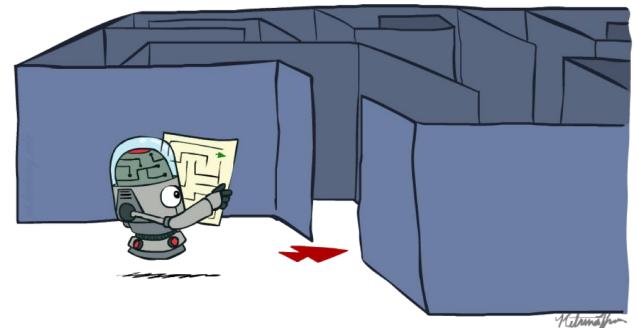
### CS 411: Artificial Intelligence I

#### Search



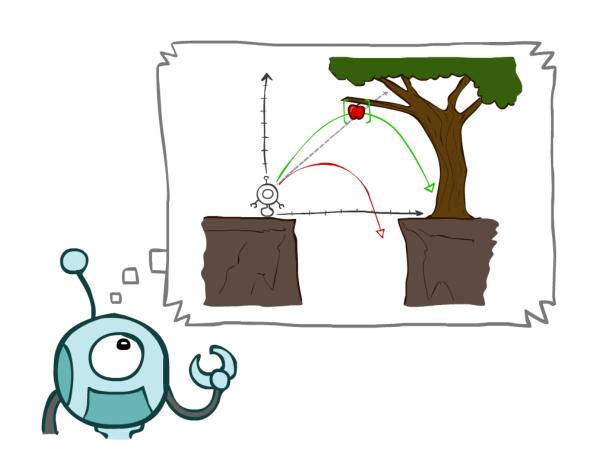
Instructor: Prof. Ian Kash

University of Illinois at Chicago

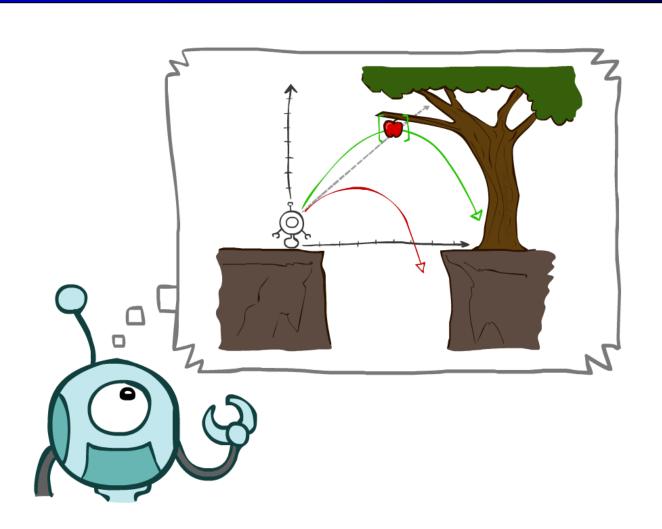
# Today

- Agents that Plan Ahead
- Search Problems

- Uninformed Search Methods
  - Depth-First Search
  - Breadth-First Search
  - Uniform-Cost Search



