

Lazy Evaluation

Principles of Functional Programming

Lazy Evaluation

The proposed implementation suffers from a serious potential performance problem: If tail is called several times, the corresponding lazy list will be recomputed each time.

This problem can be avoided by storing the result of the first evaluation of tail and re-using the stored result instead of recomputing tail.

This optimization is sound, since in a purely functional language an expression produces the same result each time it is evaluated.

We call this scheme *lazy evaluation* (as opposed to *by-name evaluation* in the case where everything is recomputed, and *strict evaluation* for normal parameters and val definitions.)

Lazy Evaluation in Scala

Haskell is a functional programming language that uses lazy evaluation by default.

Scala uses strict evaluation by default, but allows lazy evaluation of value definitions with the lazy val form:

```
lazy val x = expr
```

Exercise:

Consider the following program:

```
def expr =
  val x = { print("x"); 1 }
  lazy val y = { print("y"); 2 }
  def z = { print("z"); 3 }
  z + y + x + z + y + x
expr
```

If you run this program, what gets printed as a side effect of evaluating expr?

```
0 zyxzyx 0 xzyz
0 xyzz 0 zyzz
0 something else
```

Exercise:

Consider the following program:

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def expr =
  val x = { print("x"); 1 }
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  z + y + x + z + y + x
expr
```

If you run this program, what gets printed as a side effect of evaluating expr?

```
0 zyxzyx X xzyz
0 xyzz 0 zyzz
0 something else
```

Lazy Vals and Lazy Lists

Using a lazy value for tail, TailLazyList.cons can be implemented more efficiently:

```
def cons[T](hd: T, tl: => LazyList[T]) = new TailLazyList[T]:
  def head = hd
  lazy val tail = tl
  ...
```

Seeing it in Action

To convince ourselves that the implementation of lazy lists really does avoid unnecessary computation, let's observe the execution trace of the expression:

```
lazyRange(1000, 10000).filter(isPrime).apply(1)
```

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```
Let's abbreviate cons(1000, lazyRange(1000 + 1, 10000)) to C1.
```

```
C1.filter(isPrime).apply(1)
```

```
Let's abbreviate cons(1000, lazyRange(1000 + 1, 10000)) to C1.
     C1.filter(isPrime).apply(1)
 --> (if C1.isEmpty then C1
                                              // by expanding filter
      else if isPrime(C1.head) then cons(C1.head, C1.tail.filter(isPrime))
      else C1.tail.filter(isPrime))
      .applv(1)
 --> (if isPrime(C1.head) then cons(C1.head, C1.tail.filter(isPrime))
      else C1.tail.filter(isPrime))  // by eval. if
      .apply(1)
```

```
Let's abbreviate cons(1000, lazyRange(1000 + 1, 10000)) to C1.
     C1.filter(isPrime).apply(1)
 --> (if C1.isEmpty then C1
                                              // by expanding filter
      else if isPrime(C1.head) then cons(C1.head, C1.tail.filter(isPrime))
      else C1.tail.filter(isPrime))
      .apply(1)
 --> (if isPrime(C1.head) then cons(C1.head, C1.tail.filter(isPrime))
      else C1.tail.filter(isPrime))  // by eval. if
      .apply(1)
 --> (if isPrime(1000) then cons(C1.head, C1.tail.filter(isPrime))
      else C1.tail.filter(isPrime))  // by eval. head
      .applv(1)
```

```
-->> (if false then cons(C1.head, C1.tail.filter(isPrime)) // by eval. isPrime
    else C1.tail.filter(isPrime))
    .apply(1)
```

```
-->> (if false then cons(C1.head, C1.tail.filter(isPrime)) // by eval. isPrime
    else C1.tail.filter(isPrime))
    .apply(1)

--> C1.tail.filter(isPrime).apply(1) // by eval. if
```

```
-->> (if false then cons(C1.head, C1.tail.filter(isPrime)) // by eval. isPrime
    else C1.tail.filter(isPrime))
        .apply(1)

--> C1.tail.filter(isPrime).apply(1) // by eval. if

-->> lazyRange(1001, 10000) // by eval. tail
        .filter(isPrime).apply(1)
```

