# Measuring Performance: Evaluating Variable Reduction Techniques

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Loading Packages	
library(caret)	
<pre>## Warning: package 'caret' was built under R version 3.4.4 ## Loading required package: lattice ## Loading required package: ggplot2 ## Warning: package 'ggplot2' was built under R version 3.4.4 #library(data.table) library(gbm)</pre>	
<pre>## Loading required package: survival ## ## Attaching package: 'survival' ## The following object is masked from 'package:caret': ## ## cluster ## Loading required package: splines ## Loading required package: parallel</pre>	
## Loaded gbm 2.1.3	
library(pROC)	
## Warning: package 'pROC' was built under R version 3.4.4	

```
##
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
library(plyr)
library(dplyr)
## Warning: package 'dplyr' was built under R version 3.4.4
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:plyr':
##
       arrange, count, desc, failwith, id, mutate, rename, summarise,
##
##
       summarize
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
#library(DMwR)
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
       combine
library(ggplot2)
library(leaps)
library(limma)
#library(DT)
library(knitr)
## Warning: package 'knitr' was built under R version 3.4.4
```

## Setting Working directory

```
#reading in dataset
setwd("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878")
chr1_gm12878_f <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/chr1_gm12878_
#set directory for selection techinques
setwd("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduction")</pre>
```

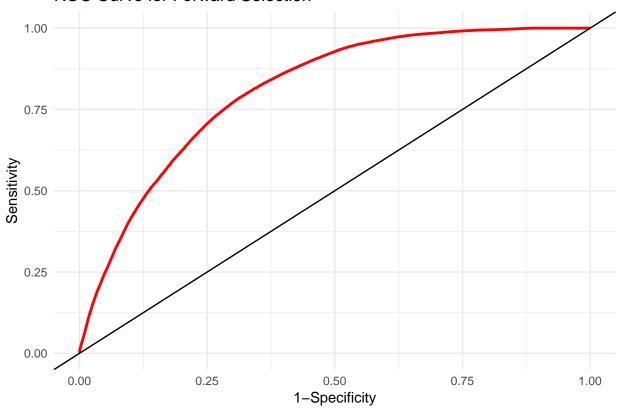
## Variable Selection Techniques

#### Forward Selection

```
#rds objects for dataset
auc.model.fwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduc
cv.preds.fwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduct
#rds object for roc and aucs
enetlst_fwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reducti</pre>
auc.fwd <- round(mean(enetlst_fwd[[3]]),3)</pre>
auc.fwd
## [1] 0.81
#0.810
vars.fwd <- na.omit(cv.preds.fwd[,which.max(auc.model.fwd)])</pre>
vars.fwd[grep("_dist",vars.fwd,invert = TRUE)] <- unlist(lapply(vars.fwd[grep("_dist",vars.fwd,invert =</pre>
chr1_gm12878_fwd <- chr1_gm12878_f[,which((names(chr1_gm12878_f) %in% vars.fwd) | names(chr1_gm12878_f)
dim(chr1_gm12878_fwd)
## [1] 247632
#247632 29
names(chr1_gm12878_fwd)
## [1] "y"
                                         "complex_dist"
   [3] "inversion_dist"
##
                                         "mobile_element_insertion_dist"
## [5] "low_complexity_dist"
                                         "LTR_dist"
## [7] "RC_dist"
                                         "Gm12878_WeakTxn"
## [9] "Gm12878_Heterochromlo"
                                         "Gm12878_TxnElongation_dist"
## [11] "Gm12878_WeakTxn_dist"
                                         "Gm12878_Heterochromlo_dist"
## [13] "Gm12878_WeakPromoter_dist"
                                         "Gm12878_Insulator_dist"
## [15] "Gm12878_T"
                                         "Gm12878_CTCF_dist"
## [17] "Gm12878_PF_dist"
                                         "Gm12878_T_dist"
## [19] "Gm12878_TSS_dist"
                                         "Gm12878_DNaseI"
## [21] "Gm12878_DNaseI_dist"
                                         "Gm12878_H3k27ac"
## [23] "Gm12878_H3k9ac"
                                         "Gm12878_H4k20me1"
## [25] "Gm12878_H2az_dist"
                                         "Gm12878_H3k36me3_dist"
## [27] "Gm12878_H3k9ac_dist"
                                         "Gm12878_H3k9me3_dist"
## [29] "Gm12878_H4k20me1_dist"
setwd("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878")
saveRDS(chr1_gm12878_fwd, "chr1_gm12878_fwd.rds")
rocdat.fwd <- data.frame(sensitivity=rowMeans(enetlst_fwd[[1]]), specificity=rowMeans(enetlst_fwd[[2]])</pre>
rocdat.fwd$Selection <- "fwd"</pre>
ggplot(rocdat.fwd, aes(x=specificity, y=sensitivity)) +
  geom_line(size=1, color="red") +
```

```
xlab("1-Specificity") +
ylab("Sensitivity") +
xlim(0, 1) +
ylim(0, 1) +
geom_abline(intercept=0, slope=1) +
theme_minimal() +
ggtitle("ROC Curve for Forward Selection")
```

