alice's private key gets compromised due to Eve stealing her hard drive. Alice authenticates with the CA and sends a complaint stating her private key is no longer confidential. In return, the CA puts Alice's public key on the revocation list. The next time Bob wants to send a message to Alice, he first verifies the revocation list to conclude the last version of Alice's public key is no longer in use. However, the revocation list of the CA continuously grows with every additional hard drive Eve can steal thereby increasing the required time to download and verify the revocation list.

To partially get around the issue of revocation lists, certificates contain an expiration date. After expiration, a certificate should no longer be trusted. However, this requires keypair owners to contact CAs more frequently to sign new certificates each time the previous one has expired. Clearly, this puts a high computational demand on the authentication procedure of the CAs as well.

## 3.1.2 OpenPGP and Web of Trust

An alternative to the traditional PKI setting relying on CAs is a web of trust. In a web of trust as originally proposed by Zimmerman, any entity can rate the trustworthiness of a public key. For example, if Bob receives Alice's public key personally during a date, the public key can be considered more trustworthy than when Bob receives Alice's key via e-mail. Web of trust systems allow users to vet for the authenticity other users' keys in the system. A standardised web of trust system is OpenPGP [32].

The major advantage of a web of trust is that there no longer needs to be a CA with highly secure infrastructure as the publication of certificates now becomes a shared responsibility.

However, web of trust infrastructures present some issues, such as usability [114]. In addition, users are now required to judge for themselves whether they can trust a public key or not. This gives more responsibility to users than most of them can handle without proper knowledge of the consequences to their actions.

# 3.2 Identity-Based Encryption

The concept of identity-based cryptography was proposed by Shamir [109] in 1984. In identity-based cryptography any string can be a valid public key for encryption or signature schemes thereby eliminating the need for digital certificates. Identity-based cryptography proves to be particularly elegant if the public key is related to an attribute that uniquely identifies the identity of the user like an e-mail address, an IP address or a telephone number. Consequently, identity-based cryptography reduces system complexity and the cost for establishing and managing the PKI [8].

#### 3.2.1 Definition

A generic *Identity-Based Encryption* (IBE) scheme is composed of four probabilistic polynomial time algorithms [26]:

- **IBE.Setup**(1<sup> $\lambda$ </sup>) On input of a security parameter  $\lambda$ , outputs a master secret  $sk_{msk}$  and public parameters params.
- **IBE.Extract**( $params, sk_{msk}, id$ ): Takes public parameters params, the master secret  $sk_{msk}$ , and an id as input and returns the private key  $s_{id}$  corresponding to the identity id.
- **IBE.Encrypt**(params, id, m): Returns the encryption c of the plaintext message m on the input of the public parameters params, the id, and the arbitrary length message m.
- IBE.Decrypt( $s_{id}, c$ ): Decrypts the ciphertext c = IBE.Encrypt(params, id, m) back to the plaintext message m on input of the private key  $s_{id}$  corresponding to the receiving identity id.

Figure 3.1 illustrates the IBE generic algorithms. A trusted *Public Key Generator* (PKG) generates a master private key  $sk_{msk}$  and public parameters params on input of the security parameter  $\lambda$ . Next, the PKG publishes the public parameters params while storing  $sk_{msk}$  preferably in encrypted format on a local disk. If Alice wants to send a confidential plaintext message m to Bob, it suffices for her to know the public parameters params and the id  $id_{Bob}$ , uniquely identifying Bob. Then, Alice encrypts the message to a ciphertext c that is sent over an insecure channel to Bob. On receipt of the ciphertext, Bob authenticates to the PKG over a secure channel

1.  $\langle sk_{msk}, params \rangle \leftarrow \text{IBE.Setup}(1^{\lambda})$ 2. publish params5.  $s_{\text{id}_{Bob}} \leftarrow \text{IBE.Extract}(params, sk_{msk}, \text{id}_{Bob})$ PKG

4. Bob authenticates as  $\text{id}_{Bob}$ c

Alice

Bob

3.  $c \leftarrow \text{IBE.Encrypt}(params, \text{id}_{Bob}, m)$ 6.  $m \leftarrow \text{IBE.Decrypt}(s_{\text{id}_{Bob}}, \text{id}_{Bob}, c)$ 

Figure 3.1: Generic identity-based encryption scheme. The blue arrow denotes an insecure channel that can be eavesdropped.

to request his private key  $sk_{id_{Bob}}$ . Subsequently, the PKG generates the private key  $sk_{id_{Bob}}$  corresponding to Bob's identity  $id_{Bob}$  on input of the master secret key  $sk_{msk}$ , Bob's id  $id_{Bob}$  and public parameters params. Subsequently, the PKG sends  $sk_{id_{Bob}}$  over the same secure channel. Bob has now all the required information to decrypt the ciphertext c to its original plaintext message m.

#### 3.2.2 Comparison with PKI Schemes

Now we turn to overview the main advantages and disadvantages of generic IBE schemes when compared to more traditional PKI systems.

#### Disadvantages

The disadvantages of IBE are the following when compared to PKI.

SINGLE POINT OF FAILURE: The PKG generates every private key  $sk_{id}$  in the system thereby creating a single point of failure. If a PKG disconnects due to an excessive amount of extraction requests, new users can no longer receive their private keys. However, users already owning a secret key can continue decrypting ciphertexts since this requires no additional communication with the PKG. A PKI system often consists of a hierarchy of CAs. Consequently, an offline CA only takes down a specific part of the PKI. However, an offline CA can no longer issue certificates either.

KEY ESCROW: The PKG is required to be trusted since it learns  $sk_{id}$  for every entity in the system. A malicious PKG server could use this information to start eavesdropping on the insecure channel between Alice and Bob (the blue arrow in Figure 3.1) while decrypting all ciphertexts that are being sent over. The undesired property that private keys have to be shared with a trusted third party is often called

key escrow in literature [5]. Since traditional PKIs only authenticate key pairs, key escrow is not an issue.

REVOCATION OF PUBLIC KEYS: Generic IBE schemes do not support revocation of public keys. However, Bob's private key  $sk_{id_{Bob}}$  can still get compromised if he is careless with its storage. In fact, the research community has focused on the revocation of IBE keys extensively [21, 25, 72, 86]. Key revocation often requires additional infrastructure that complicates the elegancy of a generic IBE scheme. The major drawback of revoking Bobs key is that Bob can no longer receive encrypted messages because his public key is part of his identity. Therefore, a pragmatic solution to this issue could be to append expiration dates to public keys. Consequently, public keys will only be valid for a limited amount of time thereby restricting the damage that can be done with a compromised private key [26]. Conversely, traditional PKIs publish revocation lists. Although these revocation list are a burden to the complexity of the PKI's infrastructure, they support a necessary feature for practical key management systems.

#### Advantages

IBE provides the following advantages when compared to PKI.

COMPLEXITY OF THE SYSTEM: Only one PKG suffices to realise the IBE scheme, which relaxes expensive infrastructure requirements on the system. Due to the support of revocation lists and the often hierarchical organisation, PKI systems are complex structures with a high amount of redundancy.

USER FRIENDLINESS: Users without a background on cryptographic primitives no longer have to make conscious decisions on key lengths or the randomness of their keys. In an IBE system a public key is a string available to anyone in the system. This is generally conceived as more transparent to users lacking a background on cryptography. An average user knows what a username or an e-mail address represents and to whom it belongs while an authenticated public key is generally not a familiar concept.

OPT-IN BY DEFAULT: Another useful property of an IBE scheme is that a recipient is not required to actively subscribe to a hierarchy of CAs neither a web of trust before a sender can start sending him messages. In this way, the possibility to send encrypted messages becomes inherently part of any system in which users are assigned unique identifiers. This is particularly useful in systems where the majority of the users has no knowledge about cryptographic primitives. Users do no longer need to generate a key pair neither subscribe to a third party infrastructure. It suffices to recall how their connections can be uniquely identified in the system to learn their public keys.

#### 3.2.3 Security of IBE

IBE schemes follow similar security notions as generic public key systems. Therefore, definitions of security are often subtle as different levels of security can be distinguished. In literature, the security notions mostly considered are *indistinguishability* under chosen plaintext attack (IND-CPA) and indistinguishability under chosen ciphertext attack (IND-CCA). Anonymity of the encryption scheme is an additional property of the scheme that is often desired [16].

For a more in depth discussion on IND-CPA and IND-CCA, the reader is referred to Boneh and Franklin [26], whereas for a more formal description of ciphertext anonymity the reader is referred to Abdalla et al. [4].

#### Indistinguishability Under Chosen Plaintext Attack

Indistinguishability under chosen plaintext attack (IND-CPA) is described by the negligible advantage an adversary has in trying to distinguish which of both given plaintext messages  $m_0$  and  $m_1$  generated a ciphertext c. It captures the notion of semantic security, i.e. any ciphertext c should not give more information about the original plaintext m than any other random binary string of the same length.

IND-CPA is best defined with the help of a game that challenges the adversary. The advantage of the adversary in winning the IND-CPA game illustrated in Game 1, is defined as

$$Adv = |\Pr\left[b = b'\right] - \frac{1}{2}|$$

If the adversary has negligible advantage trying to win the IND-CPA game, the IBE system is said to be IND-CPA secure. More formally, an IBE system is IBE-IND-CPA secure if for every adversary with advantage Adv in winning the IBE-IND-CPA game illustrated in Game 1 there exists a negligible function  $\mu(\lambda)$  such that  $Adv \leq \mu(\lambda)$ .

#### Indistinguishability Under Chosen Ciphertext Attack

Indistinguishability under chosen ciphertext (IND-CCA) is a more demanding level of security. Therefore, an algorithm that is IND-CCA secure is considered more secure than an IND-CPA secure algorithm. IND-CCA security implies that an adversary has no advantage in trying to distinguish which of both given plaintext messages  $m_0$  and  $m_1$  generated a ciphertext c even if the adversary has access to a list of (plaintext, ciphertext)-tuples.

IND-CCA is defined with the help of a game that challenges an adversary similar to the IND-CPA game. Compared to the IND-CPA game, the IND-CCA game contains two additional steps in which the adversary gets access to another oracle. The advantage of the adversary in winning the IND-CCA game illustrated in Game 2, is defined as

$$Adv = |\mathrm{Pr}\left[b = b'\right] - \frac{1}{2}|$$

If the adversary has negligible advantage trying to win the IND-CCA game, the IBE system is said to be IND-CCA secure. More formally, an IBE system is

#### Game 1 Generic IBE-IND-CPA Game [3]

**Goal**: An adversary is challenged by a game to check the IND-CPA security of an IBE scheme.

**Result**: This IBE-IND-CPA Game helps to define the concept of IND-CPA security for IBE schemes.

- 1. The challenger runs  $\langle sk_{msk}, params \rangle \leftarrow \texttt{IBE.Setup}(1^{\lambda})$  and returns params to the adversary.
- 2. The adversary can start querying an oracle  $O_{Extract}(id_i)$  that returns a private key  $sk_{id_i} \leftarrow IBE.Extract(params, sk_{msk}, id)$  corresponding to an adversary defined identity  $id_i$ .
- 3. The adversary picks two equal length plaintext messages  $m_0$  and  $m_1$  and an identity  $id_{encrypt}$ . The adversary honestly passes  $\langle m_0, m_1, id_{encrypt} \rangle$  to the challenger.
- 4. The challenger picks a random bit b and executes  $c \leftarrow \mathtt{IBE.Encrypt}(params, \mathtt{id}_{encrypt}, m_b)$ . The challenger gives c to the adversary.
- 5. The adversary continues querying the oracle  $O_{Extract}(id_i)$  adaptively.
- 6. The adversary outputs a bit b' based on the ciphertext c. If b = b' the adversary wins the game. If  $b \neq b'$  or if the adversary queried the oracle  $O_{Extract}(id_i)$  with  $id_i = id_{encrypt}$  during step 2 or step 5, the adversary loses the game.

IBE-IND-CCA secure if for every adversary with advantage Adv in winning the IBE-IND-CCA game illustrated in Game 2 there exists a negligible function  $\mu(\lambda)$  such that  $Adv \leq \mu(\lambda)$ .

In literature a distinction is often made between a *non-adaptive* case (IND-CCA1) and an *adaptive* case (IND-CCA2) of IND-CCA. In the non-adaptive case, step 6 and 7 from Game 2 are not allowed. More precisely, an IBE scheme that satisfies Game 2 is said to be IND-CCA2 secure.

#### Anonymous Identity-Based Encryption

An IBE scheme is called anonymous (ANO-IBE) when the ciphertext does not leak the identity of the recipient. In the overview illustrated in Figure 3.1, this implies that no eavesdropper on the insecure channel between Alice and Bob could derive that Bob is the recipient based on the information in the ciphertext c [30].

ANO-IBE is defined with the help of a game that challenges an adversary similar to the IND-CPA game. An IBE system is said to be anonymous if the adversary

#### Game 2 Generic IBE-IND-CCA Game [3]

**Goal**: An adversary is challenged by a game to check the IND-CCA security of an IBE scheme.

**Result**: This IBE-IND-CCA Game helps to define the concept of IND-CPA security for IBE schemes.

- 1. The challenger runs  $\langle sk_{msk}, params \rangle \leftarrow \mathtt{IBE.Setup}(1^{\lambda})$  and returns params to the adversary.
- 2. The adversary can start querying an oracle  $O_{Extract}(id_i)$  that returns a private key  $sk_{id_i} \leftarrow IBE.Extract(params, sk_{msk}, id)$  corresponding to an adversary defined identity  $id_i$ .
- 3. The adversary can start querying another oracle  $O_{Decrypt}(sk_{id_i}, c_j)$  that returns a plaintext  $m_j \leftarrow \mathtt{IBE.Decrypt}(sk_{id_i}, c_j)$  corresponding to an adversary defined ciphertext  $c_j$  and identity  $\mathtt{id}_i$ .
- 4. The adversary picks two equal length plaintext messages  $m_0$  and  $m_1$  and an identity  $id_{encrypt}$ . The adversary honestly passes  $\langle m_0, m_1, id_{encrypt} \rangle$  to the challenger.
- 5. The challenger picks a random bit b and executes  $c \leftarrow \mathtt{IBE.Encrypt}(params, \mathtt{id}, m_b)$ . The challenger gives c to the adversary.
- 6. The adversary continues querying the oracle  $O_{Extract}$  (id<sub>i</sub>) adaptively.
- 7. The adversary continues querying the oracle  $O_{Decrypt}(sk_{id_i}, c_j)$  adaptively.
- 8. The adversary outputs a bit b' based on the ciphertext c. If b = b' the adversary wins the game. Otherwise, the adversary loses the game. If the adversary queried the oracle  $O_{Extract}(id_i)$  with  $id_i = id_{encrypt}$  during step 2 or step 6 or if the adversary queried the oracle  $O_{Decrypt}(sk_{id_i}, c_j)$  with  $c_j = c$  during step 3 or step 7, the adversary loses the game as well.

has negligible advantage trying to win the ANO-IBE game in Game 3. Again, the advantage of the adversary in winning the IND-CCA game illustrated in Game 2, is defined as

$$Adv = |\Pr\left[b = b'\right] - \frac{1}{2}|$$

More formally, an IBE system is ANO-IBE secure if for every adversary with advantage Adv in winning the ANO-IBE game illustrated in Game 3 there exists a negligible function  $\mu(\lambda)$  such that  $Adv \leq \mu(\lambda)$ .

Gentry [61] presents the first scheme which combines the notions of IND-CPA and IND-CCA with ANO-IBE. Therefore, a system is then said to be IND-ANO-CPA secure or IND-ANO-CCA secure if it satisfies a modified version of the game in Game 3. For a more detailed discussion on the topic the reader is referred to the original paper [61].

#### Game 3 Generic ANO-IBE Game [3]

**Goal**: An adversary is challenged by a game to check the ANO-IBE security of an IBE scheme.

**Result**: This ANO-IBE Game helps to define the concept of ANO-IBE security for IBE schemes.

- 1. The challenger runs  $\langle sk_{msk}, params \rangle \leftarrow \mathtt{IBE.Setup}(1^{\lambda})$  and returns params to the adversary.
- 2. The adversary can start querying an oracle  $O_{Extract}(id_i)$  that returns a private key  $sk_{id_i} \leftarrow IBE.Extract(params, sk_{msk}, id_i)$  corresponding to an adversary defined identity  $id_i$ .
- 3. The adversary picks a plaintext message m and an identity  $id_{encrypt}$ . The adversary honestly passes  $\langle m, id_{encrypt} \rangle$  to the challenger.
- 4. The challenger picks a random bit b and computes c ← IBE.Encrypt(params, id<sub>encrypt</sub>, m) if b = 0. If b = 1, the challenger computes c ← IBE.Encrypt(params, id<sub>encrypt</sub>, r) where r is a random bit sequence with the same length as the message m. The challenger gives c to the adversary.
- 5. The adversary continues querying the oracle  $O_{Extract}(id_i)$  adaptively.
- 6. The adversary outputs a bit b' based on the ciphertext c. If b = b' the adversary wins the game. If  $b \neq b'$  or if the adversary queried the oracle  $O_{Extract}(id_i)$  with  $id_i = id_{encrypt}$  during step 2 or step 5, the adversary loses the game.

#### 3.2.4 Overview

Although Shamir [109] easily constructed an identity-based signature scheme based on RSA in 1984, the practical use of IBE remained an open problem until the introduction of bilinear maps. Boneh and Franklin [26] proposed the first practically usable IBE scheme based on the Weil pairing, however, the security proof still relies on the random oracle assumption. At the same time, Sakai and Kasahara [101] proposed a different IBE scheme independently from Boneh and Franklin. The scheme from Sakai and Kasahara initially received less attention, because the original presentation is in Japanese and lacking a security proof. Subsequently, Sakai and Kasahara [106] proposed an extended version of their original scheme which is proven IND-CCA secure in the random oracle model by Chen et al. [37]

Canetti et al. [34] introduced the first secure IBE scheme without relying on the random oracle model. Nevertheless, the attacker model in [34] requires the adversary to declare upfront which identity id is targeted during step 5 of the CCA Game (Algorithm 2) and step 4 of the CPA Game. Therefore, the scheme by Boneh and Franklin [26] is considered more secure as attackers can adaptively choose the targeted identity. Later, Boneh and Boyen [23] presented a variant to [34] which also realises only selective ID security.

Waters [112] is the first to present a scheme that is IND-CCA secure in the standard model. Drawback of the scheme from Waters [112] is that it requires large public parameters. Gentry [61] proposes a more efficient alternative to this scheme in the standard model while achieving shorter public parameters. However, the scheme from Gentry relies on a complicated hardness assumption called q-BDHE. It is only after the introduction of the Dual System paradigm by Waters [113] in 2009 that IND-CCA security can be achieved in the standard model based on reasonable assumptions. De Caro et al. [36] are the first to define an IND-ANO-CCA secure IBE scheme on the Dual System construction of Waters [113].

