Artifact for Multi-Language Probabilistic Programming

Many different probabilistic programming languages exist that specialize to specific kinds of probabilistic programs, broadly falling into the categories of approximate and exact inference.

This artifact for Multi-Language Probabilistic Programming provides the MultiPPL compiler. MultiPPL is a host compiler of two syntactically and semantically different probabilistic programming languages: an approximate language leveraging importance sampling, and an exact language using binary decision diagrams (BDDs) for knowledge compilation. Our work demonstrates sound interoperation of these two languages under a Matthews and Findler-style multi-language framework[3].

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1 Artifact Availability

The provided artifact contains the following source, development dependencies, and executables:

- This README
- The multippl source code as a separate multippl-source.tar.gz file.
- A docker image containing the following
 - executables for development: cargo, rustc, tree-sitter, cargo-nextest, ghc, bc
 - the multippl source code, located at /data/multippl-source
 - executables for benchmarking:
 - * multippl our software artifact
 - * python with pyro preinstalled, our benchmark's approximate inference alternative
 - * psi, our benchmark's exact inference alternative
 - * dice, used to derive components of the ground truth.
 - * multippl-benchmark, a shell script which runs the benchmarks and tabulates our results.

2 Quick Start

2.1 Hardware Requirements

There are no explicit hardware requirements for the mulippl compiler. Large exact inference programs will eventually encounter memory limitations and slow down the samples produced, but this has not been an issue for networks in our evaluations.

2.2 Running multippl

The attached docker image has it's entrypoint set to the multippl binary:

- \$ wget https://zenodo.org/records/<TBD>/files/multippl-docker.tar.gz
- \$ docker load --input multippl-docker.tar.gz
- \$ docker run --rm multippl:latest --steps <STEPS> --file <FILE>

Will invokes multippl, where --step is the number of samples taken in the evaluation, and --file refers to a valid MultiPPL program.

To run multippl on a file outside of the docker image you must bind a docker mount to the image. Given a file example/beta-bernoulli.yo, bind the mount using -v or --volume <HOSTPATH>:<BINDPATH>:

Notes:

- --rm removes all state from the docker container after execution
- --file can be relative to the /data directory.
- /data contains multippl-source/ so binding directly to /data will lose access to these provided source files.

2.3 Running multippl-benchmark

To run a our benchmarks single-threaded for 100 runs and cache the resulting tables in a local logs/ directory, use the following command:

PSI will time out on 700 evaluations, which is the most time consuming portion of the benchmark. To reduce the running time, it may be prudent to limit PSI to only 10 runs, relying on the provided standard error to reflect the numbers provided:

To do a "quick evaluation" with only 10 runs, a separate flag exists for the rest of the benchmark:

Tables will be cached to logs/hybrid.rich and logs/discrete.rich.

3 MultiPPL

MultiPPL uses tree-sitter to parse syntax with the full grammar defined in tree-sitter-multippl/grammar.js. Here we describe each sub-language in our framework and how to interoperate between the Cont and Disc languages by example, and provide a summarization of the tree-sitter grammar provided. The examples/ folder contains all programs documented.

```
A MultiPPL program is introduced using exact { ... } or sample { ... } blocks: choice('exact, 'sample') '{' <expr> '}'
```

Here, choice denotes an alternative and comes from the tree-sitter metalanguage, while <expr> comes from the chosen expression language of Disc (exact) or Cont (sample). Single-quoted characters denote requisite symbols.

MultiPPL supports procedures, which similarly require a sample or exact keyword to describe where the function is allowed to run:

```
choice('sample', 'exact') 'fn' <id> '(' repeat(<id>) ')' '{' <expr> '}'
```

From tree-sitter we use repeat for zero-or-more repetitions, <id> is a placeholder for a variable (defined as x in each grammar), and <expr> once again corresponds to the chosen expression language.

