

Translation of For

Principles of Functional Programming

For-Expressions and Higher-Order Functions

The syntax of for is closely related to the higher-order functions map, flatMap and filter.

First of all, these functions can all be defined in terms of for:

```
def mapFun[T, U](xs: List[T], f: T => U): List[U] =
  for x <- xs yield f(x)

def flatMap[T, U](xs: List[T], f: T => Iterable[U]): List[U] =
  for x <- xs; y <- f(x) yield y

def filter[T](xs: List[T], p: T => Boolean): List[T] =
  for x <- xs if p(x) yield x</pre>
```

Translation of For (1)

In reality, the Scala compiler expresses for-expressions in terms of map, flatMap and a lazy variant of filter.

Here is the translation scheme used by the compiler (we limit ourselves here to simple variables in generators)

1. A simple for-expression

```
for x <- e1 yield e2
```

is translated to

```
e1.map(x \Rightarrow e2)
```

Translation of For (2)

2. A for-expression

```
for x <- e1 if f; s yield e2
```

where f is a filter and s is a (potentially empty) sequence of generators and filters, is translated to

```
for x \leftarrow e1.withFilter(x \Rightarrow f); s yield e2
```

(and the translation continues with the new expression)

You can think of withFilter as a variant of filter that does not produce an intermediate list, but instead applies the following map or flatMap function application only to those elements that passed the test.

Translation of For (3)

3. A for-expression

```
for x <- e1; y <- e2; s yield e3
```

where s is a (potentially empty) sequence of generators and filters, is translated into

```
e1.flatMap(x \Rightarrow for y \leftarrow e2; s yield e3)
```

(and the translation continues with the new expression)

Example

Take the for-expression that computed pairs whose sum is prime:

```
for
    i <- 1 until n
    j <- 1 until i
    if isPrime(i + j)
yield (i, j)</pre>
```

Applying the translation scheme to this expression gives:

```
(1 until n).flatMap(i =>
  (1 until i)
   .withFilter(j => isPrime(i+j))
   .map(j => (i, j)))
```

This is almost exactly the expression which we came up with first!

Exercise

Translate

```
for b <- books; a <- b.authors if a.startsWith("Bird")
yield b.title</pre>
```

into higher-order functions.

Exercise

```
for b <- books; a <- b.authors if a.startsWith("Bird")
yield b.title</pre>
```

The expression above expands to which of the following two expressions?

```
books.flatMap(b =>
    b.authors.withFilter(a =>
        a.startsWith("Bird")).map(a => b.title))
books.map(b =>
    b.authors.flatMap(a =>
    if a.startsWith("Bird") then b.title))
```

Generalization of for

Interestingly, the translation of for is not limited to lists or sequences, or even collections;

It is based solely on the presence of the methods map, flatMap and withFilter.

This lets you use the for syntax for your own types as well — you must only define map, flatMap and withFilter for these types.

There are many types for which this is useful: arrays, iterators, databases, optional values, parsers, etc.

For and Databases

For example, books might not be a list, but a database stored on some server.

As long as the client interface to the database defines the methods map, flatMap and withFilter, we can use the for syntax for querying the database.

This is the basis of data base connection frameworks such as Slick or Quill, as well as big data platforms such as Spark.