Although all these references contributed to the evolution of IBE, not all of these schemes are generally ANO-IBE. The IBE scheme from Boneh and Franklin [26] is IND-ANO-CCA secure since IBE systems in the random oracle model are ANO-IBE. In the standard model, it appeared to be harder to construct ANO-IBE schemes at first sight, e.g. it can be proven that the scheme from Boneh and Boyen [23] is not anonymous in its original form. The scheme from Gentry [61] was the first anonymous IBE scheme in the standard model. Boyen and Waters [30] published almost synchronously another IBE scheme in the standard model that is also IND-ANO-CCA secure. In 2010, Ducas [48] showed that even schemes that were first considered not anonymous like the one from Boneh and Boyen [23] but also [24, 112] can be proven anonymous when relying on asymmetric pairings thereby making anonymity a more common property in IBE schemes.

#### 3.2.5 Most Attractive IBE Schemes

In the standard model mainly the anonymous IBE constructions from Gentry [61] and De Caro et al. [36] have the most satisfying properties. However, IBE constructions in

the standard model often come at the cost of higher computational requirements [29]. Certainly the scheme from De Caro demands a higher amount of computational resources since it relies on composite order groups. Although methods [56, 83] have been developed to convert IBE schemes from composite order groups to single order prime groups, these methods do not apply to the scheme from De Caro et al. [82]

From all schemes discussed in Section 3.2.4 the ones initially developed by Boneh and Franklin [26] and Sakai and Kasahara [106] are the most attractive ones in the random oracle model due to properties of anonymity and non-selective security. Consequently, both schemes have found description in an informational RFC document. Sakai and Kasahara IBE is described in RFC 6508 [69] and RFC 6509 [68]. Boneh and Franklin IBE can be found in RFC 5409 [89].

The ANO-IND-CCA secure scheme from Boneh an Franklin [26] is included in Algorithm 4 since it is valuable for the remainder of the text.

### 3.3 Broadcast Encryption

Another relevant aspect of encryption in OSNs is broadcasting one encrypted ciphertext to multiple users. To this means,  $Broadcast\ Encryption\ (BE)$  was introduced by Fiat and Naor [53], as a public-key generalisation to a multi user setting. In particular, a BE scheme allows a user to encrypt a plaintext message m to a subset  $\mathcal{S}$  of users in a public key system, such that, only users in the set  $\mathcal{S}$  are able to decrypt the resulting ciphertext c. The computational overhead of a BE is generally bounded by the ciphertext and the number of recipients.

#### 3.3.1 Definition

A generic Broadcast Encryption (BE) scheme is composed of four probabilistic polynomial time algorithms:

- **BE.Setup**( $1^{\lambda}$ ): On input of a security parameter  $\lambda$ , generates the public parameters params of the system.
- **BE.KeyGen**(params): Returns the public and private key ( $pk_i, sk_i$ ) for each user i while taking the public parameters params into account.
- **BE.Encrypt** (m, S): Takes a set of public key values  $S = \{pk_i \dots pk_{|S|}\}$  corresponding to users i in the system along with a plaintext message m to generate a corresponding ciphertext c.
- **BE.Decrypt**( $c, sk_i$ ): Reconstructs m from c using the private key  $sk_i$  if the corresponding public key  $pk_i \in \mathcal{S}$ . Otherwise, return  $\perp$ .

Note that this definition is stated generically enough to allow all kinds of public keys to be used. Consequently, not only traditional PKIs can benefit from BE schemes, but also IBE schemes in which a public identifier  $id_i$  serves as a public key  $pk_i$ .

### Algorithm 4 IND-ANO-CCA Boneh and Franklin IBE [26]

Goal: Alice wants to send an IBE encrypted message to Bob.

**Result**: Alice sends an IBE encrypted ciphertext c that is successfully decrypted by Bob.

- 1. Setup( $1^{\lambda}$ ):
  - a) Execute setup algorithm  $\langle q, G_1, G_2, e : G_1 \times G_2 \to G_T, P \in G_1 \rangle \leftarrow \mathcal{G}\left(1^{\lambda}\right)$  to generate the parameters
    - i. A large prime q
    - ii. Gap groups  $G_1$  and  $G_2$  of order q
    - iii. An admissible bilinear map  $e: G_1 \times G_2 \to G_T$
    - iv. A random generator  $P \in G_1$
  - b) Choose a uniformly random  $sk_{msk} \in \mathbb{Z}_q^*$  and compute  $P_{pub} = sk_{msk}P$
  - c) Choose cryptographic hash functions
    - i.  $H_1: \{0,1\}^* \to G_1$
    - ii.  $H_2: G_2 \to \{0,1\}^l$
    - iii.  $H_3: \{0,1\}^l \to (0,1)^l$
- 2. Extract( $params, sk_{msk}, id$ ):
  - a) Compute  $Q_{id} = H_1(id) \in G_1$
  - b) Set the private key of id to  $sk_{id} = sk_{msk}Q_{id}$
- 3. Encrypt(params, id, m):
  - a) Compute  $Q_{id} = H_1\{id\}$
  - b) Choose a random  $sigma \in (0,1)^l$
  - c) Compute  $r = H_3\{sigma, m\}$
  - d) Encrypt the plaintext message m to the ciphertext c as

$$c = \langle rP, sigma \oplus H_2(g_{id}^r), m \oplus H_3(sigma) \rangle = \langle U, v, w \rangle$$
  
with  $g_{id} = e(Q_{id}, P_n ub) \in G_T$ 

- 4.  $Decrypt(sk_{id}, c)$ : Decrypt the ciphertext c back to the plaintext message m as follows
  - a) Compute  $sigma = v \oplus H_2\left(e\left(sk_{id}, U\right)\right)$
  - b) Compute  $m = w \oplus H_3$  (sigma)
  - c) Set  $r = H_3$  (sigma, m). Test that U = rP. If not, reject the ciphertext.
  - d) Output m as the decryption of c

#### 3.3.2 Overview

The issue of encrypting one message to reach multiple recipients has been widely studied in literature since its first introduction by Fiat and Naor [53]. This section highlights the most important evolutions of BE in literature, however it only considers the most relevant publications to our goal: achieving user-friendly broadcast encryption for OSNs.

#### Broadcast Encryption

The implementation from Fiat and Naor [53] requires a ciphertext of size  $O\left(t\log^2 t\log n\right)$  to be secure against t colluding users. The first fully collusion resistant scheme was proposed by Naor et al. [96] thereby making the ciphertext size independent of the number of colluding users. A collusion resistant BE scheme refers to a broadcast encryption scheme that is secure even if all users that are not in the recipient set  $\mathcal{S}$  would collaborate. Halevy and Shamir [71] further reduce the required ciphertext length for collusion resistant schemes which is followed by many [47, 67, 84] achieving ciphertext sizes only dependent on the number of revoked users O(r). Boneh, Gentry and Waters [24] are the first to consider utilisation of bilinear maps to realise constant size ciphertexts and O(n) public keys.

#### Identity-Based Broadcast Encryption

Sakai and Furukawa [105] are the first to define a collusion resistant *Identity Based Broadcast Encryption* (IBBE) scheme. Independently, Delerablée [45] realises a similar IBBE scheme and claims to be the first as well. The size of the public key in both schemes is proportional to the maximum size of the intended set of recipients while realising short ciphertexts and private keys.

Back et al. [8] define an IBBE scheme that requires only one pairing computation, proven secure under the random oracle assumption where the attacker ties himself to a selective-ID attack. Later, Gentry and Waters [62] achieve identity based broadcast encryption with sublinear ciphertexts. The proposed scheme is proven secure against the stronger notion of adaptive security where the attacker can adaptively alter its queries depending on earlier received information. Barbosa and Farshim [10] proposed an identity-based key encapsulation scheme for multiple parties which is an extension of mKEM as considered by Smart [111] to the identity-based setting. An mKEM is a  $Key\ Encapsulation\ Mechanism\$ which takes multiple public keys as input. An encrypted message under mKEM consists of an encapsulated session key k and a symmetric encryption  $E_k\ (m)$  of the plaintext message m under k. However, the scheme from Smart [111] is only proven secure under the random oracle assumption.

#### Anonymous Broadcast Encryption

All earlier mentioned references describing BE require the intended set of recipients S to be published to realise higher efficiency. Barth, Boneh and Waters [13] are the first to design a BE scheme that takes the anonymity of the recipient into account.

**Definition 3.1 (Anonymity).** A BE scheme is said to be *anonymous* if it hides who is included in the recipient set S. That is, no entity inside or outside S can derive the identity of recipients included in S from the broadcasted ciphertext in polynomial time.

The proposed anonymous broadcast encryption (ANOBE) scheme from Barth, Boneh and Waters [13] implies a linear dependency of the ciphertext on the number of recipients and can only be proven secure in the random oracle model. Libert et al. [85] propose an alternative ANOBE scheme that is proven secure in the standard model. Both schemes propose a tag based system that allows efficient decryption at the cost of making the public master key linear dependent on the total number of users. Krzywiekci et al. [79] propose a scheme that is proportional to the number of revoked users, although the security proof is rather informal. Yu et al. [116] design an architecture that even hides the number of users in the recipient set using Attribute Based Encryption (ABE) [104].

However, ABE requires that all users are assigned attributes such that only users who have a sufficient number of attributes in common can decrypt the message. In networks where the total number of users is large it can be a work intensive task to label each user with the correct attributes.

#### Outsider-Anonymous Broadcast Encryption

The notion of outsider anonymous broadcast encryption is introduced by Fazio and Perera [51].

**Definition 3.2 (Outsider Anonymity).** A BE scheme is called *outsider anonymous* if the identities of the recipients are known to the other identities in the recipient set S while remaining secret to other parties of the BE scheme.

The scheme from Fazio and Perera [51] relies on IBE to encode where a recipient is positioned in a publicly published tree to achieve sublinear ciphertexts. It is remarkable that sublinear ciphertexts are achieved while attaining recipient anonymity to all users that are outside the intended set of receivers. However, the scheme has the drawback of immediately fixing the total number of users that are allowed in the system. Furthermore, an additional architecture is required to maintain the tree of subscribed users. Although IBE is used, the scheme does not allow to represent public keys of users by their public identifiers, because the public key needs to correspond to the position of a user in the tree structure of the external architecture. In this way, most of the desirable properties of IBE disappear. Although the scheme from Fazio and Perera does not fit the requirements for user-friendly broadcast-encryption in OSNs, it is useful to remember their definition of outsider-anonymity.

#### 3.3.3 Most Attractive BE Schemes

From the aforementioned schemes the one from Libert et al. [86] contains the most attractive properties as it is proven secure in the standard model at almost no reduced

computational efficiency. The scheme supports anonymity in both identity-based BE as well as traditional asymmetric cryptosystems.

If anonymity is not an issue, different BE schemes have to be considered depending on the goals of the target application. The scheme from Libert et al. [85] certainly does not have the most desirable properties in non-anonymous BE environments since it can not benefit from higher efficiency due to the recipient being publicly known.

### 3.4 Secret Sharing

In 1979, both Shamir [108] and Blakley [20] independently proposed an algorithm achieving perfect threshold secret sharing.

**Definition 3.3 (Secret sharing scheme).** A Secret sharing scheme is a cryptographic scheme that divides a secret s into n pieces of data  $\sigma_1, \ldots, \sigma_n$  called shares. Shares are distributed over n different parties called shareholders such that only specific subsets of the distributed shares allow reconstruction of the original secret s [95].

**Definition 3.4 (Threshold scheme).** A (t, n) threshold scheme  $(t \le n)$  is a secret sharing scheme by which a trusted party securely distributes n different shares  $\sigma_i$  to n different parties  $P_i$  for  $1 \le i \le n$  such that any subset of t or more different shares  $\sigma_i$  easily allows to reconstruct the original secret s. Knowledge of t-1 or less shares is insufficient to reconstruct the original secret s [95].

**Definition 3.5 (Perfect threshold scheme).** A (t, n) threshold scheme is said to be *perfect* if no subset of fewer than t shareholders can derive any partial information on the information theoretic sense about the original secret s even with infinite computational resources [95].

Shamir's solution [108] was based on polynomial interpolation while Blakley's algorithm [20] relied on finite geometries. Blakley secret sharing uses more bits than necessary as it describes multidimensional planes. In contrast, Shamir secret sharing requires as many bits for each share as the length of the original secret.

The idea behind Shamir secret sharing is elegant in its simplicity. Shamir secret sharing is based on the principle that any polynomial f(x) of degree t-1 is uniquely defined by t points lying on the polynomial. For example, it is possible to draw only one straight line between 2 different coordinates, a quadratic is fully defined by 3 different coordinates and so on. If the trusted party randomly generates a polynomial of degree t-1 it suffices to securely distribute one of n different coordinates on the curve to each party  $P_i, 0 \le i \le n$ . A subset of at least t different shareholders has to collaborate in order to reconstruct the original polynomial by interpolation. For security reasons the polynomial f(x) is calculated in a finite field modulo a large prime number p. The complete mechanism of Shamir's threshold scheme is depicted in Algorithm 5. The mechanism behind reconstruction in Algorithm 5 follows since

#### **Algorithm 5** Shamir's (t, n) threshold scheme [95]

**Goal**: A dealer D distributes shares of a secret s to n parties.

**Result**: If a subset of at least t out of n shareholders collaborates, they can reconstruct the original secret s.

- 1. Setup A dealer D begins with a secret integer  $s \geq 0$  it wishes to distribute among n parties
  - a) D chooses a prime  $p > \max(s, n)$  and defines  $a_0 = s$
  - b) D selects t-1 random, independent coefficients  $a_1, \ldots, a_{t-1}, 0 \le a_j \le p-1$  defining the random polynomial over  $\mathbb{Z}_p$ ,  $f(x) = \sum_{j=0}^{t-1} a_j x^j$
  - c) D computes  $\sigma_i = f(i) \mod p, 1 \le i \le n$  and securely transfers the share  $\sigma_i$  to shareholder  $P_i$ , along with a public index i.
- 2. Reconstruction Any group of t or more shareholders pool their shares. Their shares provide t distinct points  $(x,y)=(i,\sigma_i)$  allowing computation of the coefficients  $a_j, 1 \leq j \leq t-1$  of f(x) by Lagrange interpolation. The secret is recovered by calculating

$$f(0) = \sum_{i=1}^{t} y_i b_i = s$$
 with  $b_i = \prod_{1 \le j \le t, j \ne i} \frac{j}{j-i}$ 

the coefficients of an unknown polynomial f(x) of degree less than t, defined by points  $(x_i, y_i)$ ,  $1 \le i \le t$  are given by the Lagrange interpolation formula

$$f(x) = \sum_{i=1}^{t} y_i b_i \text{ with } b_i = \prod_{1 \le j \le t, j \ne i} \frac{x - x_j}{x_i - x_j}$$

A proof of this formula is omitted but can be found in [115].

#### 3.4.1 Verifiable Secret Sharing

Verifiable secret sharing [39] ensures the participating parties that received shares are consistent by providing a verification mechanism. This verification mechanism can either detect an unfair dealer during setup or participants submitting incorrect shares during the reconstruction phase. The first verifiable secret sharing schemes were *interactive*, i.e. interaction between shareholders and the trusted party was required to verify their shares. In *non-interactive verifiable secret sharing* as proposed by Pedersen [98] only the trusted party is allowed to send messages to the future shareholders. Shareholders can not communicate with each other neither can they send messages back to the trusted party. Non-interactive verifiable secret sharing is

preferred over interactive alternatives as their is no chance of shareholders accidentally leaking too much information.

Popular verifiable secret sharing schemes are Feldman's scheme [52] and Benaloh's scheme [18]. No further details are given as a basic notion of verifiable secret sharing suffices for the remainder of this text.

### 3.5 Distributed Key Generation

Distributed key generation is inspired on secret sharing. The idea behind distributed key generation is that a secret s can be shared among n shareholders without the requirement for a centralised dealer D as in Algorithm 5. In this way, a secret can be negotiated between all shareholders without any of the shareholders explicitly computing the secret. The major advantage of such a scheme is that no party in the scheme requires a higher level of trust since no party explicitly knows the secret. Similarly to the Shamir secret sharing scheme a group of t or more shareholders will need to pool their shares in order to reconstruct the secret s.

#### 3.5.1 Definition

**Definition 3.6 (Distributed key generation scheme).** A distributed key generation scheme is a (t, n) perfect threshold scheme  $(t \le n)$  that requires no trusted party. That is, a distributed key generation scheme is a cryptographic scheme that negotiates a secret s with n different parties  $P_1, \ldots, P_n$  by letting each party  $P_i$  distribute shares  $\sigma_{ij}$  of its own private secret  $\sigma_i$  with all other parties  $P_j$  where  $1 \le i \le n, 1 \le j \le n$ . At least t out of n parties will need to collude in order to compute the original secret s explicitly.

#### 3.5.2 Pedersen Distributed Key Generation

The first usable distributed key generation protocol was defined by Pedersen [99]. A later publication from Gennaro et al. [60] proves the Pedersen scheme insecure in its original form in the presence of malicious key generation centers.

Although the Pedersen scheme [99] is proven insecure, it is most instructive to describe the protocol in its original form as later schemes such as the one from Gennaro et al. [60] extensively rely on the same concepts. Therefore, the original Pedersen protocol is depicted in Algorithm 6.

The correctness of the Pedersen scheme is based on every party  $P_i$  correctly executing a Shamir (t, n)-threshold scheme. After every party has distributed its shares, each party  $P_i$  owns n points  $(i, f_j(i)) = (i, \sigma_{ji})$  from other parties  $P_j$ . By summation of all these shares  $s_i = \sum_{j \in \mathcal{Q}} \sigma_{ji} \mod p$ ,  $s_i$  represents the y-coordinate corresponding to x = i of the sum of all curves  $f_j(x)$  generated by all parties  $P_j$ . In this way, the negotiated master secret key  $sk_{msk}$  is equal to the sum of the secret keys of every party  $P_i$ , such that

$$sk_{msk} = \sum_{i \in \mathcal{Q}} sk_i \bmod p$$

In fact, the master secret key  $sk_{msk}$  is found by summing all private curves  $f_j(x)$  such that every honest party's share equally contributes to the master secret key  $sk_{msk}$ .

The other steps in the Pedersen protocol are required to verify whether all parties calculate the shares honestly. Step e) effectively verifies the correctness of the received shares. Therefore, the  $A_{ih}$  values are often called Pedersen commitments.

The scheme from Gennaro et al. [60] lets each party  $P_i$  commit to two different polynomials  $f_i(x)$  and  $g_i(x)$  since a flaw in the Pedersen scheme allows malicious parties to determine certain bits in  $sk_{msk}$  with non-negligible advantage. The details behind the scheme from Gennaro et al. are omitted since more practical DKG protocols in the asynchronous setting are already subject of extensive research.