3.1 The Disc Language

Disc syntax draws heavily from the Dice programming language [2] and Disc's inference strategy uses the same knowledge compilation engine [1] used by Dice. The largest difference between the two languages Disc is currently untyped (the type-system will arrive in the next release). Disc allows for dynamically-allocated floating point values obtained by interoperation but querying these result in undefined behavior. The syntactic differences between Disc and Dice include:

- observe statements are not bound expressions, but are instead statements.
- integers are not bit-encoded and do not need an explicit size.

3.1.1 Example: Two Coins

An illustrative, simple Disc program will flip two biased coins and observe an event that one of the two coins will land on heads:

```
exact {
  let a = flip 1.0 / 3.0 in
  let b = flip 1.0 / 4.0 in
```

```
observe a || b in
a
}
```

In this program flip will represent a coinflip with the probability of heads being flip's parameter; the first line of the program will create a Bernoulli distribution which returns true (ie: "heads") with probability 1/3 and bind this to a; on the next line we similarly create a Bernoulli distribution that is true with probability 1/4 and assign this to b. Next, observe encodes evidence that one of these variables *must* be true and the program queries for the posterior of a's distribution.

We can analytically derive the solution (or construct a probability table) to show that the posterior of this model is 2/3. Running this program with the MultiPPL compiler, we see:

In contrast to the Dice compiler, MultiPPL will take this program and produce a sampler which executes the program for as many samples as indicated by the --steps flag. For this reason, the command above only returns the expectation of the compiled distribution and does not return a representation of the underlying probability table. The final line reports the wall-clock time of execution.

Because we are compiling a Disc program, the sampled distribution is exact and is invariant to the requested number of samples. If we increase the expected number of samples to 10, we will observe that this is the same as compiling the exact distribution 10 times and taking the average of these (identical) samples.

3.1.2 Products

Disc supports products and projections, and we can use this to query for b's expectation as well:

```
exact {
  let a = flip 1.0 / 3.0 in
  let b = flip 1.0 / 4.0 in
  let ab = (a, b) in
  observe a || b in
   (ab[0], ab[1])
}
```

Compiling this query, will yield a space-delineated list of results and inform us that b's posterior mean is 0.5:

```
\ docker run multippl:latest --file examples/two-coins-prod.yo --steps 1 0.66666666666666 0.5 \
```

3.1.3 The Discrete Distribution and Probabilistic Choice

The Discrete distribution takes in a list of floats, normalizes this list so that they form a valid probability distribution, and returns an integer. Integers in Disc, however, are syntactic sugar for one-hot encodings of the represented int. For example the following program:

```
exact {
  discrete(1.5, 1.5, 3.0)
}

Is a valid query:

$ docker run multippl:latest --file examples/discrete.yo --steps 1
0.25 0.25 0.5
6ms

If-then-else expressions in Disc denote probabilistic choice.

exact {
  let p = flip 0.5 in
  if p
  then discrete(1.5, 1.5, 3.0)
  else discrete(3.0, 1.5, 1.5)
}
```

Probabilistic choice introduces some nuance and a longer discussion of probabilistic choice in the context of our core grammar can be found in our OOPSLA submission.

3.1.4 Grammar

A top-level summarization of Disc's grammar is as follows:

```
| 'flip' a
                                            // Bernoulli distributions
 | 'discrete' '(' repeat(a ',') a ')'
                                       // Discrete distributions, desugared into a sequence of
 | 'observe' a 'in' e
                                 // conditioning on hard evidence in a sequence
 | 'sample' '(' sample_e ')'
                                   // inlined interoperation with an expression e from Cont
 | 'sample' '{' sample_e '}'
                                     // interoperation with a block expression e from Cont
ANF forms
a := x
                                    // variables
                                   // values
 l v
  | '!' a
                                   // negation
  | '(' repeat(a ',') a ')'
                                   // products
  | x '[' a ']'
                                   // projections out of products
  | a binop a
                                   // binomial operations
Binomial operations
binop := '+' | '*' | '/' | '^' | '<' | '==' | '>=' | '>' | '&&' | '||'
Values
                                    // booleans
v := true | false
 | /-?\d+\.(?:\d*|)/
                             // statically known floating-point values, or floats obtained thro
 | /\d+/
                         // statically known integers, or integers obtained through interop
```

// variable binding

3.2 The Cont Language

| 'let' x '=' e 'in' e

The Cont language is a simple sampling language that uses importance sampling as its approximate inference strategy. It contains common distributions-objects, both continuous and discrete, as well as the ability to incorporate soft-evidence, sample from distributions, while-loops, and conventional branching statements.