### **ROC Curve for Forward Selection**

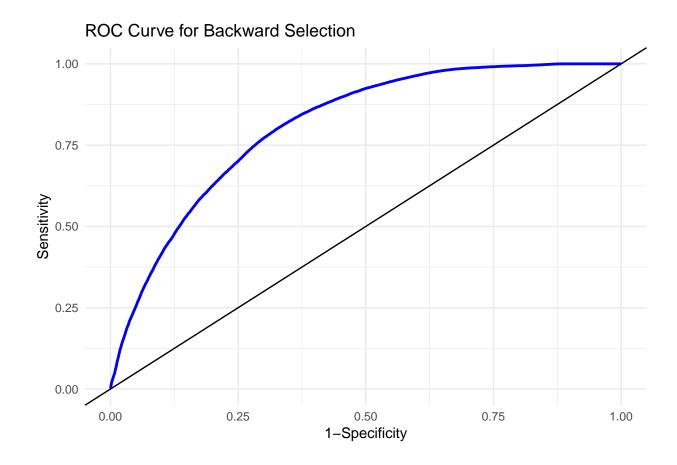


### **Backward Selection**

```
#rds object for dataset
auc.model.bwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduc
cv.preds.bwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduct
#rds object for roc and aucs
enetlst_bwd <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reducti
auc.bwd <- round(mean(enetlst_bwd[[3]]),3)
auc.bwd
## [1] 0.81
#0.81</pre>
```