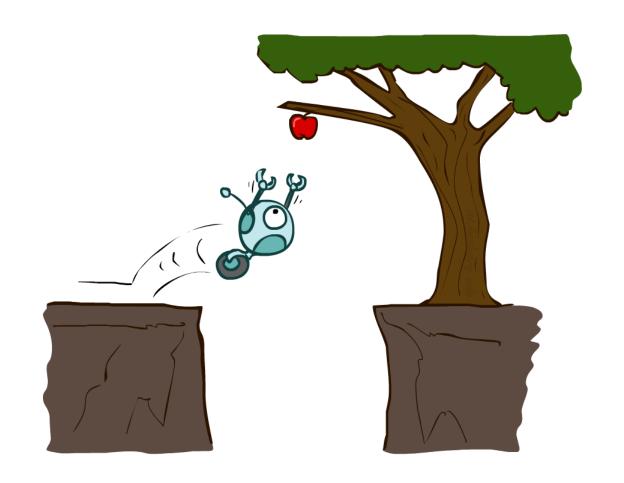
# Agents that Plan



### Reflex Agents

#### Reflex agents:

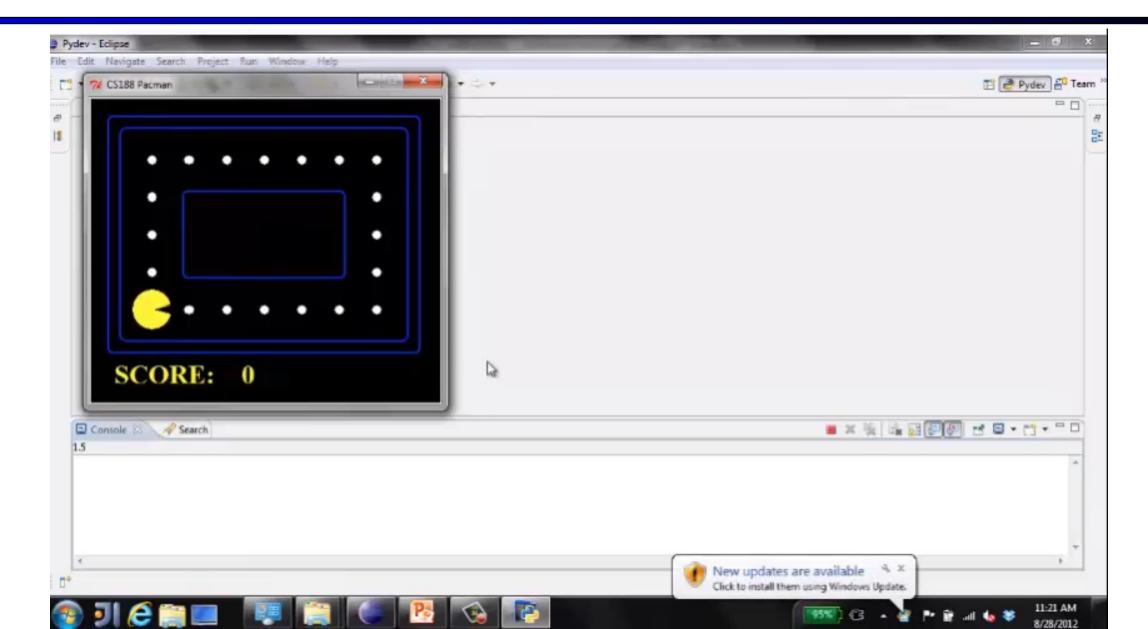
- Choose action based on current percept (and maybe memory)
- May have memory or a model of the world's current state
- Do not consider the future consequences of their actions
- Consider how the world IS
- Can a reflex agent be rational?



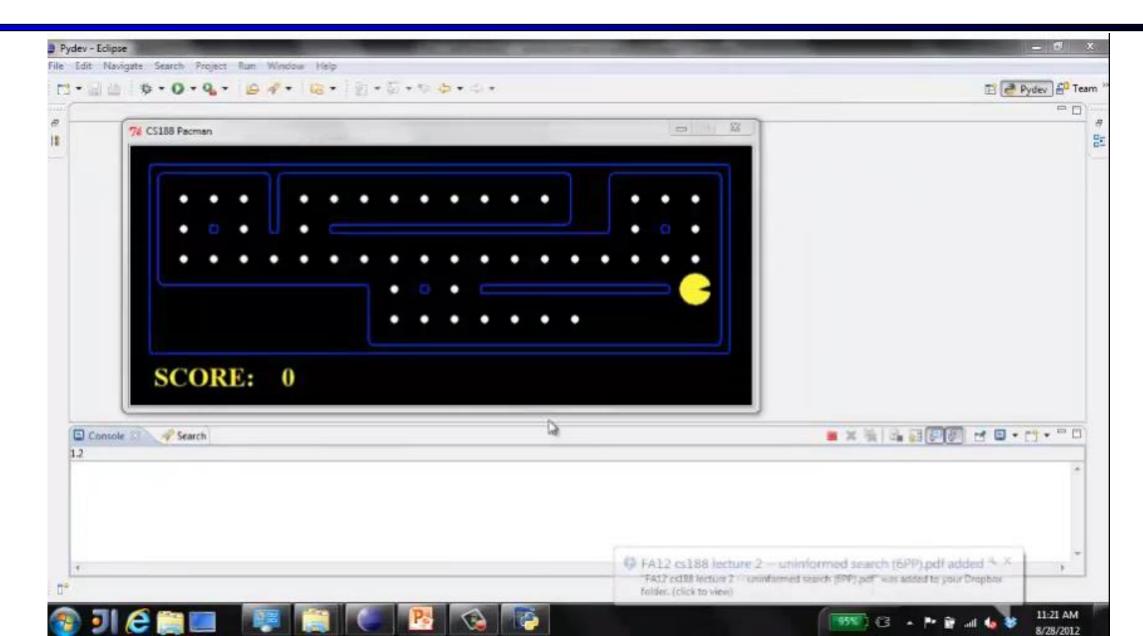
[Demo: reflex optimal (L2D1)]

[Demo: reflex optimal (L2D2)]