### 3.6 Summary

The aforementioned cryptographic building blocks constitute the required tools to design a practical encryption scheme for OSNs in Chapter 4.

This chapter started with the introduction of Public Key Infrastructures (PKIs). In a next section, Identity-Based Encryption (IBE) was presented as a possible alternative to traditional PKIs. In addition, the basics of Broadcast Encryption (BE) were highlighted. Finally, secret sharing and Distributed Key Generation (DKG) were introduced as a mechanism to get around the IBE key escrow property.

### Algorithm 6 Pedersen's distributed key generation [99]

**Goal**: A master secret key  $sk_{msk}$  is negotiated with n uniquely numbered parties  $\{P_1, \ldots, P_n\}$  without any of the parties explicitly computing the secret  $sk_{msk}$ .

**Result**: If a subset of at least t out of n parties colludes, they can reconstruct the original secret s.

- 1. Setup At initialisation, a setup algorithm  $\langle p, g \rangle \leftarrow \mathcal{G}\left(1^{\lambda}\right)$  is executed that returns a large prime number p and a generator g of  $\mathbb{Z}_p$  on input of a security parameter  $\lambda$ . After execution of  $\mathcal{G}\left(1^{\lambda}\right)$  each party  $P_i, 1 \leq i \leq n$  should do the following:
  - a)  $P_i$  generates a random private key  $sk_i \in \mathbb{Z}_p$  and publishes the corresponding public key  $pk_i = g^{sk_i}$
  - b)  $P_i$  chooses t-1 uniformly random independent coefficients  $a_{i,1},\ldots,a_{i,t-1},0\leq a_{i,j}\leq p-1$  defining a random polynomial  $f_i(x)$  over  $\mathbb{Z}_p$ ,  $f_i(x)=\sum_{h=0}^{t-1}a_{i,h}x^h$ .
  - c)  $P_i$  commits to the coefficients  $a_{i,1}, \ldots, a_{i,t-1}, 0 \le a_{i,h} \le p-1$  by broadcasting  $A_{ih} = g^{a_{i,h}} \mod p$  for  $h = 1, \ldots, t$  to all other parties.
  - d)  $P_i$  computes the share  $\sigma_{ij} = f_i(j) \mod p$  and securely transfers the share  $\sigma_{ij}$  to party  $P_j$  along with a signature  $S_{P_i}(\sigma_{ij})$  authenticating the share.  $P_i$  keeps  $\sigma_{ii}$  to itself.
  - e)  $P_i$  verifies for each share  $\sigma_{ji}$  received from  $P_j$  whether it is consistent by verifying that

$$g^{\sigma_{ji}} = \prod_{h=0}^{n-1} \left(A_{jh}\right)^{i^h} \bmod p$$

If the check fails for an index j,  $P_i$  broadcasts a complaint against  $P_j$  along with the received share  $\sigma_{ji}$  and its signature  $S_{P_j}(\sigma_{ij})$ . If a party receives t complaints, he is excluded from the set of participating parties Q.

- f) The master public key is calculated as  $pk_{msk} = \prod_{j \in \mathcal{Q}} pk_j \mod p$ . The public verification values are calculated as  $A_h = \prod_{j \in \mathcal{Q}} A_{jh} \mod p$  for  $k = 1, \ldots, t$ . Each player  $P_i$  computes his share of the secret as  $s_i = \sum_{j \in \mathcal{Q}} \sigma_{ji}$ .
- 2. Reconstruction Any group of t or more shareholders pool their shares. Their shares provide t distinct points  $(x, y) = (i, s_i)$  allowing computation of the coefficients  $a_j, 1 \le j \le t 1$  of f(x) by Lagrange interpolation. The master secret key is recovered by calculating

$$sk_{msk} = \sum_{i \in \mathcal{Q}} s_i b_i$$
 with  $b_i = \prod_{i \in \mathcal{Q}, i \neq h} \frac{h}{h - i}$ 

4

# Design of a Practical Encryption Scheme for Online Social Networks

This chapter effectively designs an encryption scheme for practical use in OSNs. In the first section (Section 4.1), a model is developed that allows to describe the current OSN situation. By defining every considered entity in the OSN, the resulting model serves as the framework in which we design our future constructions. In a next step (Section 4.2), the different threats within the model are defined. The section on the threat model first highlights the current privacy threats, followed by a definition of the considered adversaries and the assumptions on these adversaries. In Section 4.3 our proposal is derived by stating cryptographic goals based on the earlier threat model. This is followed by design decisions on how to achieve these goals and how this impacts our model. Section 4.3 is concluded with a concrete proposal in the form of an algorithm along with an evaluation section motivating why our cryptographic design goals are successfully met.

#### 4.1 Model of the Current Situation

The most commonly accepted definition of an *Online Social Network* (OSN) in literature is from Boyd and Ellison [28]. However, since this definition is still too generic for the remainder of this text a slightly modified version is presented here.

**Definition 4.1 (Online Social Network [28]).** An *Online Social Network* (OSN) is a web-based service that allows users to:

- 1. Construct a public or semi-public profile within a bounded system
- 2. Articulate a list of other users with whom they share a connection.
- 3. View, traverse and share content with their list of connections and those made by others within the system

For the definition of our OSN model we focus on messages sent by users. Therefore, we define several different entities that are present in our model.

**Definition 4.2 (OSN user).** An OSN user U is any entity that has a profile on the OSN and thus identifiable by a unique identifier  $id_U$ . The set containing all users of an OSN is denoted U.

# 4. Design of a Practical Encryption Scheme for Online Social Networks

An OSN user can perform different activities within the infrastructure of the OSN. Depending on the performed activity, the user is labeled as one of three different roles: a sender, a friend or an intended recipient.

**Definition 4.3 (Sender).** A sender A is an OSN user who broadcasts a message m over the OSN infrastructure to varying subsets of OSN users, called the *intended* recipient set S, such that  $S \subseteq U$ .

**Definition 4.4 (Intended recipient).** An *intended recipient* of a plaintext message m is an OSN user who is explicitly designated by a sender A to have access to the content of m.

**Definition 4.5 (Friend).** An OSN user who shares a connection with another OSN user U in the OSN infrastructure, is called a *friend of the user* U.

Different entities within the OSN have access rights to the profile  $id_U$  of a user U. If abstraction is made of entities with access to only specific content, it suffices to define four different sets of entities, each with their own access rights: the set of the user's friends  $\mathcal{F}_U$ , the intended recipient set  $\mathcal{S}$ , the set of entities with access to the OSN  $\mathcal{V}$  and the set of entities with access to the user's profile  $\mathcal{V}_U$ .

**Definition 4.6 (Friends set).** The set of all friends associated to a user U is the friends set  $\mathcal{F}_U$ , such that  $\mathcal{F}_U \subseteq \mathcal{U}$ .

**Definition 4.7 (Intended recipient set).** The intended recipient set of a message m is the set of all intended recipients of m. The intended recipient set S takes the form of a list of id's uniquely identifying other users' profiles in the OSN infrastructure.

**Definition 4.8 (Viewers set).** Any entity that is given access to the OSN belongs to the *viewers set* V.

**Definition 4.9 (Profile viewers set).** All viewers with access to non-public content of a profile  $id_U$  of a user U are in the *profile viewers set*  $\mathcal{V}_U \subseteq \mathcal{V}$ .

Many different entities can be part of the set V, e.g. OSN users, advertising companies, system administrators of the OSN or software applications specifically developed for the OSN. Usually, the OSN determines who is part of V. Therefore, a user U often has limited control in who is a member of  $V_U$ .

As illustrated by Figure 4.1, Sender A wants to broadcast a message m over the OSN infrastructure to the intended recipient set S. As A only wants to share the message with a specific group of friends, A defines the intended recipient set S, such that  $S \subset \mathcal{F}_A$ . Next, A sends m to the OSN's distribution server along with the intended recipient set S. The OSN Server further distributes the message to all users in S. Also a subset of third party applications and advertisers get access to the distributed message if they are inside the viewers group  $\mathcal{V}_A$ . Every entity who has access to the message is coloured blue in Figure 4.1.

Figure 4.1 illustrates previous definitions applied to an OSN as it is often encountered on the internet. The different sets in Figure 4.1 are defined as follows:

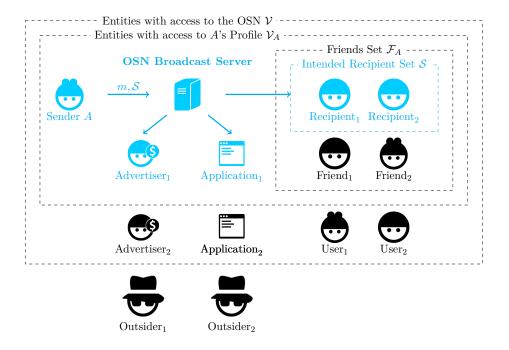


Figure 4.1: Model of the current OSN situation. Entities with access to the message m are coloured blue.

• The intended recipient set,

$$S = \{\text{Recipient}_1, \text{Recipient}_2\}$$

• The set of friends of Sender A,

$$\mathcal{F}_A = \{\mathcal{S}, \operatorname{Friend}_1, \operatorname{Friend}_2\}$$

• The set of viewers who have access to the profile of Sender A,

$$\mathcal{V}_A = \{\mathcal{F}_A, \operatorname{Sender}\ A, \operatorname{Advertiser}_1, \operatorname{Application}_1\}$$

• The set of entities with access to the OSN,

$$\mathcal{V} = \{\mathcal{V}_A, \mathrm{User}_1, \mathrm{User}_2, \mathrm{Advertiser}_2, \mathrm{Application}_2\}$$

• The set of all users in the OSN,

$$\mathcal{A} = \{\mathcal{F}_A, \text{Sender } A, \text{User}_1, \text{User}_2\}$$

The OSN's infrastructure stores almost everything within the viewer set  $\mathcal{V}$ . The profiles of all users within the friends set  $\mathcal{F}_A$ , the list of id's within the intended

# 4. Design of a Practical Encryption Scheme for Online Social Networks

recipient set S, access rights of applications and advertisers that are part of  $V_A$  and access rights of entities within the set V are all explicitly stored somewhere on the servers of the OSN.

Note that not all OSNs support the functionality to define intended recipient sets  $\mathcal{S}$  on a per message basis. In OSNs like Twitter the standard privacy settings are such that message are always published publicly. Therefore, the model from Figure 4.1 only holds for a specific subset of OSNs like Facebook or Google+. More public OSNs like Twitter would require less sets of entities to model their behaviour.

It requires almost no additional effort to transform the model from Figure 4.1 such that it also takes the sharing of other media than messages into account. The model could then adopted for use on OSNs like Youtube or Instagram as well. However, this falls out of the scope of this thesis.

#### 4.2 Threat Model

The threat model considers all entities and how they pose a threat in the aforementioned security model.

#### 4.2.1 Privacy Threats

Currently an OSN as illustrated in Figure 4.1 presents several issues that can be classified as either misplaced trust in the OSN provider or dependency on the OSN's privacy infrastructure.

#### Misplaced Trust in the OSN Provider

Users have to trust the OSN provider, however this trust is often misplaced on several fronts.

TRUST IN THE INTENDED RECIPIENT SET There is a mismatch between the expectations of Sender A and the functionality of the OSN. A user has higher demands on the specification of the intended recipient set than effectively implemented by the OSN. When a privacy-aware user like sender A takes the effort to define an intended recipient set S, A expects to have full control on who has access to the messages m. In reality, sender A only has partial control since the OSN determines all other entities in  $\mathcal{V}_A$  that are not part of sender A's friend list  $\mathcal{F}_A$ . In some OSNs a user first has to give permission to third party applications before access is granted to the user's content. Note that this gives more control to OSN users on determining who is inside the viewers set  $\mathcal{V}_A$ . Nevertheless, in practice it is still hard to get a concise overview from the OSN on everyone inside  $\mathcal{V}_A$ .

TRUST IN THE BROADCASTING MECHANISM Any user broadcasting messages over the OSN infrastructure has to trust the OSN that it effectively operates as claimed. If the OSN broadcast server in Figure 4.1 would accidentally broadcast messages publicly despite of the sender's privacy settings, the privacy of the sender is breached.

Even more worrisome is the fact that the sender will almost certainly never discover these privacy violations.

TRUST IN THE DATA STORAGE POLICY All messages are stored on the infrastructure provided by the OSN. However, every sender has to trust the OSN will treat this data responsible. Nevertheless, most OSN data storage policies store all content for an unlimited amount of time on their servers. The sender thereby loses the control over his own data and to whom and how long it is still available.

MISMATCH OF NEEDS Besides the earlier mentioned issues, the OSN often operates with a corporate mentality. Although the user desires a relatively private OSN environment, the needs of the OSN are different. The OSN has no initiative to stop adding advertisers and applications to the set of entities with access to a sender's profile  $\mathcal{V}_A$ . The more information advertising companies receive from the OSN provider, the better they can tailor advertisements to the user. The more third party applications rely on the OSNs infrastructure, the more appealing the OSN business model looks like. Therefore, OSNs have often not enough incentives to offer stricter access control policies to their users.

#### Dependency on the OSN's Privacy Infrastructure

Often, users are also dependent on the privacy infrastructure as it is currently provided by the OSN.

DEPENDENCY ON ACCESSIBILITY OF INFRASTRUCTURE Users of the OSN have to rely on the security of the OSN's infrastructure. If one of the outsiders in Figure 4.1 would succeed in hacking the OSN's digital infrastructure, he would have immediate access to all sensible information stored on the OSN's servers. Similarly, local governments can subpoen the OSN to disclose sensible information on certain users with the argument of national security.

DEPENDENCY ON PRIVACY PREFERENCES Another significant point is that the OSN fully determines which access policies are supported. Not all OSNs offer the definition of an intended recipient set on a per message basis. Even OSNs currently supporting this functionality can suddenly stop offering the service. Moreover, nothing prevents OSN providers from changing their privacy policy on a regular basis, thereby complicating users to define the access policy of their choice.

#### 4.2.2 Adversaries

We consider adversaries that are honest but curious, i.e. passive adversaries that do not actively try to prevent the broadcasting process but are curious for the broadcasted content. An adversary in the earlier defined model, is any computationally bounded entity trying to violate one or several of the following properties:

1. **Confidentiality:** The entity tries to violate the confidentiality of encrypted messages, i.e. uncovering information within a broadcasted ciphertext. This

# 4. Design of a Practical Encryption Scheme for Online Social Networks

can either be the intended recipient set S or the actual content of the plaintext message m.

- 2. **Integrity:** The entity tries to violate the integrity of encrypted messages, i.e. changing the ciphertext c or the plaintext m such that it differs from the way it was originally drafted by the sender.
- 3. Availability: Any entity apart from the original sender, tries to prevent messages from being broadcasted by bringing down parts of the architecture.

#### 4.2.3 Assumptions

The threat model can narrow down the capabilities of entities in the model to achieve well-defined adversaries. However, an architecture protecting against more restricted adversaries is considered less secure.

#### Assumptions on the OSN

OSNs are assumed not to violate integrity neither availability. Nothing can be done to prevent the OSN from actively altering its own resources to bring down the proposed IBE architecture. It can not be prevented that a user of IBE on the OSN infrastructure gets blocked by the OSN provider. Neither can it be prevented that OSNs delete messages because they are encrypted. OSNs can also easily impersonate the owner of a profile in their infrastructure. Therefore, from this moment onwards, OSNs are assumed not to act as an active adversary. It is assumed that as soon as privacy aware users notice this kind of OSN behaviour, they will adopt to more reliable OSN alternatives. However, our assumptions do not prevent the OSN from trying to passively break confidentiality as they have every motivation for it in the context of their current business model.

Another assumption on the OSN's infrastructure is that the authentication mechanism of the OSN is secure. This is primarily important for the authenticity of the broadcasted messages on a user's profile as further discussed in Section 4.3.2.

Previous assumptions on the OSN are ideal assumptions that will probably hold as long as only the minority of the OSN users applies encryption mechanisms to their network. It is still unknown how OSNs will react when our proposal finds common acceptance in their wide user base.

Furthermore, it is assumed that the OSN does not rely on traffic analysis to derive more information on the encrypted content. For example, suppose a user just visited a URL to an external news website broadcasted over the OSN infrastructure. With high probability the message broadcasted immediately after the user's visit, is a reaction to the content in the article. Furthermore, if Bob visits Alice's profile on a daily basis, almost certainly Bob regularly includes Alice as a recipient in his broadcasted messages as well.

Note that the latter assumption is not valid in practice. Generally, the ability of traffic analysis is countered by generating dummy traffic. However, protecting against traffic analysis falls out of the scope of this thesis.

#### Assumptions on the User

In order to achieve a strong encryption mechanism, users are unlimited in their abilities to behave as an adversary. However, one subtle assumption is made on users that are part of S. Users in S are assumed not to break their social contract. That is, if a sender broadcasts a confidential message to a selected set of recipients, the recipients are assumed not to decrypt the encrypted message and rebroadcast the confidential content to any entity not in the original recipient set S. In fact, no existing encryption mechanism provides protection against such misbehaviour, although traitor tracing schemes [38] discourage users from treating by indicating who broke his social contract. However, for the remainder of this text intended recipients are assumed trustworthy in that they do not break the social contract. The remainder of their abilities is not restricted by further assumptions.

## 4.3 Our Proposal

Our well-defined security model is used as a framework to define a concrete proposal protecting against the earlier defined adversaries.

#### 4.3.1 Cryptographic Goals

The general design goals (Section 1.3) stated that a new privacy enhancing architecture for OSNs should be user friendly, applicable and immediately ready to use. Besides from these general design goals, it is now possible to define specific cryptographic requirements as well. A well-designed encryption scheme should be able to achieve the following cryptographic goals when publishing a message m to a set of intended recipients  $\mathcal{S}$  on an OSN with the help of an encryption scheme:

- Confidentiality: The message is protected from disclosure to unauthorised parties, i.e. all entities that are not explicitly in the recipient set S.
- Outsider recipient anonymity: The intended recipients of a broadcasted message should be anonymous to any entity not included in S. This implies that even the OSN is not required to know who the recipients are. (Definition 3.2 gives a more formal definition of outsider-anonymity).
- No redundancy: The message should be published only once to reach every recipient in S.
- Authenticity: The recipients of the message have reasonable assurances of the message's origin.
- **Integrity:** The recipients are assured the message is distributed in its original form as posted by the sender.
- No key escrow: Private keys are only disclosed to the owners of the public key. No other entity should be able to have more information on one's secret key in the information theoretic sense.

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- **Key validation:** All users of the system should be able to verify the correctness of their private keys.
- Limited key validity: Private keys of users should only be valid for a limited period of time to limit the damage of potentially lost private keys.

#### 4.3.2 Design Decisions

In this section, our architecture is further developed by keeping the aforementioned cryptographic design goals in mind.