3.2.1 An Approximate Beta-Bernoulli

A example of using Cont to find the posterior of a Beta-Bernoulli process, would like the following:

```
sample {
  p <- ~ beta(1.0, 1.0);
  observe true from bern(p);
  observe false from bern(p);
  observe false from bern(p);
  p
}</pre>
```

This program first samples from a Beta(1, 1) distribution with the unary \sim operator. The result is a value with uniform probability between 0 and 1, which is assigned to the variable p, which will be used to parameterize the Bernoulli's distribution. This distribution then incorporates three observations into its importance weighting, which is used to score the final query's posterior which is the final line of the program. Because of conjugacy, we know that the correct posterior is a Beta distribution with

$$\alpha = 2$$

and

$$\beta = 3$$

, with an expectation of

$$2/(2+3) = 0.4$$

1. running Running multipp1, we see that 100 samples produces the following expectation of the posterior:

In this command, --rng 1 indicates a seed, --file points to the relative path of the program in the docker container, and --steps 100 defines the number of samples to produce. Increasing this number of samples, we see that our approximation converges closer to the correct value:

3.2.2 While-loops

Four data points for inference is quite limited, requiring many samples to produce an adequate result. We may want to increase how much evidence we give our program with Cont's while-loop:

```
sample {
  p ~ beta(1.0, 1.0);
  x <- 10;
  while (x > 0) {
```

```
observe true from bern(p);
observe false from bern(p);
observe false from bern(p);
x <- x - 1;
()
};
p</pre>
```

In the first line of our program, we use a binding \sim which is syntactic sugar for p <- \sim beta(1.0, 1.0). Notably, all Cont statements terminate with semicolons including while-loops – this differs from conventional imperative programs. All blocks also return expressions and so here we provide unit () to the block in this while-loop, which always discards it's final value. The posterior of this program is Beta(1+10, 1+20) with a mean of

$$11/32 = 0.34375$$

3.2.3 Branching and Lists

Cont supports branching and control flow through if statements. To define a multi-modal Gaussian distribution, we can use samples from a Bernoulli distribution, and use this to select one of two modes:

```
sample {
  m ~ bern(0.5);
  if m {
     ~normal(1.0, 0.5)
  } else {
     ~normal(-1.0, 0.5)
  }
}
```

To perform parameter estimation for this model, we would want to write some function to perform the same scoring over both modes:

```
sample fn score (p, ev) {
  m ~ bern(p);
  if m {
    observe ev from normal(1.0, 0.5); ()
  } else {
```

```
observe ev from normal(-1.0, 0.5); ()
}
sample {
  p ~ beta(1.0, 1.0);
  score(p, 1.0);
  score(p, 1.0);
  score(p, 1.0);
  p
}
```

The three observations above will begin to skew our posterior towards the Gaussian distribution with a mode of 1.0:

Cont has limited support for lists and includes the head, tail, and push functions. We can represent the same program above with a list of our evidence and iterate through this list using a while loop:

```
sample fn score (p, ev) {
  m ~ bern(p);
  if m {
    observe ev from normal(1.0, 0.5); ()
  } else {
    observe ev from normal(-1.0, 0.5); ()
  }
}
sample {
  p \sim beta(1.0, 1.0);
  evidence <- [1.0, 1.0, 1.0];
  i <- 3;
  while (i > 0) {
    score(p, evidence[i - 1]);
    i < -i - 1;
    ()
  };
 p
}
```

And we can confirm that running this program with the same seed will yield the same result as before:

3.2.4 Grammar

| 'uniform' '(' a ',' a ')'

| 'normal' '(' a ',' a ')'

| 'discrete' '(' repeat(a ',') a ')'

| 'beta' '(' a ',' a ')'

A simplified summary of Cont's tree-sitter grammar is as follows:

Variables x

```
Expressions
e := a
                                               // all ANF forms
  | 'while' a '{' e '}'
                                               // while loops
  | x '()' | x '(' repeat(x ',') x ')'
                                               // function application
  |'if' '(' a ')' '{' e '}' 'else' '{' e '}' // control flow
  | x '<-' e ';' e
                                               // variable binding
  | e ';' e
                                               // sequencing
  | '~' e
                                               // sampling an expression
 | x '~' e ';' e
                                      // sugar for binding a sample: x <- (~e); e
  | 'observe' a 'from' a
                                               // conditioning on soft evidence
 | 'exact' '(' exact_e ')'
                                      // inlined interoperation with an expression e from Disc
 | 'exact' '{' exact_e '}'
                                      // interoperation with a block expression e from Disc
ANF forms
                                                 // variables
a := x
                                                 // values
  | V
  | '!' a
                                                 // negation
  | x '[' a ']'
                                                 // projections
                                                 // binomial operations
  | a binop a
  | '(' repeat(a ',') a ')'
                                                 // products
  | '[' a ']' | '[' repeat(a ',') a ']'
                                                 // vectors
  | 'head' '(' a ')' | 'tail' '(' a ')'
                                                 // vector operations
  | 'push' '(' a ',' a ')'
                                                 // vector operations
  | 'bern' '(' a ')'
                                                 // Bernoulli distributions
  | 'poisson' '(' a ')'
                                                 // Poisson distributions
```

// Uniform distributions

// Normal distributions

// Discrete distributions

// Beta distributions

```
Binomial operations
binop := '+' | '*' | '/' | '^' | '<' | '<=' | '==' | '>=' | '>' | '&&' | '||'
Values
v := true | false
                                                 // booleans
  | /-?\d+\.(?:\d*|)/
                                                 // floating-point values
  | /\d+/
                                                 // integers
  | '[]' | '[' repeat(v ',') v ']'
                                                 // vectors
  | '()' | '(' repeat(v ',') v ')'
                                                 // products
  | 'bern' '(' v ')'
                                                 // Bernoulli distributions
  | 'poisson' '(' v ')'
                                                 // Poisson distributions
  | 'uniform' '(' v ',' v ')'
                                                 // Uniform distributions
  | 'normal' '(' v ',' v ')'
                                                 // Normal distributions
  | 'beta' '(' v ',' v ')'
                                                 // Beta distributions
  | 'discrete' '(' repeat(v ',') v ')'
                                                 // Discrete distributions
```

3.3 Interoperation

MultiPPL provides a framework in which Cont and Disc can seamlessly interoperate through boundary operators, mutually defined in each language.

An example of this is when we have components of a program which we would like to model exactly, but we would like to use this in a larger program which needs more flexibility and can be resoned about approximately. For instance, in the following program, we model a packet traversing a ladder-like network topology of of unbounded length. At each "rung" on the ladder, a unbiased node is selected for the packet to continue its traversal, and we can model each node's failure rate exactly.

```
exact fn rung (s1) {
  let route = flip 0.5 in

let s2 = if route then s1 else false in
  let drop2 = flip 0.005 in
  let go2 = s2 && !drop2 in

let s3 = if route then false else s1 in
  let drop3 = flip 0.001 in
  let go3 = s3 && !drop3 in

go2 || go3
```

The above function models a partial traversal through this ladder network, and returns a Boolean representing whether or not the packet was able to navigate through this sub-

network without getting dropped. We want to query on the probability that a packet will successfully traverse all of these intermediate steps without getting dropped, but the network has unbounded length, which cannot be modelled exactly.

```
sample {
    ix ~ poisson(20.0);
    ix <- ix + 1;
    traversed <- true;
    while ix > 0 {
        traversed <- exact(rung(traversed));
        ix <- ix - 1;
        ()
    };
    traversed
}</pre>
```

Using Cont, we can model the length of this network using a Poisson distribution (with an average topology size of 20 rungs). We then can iterate over each subnetwork and return a sample encapsulating the success of the packet's traversal.