# Video of Demo Reflex Optimal

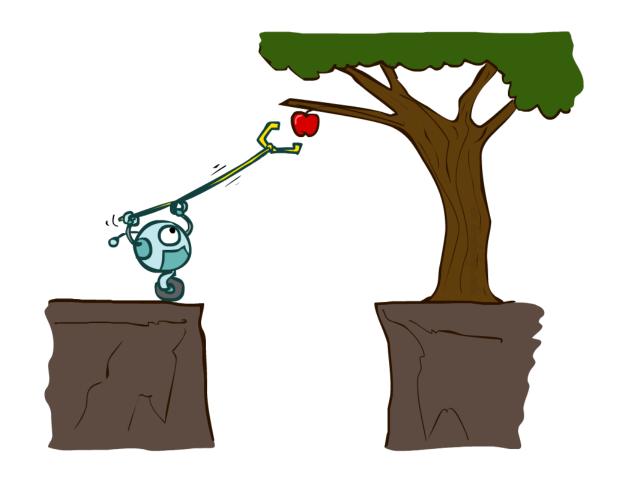


#### Video of Demo Reflex Odd



## Planning Agents

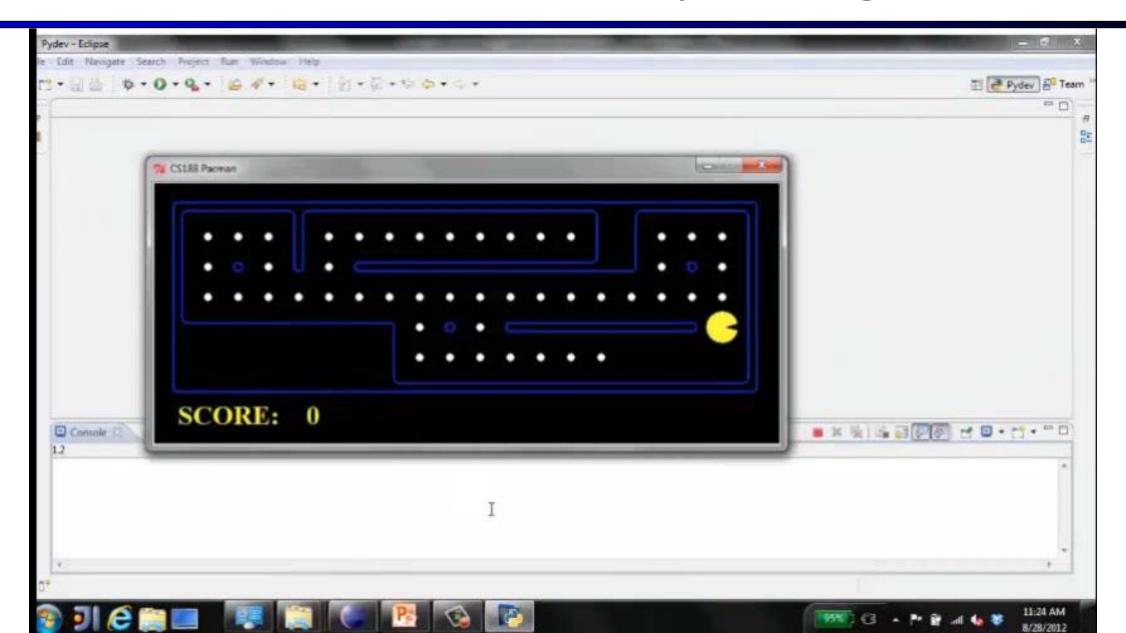
- Planning agents:
  - Ask "what if"
  - Decisions based on (hypothesized) consequences of actions
  - Must have a model of how the world evolves in response to actions
  - Must formulate a goal (test)
  - Consider how the world WOULD BE
- Optimal vs. complete planning
- Planning vs. replanning



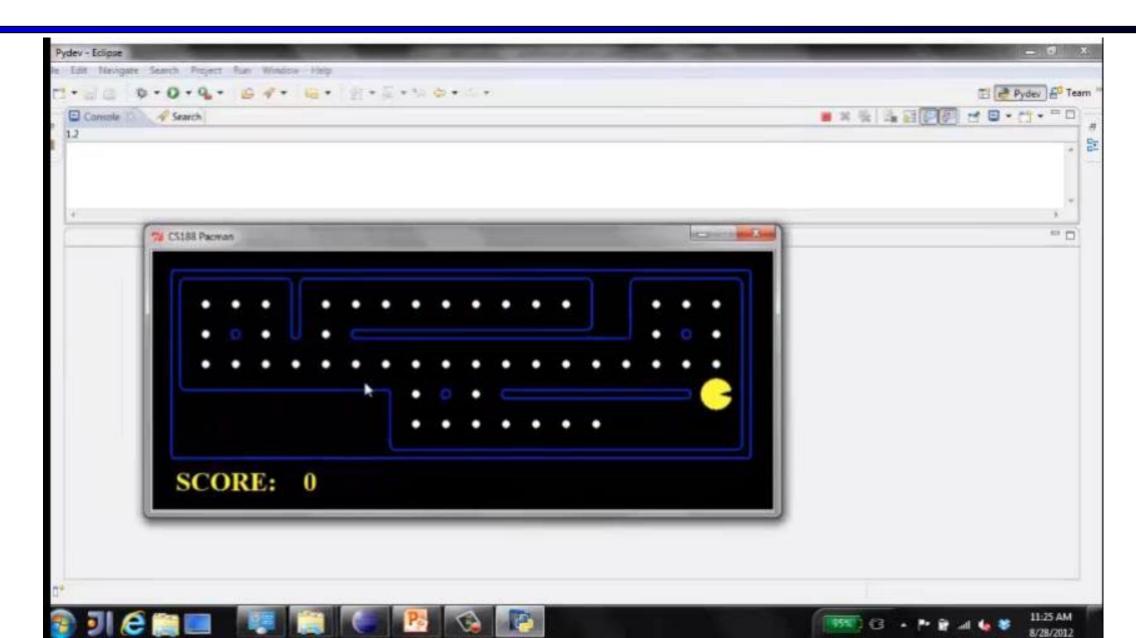
[Demo: replanning (L2D3)]