#### Confidentiality

Confidentiality is achieved by applying an encryption scheme before broadcasting a message. Current solutions like Scramble [15] and Persona [7] rely on rather classic PKIs thereby requiring the OSN user to subscribe to a third party key infrastructure. These key infrastructures are required to authenticate and store the public keys of all security aware users. However, this does not correspond to the general design goals from Section 1.3 stating that the proposed solution should be both user friendly and immediately ready to use.

Identity-based encryption (IBE) can achieve both confidentiality and the general design goals of usability and applicability. During the design of our scheme, three IBE schemes were considered as a potential candidate: Boneh and Franklin IBE [26], Sakai and Kasahara IBE [106] and Gentry IBE [61]. For a more elaborate discussion on why only these schemes were considered, the reader is referred to Section 3.3.2.

Table 4.1 lists the different security properties of all schemes. The Gentry IBE scheme has the highest security level since it is the only scheme proven secure in the standard model. In the random oracle model, Boneh and Franklin IBE is preferred over Sakai and Kasahara IBE since it relies on the BDH assumption which is more widely accepted than the stronger BDHI assumption.

The execution times of all considered IBE schemes are illustrated in Table 4.2. We conducted our measurements on an Intel Core 2.4 GHz i5 processor with 8 Gb of 1600 MHz DDR3L onboard memory. Pairing computations were implemented using the multi-precision MIRACL library [107]. The Gentry IBE scheme was first transformed to the asymmetric setting to give a fair basis of comparison. The exact transformed Gentry IBE scheme is depicted in Appendix A.

Table 4.2 clearly illustrates the price there is to pay for security in the standard model. Therefore, Boneh and Franklin IBE was chosen as the preferred IBE scheme despite the dependency on the random oracle assumption.

IBE requires that OSN profiles can be uniquely identified by a unique public identifier id. However, the decision on which string to use as identifier is highly dependent on the underlying OSN and therefore implementation dependent.

	Security Proof			
IBE Scheme	IND-ANO-CCA	Standard model	Assumption	
Boneh and Franklin	✓	Х	BDH	
Sakai and Kasahara	$\checkmark$	×	BDHI	
Gentry	$\checkmark$	$\checkmark$	q-BDHE	

Table 4.1: Security comparison of considered IBE schemes

	Execution time (ms)			
IBE Scheme	IBE.Setup	IBE.Extract	IBE.Encrypt	IBE.Decrypt
Boneh and Franklin Sakai and Kasahara Gentry	368.10 1257.72 24.49	13.84 20.49 37.46	271.90 319.83 1136.65	252.82 259.17 911.32

Table 4.2: Performance comparison of considered IBE schemes in MIRACL

#### Outsider Recipient Anonymity

The outsider anonymity requirement from Section 4.3.1 is imposed on the recipient set since our solution is developed in the context of OSNs where user interaction plays an important role. Therefore, it is useful that members of the intended recipient set S know each other. For example, suppose that Alice broadcasts an encrypted message intended to Bob and Dylan using a scheme that fully hides the identity of the recipients. This implies that  $id_{Bob}$ ,  $id_{Dylan} \in S$ . As a reaction to Alice's message, Bob wants to write a reply to start a discussion. However, as Bob does not know which other users are allowed to see Alice's message, he can now only encrypt his reply to Alice thereby preventing Dylan from joining the discussion. Nevertheless, this discussion could have been useful to Dylan as well because otherwise Alice would not have included Dylan as a recipient in S in the first place.

From the outsider-anonymity requirement, it immediately follows that users not necessarily need to be friends to receive each other's messages. In the specific example of Alice, Bob and Dylan, it could be that Bob and Dylan both have Alice as a common friend while no immediate friend connection exists between Bob and Dylan. This should be taken into consideration when determining the identifiers of Bob's and Dylan's profiles,  $id_{Bob}$  and  $id_{Dylan}$  respectively.

As discussed in Section 3.3.2, broadcast encryption schemes can be made more efficient if the recipient set S is public. Although user interaction is important, the intended recipient set cannot be disclosed publicly. Consider the example in which Bob's girlfriend celebrates her birthday in a few weeks. When Bob's girlfriend notices that Bob broadcasted an encrypted message to all her friends without including her as a recipient, she will probably know Bob is up to something. This is just one specific example that illustrates the negative impact on security, broadcasting

# 4. Design of a Practical Encryption Scheme for Online Social Networks

of the recipient set S can have on real life situations. Depending on the context, information can be deduced about the message without decrypting it to plain text.

#### No redundancy

From the no redundancy requirement it immediately follows that a broadcast encryption scheme should be used, preferably one that hides the anonymity of recipients in the intended recipient set  $\mathcal{S}$  to the outside world. However, apart from the outsider-anonymous broadcast encryption scheme from Fazio and Perera [51], to our knowledge no efficient schemes of this kind are described in literature. Since the BE scheme from Fazio and Perera does not fully benefit from the advantages of IBE, the ANOBE scheme from Libert et al. [85] is preferred for further implementation. Since recipients still have to know who else is included in  $\mathcal{S}$ , the list of ids within  $\mathcal{S}$  is concatenated to the plaintext message before encryption.

The scheme from Libert et al. also offers non-repudiation by using signature schemes. Note however, that a trusted authority authorising and publishing the public keys is required for the implementation of signature schemes. Because the general design goals were applicability and user friendliness, no third party PKI is incorporated in our scheme. Therefore, the implemented scheme does not rely on signatures as in the original proposal from Libert et al. [85].

If the security parameter is chosen to be  $\lambda$ , the IBE scheme in Algorithm 4 can only encrypt messages with a maximum length of l bits. This can be seen since in the last step of IBE.Encrypt the message m is encrypted by an XOR operation with the result of a hash function  $H_3: \{0,1\}^l \to \{0,1\}^l$ . Since asymmetric IBE schemes can only encrypt these fixed length messages, the scheme from Libert et al. [85] is altered such that the ciphertext in the original proposal contains a with IBE encrypted symmetric session key k that is the same for each user in the recipient set  $\mathcal{S}$  on a per message basis. The actual plaintext is then encrypted with a symmetric encryption scheme based on a mode of operation to support longer message lengths.

#### Authenticity and Integrity

Authenticity and integrity can be achieved at the same time by relying on an authenticated encryption scheme. The integrity of a message is then as strong as the security guarantees of the authenticated encryption scheme.

Note however, that the authentication mechanism still relies on the security guarantees of the OSN. Since no third party PKI mechanism is used, there is no trusted party verifying the identity corresponding to a public key. In OSNs this is not an issue if IBE is used with unique profile identifiers as a public key. Consequently, such an IBE scheme ensures that messages encrypted under a public identifier can only be seen by the owner of the corresponding OSN profile. Verifying whoever owns the OSN profile remains the responsibility of the OSN and the judgement of the OSN profile's connections. However, if the authentication mechanism of the OSN is inadequate, anyone could login to a user's profile to impersonate the actual owner

of the profile. Therefore, our proposed solution can not be more secure than the authentication mechanism of the OSN.

In more traditional communication schemes, authenticated encryption uses the symmetric key as agreed during an authenticated key agreement protocol like the Station-to-Station protocol [46]. Authenticity of ciphertexts generated by the authenticated encryption scheme than immediately follows from the usage of the same symmetric session key k as earlier agreed during the protocol. However, since in the proposed solution every OSN user should be able to immediately broadcast confidential messages to other users of the OSN, no key agreement protocols will are used. With the publication of only one broadcast ciphertext, every user in the intended recipient set S should be immediately able to decrypt it to the original plaintext message m. Therefore, there is no real authenticity in the value of the tag t generated by the authenticated encryption scheme because anyone with access to the user's profile could have chosen a random symmetric session key k and have used it as an input to the authenticated encryption scheme. Unless, the only one with access to the user's profile is the actual owner of the profile. Therefore, the authenticity guaranteed by the authenticated encryption scheme boils down to the security of the authentication mechanism as powered by the OSN.

#### No Key Escrow and Key Validation

IBE schemes inherently imply key escrow which is undesired in most practical systems, as also described in Section 3.2.2. To circumvent the key escrow property of IBE schemes, multiple PKGs are used implementing a distributed key generation (DKG) mechanism for IBE. Users can then verify their private keys by relying on the basics of commitment schemes (Definition 2.42).

For the exact details on how a commitment scheme can achieve this verification mechanism, the reader is immediately referred to the exact proposed scheme in Section 4.3.4.

#### Limited Key Validity

IBE schemes do not allow revocation of public keys (Section 3.2.2). A solution to this drawback is provided by concatenating an expiration date to all public identifiers id. However, these expiration dates should be publicly available to all OSN users since they are part of the public IBE key. To avoid the management of a third party infrastructure keeping track of expiration dates of all users, a special type of function could be used mapping identifiers id to dates. An example of such a function is shown in Algorithm 7.

Algorithm 7 is constructed such that step 1 to 4 only need to be executed once. The sender then stores values  $d_1, h_1, m_1$  locally and only repeats step 5 for each recipient of the message. The exact implementation details could be hidden from the user in software. Different variants of Algorithm 7 could be applied as well. The most important aspect is that everyone in the system uses the same function to map strings to expiration dates.

#### Algorithm 7 A function mapping strings to dates

**Goal**: Avoid a third party infrastructure that keeps track of expiration dates of key pairs in an IBE system

**Result**: On input of a public identifier id the algorithm returns an expiration date in the form d/M/y h:m.

- 1. Choose a hash function  $H: \{0,1\}^* \to \{0,1\}^l$  mapping binary strings of arbitrary length to binary strings of a fixed length l.
- 2. Calculate r = H (id) and interpret the result r as an integer.
- 3. Calculate  $tot_m = r \mod 40320 = r \mod (60 \cdot 24 \cdot 28)$ , where  $tot_m$  denotes the expiration time in minutes within a certain month.
- 4. Calculate three integers  $d_1, h_1, m_1$  denoting an expiration day, hour and minute respectively with  $1 \le d_1 \le 28$ ,  $0 \le h_1 \le 23$ ,  $0 \le m_1 \le 59$  as follows
  - a) The expiration minute is calculated as  $m_1 = tot_m \mod 60$
  - b) The expiration hour is calculated as  $h_1 = \frac{tot_m}{60} \mod 24$
  - c) The expiration day is calculated as  $d_1 = \frac{tot_m}{60\cdot24}$

It can be shown that  $d_1, h_1, m_1$  are chosen uniformly random within their boundaries if the random oracle assumption holds for the hash function  $H(\cdot)$ .

- 5. Let nowIsEarlierThan( $d_1$ ,  $h_1$ ,  $m_1$ ) be a function that returns true if the current time d/M/y h:m is before  $d_1/M/y$   $h_1:m_1$  and false otherwise. Output the expiration date as
  - a) If nowIsEarlierThan $(d_1, h_1, m_1) = \text{true}$ , return  $d_1/M/y$   $h_1: m_1$ .
  - b) If nowIsEarlierThan( $d_1$ ,  $h_1$ ,  $m_1$ ) = false and M+1  $\leq$  12, return  $d_1$ /M/y  $h_1$ : $m_1$ .
  - c) Else return  $d_1/1/(y+1)$   $h_1:m_1$

#### 4.3.3 Updated Model

For the sake of completeness, PKGs are added as an additional entity to our model.

**Definition 4.10 (PKG in our security model).** A *Public Key Generator* (PKG) is an entity in the security model that never colludes with any other entity in the model since its prime motivation is to improve the current security situation in OSNs.

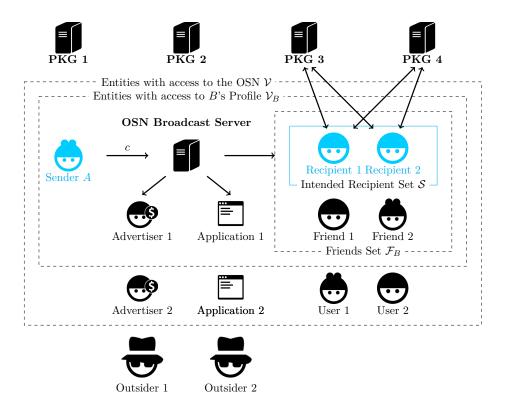


Figure 4.2: Model of the desired OSN situation. Entities with the ability to decrypt the ciphertext are coloured blue.

In the threat model, PKGs are considered to always behave as described in the DKG protocol, although this is a simplification of a PKG as it is often encountered in real-world applications. However, considering PKGs as malicious requires far more complex distributed key generation algorithms which are out of the scope of this thesis. For DKG protocols that can be used in more hostile PKG environments as encountered in practice, the reader is referred to Kate et al. [78].

Figure 4.2 illustrates the changes on the original model of the OSN situation in Figure 4.1. At the top of Figure 4.2 four PKGs are introduced implementing a (t,n) DKG protocol with t=2 and n=4 (Section 3.5). Double arrows represent the secure authentication process in which the recipients communicate with the PKG to receive a share of their secret key. In Figure 3.1 this communication was illustrated

# 4. Design of a Practical Encryption Scheme for Online Social Networks

by two separate single arrows between the PKG and Bob. However, abstraction is made of the exact communication protocol between the recipients and the PKG.

Apart from the newly introduced PKGs, Figure 4.2 differs from Figure 4.1 in several ways. Sender A no longer specifies the set of intended recipients S to the OSN broadcast server. Therefore, the OSN broadcast server delivers the message to all entities with access to A's profile  $\mathcal{V}_A$ . Note that even Friend 1 and 2 are able to see the broadcasted message which was not the case in Figure 4.1. However, since the broadcasted message is actually a ciphertext c of the original message m, only the entities in blue will be able to read the confidential content of the original plaintext message m.

#### 4.3.4 Scheme

Taking all aforementioned cryptographic design decisions into account results in the scheme presented in Algorithm 8.

#### 4.3.5 Evaluation

Algorithm 8 achieves the earlier stated cryptographic design goals from Section 4.3.1. However, it is too early to conclude on the more general design goals from the introduction (Section 1.3) since the achievement of these goals is implementation dependent. The cryptographic goals are realised as follows:

CONFIDENTIALITY The proposed scheme achieves confidentiality as in [26, 85], because a session key k can only be obtained if the recipient holds the corresponding secret key  $s_{id_i}$  to an identifier  $id_i$  that is included in S. Confidentiality of k is thus guaranteed by ANO-IND-CCA secure Boneh and Franklin IBE [26]. Confidentiality of the plaintext message m than immediately follows from the confidentiality of the authenticated encryption in step 5 of Publish.

OUTSIDER RECIPIENT ANONYMITY Our solution is made anonymous by relying on the ANO-IBE scheme from Boneh and Franklin [23]. Furthermore, the broadcasting mechanism is inspired by the BE scheme from Libert et al. [85] which is recipient anonymous as well. The BE scheme is applied to broadcast k. In terms of efficiency, users are required to decrypt  $w_i$  on average  $O(\eta/2)$  before obtaining k due to the anonymity of the BE scheme. Both Barth et al. [13] and Libert et al. [85] propose using a tag based system to hint users where they can find their symmetric key. However, it was deliberately decided not to implement such property in the scheme as it introduces a dependency of the public parameters linear in the total number of users in the system.

Algorithm 8 is outsider recipient anonymous due to the concatenation of the recipient set to the plaintext message m in step 4 of Publish.

NO REDUNDANCY The broadcast message  $\mathcal{B}$  should only be published once since  $\mathcal{B}$  contains a concatenation of  $w_i$  describing the with IBE encrypted session key k for every recipient i in  $\mathcal{S}$ .

AUTHENTICITY AND INTEGRITY Authenticity and integrity are guaranteed by the authenticated symmetric encryption scheme and the authentication mechanism of the OSN. If the assumptions on the OSN's authentication mechanism hold, only the owner of an OSN profile should be able to actively broadcast messages in name of the corresponding profile identifier  $\mathtt{id}_i$ .

No key escrow and key validation. Key escrow is avoided by the DKG protocol that is part of both the Setup and KeyGen stages of the algorithm. The last verification of the KeyGen step of Algorithm 8 validates the correctness of a users' shares. However, this check does not ensure security against malicious PKGs since the Pedersen protocol [99] is insecure in the presence of malicious PKGs. That is, malicious PKGs can still affect the outcome of certain bits of the shared master secret key  $sk_{msk}$  with non-negligible advantage. To circumvent these issues, the DKG scheme from Gennaro et al. [60] should be implemented. However, since the scheme is developed in a threat model where PKGs are assumed trustworthy, this concern falls out of the scope of this thesis. Implementation of the DKG protocol from Gennaro et al. [60] occurs similar to the scheme from Pedersen [99] since it relies on the same mathematical concepts. Therefore, adapting Algorithm 8 to a more hostile DKG environment should be straightforward.

LIMITED KEY VALIDITY For the sake of clarity, concatenation of expiration dates with public keys is not explicitly included in Algorithm 8. However, with the help of Algorithm 7 this should be trivial since only the interpretation of the identifier symbol  $id_i$  changes from a permanent identifier of a user to only a temporary identifier when concatenated with an expiration date.

The proposed solution can be used in any OSN that assigns unique public identifiers, such as usernames. Since the public keys are represented as strings, users are not required to upload keys to an additional third party server. Distributed key generation solves the key escrow issues that come with IBE solutions.

# 4.4 Summary

We started this chapter with the definition of a security model describing the current OSN situation. With the help of this model, we defined privacy threats in the model along with an adversary definition and assumptions on potential adversaries. In this framework, cryptographic objectives were set that defined the boundaries of our further design decisions. From these design decisions, it followed that a PKG had to be included as an additional entity of the security model. After the presentation of an updated security model Algorithm 8 was developed and evaluated. The result is a scheme that protects against the adversaries from our model and achieves the aforementioned design goals.

We further showed the feasibility of applying Algorithm 8 to existing OSNs by effectively implementing it on an existing OSN. The results of our implementation process are further discussed in Chapter 5.

**Algorithm 8** An outsider recipient anonymous identity-based broadcast encryption scheme

**Setup**( $\lambda$ , t, n): Outputs the public params of the system with respect to the security parameter  $\lambda$ , the number of PKGs n and the threshold t.

- 1. On input of security parameter  $\lambda$  generate a prime q, two groups  $G_1, G_2$  of order q, and an admissible bilinear map  $e: G_1 \times G_2 \to G_T$ . Choose random generators  $P \in G_1$  and  $Q \in G_2$ .
- 2. Choose cryptographic hash functions  $H_1: \{0,1\}^* \to G_1$ ,  $H_2: G_T \to \{0,1\}^l$  and  $H_3: \{0,1\}^l \to \{0,1\}^l$ , such that  $H_1, H_2$  can be modelled as random oracles.
- 3. Each PKG j generates n-1 shares  $\sigma_{jv}$  of a Pedersen VSS scheme by executing DKG. Setup, and redistributing the n-1 shares  $\sigma_{jv}$  with the other v PKGs.
- 4. Each PKG j publishes  $P_{pub}^{(j)} = s_j P$ , s.t.,  $s_j = \sum_{v=1}^n \sigma_{jv}$ .