Evaluating this for 1000 samples, we can find the expectation of this model to be:

Similarly, we can use the sample keyword inside of a Disc program to use a Cont value in a Disc context. The MultiPPL compiler will also provide some syntactic sugar when performing variable look-ups and will attempt to perform interoperation wherever possible (as in the case of Cont's traversed variable binding in the above program).

For more examples of interoperation, we refer users to our submission and provided benchmarks.

4 MultiPPL Artifact Evaluation: Validation

The multippl compiler is responsible for providing L1 and wall-clock evaluations for an approximate inference evaluations in Fig 11 and a discrete probabilistic program evaluation in Fig 14.

4.1 Hardware Requirements

There are no explicit hardware requirements for to produce Fig 11 and Fig 14. These are able to run on commercial hardware on a single thread, but a full evaluation will take >200 hours.

Of the $>\!200$ hours 6hrs are spent evaluating the tabulated results and 200 hours are spent waiting for 400 PSI programs (100 runs in 4 evaluations) to reach a timeout of 30 minutes. Parallelizing this evaluation is not advised without large amounts of RAM, as the most expensive PSI benchmark, the \sim bayesnets/alarm evaluation, takes up 17.2G per thread of residential memory. Close behind alarm is the PSI bayesnets/insurance and grids/81 evaluations, which uses \sim 15G per thread of residential memory. Using less RAM than this should be acceptable on a single threaded evaluation, so long as a there is enough swap to compensate for the difference of the expected RAM.

The multippl-benchmark tool can use more threads to speed up evaluation and to reduce the size of the timeout, with PSI-specific flags to ensure PSI is still run single-threaded. Parallelizing any program using exact inference may cause programs to crash due to OOM errors. On a Thinkpad T14s Gen 3 with an AMD Ryzen 7 PRO 6850U (4.768GHz) CPU and 30G of RAM, the non-PSI portions of this benchmark can be safely run with 8 threads.

4.2 Running multippl-benchmark via Docker

The multippl-benchmark script is a multi-threaded benchmark evaluator, used to produce our evaluations. To run the multippl-benchmark command, invoke

\$ docker run --entrypoint multippl-benchmark multippl:latest
multippl-benchmark (all|tabulate) [OPTIONS]

subcommand: all -- run all benchmarks (psi benchmarks last), then tabulate

```
--num-threads NUM_THREADS Number of threads to use for non-psi benchmarks.
```

Default: 1.

--num-runs NUM_RUNS Number of runs to use for non-psi benchmarks.

Default: 100.

approximate benchmarks. Default: 1000.

--psi-threads PSI_THREADS Number of threads to use for psi benchmarks.

Default: 1.

--psi-runs PSI_RUNS Number of runs to use for psi benchmarks.

Default: 100.

--timeout-min TIMEOUT_MIN Number of minutes before a timeout.

Default 30.

--logdir LOGDIR Directory to store execution logs.

Defaults to \$PWD/logs.

subcommand: tabulate -- skip benchmarks and tabulate

--logdir LOGDIR Directory to store execution logs.

Defaults to \$PWD/logs.

The default strategy is to run 100 evaluations, single-threaded, for 1000 samples.

To save the cached files locally, outside of docker, bind to a volume to the /data/logs directory:

As stated above, PSI takes a considerable amount of time to produce the requisite timeouts. To reduce the running time, you may reduce the timeout duration and limit the number of runs PSI takes, relying on the provided standard error to reflect the numbers provided:

To speed up the non-PSI sections of the evaluation, you may increase the number of threads without parallelizing PSI processes:

If the final table is not produced, the log directory should be cleared and the benchmark should be re-evaluated. Alternatively, a partial view of the table can be generated with the tabulate subcommand:

4.3 Running Benchmarks Individually

To run an individual benchmark, you must first drop into an interactive zsh or bash shell:

```
$ docker run -it --entrypoint zsh multippl:latest
```

From here, you can cd into the ./multippl-source/bench folder which contains the bench.py and avg.py scripts for program execution and tabulation of a single experiment.