[Demo: mastermind (L2D4)]

# Video of Demo Replanning



#### Video of Demo Mastermind



# Search Problems



#### Search Problems

- A search problem consists of:
  - A state space





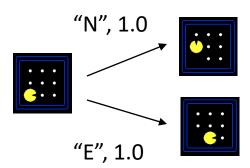








A successor function (with actions, costs)



- A start state and a goal test
- A solution is a sequence of actions (a plan) which transforms the start state to a goal state

## Search Problems Are Models



### Example: Pancakes

The chef in our place is sloppy, and when he prepares a stack of pancakes they come out all different sizes. Therefore, when I deliver them to a customer, on the way to the table I rearrange them (so that the smallest winds up on top, and so on, down to the largest at the bottom) by grabbing several from the top and flipping them over, repeating this (varying the number I flip) as many times as necessary. If there are n pancakes, what is the maximum number of flips (as a function f(n) of n) that I will ever have to use to rearrange them?

[Text: Discrete Mathematics 27 (1979) 47-57]

### Example: Pancakes

#### **BOUNDS FOR SORTING BY PREFIX REVERSAL**

William H. GATES

Microsoft, Albuquerque, New Mexico

Christos H. PAPADIMITRIOU\*†

Department of Electrical Engineering, University of California, Berkeley, CA 94720, U.S.A.

Received 18 January 1978 Revised 28 August 1978

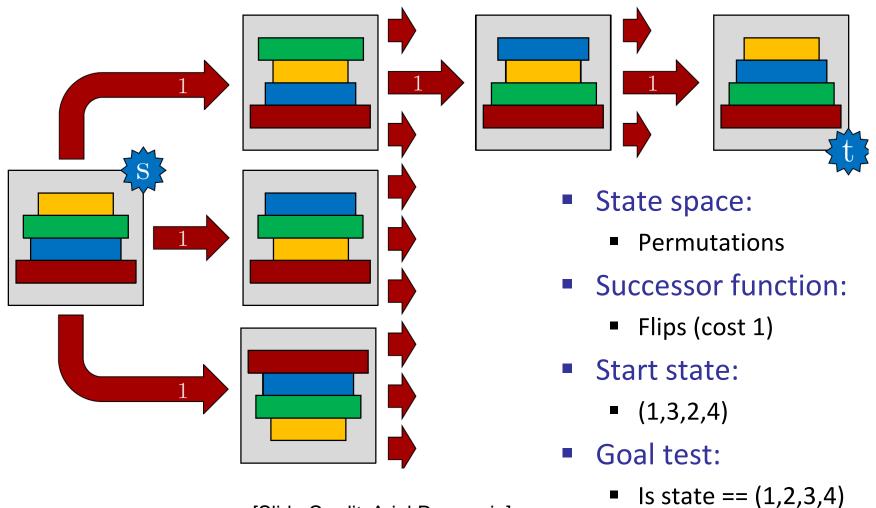
For a permutation  $\sigma$  of the integers from 1 to n, let  $f(\sigma)$  be the smallest number of prefix reversals that will transform  $\sigma$  to the identity permutation, and let f(n) be the largest such  $f(\sigma)$  for all  $\sigma$  in (the symmetric group)  $S_n$ . We show that  $f(n) \leq (5n+5)/3$ , and that  $f(n) \geq 17n/16$  for n a multiple of 16. If, furthermore, each integer is required to participate in an even number of reversed prefixes, the corresponding function g(n) is shown to obey  $3n/2 - 1 \leq g(n) \leq 2n + 3$ .