The master secret key  $sk_{msk} = \sum_{j \in \Lambda} b_j s_j$  for  $b_j = \prod_{z \in \Lambda} \frac{z}{z-j}$  cannot be retrieved unless  $\Lambda$  is a subset of size t different PKG servers. The following parameters are published publicly:

$$params = \{q, G_1, G_2, e, P, Q, H_1, H_2, H_3, t, n, P_{pub}^{(0)}, \dots, P_{pub}^{(n)}\}\$$

KeyGen({PKG<sub>0</sub>,...,PKG<sub>t</sub>}, id<sub>i</sub>): On input of a user id<sub>i</sub> the subset  $\Lambda$  of size t of PKG servers, generates a valid private key for id<sub>i</sub>.

- 1. User with identifier  $id_i$ , authenticates to  $\Lambda$  or all PKGs and sends  $id_i$ .
- 2. Each PKG computes  $Q_{id_i} = H_1(id_i)$ , and  $Q_{priv,id_i}^{(j)} = s_j Q_{id_i}$ , where  $s_j$  is the secret share from PKG j.
- 3. The user  $id_i$  computes the shared public parameter P using the Lagrange coefficients  $b_i$  as follows:

$$P = \sum_{j \in \Lambda} b_j P_{pub}^{(j)}$$
 for  $b_j = \prod_{z \in \Lambda} \frac{z}{z - j}$ 

- 4. All PKGs in  $\Lambda$  return  $Q_{priv, \mathtt{id}_i}^{(j)}$  to the corresponding user  $\mathtt{id}_i$  over a secure channel.
- 5. Each user verifies for each  $Q_{priv,id_i}^{(j)}$  value whether,

$$e\left(Q_{priv, \mathtt{id}_i}^{(j)}, P\right) \stackrel{?}{=} e\left(Q_{\mathtt{id}_i}, P_{pub}^{(j)}\right)$$

Next,  $id_i$  calculates the private key  $sk_{id_i}$  using the Lagrange coefficients  $b_i$  as follows:

$$sk_{\mathtt{id}_i} = \sum_{j \in \Lambda} b_j Q_{priv,\mathtt{id}_i}^{(j)}$$
 for  $b_j = \prod_{z \in \Lambda} \frac{z}{z - j}$ 

In this way, no user or PKG learns the master key  $sk_{msk}$  of the system. This algorithm combines DKG.Reconstruct, IBE.Extract and BE.KeyGen algorithms.

**Publish**(params, S, m): Takes the message m, the subset S of size  $\eta$  and the public parameters params, output a broadcast message B.

- 1. Generate a random symmetric session key  $k \leftarrow \{0,1\}^l$ .
- 2. Choose a random value  $\rho \in \{0,1\}^l$  and compute r as a hash of concatenated values  $r = H_3(\{\rho \parallel k\})$
- 3. For each recipient  $id_i \in \mathcal{S}$ , compute the ciphertext, running the IBE.Encrypt algorithm, as follows.

$$w_i = \rho \oplus H_2\left(g_{\mathtt{id}_i}^r\right) \quad \text{where} \quad g_{\mathtt{id}_i} = e\left(Q_{\mathtt{id}_i}, P_{pub}\right) \in G_T$$

4. Let w be a randomised concatenation, then the authenticated data  $\mathcal{A}$  is computed as

$$\mathcal{A} = \{ \eta \parallel rP \parallel k \oplus H_3 (\rho) \parallel w_1 \parallel w_2 \parallel \dots \parallel w_{\eta} \}$$

$$= \{ \eta \parallel U \parallel v \parallel w \} \text{ for } w = \{ w_1 \parallel w_2 \parallel \dots \parallel w_{\eta} \}$$

And  $\mathcal{M}$  a concatenation of the intended recipient set  $\mathcal{S}$  and the plaintext message m, such that  $\mathcal{M} = \{m \parallel \mathcal{S}\}$ . (BE.Encrypt)

5. Apply authenticated symmetric encryption

$$\langle c, t \rangle \leftarrow \mathbb{E}_k(\mathcal{M}, \mathcal{A})$$

6. The following message is then published in the OSN

$$\mathcal{B} = \{ \mathcal{A} \parallel t \parallel c \}$$

Retrieve(params,  $sk_{id_i}$ ,  $\mathcal{B}$ ): on input of the broadcast message  $\mathcal{B}$  and the private key  $sk_{id_i}$  of user  $id_i$ , reconstruct the plaintext message m. This algorithm comprises the {IBE,BE}.Decrypt algorithms. For each  $i \in \{\}$ 

- 1. Compute  $w_i \oplus H_2\left(e\left(sk_{\mathtt{id}_i}, U\right)\right) = \rho$  for  $sk_{\mathtt{id}_i}$ , and  $v \oplus H_3\{\rho\} = k$
- 2. Set  $r = H_3(\rho, k)$ . Verify  $U \stackrel{?}{=} rP$ . If the check fails, try next  $W_i$  and return to 1.
- 3. Retrieve  $\langle \mathcal{M}, t' \rangle \leftarrow D_k(c, \mathcal{A})$
- 4. Verify whether  $t' \stackrel{?}{=} t \in \mathcal{B}$ , and return m. Otherwise return  $\perp$ .

5

# **Implementation**

To show the viability of our solution, Algorithm 8 is implemented on Facebook, currently the OSN with the largest total number of users on the internet. The user interface of our implementation relies on Scramble, an existing open-source Firefox plugin for broadcast encryption on OSNs.

The structure of this chapter is as follows. The different components in the existing Scramble architecture are highlighted before turning to adaptation of the existing architecture (Section 5.1). Next, a discussion follows on how the practical details of the cryptographic building blocks and parameters from Algorithm 8 are implemented (Section 5.2). Furthermore, the structure of our code along with encountered implementation issues is described (Section 5.3). This is concluded by a performance analysis (Section 5.4) and a list of limitations of our current implementation (Section 5.5).

#### 5.1 Software Architecture

The high level structure of the current Scramble implementation is presented along with the required changes to adapt it for our IBE architecture.

#### 5.1.1 Software Environment

Despite the avoidance of complex third party infrastructures, some software is needed that effectively implements Algorithm 8 in a user-friendly way. Ideally, this is an easy-to-install piece of software that runs as an additional layer on top of the current infrastructure of the OSN user. Therefore, it was chosen to implement Algorithm 8 in the form of a browser extension.

Since Scramble [15] already has a user friendly interface that supports all required use cases to implement encryption on OSNs, it is natural to integrate our IBE scheme into Scramble. Besides from Scramble being open source and lightweight, the most important trigger to modify the existing Scramble code is that it is developed at KU Leuven <sup>1</sup>.

<sup>&</sup>lt;sup>1</sup>The scramble code can be downloaded at https://www.cosic.esat.kuleuven.be/scramble/

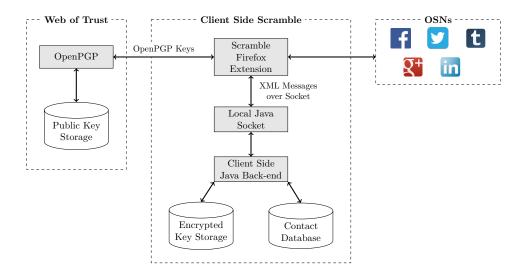


Figure 5.1: Original Scramble Architecture

#### 5.1.2 Existing Environment

Scramble [15] is a Firefox extension that relies on OpenPGP [32] for encryption, access control and key management. Due to the use of OpenPGP, Scramble works independent of the underlying OSN. In fact, Scramble functions as an encryption and decryption tool for any website offering users the possibility to submit content. However, users who want to be part of the recipient set of the uploaded messages need to upload a public key to the OpenPGP network beforehand. The architecture overview of the Scramble environment is illustrated in Figure 5.1.

Since Scramble is a Firefox extension, the user interface (UI) is implemented in Javascript. Although Javascript is ideal for synchronous UIs, it is not the desired programming language for computational demanding tasks such as encryption and decryption. Therefore, Scramble communicates with a back-end in Java that implements all cryptographic operations. Every time a user selects a computation intensive task in the Javascript UI, the Firefox extension sends an XML message requesting the result from the client side Java back-end. The Java back-end processes the request and immediately sends the result back to the UI in another XML message. Sending and receiving of XML messages between Firefox extension and Java back-end, takes place synchronously over a local Java socket listening on an internal port.

Due to Scramble's dependency on OpenPGP for key management, the Firefox extension communicates with a web of trust (Section 3.1.2) storing all public keys of users who subscribed to the OpenPGP network. Since the OpenPGP network stores more keys than a Scramble user needs, Scramble offers the functionality to store public keys from the OpenPGP network locally in a contact database via the client side Java back-end. In addition, the client-side Java back-end has access to an encrypted list of the user's private keys corresponding to public keys that are already part of the OpenPGP network. With the help of a passphrase the Java back-end has access to these private keys to allow decryption of received messages.

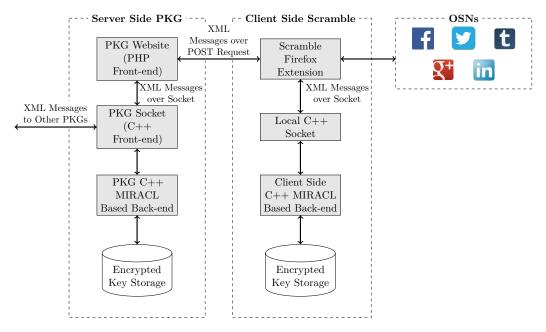


Figure 5.2: New Scramble Architecture

## 5.1.3 Changes to the Existing Environment

The altered Scramble architecture is schematically illustrated in Figure 5.2. Scramble still offers the original OpenPGP functionality as an alternative to our IBE implementation. However, for reasons of conciseness Figure 5.2 omits the original implementation although it coexists with our IBE functionality.

The new client side Scramble architecture implements a C++ based back-end instead of the earlier Java back-end because the most efficient pairing-based multi precision libraries are written in C. In fact only two pairing-based libraries are widely accepted in practical implementations: MIRACL [107] and PBC [2]. MIRACL was preferred over PBC since it is generally faster in its pairing computations. All core algorithms of MIRACL are implemented in C while a C++ wrapper allows object-oriented programming.

The contact database is removed from the original Scramble implementation as illustrated in Figure 5.1 since public keys no longer have to be explicitly stored in the architecture. More specifically, since Scramble can rely on IBE, the public keys are inherently part of the supported OSN. Therefore, the Firefox extension falls back on a number of calls to supported OSN APIs in order to get all public keys of one's connections.

Figure 5.2 exchanges the web of trust from Figure 5.1 for a DKG infrastructure in order to support IBE without key escrow. For clarity, only one PKG is shown since all PKGs will have the same structure. The PKG supports two front-ends: a C++ based front-end and a PHP based front-end.

The C++ based front-end of the PKG only serves as a front-end during execution of the DKG protocol. Negotiation of the shares is implemented over synchronous

sockets. At the startup of the PKG socket, the administrator is asked for a secret passphrase. Then, the sockets start listening on a predetermined port until all shares are correctly negotiated. Once all PKGs have exchanged their shares, the PKG calculates its public parameters and finishes the Setup step from Algorithm 8. The coefficients of the secret polynomial are encrypted with the earlier specified passphrase along with the negotiated secret share. After storage of these secret parameters, the C++ socket starts listening on another port to handle requests from the PHP front-end. Handling of private key extraction requests is multithreaded to handle requests of multiple clients at the same time.

The PHP based front-end receives private key extraction queries from the Scramble Firefox extension in the form of POST requests. The PKG communicates the requested id to the listening C++ socket in the form of an XML message. After the required MIRACL based pairing computations, the PKG socket sends the response back to the PHP webpage such that it is published in the form of an XML message over HTTPS [102].

Note that the new architecture from Figure 5.2 can be applied to virtually any OSN that identifies its users with publicly available identifiers. However, Scramble is made more user friendly by implementing OSN specific API calls. Currently, an implementation for Facebook serves as a proof of concept. Further extension to support other OSNs could be subject of future work.

# 5.2 Implementation Details

The implementation of Algorithm 8 still requires some practical design decisions that are further discussed in this section.

#### 5.2.1 Type of Elliptic Curve

For bilinear pairings, the underlying elliptic curve determines which groups are used for the bilinear pairing  $e: G_1 \times G_2 \to G_T$  and thus the security level of the application. The MIRACL library supports 5 different curves and 6 different security levels. However, the Barreto-Lynn-Scott (BLS) curve [12] is preferred since it provides the highest level of security in MIRACL. BLS curves rely on Ate pairings [73] with an embedding degree of 24. Consequently, BLS curves are considered suitable for a security level of 256 bits.

## 5.2.2 Authenticated Encryption Scheme

An AES-GCM [94] implementation is used for the authenticated encryption scheme in Algorithm 8 since it is one of the more efficient authenticated encryption schemes unencumbered by patents. The AES-GCM implementation as provided by MIRACL relies on authentication tags of 128 bits. Apart from a symmetric key of 128, 192 or 256 bits, AES-GCM also requires an Initialisation Vector (IV). The recommended length of the IV is 96 bits because it can be handled more efficiently [74].

#### 5.2.3 Key Lengths

Since the maximum level of security in MIRACL is determined by the BLS curve, all implemented key lengths in Algorithm 8 follow from the 256 bits security level (l=256). Note that in Step 1 of Retrieve the decryption of a recipient's session key is calculated as:

$$w_i \oplus H_2\left(e\left(sk_{\mathtt{id}_i}, U\right)\right) = \rho$$

followed by

$$v \oplus H_3\{\rho\} = k$$

with

$$H_2: G_T \to \{0,1\}^l$$

Since l=256,  $w_i$  and  $\rho$  are binary sequences of 256 bits. Hence,  $\rho$  only contains sufficient randomness to securely encrypt a session key k of the same length. The full 256 bit k is not completely used for symmetric encryption as the AES-GCM scheme still requires an IV as well. Since the randomness and key freshness of the IV is at least as important as the secrecy of k [49], it was deliberately chosen not to apply key derivation functions to construct a separate symmetric encryption key and IV from the same value k. Therefore, the first 128 bits of k are used as the symmetric key of AES-GCM, while the second 96 bits function as an IV. According to NIST, such practice should ensure confidentiality at least until 2030. However, if a higher level of security should be required, key derivation on k could be considered.

#### 5.2.4 Hash Functions

The hash function  $H_1: \{0,1\}^* \to G_1$  is implemented using the MIRACL function call hash\_to\_group. Hash function  $H_2: G_T \to \{0,1\}^{256}$  relies on the MIRACL hash\_to\_aes\_key function. Both  $H_1$  and  $H_2$  internally fall back on SHA-256 [97]. The MIRACL provided SHA-256 algorithm is used for implementation of the hash  $H_3: \{0,1\}^{256} \to \{0,1\}^{256}$  as well.

## 5.2.5 Generating Random Numbers

Random numbers are generated based on the MIRACL build-in strong random number generator. The provided strong random generator is initialised with a time-of-day value and a binary array of 1024 bits read from /dev/urandom. These values are then used as a seed for the generation of random numbers. The practical implementation of the MIRACL strong random generator is based on an advice published by RSA Laboratories in [90].

#### 5.2.6 Public Key

The decision on which string to use as a public IBE key id is dependent on the underlying OSN. The desired properties for id are the following:

- 1. The public key should uniquely identify the user
- 2. The public key should be mandatory for every user of the social network
- 3. The public key should not change frequently over time
- 4. The public key should be an inherent part of the infrastructure of the social network. That is, the previous three properties are already ensured by the provider of the social network.
- 5. The public key should be publicly available, even to users that are not part of the set of entities with access to the user's profile  $\mathcal{V}_{id}$

In Facebook the best key satisfying these properties is a Facebook username. A Facebook username is ensured to be unique since it is part of a profile's URL, e.g. http://www.facebook.com/profile.name where profile.name functions as id. Moreover, the Facebook policy ensures this username is mandatory for every user and can only be changed once. Lastly, the Facebook username is also public to outsiders using the Facebook API thereby fulfilling all the required conditions for an IBE key in our architecture.

# 5.3 Implemented Code

The complete implementation of our solution can be found at https://bit.ly/ibeforosns. The code is originally developed on OS X 10.9 and compiled with GNU g++ 4.7. Portability to other platforms is currently not supported.

This section briefly overviews the structure of our code and the encountered issues during implementation.

#### 5.3.1 Server Side Implementation

All software code on the server side implements the Setup and KeyGen steps from Algorithm 8.

#### Code Structure

All C++ functions implemented by the server side C++ MIRACL based back-end are illustrated in Figure 5.3. The following classes are defined:

**PKG** is a class providing all functionality to compute the shares from the DKG protocol and to keep track of the current state of the PKG server.

**DKGMessage** represents a message PKGs use to negotiate in the DKG protocol. A DKGMessage has either DKGMessageType P\_MESSAGE or SHARE\_MESSAGE.

share\_t is the definition of a structure containing: the serverId owning the share j = x, the share value  $\sigma_{jv} = y$  and the server who generated the share v = shareGenerator where j, v and  $\sigma_{jv}$  refer to the mathematical symbols used in Algorithm 8.

```
DKGMessage
- P : G2
- int : receiver
- int : sender
- share t : share
- DKGMessageType : type
+ DKGMessageType(int sender, int receiver, G2 P)
+ DKGMessageType(int sender, int receiver,
share_t share)
+ DKGMessage(string xmlString)
+ G2 getP()
+ string printType()
+ int getReceiver()
+ int getSender()
+ share_t getShare()
+ DKGMessageType getType()
+ string toString()
 init(int sender, int receiver, DKGMessageType)
```

```
share_t
+ x : int
+ y : Big
+ shareGenerator : int
```

```
PKG
 lastReceivedShareGenerator: int
- myShares : share_t *
 nbOfShares : int
- P : G2
- pfc : PFC *
 poly : Big *
 portNb: int
 secret : Big
- receivedShares : share_t *
- secret : Big
- serverId : int
-sj: Big
-sjP : G2
- ServerState : state
+ PKG(int serverId, int portNb, int
nbOfShares, int threshold, Big order, PFC
*pfc, G2 P, Big s)
+ PKG(int serverId, int portNb, int
nbOfShares, int threshold, Big order, PFC
*pfc, Bigs)
+ G1 extract(char * id)
+ int getLastReceivedShareGenerator()
+ G2 getP()
+ int getServerId()
+ share_t getShareOf(int serverId)
+ G2 getSiP()
+ ServerState getState()
+ string printState()
+ void setP(G2 P)
+ void setShare(share_t share)
+ void getSharesFrom(vector
<PKG>serverList)
```

Figure 5.3: Class Diagram of Server Side C++ MIRACL Based Back-end

The server side implementation also provides a procedural PKG socket denoted "C++ Front-end" in Figure 5.2. The server code achieves Setup and KeyGen in the following way:

SETUP Every PKG socket initialises the DKG protocol by calling the constructor PKG(int serverId, int portNb, int nbOfShares, int threshold, Big order, PFC \*pfc, Big s) where serverId corresponds to the unique PKG identifier, nbOfShares corresponds to the total number of PKG servers n, threshold is the threshold number of servers t that can construct the shared secret  $sk_{msk}$ , order is the order q of the gap groups  $G_1$  and  $G_2$ , \*pfc is a pointer to a MIRACL pairing-friendly curve object and s corresponds to the uniformly random generated secret  $sk_i$  from the Pedersen DKG protocol in Algorithm 6. Only the PKG socket with serverId = 1 is initialised with the constructor PKG(int serverId, int portNb, int nbOfShares, int threshold, Big order, PFC \*pfc, G2 P, Big s) which requires an additional P value. After initialisation all sockets wait for the PKG with serverId = 1 to send a DKGMessage of type P\_MESSAGE containing the public P value. Once all PKGs have setup their secret polynomial along with the received P value, all PKGs start distributing their shares in ascending order of their serverId values. These DKGMessages are of type SHARE\_MESSAGE and contain a share in the

form of a share\_t structure.