vars.bwd <- na.omit(cv.preds.bwd[,which.max(auc.model.bwd)])</pre>

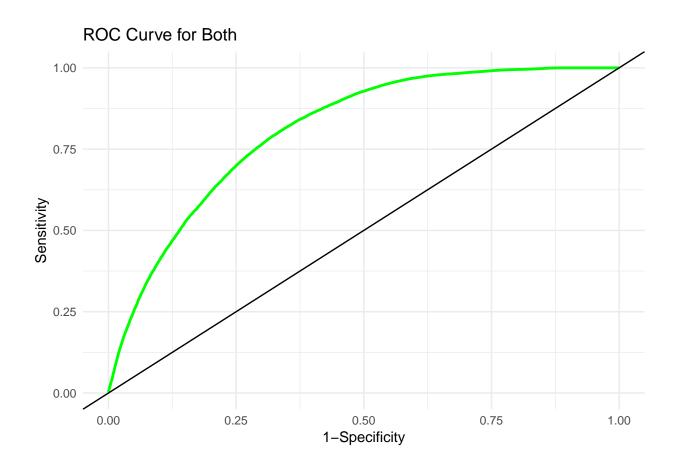
```
vars.bwd[grep("_dist",vars.bwd,invert = TRUE)] <- unlist(lapply(vars.bwd[grep("_dist",vars.bwd,invert =</pre>
chr1_gm12878_bwd <- chr1_gm12878_f[,which((names(chr1_gm12878_f) %in% vars.bwd) | names(chr1_gm12878_f)
dim(chr1_gm12878_bwd)
## [1] 247632
                  35
#247632
names(chr1_gm12878_bwd)
                                         "A"
  [1] "y"
##
  [3] "B"
##
                                         "complex_dist"
                                         "mobile_element_insertion_dist"
## [5] "inversion_dist"
## [7] "SINE"
                                         "low_complexity_dist"
## [9] "LTR_dist"
                                         "RC_dist"
## [11] "SINE_dist"
                                         "Gm12878_WeakTxn"
## [13] "Gm12878_Repressed"
                                         "Gm12878_Heterochromlo"
## [15] "Gm12878_TxnElongation_dist"
                                         "Gm12878_WeakTxn_dist"
## [17] "Gm12878_Repressed_dist"
                                         "Gm12878_Heterochromlo_dist"
## [19] "Gm12878_WeakPromoter_dist"
                                         "Gm12878_Insulator_dist"
## [21] "Gm12878_T"
                                         "Gm12878_CTCF_dist"
## [23] "Gm12878_T_dist"
                                         "Gm12878_TSS_dist"
## [25] "Gm12878_DNaseI"
                                         "Gm12878_DNaseI_dist"
## [27] "Gm12878_H3k27ac"
                                         "Gm12878 H3k36me3"
## [29] "Gm12878_H3k9ac"
                                         "Gm12878_H4k20me1"
## [31] "Gm12878_H2az_dist"
                                         "Gm12878_H3k4me2_dist"
## [33] "Gm12878_H3k9ac_dist"
                                         "Gm12878\_H3k9me3\_dist"
## [35] "Gm12878 H4k20me1 dist"
setwd("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878")
saveRDS(chr1_gm12878_bwd, "chr1_gm12878_bwd.rds")
rocdat.bwd <- data.frame(sensitivity=rowMeans(enetlst_bwd[[1]]), specificity=rowMeans(enetlst_bwd[[2]])</pre>
rocdat.bwd$Selection <- "bwd"</pre>
ggplot(rocdat.bwd, aes(x=specificity, y=sensitivity)) +
  geom_line(size=1, color="blue") +
  xlab("1-Specificity") +
  ylab("Sensitivity") +
  xlim(0, 1) +
  ylim(0, 1) +
  geom_abline(intercept=0, slope=1) +
  theme minimal() +
  ggtitle("ROC Curve for Backward Selection")
```



#### Both

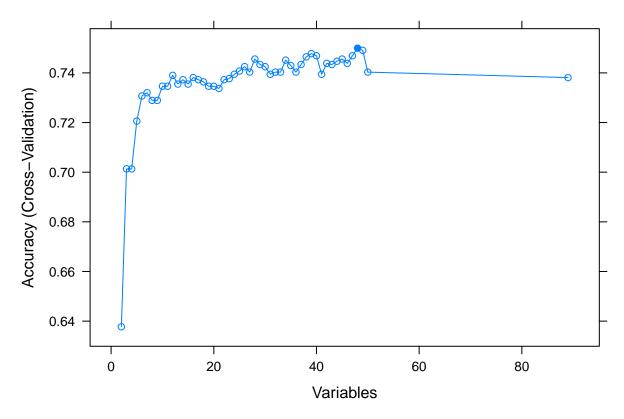
```
#rds objects for datasets
auc.model.both <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduc
v.preds.both <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduc
#rds object for roc and aucs
enetlst_both <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduct
auc.both <- round(mean(enetlst_both[[3]]),3)
auc.both
## [1] 0.809
#0.809
vars.both <- na.omit(cv.preds.both[,which.max(auc.model.both)])
vars.both[grep("_dist",vars.both,invert = TRUE)] <- unlist(lapply(vars.both[grep("_dist",vars.both,invert)])
chr1_gm12878_both <- chr1_gm12878_f[,which((names(chr1_gm12878_f) %in% vars.both) | names(chr1_gm12878_dim(chr1_gm12878_both))
## [1] 247632 27</pre>
```

```
#247632
names(chr1_gm12878_both)
## [1] "y"
                                         "complex_dist"
## [3] "mobile_element_insertion_dist" "low_complexity_dist"
## [5] "LTR_dist"
                                         "Gm12878_Heterochromlo"
## [7] "Gm12878_TxnElongation_dist"
                                         "Gm12878_WeakTxn_dist"
## [9] "Gm12878_Heterochromlo_dist"
                                         "Gm12878_Insulator_dist"
## [11] "Gm12878_R"
                                         "Gm12878_T"
## [13] "Gm12878_CTCF_dist"
                                         "Gm12878_PF_dist"
## [15] "Gm12878_TSS_dist"
                                         "Gm12878_DNaseI"
## [17] "Gm12878_DNaseI_dist"
                                         "Gm12878_H3k27ac"
## [19] "Gm12878_H3k79me2"
                                         "Gm12878_H3k9ac"
## [21] "Gm12878_H3k9me3"
                                         "Gm12878_H4k20me1"
## [23] "Gm12878_H2az_dist"
                                         "Gm12878_H3k36me3_dist"
## [25] "Gm12878_H3k4me2_dist"
                                         "Gm12878_H3k9ac_dist"
## [27] "Gm12878_H4k20me1_dist"
setwd("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878")
saveRDS(chr1_gm12878_both, "chr1_gm12878_both.rds")
rocdat.both <- data.frame(sensitivity=rowMeans(enetlst_both[[1]]), specificity=rowMeans(enetlst_both[[2]
rocdat.both$Selection <- "both"</pre>
ggplot(rocdat.both, aes(x=specificity, y=sensitivity)) +
  geom_line(size=1, color="green") +
 xlab("1-Specificity") +
 ylab("Sensitivity") +
 xlim(0, 1) +
  ylim(0, 1) +
  geom_abline(intercept=0, slope=1) +
  theme_minimal() +
  ggtitle("ROC Curve for Both")
```