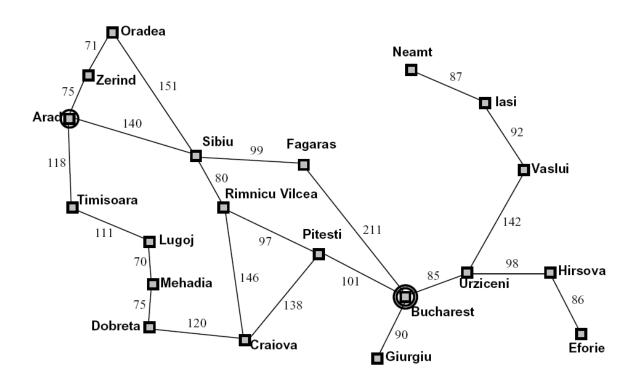
[Text: Discrete Mathematics 27 (1979) 47-57, Images: Wikipedia]

# Example: Pancakes



[Slide Credit: Ariel Procaccia]

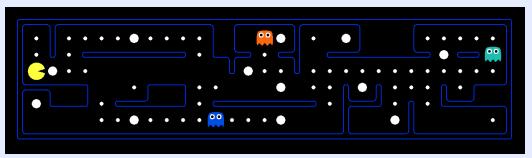
## Example: Traveling in Romania



- State space:
  - Cities
- Successor function:
  - Roads: Go to adjacent city with cost = distance
- Start state:
  - Arad
- Goal test:
  - Is state == Bucharest?
- Solution?

## What's in a State Space?

The world state includes every last detail of the environment



A search state keeps only the details needed for planning (abstraction)

- Problem: Pathing
  - States: (x,y) location
  - Actions: NSEW
  - Successor: update location only
  - Goal test: is (x,y)=END

- Problem: Eat-All-Dots
  - States: {(x,y), dot booleans}
  - Actions: NSEW
  - Successor: update location and possibly a dot boolean
  - Goal test: dots all false

### State Space Sizes?

#### World state:

Agent positions: 120

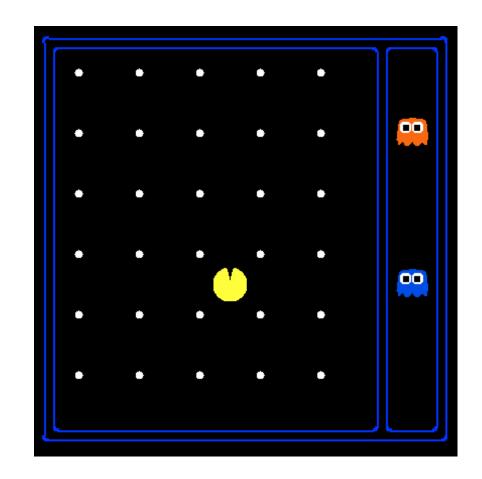
■ Food count: 30

Ghost positions: 12

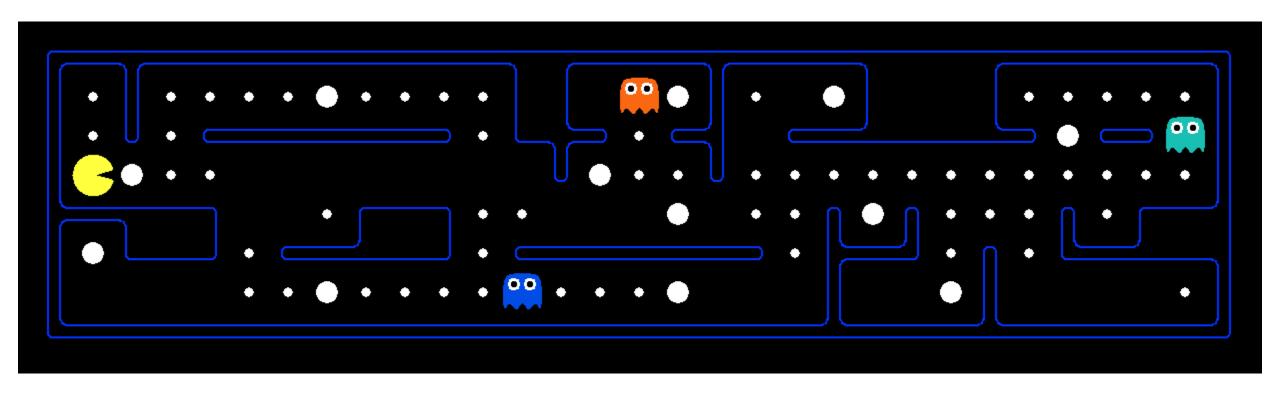
Agent facing: NSEW

#### How many

- World states?
   120x(2<sup>30</sup>)x(12<sup>2</sup>)x4
- States for pathing?120
- States for eat-all-dots?
   120x(2<sup>30</sup>)