The toString() function of a DKGMessage object allows to serialise a DKGMessage to an XML message that can be sent over the C++ socket infrastructure. At receipt of an XML message the PKG socket calls DKGMessage(string xmlString) to reconstruct the original DKGMessage object.

KEYGEN Once all PKGs have verified their shares, the C++ socket starts listening on another port that communicates with the PKG website as illustrated in Figure 5.2. The Scramble plugin can then publish a POST request to the PKG website in order to receive its secret key. The PKG website forwards this request to the C++ socket in the form of an XML message. The socket replies to this request by executing extract(char \* id) and returning an XML message containing the resulting serialised G1 object.

#### Encountered Issues

MULTITHREADING To ensure the PKG implementation can resist intensive traffic, the extract(char \* id) function is multithreaded. However, multithreading MIRACL requires the complete library to be recompiled. Furthermore, every algorithm relying on elliptic curves should start with the initialisation of a MIRACL PFC object which allocates the required memory resources on the heap. After destruction of this PFC object, no further MIRACL calls can be made. Therefore, every PKG object is initialised with a pointer to a PFC object that is never freed at run-time.

DKG IN THE DISTRIBUTED SETTING The first attempt to construct a DKG protocol was made by altering the implementation from Kate and Goldberg [78]. However, it took us several days to compile the original code on OS X. Furthermore, all obtained executable files were corrupted by segmentation faults. After one intensive week of trial and error still no satisfying results were obtained. Consequently, it was decided to implement our own DKG protocol to show at least the viability of our solution.

DESERIALISING MIRACL OBJECTS MIRACL objects can be transformed to printable strings. However, despite the popularity of MIRACL, originally no functionality for the conversion of strings back to MIRACL objects was provided. Therefore, we introduced additional functions in the MIRACL library that support deserialising objects for use in network communication.

#### 5.3.2 Client Side Implementation

Software code describing the client side implementation achieves the required functionality for the Publish and Retrieve steps from Algorithm 8.

#### Code Structure

All C++ functions implemented by the client side C++ MIRACL based back-end are illustrated in Figure 5.4. The following classes are defined:

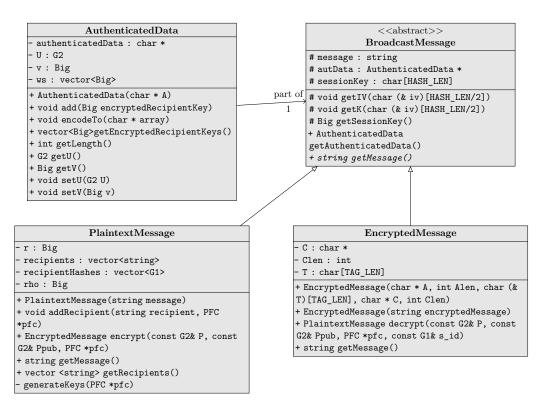


Figure 5.4: Class Diagram of Client Side C++ MIRACL Based Back-end

**AuthenticatedData** describes the data that is authenticated by the AES-GCM implementation. AuthenticatedData corresponds to  $\mathcal{A}$  in Algorithm 8.

**BroadcastMessage** is an abstract class that forms the base class of PlaintextMessage and EncryptedMessage. BroadcastMessage contains properties and functions EncryptedMessage and PlaintextMessage have in common.

**PlaintextMessage** corresponds to a BroadcastMessage as it is constructed by the sender before encryption.

**EncryptedMessage** corresponds to a BroadcastMessage as it is sent over the OSN in encrypted form.

The client side implementation also provides a procedural local C++ socket implementation that relies on the classes from the class diagram in Figure 5.4 to communicate with the Firefox extension, as illustrated in Figure 5.2. The client side code realises Publish and Retrieve as follows:

PUBLISH When a user broadcasts a message, he inputs the desired plaintext message in the Firefox extension and selects the ids of the intended recipients. The Firefox extension sends this data to the C++ back-end via the local C++ socket from Figure 5.2. The C++ socket then initialises a PlaintextMessage object with the help of constructor PlaintextMessage(string message) and adds the recipients with

addRecipient(string recipient, PFC \*pfc). After initialisation, the function getMessage() can return the plaintext message m without the concatenated intended recipient set S. The recipients of a PlaintextMessage can be retrieved with the getRecipients() function. A PlaintextMessage object is encrypted by calling encrypt(const G2& P, const G2& Ppub, PFC \*pfc) where P and Ppub denote the public parameters and \*pfc is a pointer to a MIRACL pairing-friendly curve object. The returned result is an EncryptedMessage object.

RETRIEVE When the local C++ socket receives an XML message containing an encrypted broadcast message, an EncryptedMessage object is initialised with the help of the constructor EncryptedMessage(string encryptedMessage). After object construction, the getMessage() function returns a string of the ciphertext \$\mathcal{B}\$ from Algorithm 8 in base64 encoding [75]. An EncryptedMessage object can be decrypted by calling decrypt(const G2& P, const G2& Ppub, PFC \*pfc, const G1& s\_id) where P and Ppub denote the public parameters, \*pfc is a pointer to a MIRACL pairing-friendly curve object and s\_id is the user's secret key. The returned result is a PlaintextMessage object.

#### Encountered Issues

The most important improvement during the implementation of the client side software code was precomputing the public parameters. MIRACL provides function calls to precompute points in  $G_2$  for multiplication and points in  $G_T$  for exponentiation. Since the public parameters do not change during the lifetime of our infrastructure these parameters only need to be precomputed once. The execution times for the Retrieve step in Table 5.3 are three times as fast than without precomputation.

During the implementation process our code slowly evolved from procedural code to the object oriented code in Figure 5.4. After introduction of the function call decrypt(G2 P, G2 Ppub, PFC \*pfc, G1 s\_id), we noticed very slow decryption times. The reason for the decrease in decryption time is explained by the handling of function arguments in C++. Normally, C++ creates a new object for every function argument. Consequently, the P and Ppub objects lost their internal state along with their precomputed values. This was resolved by altering the function call to decrypt(const G2& P, const G2& Ppub, PFC \*pfc, const G1& s\_id).

# 5.4 Performance Analysis

All performance experiments were conducted on an Intel Core 2.4 GHz i5 processor with 8 Gb of 1600 MHz DDR3L onboard memory. Execution times arise from the aforementioned implementation details applied to Algorithm 8. The results are illustrated in Table 5.1, Table 5.2 and Table 5.3 and further discussed in this section.

#### 5.4.1 Setup

For every PKG v, PKG j needs to compute and communicate an additional share  $\sigma_{jv}$ . Therefore, the execution time of the Setup stage from Algorithm 8 is mainly

Total number of PKGs $n$	Setup Time (ms)
2	66.6
5	112.6
10	116.8
15	123.2
50	142.3

Table 5.1: Performance of the Setup stage in function of the total number of PKGs.

Setup Time (ms)
1175.4
2785.0
5781.2
8625.8
29318.4

Table 5.2: Performance of the KeyGen stage in function of the threshold number of PKGs.

dependent on the total number of PKGs n. Although negligible, the setup stage also contains a dependency on the threshold parameter t since it determines the order of the generated polynomials. However, the execution times listed in Table 5.1 mainly consist of communication overhead due to the synchronous sockets. Since our current implementation is only simulated in a local environment by sockets listening on different ports, setup times are expected to increase when translated to a distributed setting.

## 5.4.2 KeyGen

The larger the threshold t of the DKG protocol, the more PKGs need to be consulted. For every contacted PKG, two additional pairing computations are required due to the check in step 5 of the KeyGen stage in Algorithm 8. The execution times in Table 5.2 primarily consist of these pairing computations in addition to the communication overhead. Analogous to the execution times of the Setup stage, the contribution by communication overhead is expected to increase in a distributed DKG environment.

#### 5.4.3 Publish

Encryption times are linearly dependent on the number of intended recipients since more intensive pairing computations are required for each additional user included in the intended recipient set, as illustrated by Table 5.3.

	Execution 7	Γime (ms)
Number of Recipients	Publish	Retrieve
1	284.5	275.4
10	2564.5	460.9
15	3799.6	560.6
50	12300.5	1237.8
100	25867.7	2260.2

Table 5.3: Performance of the Publish and Retrieve stages in function of the number of intended recipients.

#### 5.4.4 Retrieve

Each recipient has to decrypt  $w_i$  an average of  $\eta/2$  times to retrieve the secret session key k. However, the experiments as shown in Table 5.3 measured the worst-case execution time for the Retrieve stage of Algorithm 8 since the recipient had to decrypt all  $w_i$  values before retrieving k in the last attempt. Only after recovering k, the recipient can decrypt the ciphertext using AES-GCM.

In future optimisations of our current implementation, techniques of randomness reuse should be considered. The concept of randomness reuse as originally proposed by Kurosawa [80] introduces a deterministic component to random elements of a BE scheme such that shorter ciphertexts and computationally more efficient schemes can be achieved. However, randomness reuse should be applied with great care as it can significantly reduce the security level of a scheme. Since randomness reuse depends on the underlying BE scheme, an extensive analysis of the scheme should precede implementation of randomness reuse techniques. Therefore, randomness reuse is currently not included in our implementation.

# 5.5 Current Limitations

The algorithm as it is currently implemented only serves as a proof of concept since it lacks a number of requirements needed for secure use in practice. These aspects were not implemented due to the limited time available. Since all core requirements for the protocol in Algorithm 8 are present, only the aspects for practical usage in more hostile environments are missing. However, including these aspects should be straightforward and is only a matter of implementation instead of deliberate design decisions.

#### 5.5.1 Client Side

Since the IBE scheme is integrated in the existing Scramble UI, our current prototype does not require drastic adaptations to the client side implementation. The major drawback of our IBE proposal is that it makes the Scramble plugin more dependent on the underlying OSN. Consequently, every OSN should be separately integrated

into the Scramble plugin since each OSN offers its own API calls for reading out friend connections. More OSNs than Facebook should be actively supported by the IBE Scramble tool to motivate wide user adaptation of the plugin. However, the open-source license of Scramble motivates tech-savvy users to extend the current implementation for support of their own favourite OSNs.

#### 5.5.2 Server Side

In its present form, the PKG is only simulated in a local environment. Therefore, it suffices to rely on synchronous communication over C++ sockets each listening on a different port. However, before adaption to a world-wide DKG network is possible, the protocol should take more asynchronous aspects into account such as connection-loss, DOS-attacks or undelivered packets. Kate et al. [78] propose a more advanced DKG protocol in the asynchronous setting that could be adapted for our IBE setting.

Since the DKG protocol is currently simulated in a local environment, all PKG sockets communicate their XML messages in plain text. More secure socket protocols should be considered such as SSL [57] for adoption to a more hostile distributed setting.

Furthermore, the current assumptions on the PKGs (Section 4.3.3) are too severe for practical environments. In practice, the current Pedersen DKG scheme [99] is insecure and is better replaced by the one from Gennaro et al. [60]. If all mentioned updates on the current server side scheme are effectively achieved, more relaxed assumptions on the PKG are in place. With less stringent PKG assumptions, the DKG network could even be partially supported by the OSN providers to improve their privacy-friendly image.

#### 5.5.3 Limitations Effecting Both Client and Server

Currently, private key extraction takes the form of a POST request over HTTPS [102]. Although the PKGs publish the response in plain text to their PHP website, the communication is encrypted by a self-signed SSL certificate. Ideally, this certificate is signed by a world-wide trusted CA such that the client-side implementation can effectively verify whether it is communicating with a valid PKG.

Although web communication between the client side Scramble tool and the server side PKG is already encrypted, a client can request the private key parameters for every id since there is no authentication mechanism checking the user's identity. However, Facebook provides third party authentication in its API. If a Facebook login dialogue is integrated in the Scramble UI, the returned Facebook authentication token serves as a proof to the PKG that the requester of the private key resembles the owner of the corresponding Facebook profile.

# 5.6 Summary

In this chapter we summarised the implementation process of applying Algorithm 8 to Facebook in the form of a Firefox extension called Scramble. After an overview of the existing Scramble architecture, adaptations to the existing architecture were proposed to enable implementation of the design from Chapter 4. The multi-precision library MIRACL was used to implement all algebraic computations. In a next section we uncovered how our code was structured and the issues we encountered for both the client and server side of our application. This was followed by a performance evaluation which showed the overhead of our implementation is tolerable for practical usage in OSNs. We concluded the chapter with the limitations of our current proof of concept and proposed how these could resolved straightforwardly.

6

# Conclusion

This last chapter concludes by presenting an overview of the discussed topics along with the achieved research results. Furthermore, we summarise the limitations of our current solution, possible future work and in which other domains our techniques can bring added value.

The minimal additional architectural support and the increased ease of key management represent a major motivation to implement IBE in OSNs. We show that using secret sharing and multi-PKGs there is no need to have a single trusted party, assuming that at most t-1 of the PKGs are compromised. Furthermore, the multiple PKG infrastructure can be maintained by several organisations, motivated by increased privacy in OSNs.

The construction of a practical usable IBE algorithm for OSNs started with the definition of a security model describing all considered entities in the model, possible adversaries and assumptions on these adversaries. The defined model than served as a framework to state cryptographic design goals that were achieved by relying on earlier defined cryptographic building blocks. As a proof of concept, we implemented our solution by extending Scramble for support of our proposed algorithm in Facebook, thereby demonstrating our proposal presents a tolerable overhead to end-users.

The resulting implementation is an architecture in the form of a client side Firefox plugin in combination with a server side PKG implementation that is user friendly, practically applicable and immediately ready to use.

USER FRIENDLY The implementation is more user friendly than previous alternatives since public keys are recognisable user ids. In contrast to the abstract notion of a public key stored and authenticated on a complex public key infrastructure, users can immediately relate owners to their public keys. Since the public keys are unique profile identifiers, users can judge the authenticity of public keys based on the key owner's profile information and connections in the OSN infrastructure. User friendliness is further increased by relying on OSN API calls for key management such that no third party PKI is required.

PRACTICALLY APPLICABLE The presented solution is practically applicable since it requires no changes to the current OSN infrastructure. This enables users to rely on

our solution even in OSN environments that are reluctant to support these forms of increased confidentiality.

Immediately ready to use. Users are no longer required to subscribe to an additional third party infrastructure before being able to send encrypted messages. Therefore, it is possible to share content with users not holding private keys to their identity since the valid public key is directly represented by their id in the OSN. This forces curious users to register if they wish to view the protected content shared with them. Privacy concerned users relying on cryptographic primitives are then no longer an isolated breed limited to communication with other privacy aware peers. Conversely, they serve as pioneers motivating other users in their environment to turn to similar solutions.

However, the presented implementation is only a proof of concept since it is currently only applicable as a Firefox extension on Facebook. We endeavour to obtain a full open source project that supports different browsers and OSNs. Furthermore, the server side implementation of our current solution is only simulated in a local environment. For use in distributed environments such as the internet, more advanced DKG protocols in the asynchronous setting should be considered. Another limitation of the achieved implementation is that it does not include an authentication mechanism with the OSN environment. Before translating our current mechanism to a practical environment, all these limitations should be resolved. However, responding to these issues is only a matter of implementation. Therefore, the current implementation definitely lays the foundation for practical usable IBE on OSNs.

There are some important open challenges that call for further research. Although the execution times achieved by our prototype are tolerable, techniques of randomness reuse probably result in even higher performance gains. In addition, a more formal security discussion of our scheme is desirable and can be subject of future work.

We conclude this work by emphasising the applicability of our current scheme to other domains than broadcasting of messages on OSNs. The presented architecture can be applied to other media than text messages such as photos and videos. Consequently, the algorithm can find adoption in a wider set of OSNs like Youtube, Instagram and Snapchat. The proposed broadcasting scheme is also valuable for e-mail applications with multiple recipients. With the increasing influence of internet on our daily communication, the amount of broadcasting applications is even expected to increase. Consequently, although this thesis covers application of IBE in an OSN environment, it implements the groundwork for many promising features an IBE scheme with multiple PKGs has to offer in future applications.

# Appendices



# Gentry's IBE Scheme

Gentry [61] proposed the first IND-ANO-CCA secure scheme in the standard model. However, the original proposed scheme from Gentry relies on symmetric pairings which are proven less secure than asymmetric pairings in literature [6, 11, 76]. A transformed version of Gentry's scheme to the asymmetric setting can be found in Algorithm 9.

For reasons of conciseness, it was decided to rely on multiplicative notation in the gap groups as well, although this is in contrast with the additive convention used in the remainder of this thesis.

The correctness of the transformed scheme in Algorithm 9 can be proven as follows.

$$\begin{split} e\left(T, U_{\mathrm{id},2}U_{\mathrm{id},3}^{\beta}\right) V^{r_{\mathrm{id},2}+r_{\mathrm{id},3}\beta} \\ &= e\left(P_{1}^{s(\alpha-\mathrm{id})}, \left(U_{2}U_{3}^{\beta}\right)^{\frac{1}{\alpha-\mathrm{id}}} Q_{2}^{\frac{-\left(r_{\mathrm{id},2}+r_{\mathrm{id},3}\beta\right)}{\alpha-\mathrm{id}}}\right) e\left(P_{1}, Q_{2}\right)^{s\left(r_{\mathrm{id},2}+r_{\mathrm{id},3}\beta\right)} \\ &= e\left(P_{1}^{s(\alpha-\mathrm{id})}, \left(U_{2}U_{3}^{\beta}\right)^{\frac{1}{\alpha-\mathrm{id}}}\right) = e\left(P_{1}, U_{2}\right)^{s} e\left(P_{1}, U_{3}\right)^{s\beta} \end{split}$$

Thus, the check passes. Moreover, as in the ANO-IND-CPA scheme,

$$e\left(T,U_{\mathrm{id}}\right)V^{r_{\mathrm{id},1}}=e\left(P_{1}^{s\left(\alpha-\mathrm{id}\right)},U_{1}^{\frac{1}{\alpha-\mathrm{id}}}Q_{2}^{\frac{-r_{\mathrm{id},1}}{\alpha-\mathrm{id}}}\right)e\left(P_{1},Q_{2}\right)^{sr_{\mathrm{id},1}}=e\left(P_{1},U_{1}\right)^{s},$$

as required.