Additionally, runall.sh is the source file for multippl-benchmark and tabulate.py is invoked to produce the final tables in the multippl-benchmark tabulate subcommand.

The bench/ folder structure is as follows:

- arrival/ contains subdirectories tree-15, tree-31, and tree-63.
- bayesnets/ contains subdirectories alarm, and insurance.
- grids/ contains subdirectories 3x3, 6x6, and 9x9 corresponding to the 9, 36, and 81 evaluations in Fig 11.

• gossip/ contains subdirectories g4, g10, and g20

Each directory has a mainfile corresponding to the benchmarked tool:

- main.psi refers to the PSI program evaluated
- main.py refers to the Pyro program evaluated
- main.yo refers to a MultiPPL program with interoperation that is evaluated. We call this file diag.yo for the grids evaluations, as this specifies the collapsing strategy for interoperation.
- cont.yo refers to a MultiPPL program which only defines a Cont program.
- exact.yo refers to a MultiPPL program which only defines a Disc program.
- truth.py (or sometimes a secondary functionality of main.py) contains the derived groundtruth, used to calculate L1 distance.

Each experiment's subdirectory contains a symlink to bench.py in ./multippl-source/bench/. A benchmark is run by invoking python bench.py in the subdirectory that generates logs in the current directory. Note that these benchmarks default to using half of the threads visible to docker and do **not** run PSI by default. For example:

```
$ docker run -it --entrypoint zsh multippl:latest
# in the docker shell
$ cd ./multippl-source/bench/arrival/tree-15
$ python bench.py --help
usage: bench.py [-h] [--psi] [--num-runs NUM_RUNS] [--num-steps NUM_STEPS]
                [--initial-seed INITIAL_SEED] [--noti] [--threads THREADS]
                [--logdir LOGDIR]
options:
 -h, --help
                        show this help message and exit
  --psi
  --timeout-min TIMEOUT_MIN
 --num-runs NUM_RUNS
 --num-steps NUM_STEPS
 --initial-seed INITIAL_SEED
 --noti
  --threads THREADS
 --logdir LOGDIR
```

Running bench.py will produce cached tables and data files in the parent directory of the runlogs.

5 Development

5.1 Nix Development and Running Benchmarks via Nix

MultiPPL uses nix's flakes for development. Using the source contained in multippl-source.tar.gz and a flake-enabled nix binary, the following commands enable nix development:

```
tar -xvzf multippl-source.tar.gz
cd multippl-source
git init
```

- nix development shell.
- nix flake check runs cargo nextest run and checks our nix derivations.
- nix build .#multippl .#multippl-benchmark .#multippl-docker produces the multippl, and multippl-benchmark executables alongside the included docker images.
- \bullet nix run .#multippl-benchmark -- <ARGS> runs the multippl-benchmark $\operatorname{executable}$

References

- [1] Steven Holtzen. *Rsdd*. Northeastern Probabilistic Programming Laboratory. URL: https://github.com/neuppl/rsdd (visited on 12/30/2024).
- [2] Steven Holtzen, Guy Van den Broeck, and Todd Millstein. "Scaling Exact Inference for Discrete Probabilistic Programs". In: *Proceedings of the ACM on Programming Languages* 4 (OOPSLA Nov. 2020), 140:1–140:31. DOI: 10/gh4jhb.
- [3] Jacob Matthews and Robert Bruce Findler. "Operational Semantics for Multi-Language Programs". In: *ACM SIGPLAN Notices* 42.1 (2007), pp. 3–10. DOI: 10.1145/1190215. 1190220.