## RFE

```
rfeModel <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduction/roc.rfeModel <- readRDS("C:/Users/Spiro Stilianoudakis/Documents/TAD_data/RData/GM12878/variable_reduct
auc.rfe <- round(pROC::auc(roc.rfeModel),3)
#0.7986
plot(rfeModel, type="b")</pre>
```

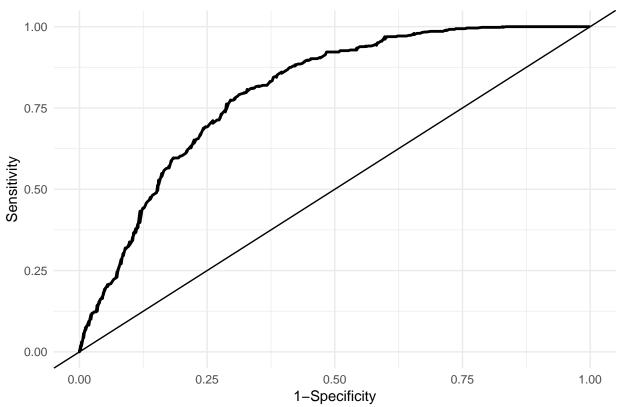


```
accdat <- rfeModel$results
accdat <- accdat[order(accdat$Accuracy, decreasing = TRUE),]
predictors(rfeModel)</pre>
```

```
[1] "Gm12878_Insulator_dist"
                                         "Gm12878_CTCF_dist"
##
    [3] "Gm12878_DNaseI_dist"
                                         "Gm12878_H2az_dist"
##
    [5]
       "Gm12878_TSS_dist"
                                         "Gm12878_H3k9ac_dist"
       "Gm12878_PF_dist"
                                         "Gm12878_WeakPromoter_dist"
##
    [9] "Gm12878_ActivePromoter_dist"
                                         "Gm12878_H3k79me2_dist"
                                         "Gm12878_H3k27ac_dist"
   [11] "Gm12878_H3k4me2_dist"
##
   [13]
       "Gm12878_WeakTxn_dist"
                                         "Gm12878_H3k36me3_dist"
       "Gm12878_TxnElongation_dist"
                                         "Gm12878 StrongEnhancer5 dist"
       "Gm12878_StrongEnhancer4_dist"
                                         "Gm12878_H3k4me1_dist"
  [17]
  [19]
        "se_GM12878_dist"
                                         "Gm12878 WE dist"
##
  [21] "Gm12878_H3k4me3_dist"
                                         "Gm12878_H4k20me1_dist"
  [23] "VMR_dist"
                                         "Gm12878_WeakEnhancer6_dist"
   [25] "Gm12878_H3k27me3_dist"
                                         "Gm12878_TxnTransition_dist"
        "Gm12878 E dist"
                                         "Gm12878_Repressed_dist"
##
   [27]
  [29]
        "DNA dist"
                                         "Gm12878_R_dist"
##
  [31]
        "Gm12878_H3k9me3_dist"
                                         "Gm12878_Heterochromlo_dist"
##
  [33] "A"
                                         "Gm12878_PoisedPromoter_dist"
##
##
   [35]
        "UCNE_dist"
                                         "Gm12878_DNaseI"
   [37]
        "Gm12878_T_dist"
                                         "SINE_dist"
   [39]
        "simple_repeat_dist"
                                         "sequence_alteration_dist"
  [41] "novel_sequence_insertion_dist" "Gm12878_WeakEnhancer7_dist"
```

```
## [43] "Gm12878_H3k36me3"
                                         "duplication_dist"
## [45] "Gm12878_H2az"
                                         "Gm12878_RepetitiveCNV15_dist"
## [47] "LTR_dist"
                                         "tandem_duplication_dist"
rocdat.rfe <- data.frame(sensitivity=roc.rfeModel$sensitivities, specificity=1-roc.rfeModel$specificiti
rocdat.rfe$Selection <- "rfe"</pre>
ggplot(rocdat.rfe, aes(x=specificity, y=sensitivity)) +
  geom_line(size=1, color="black") +
 xlab("1-Specificity") +
  ylab("Sensitivity") +
  xlim(0, 1) +
 ylim(0, 1) +
  geom_abline(intercept=0, slope=1) +
  theme_minimal() +
  ggtitle("ROC Curve for RFE")
```