## Algorithm 9 Gentry's asymmetric IBE Scheme [61]

Let  $G_1, G_2$  and  $G_T$  be groups of order p and let  $e: G_1 \times G_2 \to G_T$  be the bilinear map. The IBE system works as follows.

**Setup:** The PKG picks random generators  $P_1, g_1 \in G_1$ , generators  $Q_2, U_1, U_2, U_3 \in G_2$  and a random  $\alpha \in \mathbb{Z}_p$ . It sets  $g_1 = P_1^{\alpha} \in G_1$ . It chooses a hash function  $H_1$  and  $H_2 : \{0,1\}^* \to \{0,1\}^n$  from a family of universal one-way hash functions. The public *params* and private *masterkey* are given by

$$params = (P_1, Q_2, U_1, U_2, U_3, H_1, H_2)$$
  $masterkey = \alpha$ 

**KeyGen:** To generate a private key for identity  $id \in \mathbb{Z}_p$ , the PKG generates random  $r_{id,i} \in \mathbb{Z}_p$  for  $i \in \{1,2,3\}$ , and outputs the private key

$$d_{id} = \{(r_{id,i}, U_{id,i}) : i \in \{1, 2, 3\}\}, \text{ where } U_{id,i} = \left(U_i Q_2^{-r_{id,i}}\right)^{\frac{1}{\alpha - id}} \in G_2$$

If  $id = \alpha$ , the PKG aborts. As before, we require that the PKG always use the same random values  $\{r_{id,i}\}$  for id.

**Encrypt:** To encrypt  $m \in \{1,0\}^n$  using identity  $id \in \mathbb{Z}_p$ , the sender generates random  $s \in \mathbb{Z}_p$ , and sends the ciphertext

$$C = \left(g_1^s P_1^{-s \cdot \text{id}}, \ e(P_1, Q_2)^s, \ m \oplus H_2\left(e(P_1, U_1)^s\right), \ e(P_1, U_2)^s e(P_1, U_3)^{s\beta}\right)$$
$$= (T, V, w, Y)$$

Note that  $T \in G_1, V \in G_T, w \in \{1,0\}^n$  and  $Y \in G_T$ . We set  $\beta = H_1(\{T \mid V \mid w\})$ . Encryption does not require any pairing computations once  $e(P_1, Q_2)$ , and  $\langle e(P_1, U_i) \rangle$  have been pre-computed or alternatively included in *params*.

**Decrypt:** To decrypt ciphertext  $C = \{T \mid V \mid w \mid Y\}$  with id, the recipient sets  $\beta = H_1(\{T \mid V \mid w\})$  and tests whether

$$Y = e\left(T, U_{\mathrm{id}, 2}U_{\mathrm{id}, 3}^{\beta}\right)V^{r_{\mathrm{id}, 2} + r_{\mathrm{id}, 3}\beta}$$

If the check fails, the recipient outputs  $\perp$ . Otherwise, it outputs

$$m = w \oplus H_2\left(e\left(T, U_{\mathtt{id},1}\right) V^{r_{\mathtt{id},1}}\right)$$

B

# Nederlandse Samenvatting

Online sociale netwerken nemen een steeds prominentere plaats in ons dagelijks leven als communicatienetwerk. Desondanks, bieden de door het Online Sociaal Netwerk (OSN) aangeboden privacy instellingen vaak onvoldoende bescherming voor de toevertrouwde data. Gebruikers kunnen opnieuw zelf bepalen wie er toegang krijgt tot hun data door cryptografische technieken toe te passen.

In klassieke cryptografische systemen genereren gebruikers een private sleutel waarvan een publieke sleutel wordt afgeleid. De veiligheid van dergelijke systemen wordt gewaarborgd doordat het rekenkundig onhaalbaar is om in omgekeerde zin de private sleutel van de publieke sleutel af te leiden. Een publieke sleutel infrastructuur publiceert vervolgens de publieke sleutels van alle gebruikers. Bijgevolg kunnen gebruikers die nooit eerder communiceerden alsnog vertrouwelijke berichten uitwisselen door deze te encrypteren met elkaars publieke sleutel. Enkel de eigenaar van de private sleutel is vervolgens in staat om de berichten te decrypteren zodat de oorspronkelijke inhoud weer zichtbaar wordt.

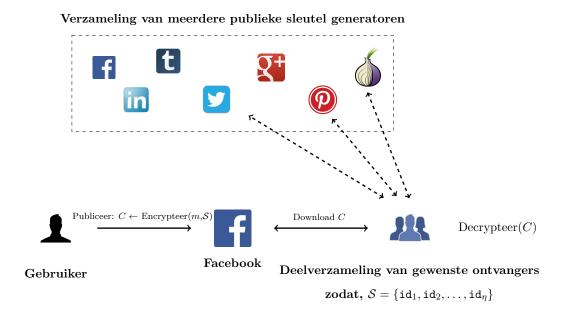
Bestaande tools voor OSNs hebben echter moeite om algemeen aanvaard te worden bij gebruikers vanwege lage gebruiksvriendelijkheid en ingewikkeld beheer van cryptografische sleutels. Gebruikers kunnen immers moeilijk bewust kiezen wat geschikte sleutellengtes zijn of welke sleutels te vertrouwen zijn, zonder kennis van cryptografische primitieven.

In deze thesis, suggereren we een praktische oplossing die gebruik maakt van identiteitsgebaseerde encryptie om sleutelbeheer te vereenvoudigen en confidentialiteit op een OSN te waarborgen. Identiteitsgebaseerde encryptie laat immers toe om als publieke sleutel een herkenbare woordsequentie te nemen die de gebruiker uniek identificeert. Op die manier wordt meteen duidelijk wie de eigenaar is van de betreffende publieke sleutel waardoor complexe publieke sleutelinfrastructuren overbodig worden.

Het nadeel van identiteitsgebaseerde encryptie is echter dat de private sleutel gegenereerd wordt door een publieke sleutel generator die bijgevolg volledig dient vertrouwd te worden. De publieke sleutel generator is immers in staat om vertrouwelijke berichten te decrypteren vermits hij de private sleutel van de ontvanger kent.

Door private sleutels op gedistribueerde wijze te genereren over verschillende

publieke sleutel generatoren, bezit elke generator slechts een deel van de gebruikers' private sleutel. Samenwerkende publieke sleutel generatoren kunnen dan geen informatie afleiden over de private sleutels zolang hun aantal geen drempelwaarde t overschrijdt. De confidentialiteit van de onderhandelde private sleutels wordt gegarandeerd zolang de verschillende generatoren geen motivatie hebben om samen te werken in deze architectuur.



Figuur B.1: Overzicht van een opstelling waarin meerdere OSNen een (n,t)-gedistribueerd publiek sleutel protocol aanbieden op basis van identiteitsgebaseerde encryptie. Een bericht m wordt gepubliceerd op Facebook voor een deelverzameling  $\mathcal S$  van ontvangers voor t=3. Het gedistribueerd sleutel protocol kan door elke organisatie ondersteund worden met een motivatie om de privacy op sociale netwerken te waarborgen.

Figuur B.1 toont een mogelijke opstelling in dewelke OSNen zelf de ondersteuning van de publieke sleutel generatoren verzorgen. Indien OSNen collectief hun gebruikersaantal zien dalen omwille van een slechte privacy policy, kan het een motivatie zijn om een dergelijke infrastructuur aan te bieden. Zeker in het kader van recente bekendmakingen van Edward Snowden over het spionageprogramma van de NSA, hebben OSNen elke motivatie om hun data te beschermen. Hoewel de OSNen bij een dergelijke opstelling geen gerichte reclame meer kunnen aanbieden, hebben ze er alle baat bij dat hun totaal gebruikersaantal niet verder afneemt. Doordat nooit meer dan t rivaliserende OSN providers geneigd zijn om hun deel van de private sleutel bekend te maken, wordt de veiligheid van de opstelling gegarandeerd. Bemerk dat de publieke sleutel generatoren ook ondersteund kunnen worden door gesubsidieerde onderzoeksinstellingen of verschillende overheden.

Geïnspireerd door het voorgaande, werken we aan de hand van identiteitsge-

baseerde encryptie een algoritme uit dat toelaat om versleutelde informatie te delen met meerdere gebruikers zonder hun identiteit aan de buitenwereld te onthullen. De oplossing laat toe om versleutelde informatie te versturen aan gebruikers die nog niet expliciet hebben ingetekend om deel uit te maken van een dergelijke infrastructuur. Ten slotte, tonen we de haalbaarheid van onze oplossing aan door een open-source prototype te ontwikkelen dat praktisch bruikbaar is op Facebook en eenvoudig te veralgemenen valt naar andere bestaande OSNen.

# Appendix



# English Paper

1

# Practical Identity Based Broadcast Encryption for Online Social Networks

Stijn Meul, Filipe Beato, Bart Preneel and Vincent Rijmen

Abstract—Nowadays Online Social Networks (OSNs) constitute an important and useful communication channel. At the same time, coarse-grained privacy preferences protect the shared information insufficiently. Cryptographic techniques can provide interesting mechanism to protect privacy of users in OSNs. However, this approach faces several issues, such as, OSN provider acceptance, user adoption, key management and usability. We suggest a practical solution that uses Identity Based Encryption (IBE) to simplify key management and enforce confidentiality of data in OSNs. Moreover, we devise an outsider anonymous broadcast IBE scheme to disseminate information among multiple users, even if they are not using the system. Finally, we demonstrate the viability and tolerable overhead of our solution via an open-source prototype.

Index Terms—identity-based encryption (IBE), broadcast encryption (BE), distributed key generation (DKG), online social networks (OSNs).

#### I. INTRODUCTION

NLINE SOCIAL NETWORKS (OSNS) such as Facebook, Google+, and Twitter are increasingly being used and have become a prominent communication channel for many millions of users. OSNs offer users an efficient and reliable channel to distribute and share information. At the same time, OSNs store large amounts of data which prompts several privacy concerns. In particular, it is possible to infer a considerable amount of sensitive information from the shared and stored content. Currently, users are allowed to configure "privacy preferences" in order to limit and select which users or groups can access the shared content. These preferences are generally too coarse-grained and difficult to configure [1]. Another problem is that these preferences do not exclude the provider along with the dangers of data leaks [2] nor external governments [3].

Stijn Meul June 6, 2014

#### A. Problem Statement

All these worrisome issues motivate the need for effective techniques to properly protect user's privacy in OSNs. Several solutions have been proposed and advocated to use cryptographic mechanisms in order to address the privacy issues, either by an add-on atop of existing OSNs [4], [5], [6], [7], or by complete new privacy-friendly architectures [8], mainly decentralized [9], [10]. In general, those solutions suffer from user adoption and key management issues as users are required to register and then share, certify and store public keys [11]. Completely new architectures represent a difficult step for users as the trade off of moving away from the commonly used

social ecosystem compared with the risk of losing interactions is high. Arguably, current centralized OSNs are here to stay and will continue to be actively used by millions of people. In light of recent events, such as Edward Snowden's whistle-blowing on US surveillance programs [3], OSN providers have all interest to maintain their users and a privacy-friendly image. Hence, it is important to protect user's sharing information and the recipient set as it can contain private and sensitive information to the user.

#### B. Main Idea

Identity Based Encryption (IBE) [12] solutions overcome the key management problem as the public key of the user can be represented by any valid string, such as the email, unique id and username. Therefore, by using a OSN username any savvy and concerned user can share encrypted content with other users who are not using the solution, thereby motivating curious ones to use the system as well. Nevertheless, IBEbased systems require a trusted central Private Key Generator (PKG) server to generate the private parameters for each user based on a master secret. Consequently, such an architecture only shifts the trusted party from the OSN to the PKG. However, this problem can be mitigated if the master secret is divided among multiple PKGs following a Distributed Key Generation (DKG) [13] protocol based on Verifiable Secret Sharing (VSS) [14]. A DKG protocol allows n entities to jointly generate a secret requiring that a threshold t of the nentities does not get compromised. In fact, each entity holds only a share of the master secret, that can be reconstructed by at least t shares.

Many OSN users are not only represented on a single OSN but on several, thus, can also hold multiple public keys. Moreover, the multi-PKG setting could be supported and maintained by several existing OSNs. In particular, collaboration between OSN providers that compete along is assumed to be a difficult task and orthogonal to their economical business model. Figure 1 depicts an overview example of the proposed model, where a user authenticates to *t*-PKGs of his choice using, e.g., a similar token as in open id protocols, to retrieve his private key. This action can be performed after the reception of encrypted content as a consequence of user curiosity. The PKG servers can also be represented by governmental entities from different continents or subsidised research institutions, with no incentives to collaborate nor overcome more powerful adversaries using legal measures [15] among at least *t*-PKGs.

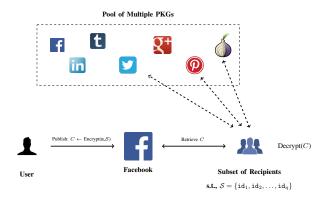


Fig. 1. Multiple (n,t)-PKG IBE for OSNs overview, for a message m published for the set  $\mathcal S$  for t=3.

#### C. Contribution:

In this paper, we propose a novel practical solution that uses IBE with multiple untrusted PKGs atop of current OSNs. We highlight the fact that those multi-PKGs can be supported by several existing OSNs under the business competition assumption, and motivated by the possible attractive incentives towards more privacy concerned audience. Along with the multi-PKG IBE model we devise an IBE broadcast encryption protocol to support multiple recipients. Using a broadcast IBE-based mechanism we allow users to share content with multiple recipients, even if they are not using the system, and, thus, enforce confidentiality of the data while hiding the recipient set. Finally, we implemented our solution on top of the Scramble Firefox extension [5], and show that only a small overhead is required.

#### D. Roadmap:

The remainder of this paper is organized as follows. Section II gives a brief overview of the cryptographic background. Next, Section III presents the model followed by the description of the suggested solution in Section IV. Section V describes the implementation details, while Section VI reviews related work. Finally, Section VII summarizes and concludes the paper.

## II. BACKGROUND

In this section we briefly overview the cryptographic tools and building blocks used in this paper. For ease of explanation we omit the definitions of the underlying cryptographic primitives. This section can, however, be skipped with no loss of continuity.

#### A. Identity Based Encryption

The concept of Identity Based Encryption (IBE) was introduced by Shamir [12], with the main idea of using any string as the public key. IBE requires no certificates as users can rely on publicly known identifiers such as an e-mail address or a telephone number, thus, reducing the complexity of establishing and managing a public key infrastructure. Boneh

and Franklin propose the first practical IBE using bilinear pairings [16], later extended by Gentry [17].

A generic IBE scheme is composed of four randomized algorithms:

## IBE.Setup:

On the input of a security parameter  $\lambda$ , outputs a master secret s and the master public parameters params.

#### IBE.Extract:

Takes the public parameters params, the master secret s, and an id and returns the private key  $d_{id}$ .

#### IBE.Encrypt:

Returns the encryption C of the message  ${\tt m}$  on the input of the params, the id, and the arbitrary length message  ${\tt m}$ .

#### IBE.Decrypt:

Reconstruct mfrom C by using the secret  $d_{id}$ .

The IBE.Setup and IBE.Extract algorithms are executed by a trusted Private Key Generator (PKG) server, whereas IBE.Encrypt and IBE.Decrypt are performed by two players, e.g., Alice and Bob. Consequently, key escrow is performed implicitly in the classic IBE scheme as the PKG holds the master secret key.

#### B. Anonymous Broadcast Encryption

Broadcast encryption (BE) was introduced by Fiat and Naor [18], as a public-key generalization to a multi user setting. A BE scheme allows a user to encrypt a message to a subset  $\mathcal{S}$  of users, such that, only the users in the set  $\mathcal{S}$  are able to decrypt the message. The computational overhead of the BE is generally bound to the ciphertext and the number of recipients. To overcome this issue, the set  $\mathcal{S}$  of recipients is generally known. Barth et al. [19] and Libert et al. [20] extended the notion of BE and introduced the notion of Anonymous Broadcast Encryption (ANOBE) scheme, where the recipient set  $\mathcal{S}$  remains private even to the members in the set. Fazio and Perera [21] suggested the notion of outsider anonymous BE that represents a more relaxed notion of ANOBE.

A generic BE and ANOBE scheme consists of four randomized algorithms:

#### BE.Setup:

On the input of a security parameter  $\lambda$ , generates the public parameters params of the system.

#### BE.KeyGen:

Returns the public and private key (pk, sk) for each user according to the params.

BE.EnTakesp the set  $S = \{pk_i \dots pk_{|S|}\}$  along with the secret message m and generates C.

#### BE.Decrypt:

Reconstructs m from C using the private key  $sk_i$  if the corresponding public key  $pk_i \in S$ . Otherwise, return  $\bot$ .

Note that the pk can be represented by the id value from the IBE scheme.

#### C. Distributed Key Generation

Distributed Key Generation (DKG) was introduced by Pedersen [13] to allow a group of entities to collaboratively setup a secret sharing environment over a public channel. Secret sharing was introduced by Shamir [22] and consists of dividing a secret s into n shares among n entities, such that, only a subset of size greater than or equal to a threshold t can reconstruct s, where  $t \geq n$ . In practice, a random secret s is generated along with a polynomial f(x) of degree t-1 such that f(0) = s, where the shares  $s_i$  are represented by different points on the polynomial. Any entity with t or more shares can reconstruct f(x) using Lagrange interpolation, and subsequently find s. Further, Chor et al. [14] suggested a Verifiable Secret Sharing (VSS) scheme to allow anyone to verify that the right shares are used. The scheme was extended by Feldman [23] and Pedersen [13].

For multiple parties to jointly generate a secret sharing s, all entities are required to participate in a DKG scheme. Each entity i involved generates a different  $s_i$  and  $f^i(x)$ , and later on distributes and verifies the shares  $s_{ij}$ . Hence, a generic DKG does not require a trusted party, as the master secret is computed as the sum of all the polynomials and can only be retrieved by joining t shares. A generic DKG protocol consists of two phases:

DKG.Setup:

Every entity i generates a random secret  $\mathbf{s}_i$  and computes a polynomial of degree t-1. The entity i Distributes a valid share  $s_{ij}$  over all the other j entities, along with the commitment to the share. Each entity j verifies the shares and computes the new share  $s_j = \sum_i s_{ij}$ . The master secret is unknown by each party, and composed by the origin point on the sum of all polynomials  $f^i(x)$ .

DKG.Reconstruct:

Each entity i broadcasts its share  $s_i$ , and with  $t \le n$  shares, one can reconstruct the master secret s.