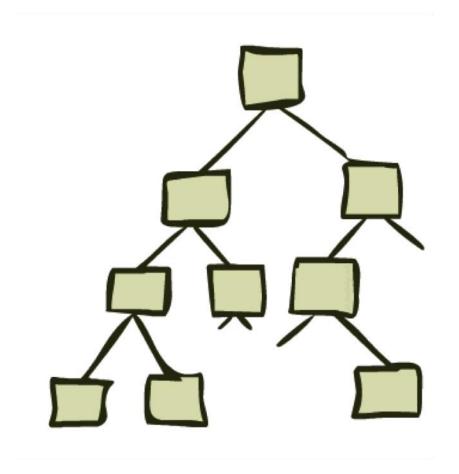


### Quiz: Safe Passage



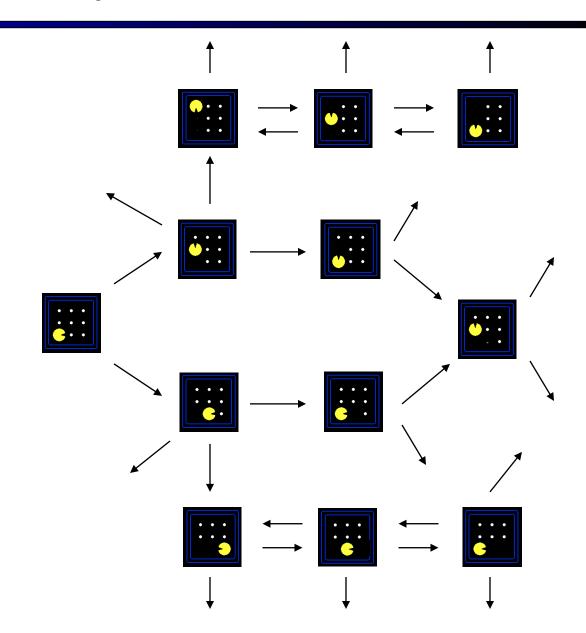
- Problem: eat all dots while keeping the ghosts perma-scared
- What does the state space have to specify?
  - (agent position, dot booleans, power pellet booleans, remaining scared time)

# State Space Graphs and Search Trees



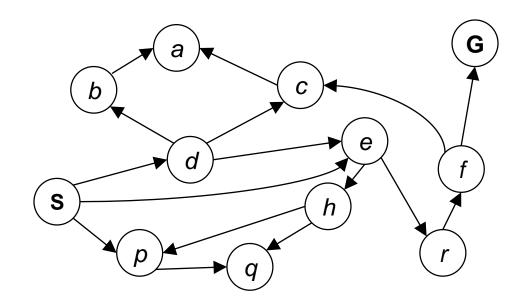
### State Space Graphs

- State space graph: A mathematical representation of a search problem
  - Nodes are (abstracted) world configurations
  - Arcs represent successors (action results)
  - The goal test is a set of goal nodes (maybe only one)
- In a state space graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea



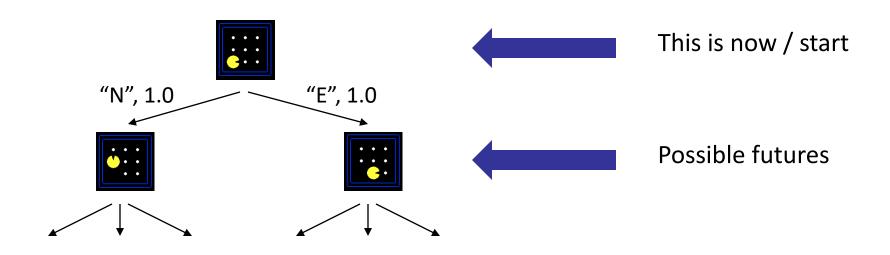
### State Space Graphs

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Tiny search graph for a tiny search problem