## **ROC Curve for RFE**



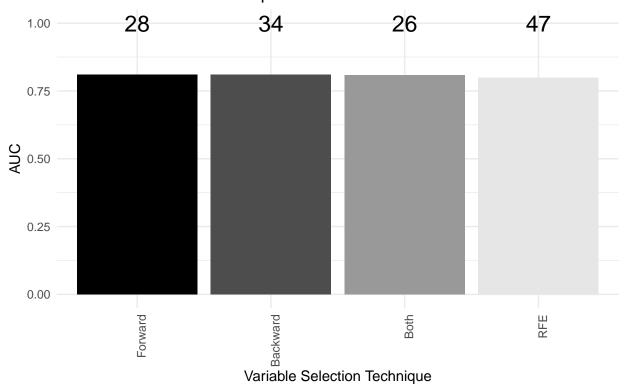
## Comparing Variable Selection Techniques

```
auc.bwd,
auc.both,
auc.rfe))
auc.plot <- auc.plot[order(auc.plot$auc, decreasing=TRUE),]
auc.plot$Selection <-factor(auc.plot$Selection,
levels=auc.plot$Selection)
#datatable(auc.plot)
kable(auc.plot)
```

Selection	auc
Forward	0.810
Backward	0.810
Both	0.809
RFE	0.799

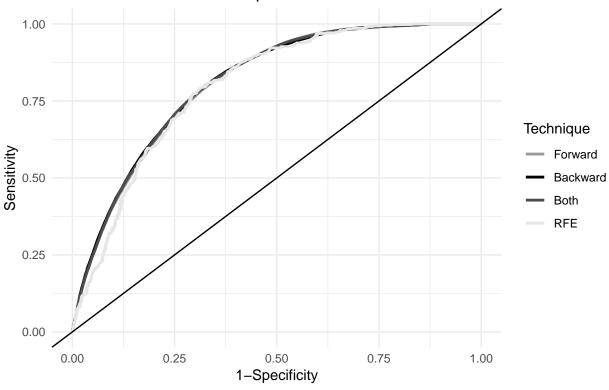
```
p<-ggplot(data=auc.plot, aes(x=Selection, y=auc, fill=Selection)) +
    xlab("Variable Selection Technique") + ylab("AUC") +
    geom_bar(stat="identity") + ylim(0,1) +
    scale_fill_manual(values=gray(c(0,.3,.6,.9)), guide=FALSE) +
    annotate("text", x=1, y=1, label= "28", size=6) +
    annotate("text", x=2, y=1, label= "34", size=6) +
    annotate("text", x=3, y=1, label= "26", size=6) +
    annotate("text", x=4, y=1, label= "47", size=6) +
    theme_minimal() +
    theme(axis.text.x = element_text(angle = 90, hjust = 1)) +
    ggtitle("Model Performance for Different \n Variable Selection Techniques")
</pre>
```