The DKG protocol is secure assuming that no adversary is able to corrupt t parties or more.

#### III. MODEL

We consider that a user u to be a member of an OSN, such as Facebook, Twitter or Google+. Such u is connected with other users in the same OSN by a friendship relation with who shares information [24]. Inherently, u aims to interact and share information  $\mathbf{m}$  with other users. Each user holds a public and private key pair which is given by an IBE identity server (composed of multiple PKG servers), such that the public key is represented by the id of the user in the OSN. Note that each user can be registered into multiple OSNs and hold different public keys and ids. We assume that the authentication between the user and the identity servers is done using a token similarly to open id, and performed under an authenticated channel, e.g., TLS.

a) Threat Model:: We consider an adversary to be any entity attempting to passively access the shared information m by monitoring the sharing channel but with no motivational incentive to tamper with the content. This can be any curious

user in the OSN, the OSN provider or even a government agency [3]. Such an adversary should not learn the content nor the identity of the members in the recipient set  $\mathcal{S}$ , otherwise we consider that the adversary breaks confidentiality and the outsider recipient anonymity of the protocol as defined in [21]. In addition, we assume that such an adversary cannot compromise more than t identity servers. Furthermore, we stress that such adversary cannot control the user computing environment. Also, it is hard to protect against a malicious recipient who copies or forwards shared content. In this case, we say that such recipient breaks the social contract. We stress that we offer no protection against traffic analysis or timing attacks.

b) Goals:: We aim to protect OSN users' privacy by ensuring confidentiality, data integrity and outsider recipient anonymity [21]. In this way we allow users to enforce access control without having to rely on the privacy preferences offered by the OSN. At the same time, we aim at limited modifications to the OSN environment. In particular, we require as little effort as possible and prior knowledge from users in order to achieve a user-friendly scheme as defined by Balsa et al. [11]. In contrast to previous solutions, users are allowed to be in the recipient set by default.

#### IV. PRACTICAL IBE FOR OSNS

In this section, we describe our system. The proposed solution is based on the IBE scheme from Boneh et al. [16] and a relaxed version of the broadcast scheme from Libert et al. [20]. Further, the system relies on a DKG protocol as described by Pedersen [13] to bootstrap multiple PKGs. In addition, we converted the schemes from using Type 1 (i.e.,  $\mathbb{G}_1 = \mathbb{G}_2$ ) to Type 3 (i.e.,  $\mathbb{G}_1 \neq \mathbb{G}_2$ ) pairings for efficiency [25] and because Type 1 pairings are no longer secure according Joux in [26].

#### A. Basic Scheme

Let  $\lambda$  be the security parameter for a security level of l bits, and  $\mathcal S$  the set of desired recipients  $u_i$  with corresponding  $\mathrm{id}_i$ , such that  $\mathcal S=\{u_1,..,u_\eta\}$  where  $\eta=|\mathcal S|$ . Let  $\mathcal G$  be a generator that satisfies the Bilinear Diffie-Helman (BDH) assumption, and  $e:\mathbb G_1\times\mathbb G_2\to\mathbb G_T$  the bilinear map such that  $e(aP,bQ)=e(P,Q)^{ab}$  for  $P\in\mathbb G_1,Q\in\mathbb G_2$  and  $a,b\in\mathbb Z_q$  as in [16] . In addition, let  $\{C,T\}\leftarrow \mathrm E_k(M)$  be any secure authenticated symmetric encryption that takes as input the plaintext M and generates ciphertext C and authentication tag T as output [27]. Similarly,  $\{M,T\}\leftarrow \mathrm D_k(C)$  be the valid authenticated decryption that takes ciphertext C as input and computes the plaintext M along with an authentication tag T. Our scheme for OSNs is composed by five randomized algorithms: Setup, KeyGen, Publish, and Retrieve.

Setup  $(\lambda, t, n)$ :

Outputs the public params of the system with respect to the security parameter  $\lambda$ , the number of PKGs n and the threshold t.

1) On input of security parameter  $\lambda$  generate a prime q, two groups  $G_1, G_2$  of order q, and

an admissible bilinear map  $e: G_1 \times G_2 \to G_T$ . Choose random generators  $P \in G_1$  and  $Q \in G_2$ .

- 2) Choose cryptographic hash functions  $H_1: \{0,1\}^* \to G_1, \ H_2: G_T \to \{0,1\}^l \ \text{and} \ H_3: \{0,1\}^l \to \{0,1\}^l \ \text{such that,} \ H_1, H_2 \ \text{can be modelled as random oracles.}$
- 3) Each PKG j generates n-1 shares  $\sigma_{jv}$  of a Pedersen VSS scheme by executing DKG. Setup, and redistributing the n-1 shares  $\sigma_{jv}$  with the other v PKGs.
- 4) Each PKG j publishes  $P_{pub}^{(j)} = s_j P$ , s.t.,  $s_j = \sum_{v=1}^n \sigma_{jv}$ .

The master secret key  $msk = \sum_{j \in \Lambda} b_j s_j$  for  $b_j = \prod_{z \in \Lambda} \frac{z}{z-j}$  cannot be retrieved unless  $\Lambda$  is a subset of size t different PKG servers. The following parameters are published publicly:

$$params = \{q, G_1, G_2, e, P, Q, H_1, H_2, H_3, t, n, P_{pub}^{(0)}, \dots, P_{pub}^{(n)}\}$$

KeyGen( $\{PKG_0, \ldots, PKG_t\}, id_i$ ):

On input of a user  $id_i$  the subset  $\Lambda$  of size t of PKG servers, generates a valid private key for  $id_i$ .

- 1) User with identifier  $id_i$ , authenticates to  $\Lambda$  or all PKGs and sends  $id_i$ .
- 2) Each PKG computes  $Q_{\mathtt{id}_i} = H_1(\mathtt{id}_i)$ , and  $Q_{priv,\mathtt{id}_i}^{(j)} = s_j Q_{\mathtt{id}_i}$ , where  $s_j$  is the secret share from PKG j.
- 3) The user  $id_i$  computes the shared public parameter P using the Lagrange coefficients  $b_j$  as follows:

$$P = \sum_{j \in \Lambda} b_j P_{pub}^{(j)} \quad \text{for} \quad b_j = \prod_{z \in \Lambda} \frac{z}{z - j}$$

- 4) All PKGs in  $\Lambda$  return  $Q_{priv, {\bf id}_i}^{(j)}$  to the corresponding user  ${\bf id}_i$  over a secure channel.
- 5) Each user verifies for each  $Q_{priv,id_i}^{(j)}$  value whether,

$$e\left(Q_{priv,\mathtt{id}_{i}}^{(j)},P\right)\overset{?}{=}e\left(Q_{\mathtt{id}_{i}},P_{pub}^{(j)}\right)$$

Next,  $id_i$  calculates the private key  $s_{id_i}$  using the Lagrange coefficients  $b_i$  as follows:

$$s_{\mathtt{id}_i} = \sum_{j \in \Lambda} b_j Q_{priv,\mathtt{id}_i}^{(j)} \quad \text{for} \quad b_j = \prod_{z \in \Lambda} \frac{z}{z - j}$$

In this way, no user or PKG learns the master key msk of the system. This algorithm combines DKG.Reconstruct, IBE.Extract and BE.KeyGen algorithms.

#### Publish (params, S, m):

Takes the message m, the subset S of size  $\eta$  and the public parameters params, output a broadcast message B.

1) Generate a random symmetric session key  $k \leftarrow \{0,1\}^l$ .

- 2) Choose a random value  $\rho \in \{0,1\}^l$  and compute r as a hash of concatenated values  $r = H_3\left(\{\rho \mid \mid k\}\right)$
- For each recipient id<sub>i</sub> ∈ S, compute the ciphertext, running the IBE. Encrypt algorithm, as follows.

$$\begin{array}{ll} w_i = & \rho \oplus H_2\left(g^r_{\mathrm{id}_i}\right) \\ & \mathrm{where} & g_{\mathrm{id}_i} = e\left(Q_{\mathrm{id}_i}, P_{pub}\right) \in G_T \end{array}$$

4) Let w be a randomised concatenation, then the authenticated data  $\mathcal{A}$  is computed as

$$\begin{array}{lcl} \mathcal{A} & = & \left\{ \eta \parallel rP \parallel k \oplus H_3\left(\rho\right) \parallel w_1 \parallel \ldots \parallel w_\eta \right\} \\ & = & \left\{ \eta \parallel U \parallel v \parallel w \right\} \\ & & \text{for} & w = \left\{ w_1 \parallel w_2 \parallel \ldots \parallel w_\eta \right\} \end{array}$$

And  $\mathcal{M}$  a concatenation of the intended recipient set  $\mathcal{S}$  and the plaintext message m, such that  $\mathcal{M} = \{m \parallel \mathcal{S}\}$ . (BE.Encrypt)

5) Apply authenticated symmetric encryption

$$\langle c, t \rangle \leftarrow \mathtt{E}_k(\mathcal{M}, \mathcal{A})$$

 The following message is then published in the OSN

$$\mathcal{B} = \{ \mathcal{A} \parallel t \parallel c \}$$

Retrieve (  $params, s_{\mathtt{id}_i}, \mathcal{B}$  ) :

on input of the broadcast message  $\mathcal{B}$  and the private key  $s_{\mathtt{id}_i}$  of user  $\mathtt{id}_i$ , reconstruct the plaintext message m. This algorithm comprises the  $\{\mathtt{IBE},\mathtt{BE}\}$ . Decrypt algorithms. For each  $i \in \{\}$ 

- 1) Compute  $w_i \oplus H_2\left(e\left(s_{\mathtt{id}_i}, U\right)\right) = \rho$  for  $s_{\mathtt{id}_i}$ , and  $v \oplus H_3\{\rho\} = k$
- 2) Set  $r = H_3(\rho, k)$ . Verify  $U \stackrel{f}{=} rP$ . If the check fails, try next  $W_i$  and return to 1.
- 3) Retrieve  $\langle \mathcal{M}, t' \rangle \leftarrow D_k(c, \mathcal{A})$
- 4) Verify whether  $t' \stackrel{?}{=} t \in \mathcal{B}$ , and return m. Otherwise return  $\perp$ .

#### B. Evaluation

Our solution achieves confidentiality, integrity and outsider recipient anonymity as in [19], [16], [21], because the session key can only be obtain if the recipient holds the corresponding secret key  $d_{\mathrm{id}_i}$  and as a consequence of the authenticated encryption. Our solution can also be used in any OSN that assigns unique public ids, such as usernames. As the public keys are represented as strings users are not required to upload keys to an additional third party server. The DKG approach solves the key escrow issues that come with IBE solutions.

In terms of efficiency, users are required to decrypt  $W_i$  on average  $O\left(n/2\right)$  before obtaining the symmetric key k. Both Barth et al. [19] and Libert et al. [20] propose using a tag based system to hint users where their symmetric key can be found. However, as a design choice we deliberately decided to not implement such property in the scheme as it introduces a linear dependency from extra public parameters to the users, i.e., there are extra public parameters that need to be shared

and verified. Using IBE allows any user in the OSN to be part of the recipient set S before registering in the system. In addition, users can reuse (a hash of) the same symmetric key k during the comments and discussion phase. If the users opt not to reuse k they can still encrypt a fresh session key to all recipients in S using k.

In contrast to classic public key infrastructure, if a public key in IBE is revoked, the user would no longer be able to use that identifier for encryption, e.g., Facebook id. Therefore, to support revocation an expiration date is concatenated to the identifier [16].

For the multi-PKG setting, a user is able to detect malicious behavior from the public commitments of the Pedersen VSS [13]. It is also required that at least t from n PKGs do not get compromised, thus, the higher threshold t the higher the level of security. In case the OSN providers would maintain the PKG infrastructure, one could rely on the assumption that direct business competitors do not collude nor get legally coerced. Furthermore, the authentication and identity verification to the different servers can be done via, for instance, an open id token. This token is generated as a proof of identity by any of the OSN providers.

#### V. PRACTICALITIES

To demonstrate the viability of our solution, we implemented a proof-of-concept prototype of the distributed identity based broadcast encryption scheme for OSNs.<sup>1</sup> In this section, we discuss the implementation details and the performance results of the cryptographic blocks.

c) Implementation:: For the client component we modified the cryptographic library from Scramble [5] as it is an available open source privacy preserving project. In addition, Scramble is implemented as a Firefox Extension compatible with Firefox 14+, but as it is written in simple Javascript it could easily be ported to other browsers, e.g., Chrome. We implemented the multiple PKG servers in PHP. The bilinear pairing and cryptographic blocks for the PKG and the client component are implemented using the multi-precision MIRACL library [28]. To overcome the limitation of accessing binary code from a browser extension implementation, a local client-server socket implementation was used to perform the cryptographic requests to the developed scheme using the MIRACL library. For the DKG protocol we implemented a primitive version of Pedersen's DKG protocol [29] to generate the collective master secret key for the (n, t)-PKG servers. Adaption to the asynchronous setting could be done with the available implementation from Kate and Goldberg [30], [31]. AES-GCM [27] was used for the authenticated encryption. For the public key the Facebook username was used, i.e., id = facebook.com/user.name.

d) Performance:: Experiments were conducted on a Intel Core 2.4 GHz i5 processor with 8 Gb of 1600 MHz DDR3L onboard memory. Table II illustrates the execution times for the scheme proposed in Section IV for  $\lambda=256$  bits. Each recipient has to decrypt  $W_i$  an average of n/2 times to retrieve the secret and subsequently decrypt the secret message m. Note

	Execution Time (ms)	
Number of Recipients	Publish	Retrieve
1	284.5	275.4
10	2564.5	460.9
15	3799.6	560.6
50	12300.5	1237.8
100	25867.7	2260.2

TABLE I
PERFORMANCE OF THE PUBLISH AND RETRIEVE STAGES IN FUNCTION
OF THE NUMBER OF INTENDED RECIPIENTS.

	Execution Time (ms)		
IBE Stage	Boneh and Franklin	Gentry	
IBE.Setup	368.10	424.49	
IBE.Extract	13.84	37.46	
IBE.Encrypt	271.90	1136.65	
IBE.Decrypt	252.82	911.32	

TABLE II
COMPARISON OF EXECUTION TIME FOR DIFFERENT IBE SCHEMES.

that efficiency comes at the cost of the recipient anonymity  $\mathcal{S}$ , as to hide  $\mathcal{S}$  it is required to produce more IBE.Encrypt calls.

We also analyzed the execution times of the IBE scheme, as it represents the most costly part of the scheme. Furthermore, our solution uses the random oracle assumption; we show in Table ?? that there is a significant computational difference between a similar scheme in the standard model, i.e., Gentry [17]. Nevertheless, we believe that our solution presents a tolerable cost to average users with 100 friends and a usual group size of 15 [32].

#### VI. RELATED WORK

The increased popularity of Online Social Networks (OSNs) and the amount of disseminated information prompted several privacy concerns. Guha et al. [6] proposed NOYB a solution that replaces the personal details of users by fake information. Later, FaceCloak [7] and Scramble [5] make use of cryptographic mechanisms to enforce privacy to the published information. Further, Persona suggest an attribute based encryption scheme for social networks. However, all the aforementioned solutions suffer from a complex key management infrastructure.

Other solutions take a more drastic approach by proposing novel, privacy-friendly architectures meant to replace existing platforms [8], [10], [9]. Besides the privacy protection offered, these solutions face a reduced user wilingness to adopt to a new platform.

Recently, Jung et al. [33] proposed a key management scheme based on dynamical IBE for decentralized OSNs. Their scheme, however, presents several problems. Foremost contains a single point of failure as a trusted party should generate the secret keys for a given id. This proposal still requires an additional public key that needs to be certified and shared among other users for the broadcasting, thus, not solving the key management issue.

<sup>&</sup>lt;sup>1</sup>Source of our implementations is available upon request.

In general all previous schemes require public parameters that should be shared and verified by users. In addition, by using an Identity-based scheme we allow users to motivate their friends to use the solution, as registered users can already encrypt messages to unregistered friends.

#### VII. CONCLUSION

Identity Based Encryption (IBE) solutions provide desirable properties to construct mechanisms to deliver privacy in OSNs. The minimal additional architectural support and the increased ease of key management represent a major motivation to implement IBE in OSNs. We show that using secret sharing and multi-PKGs there is no need to have a single trusted party, assuming that at least t-1 of the PKGs are compromised. Furthermore, the multiple PKG infrastructure can be maintained by several OSN providers, motivated by the attractive OSN privacy-friendly label, incentives towards more privacy concerned users, and considering the business model. Hence, users are provided with the option to use multiple identities, that they can use interchangeably among OSNs, e.g., use Twitter id as a public key in Facebook. In contrast to previous solutions, it is possible to share content with users not holding private keys to their identity as the valid public key is directly represented by their id in the OSN. This forces curious users to register if they wish to view the protected content shared with them. Lastly, we have extended Scramble and demonstrated that such extension presents a tolerable overhead to end-users. There are some important open challenges that call for further research. We endeavor to obtain a full open source project that supports different browsers. Items like a more detailed security discussion and efficiency improvement are also important and required. In addition, for the authentication and proof of identity we foresee several open challenges to increase user privacy and security, as well as adoption of the scheme.

#### ACKNOWLEDGMENT

This paper is the result of a one-year masters thesis. Therefore I would like to thank my promotors prof. dr. ir. Bart Preneel and prof. dr. ir. Vincent Rijmen and the KU Leuven to make this research possible. I would also like to thank my daily supervisor Filipe Beato for helping me with the reviewing, writing and implementation.

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# Master thesis filing card

Student: Stijn Meul

Title: Practical Identity-Based Encryption for Online Social Networks

UDC: 621.3

Abstract:

Currently Online Social Networks (OSNs) constitute an important and useful communication channel. However, coarse-grained privacy preferences protect the shared information insufficiently. Although cryptography provides interesting mechanisms to protect privacy, existing solutions face several issues such as, OSN provider acceptance, user adoption, key management and usability. In this thesis, we propose a practical solution that uses Identity Based Encryption (IBE) to simplify key management and enforce confidentiality of data in OSNs. By translating key generation of traditional IBE schemes to a distributed setting, our scheme prevents key escrow as long as the number of colluding key generators does not exceed a predefined threshold. Moreover, we devise an outsider anonymous broadcast IBE scheme to disseminate information among multiple users, even if they are not using the system. Apart from increased usability, the proposed solution no longer requires complex key management infrastructures keeping track of all keys in the system thereby relaxing users' prior knowledge on cryptographic primitives. The viability and tolerable overhead of our solution is demonstrated by extending an existing plugin for encryption in OSNs called Scramble. Based on the existing Scramble architecture and the MIRACL multi-precision library, we program an open-source prototype that implements our proposed solution on Facebook but can be generalised for use in any existing OSN infrastructure.

Thesis submitted for the degree of Master of Science in Electrical Engineering, option Embedded Systems and Multimedia

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