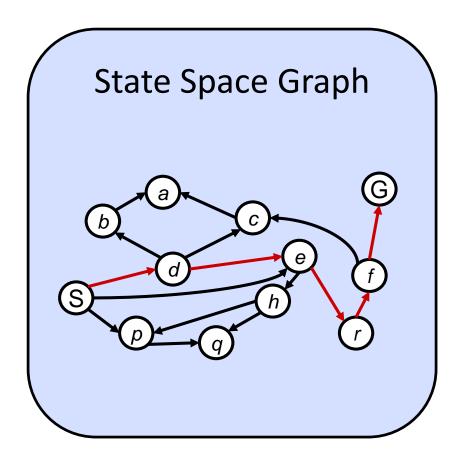
#### Search Trees



#### A search tree:

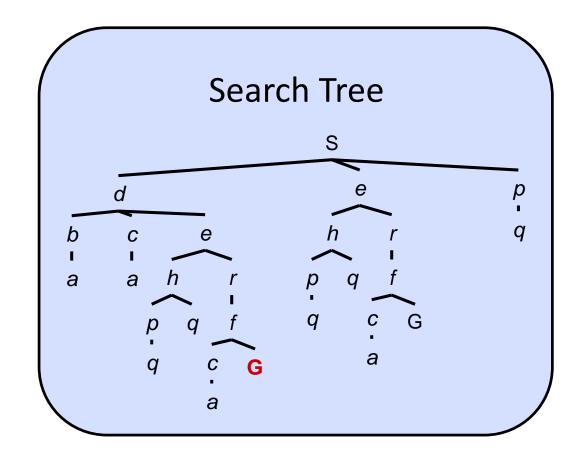
- A "what if" tree of plans and their outcomes
- The start state is the root node
- Children correspond to successors
- Nodes show states, but correspond to PLANS that achieve those states
- For most problems, we can never actually build the whole tree

## State Space Graphs vs. Search Trees



Each NODE in in the search tree is an entire PATH in the state space graph.

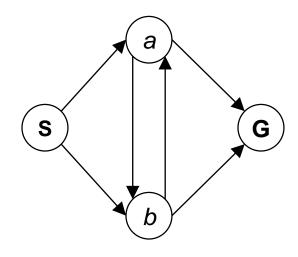
We construct both on demand – and we construct as little as possible.



## Quiz: State Space Graphs vs. Search Trees

Consider this 4-state graph:

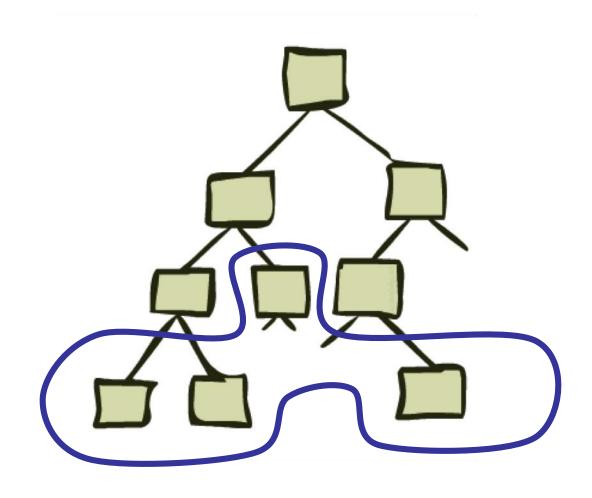
How big is its search tree (from S)?



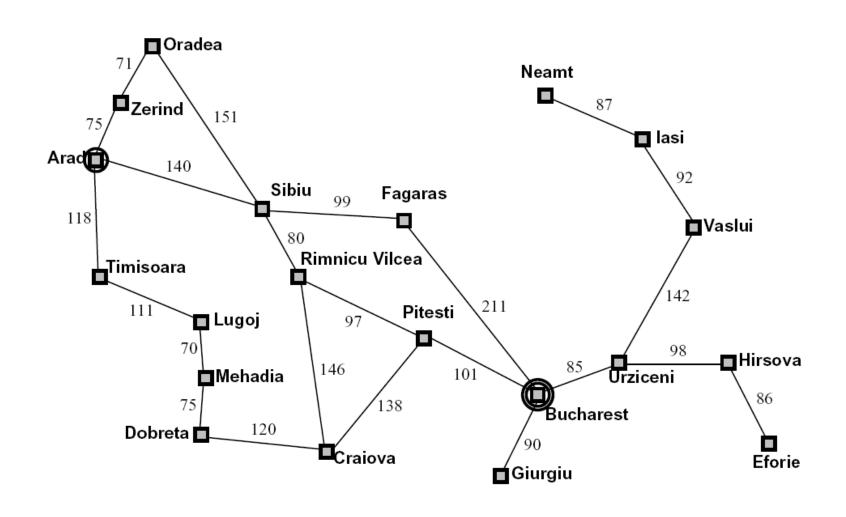


Important: Lots of repeated structure in the search tree!