# Model Performance for Different Variable Selection Techniques



```
allrocdat <- rbind.data.frame(rocdat.fwd, rocdat.bwd, rocdat.both, rocdat.rfe)</pre>
ggplot(data=allrocdat, aes(x=specificity, y=sensitivity, color=Selection)) +
  geom_line(size=1) +
  scale_colour_manual(name="Technique",
   labels=c("Forward",
             "Backward",
             "Both",
              "RFE"),
   values=c("#999999", "#000000", "#4D4D4D", "#E6E6E6")) +
  xlab("1-Specificity") +
  ylab("Sensitivity") +
 xlim(0, 1) +
 ylim(0, 1) +
  geom_abline(intercept=0, slope=1) +
  theme_minimal() +
  ggtitle("ROC Curves for Different \n Variable Selection Techniques")
```

## ROC Curves for Different Variable Selection Techniques



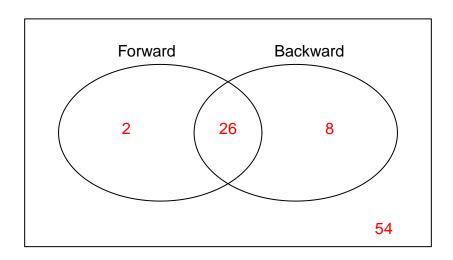
#### intersect(vars.fwd,intersect(vars.bwd,vars.both))

```
##
    [1] "Gm12878_DNaseI_dist"
                                         "Gm12878_Insulator_dist"
##
   [3] "Gm12878_TSS_dist"
                                         "Gm12878_DNaseI"
##
   [5] "Gm12878_H2az_dist"
                                         "Gm12878_H3k9ac"
  [7] "Gm12878_H3k9ac_dist"
                                         "Gm12878_Heterochromlo_dist"
  [9] "Gm12878_Heterochromlo"
                                         "Gm12878_CTCF_dist"
##
  [11] "Gm12878_H4k20me1_dist"
                                         "Gm12878_H4k20me1"
  [13] "low_complexity_dist"
                                         "Gm12878_H3k27ac"
  [15] "Gm12878_TxnElongation_dist"
                                         "Gm12878_WeakTxn_dist"
   [17] "Gm12878_T"
                                         "LTR_dist"
  [19] "complex_dist"
                                         "mobile_element_insertion_dist"
```

#### intersect(vars.fwd,intersect(vars.bwd,predictors(rfeModel)))

```
[1] "Gm12878_DNaseI_dist"
##
                                      "Gm12878_Insulator_dist"
   [3] "Gm12878_TSS_dist"
                                      "Gm12878_DNaseI"
##
    [5] "Gm12878_H2az_dist"
                                      "Gm12878 H3k9ac dist"
##
   [7] "Gm12878_Heterochromlo_dist" "Gm12878_CTCF_dist"
##
   [9] "Gm12878 H4k20me1 dist"
                                      "Gm12878 H3k9me3 dist"
  [11] "Gm12878_TxnElongation_dist" "Gm12878_WeakTxn_dist"
  [13] "Gm12878_WeakPromoter_dist"
                                     "LTR_dist"
## [15] "Gm12878 T dist"
intersect(intersect(vars.fwd,intersect(vars.bwd,vars.both)),
          intersect(vars.fwd,intersect(vars.bwd,predictors(rfeModel))))
```