The evaluation sequence continues like this until:

```
-->> (if false then cons(C1.head, C1.tail.filter(isPrime)) // by eval. isPrime
      else C1.tail.filter(isPrime))
      .apply(1)
--> C1.tail.filter(isPrime).apply(1)
                                                           // by eval. if
                                                         // by eval. tail
-->> lazvRange(1001, 10000)
      .filter(isPrime).applv(1)
The evaluation sequence continues like this until:
```

```
-->> lazvRange(1009, 10000)
     .filter(isPrime).apply(1)
```

--> cons(1009, lazyRange(1009 + 1, 10000)) // by eval. lazyRange .filter(isPrime).apply(1)

```
Let's abbreviate cons(1009, lazyRange(1009 + 1, 10000)) to C2.
```

C2.filter(isPrime).apply(1)

Assuming apply is defined like this in LazyList[T]:

```
def apply(n: Int): T =
  if n == 0 then head
  else tail.apply(n-1)
```

```
Let's abbreviate cons(1009, lazyRange(1009 + 1, 10000)) to C2.
     C2.filter(isPrime).apply(1)
 -->> cons(1009, C2.tail.filter(isPrime)).apply(1)
                                                      // by eval. filter
 --> if 1 == 0 then cons(1009, C2.tail.filter(isPrime)).head // by eval. apply
     else cons(1009, C2.tail.filter(isPrime)).tail.applv(0)
 --> cons(1009, C2.tail.filter(isPrime)).tail.apply(0) // by eval. if
```

```
Let's abbreviate cons(1009, lazyRange(1009 + 1, 10000)) to C2.
     C2.filter(isPrime).apply(1)
                                                      // by eval. filter
 -->> cons(1009, C2.tail.filter(isPrime)).applv(1)
 --> if 1 == 0 then cons(1009, C2.tail.filter(isPrime)).head // by eval. apply
     else cons(1009, C2.tail.filter(isPrime)).tail.applv(0)
 --> cons(1009, C2.tail.filter(isPrime)).tail.apply(0) // by eval. if
 --> C2.tail.filter(isPrime).apply(0)
                                                          // by eval. tail
```

```
Let's abbreviate cons(1009, lazyRange(1009 + 1, 10000)) to C2.
     C2.filter(isPrime).apply(1)
                                                      // by eval. filter
 --> cons(1009, C2.tail.filter(isPrime)).apply(1)
 --> if 1 == 0 then cons(1009, C2.tail.filter(isPrime)).head // by eval. apply
     else cons(1009, C2.tail.filter(isPrime)).tail.apply(0)
 --> cons(1009, C2.tail.filter(isPrime)).tail.apply(0) // by eval. if
 --> C2.tail.filter(isPrime).apply(0)
                                                         // by eval. tail
 --> lazyRange(1010, 10000).filter(isPrime).apply(0) // by eval. tail
```

The process continues until

```
. . .
```

--> lazyRange(1013, 10000).filter(isPrime).apply(0)

The process continues until

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```
. . .
 --> lazyRange(1013, 10000).filter(isPrime).apply(0)
 --> cons(1013, lazvRange(1013 + 1, 10000))
                                                      // by eval. lazyRange
      .filter(isPrime).applv(0)
Let C3 be a shorthand for cons(1013, lazyRange(1013 + 1, 10000).
     C3.filter(isPrime).applv(0)
 -->> cons(1013, C3.tail.filter(isPrime)).apply(0) // by eval. filter
```

The process continues until

```
. . .
 --> lazyRange(1013, 10000).filter(isPrime).apply(0)
 --> cons(1013, lazyRange(1013 + 1, 10000))
                                                     // by eval. lazyRange
      .filter(isPrime).applv(0)
Let C3 be a shorthand for cons(1013, lazyRange(1013 + 1, 10000).
     C3.filter(isPrime).apply(0)
 -->> cons(1013, C3.tail.filter(isPrime)).apply(0)
                                                      // by eval. filter
 --> 1013
                                                       // by eval. apply
```

Only the part of the lazy list necessary to compute the result has been constructed.

RealWorld Lazy List

The simplified implementation shown for LazyList has a lazy tail, but not a lazy head, nor a lazy isEmpty.

The real implementation is lazy for all three operations.

To do this, it maintain a lazy state variable, like this:

```
class LazyList[+T](init: => State[T]):
    lazy val state: State[T] = init

enum State[T]:
    case Empty
    case Cons(hd: T, tl: LazyList[T])
```