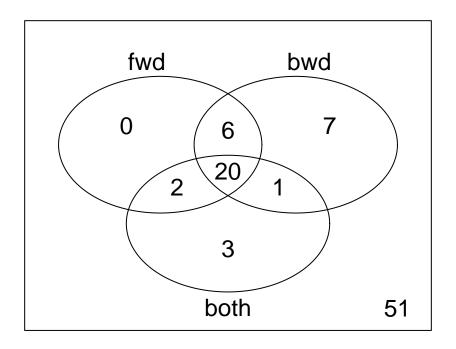
```
## [3] "Gm12878_TSS_dist"
                                       "Gm12878 DNaseI"
                                       "Gm12878_H3k9ac_dist"
## [5] "Gm12878_H2az_dist"
## [7] "Gm12878 Heterochromlo dist" "Gm12878 CTCF dist"
## [9] "Gm12878_H4k20me1_dist"
                                       "Gm12878_TxnElongation_dist"
## [11] "Gm12878_WeakTxn_dist"
                                       "LTR_dist"
fwd <- (names(chr1_gm12878_f) %in% vars.fwd)</pre>
bwd <- (names(chr1_gm12878_f) %in% vars.bwd)</pre>
both <- (names(chr1_gm12878_f) %in% vars.both)
rfe <- (names(chr1_gm12878_f) %in% predictors(rfeModel))</pre>
#fwd compared to bwd
venndatfb <- cbind(fwd,bwd)</pre>
fb <- vennCounts(venndatfb)</pre>
vennDiagram(fb, include = "both",
 names = c("Forward", "Backward"),
cex = 1, counts.col = "red")
```



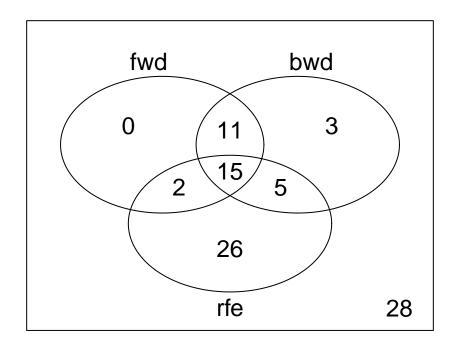
```
venndat1 <- cbind(fwd,bwd,both)
venndat2 <- cbind(fwd,bwd,rfe)
venndat3 <- cbind(fwd,bwd,both,rfe)

a <- vennCounts(venndat1)
b <- vennCounts(venndat2)
c <- vennCounts(venndat3)

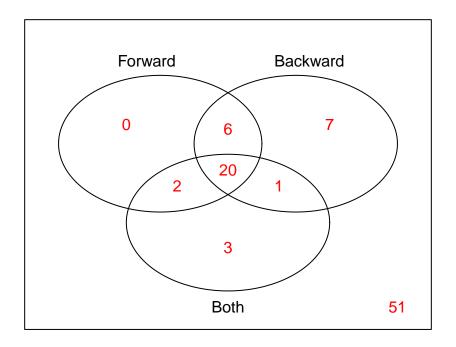
vennDiagram(a)</pre>
```



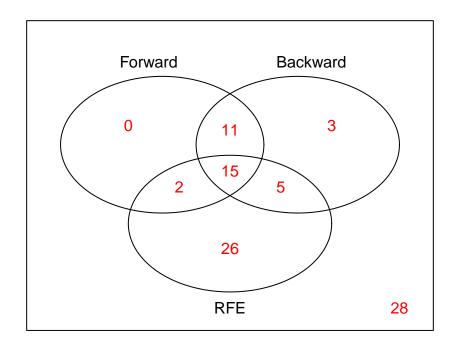
vennDiagram(b)



```
vennDiagram(a, include = "both",
  names = c("Forward", "Backward", "Both"),
  cex = 1, counts.col = "red")
```



```
vennDiagram(b, include = "both",
  names = c("Forward", "Backward", "RFE"),
  cex = 1, counts.col = "red")
```



```
vennDiagram(c, include = "both",
  names = c("Forward", "Backward", "Both", "RFE"),
  cex = 1, counts.col = "red")
```