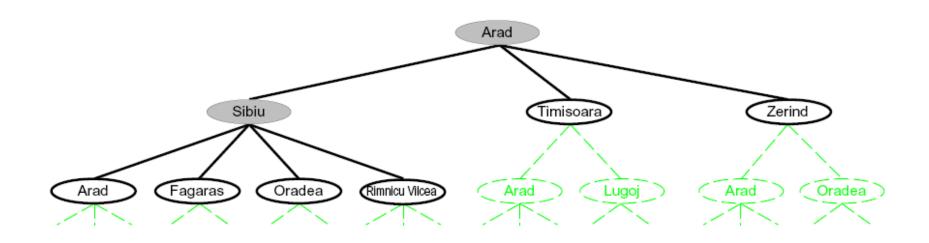
# Tree Search



# Search Example: Romania



### Searching with a Search Tree



#### Search:

- Expand out potential plans (tree nodes)
- Maintain a fringe of partial plans under consideration
- Try to expand as few tree nodes as possible

#### General Tree Search

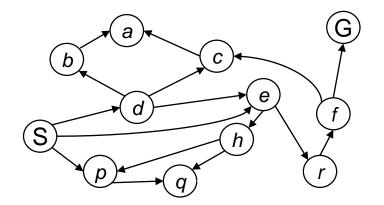
```
function TREE-SEARCH( problem, strategy) returns a solution, or failure initialize the search tree using the initial state of problem loop do

if there are no candidates for expansion then return failure choose a leaf node for expansion according to strategy

if the node contains a goal state then return the corresponding solution else expand the node and add the resulting nodes to the search tree end
```

- Important ideas:
  - Fringe
  - Expansion
  - Exploration strategy
- Main question: which fringe nodes to explore?

# Example: Tree Search



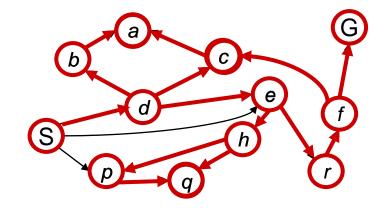
# Depth-First Search

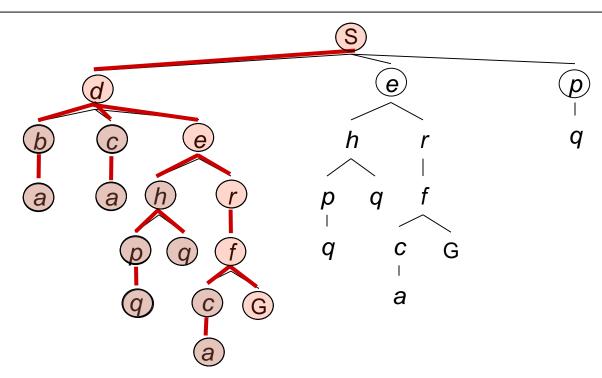


# Depth-First Search

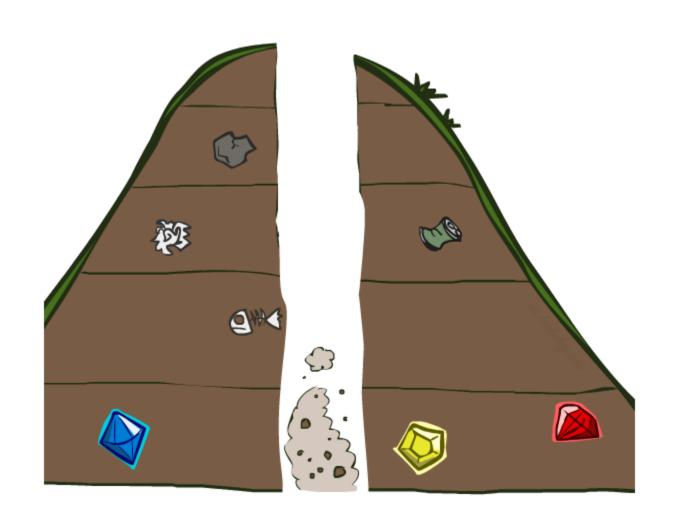
Strategy: expand a deepest node first

Implementation: Fringe is a LIFO stack



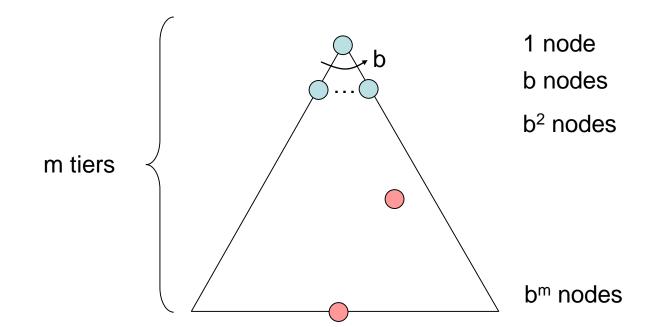


# Search Algorithm Properties



### Search Algorithm Properties

- Complete: Guaranteed to find a solution if one exists?
- Optimal: Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?
- Cartoon of search tree:
  - b is the branching factor
  - m is the maximum depth
  - solutions at various depths



- Number of nodes in entire tree?
  - $1 + b + b^2 + .... b^m = O(b^m)$

# Depth-First Search (DFS) Properties

#### What nodes DFS expand?

- Some left prefix of the tree.
- Could process the whole tree!
- If m is finite, takes time O(b<sup>m</sup>)

#### How much space does the fringe take?

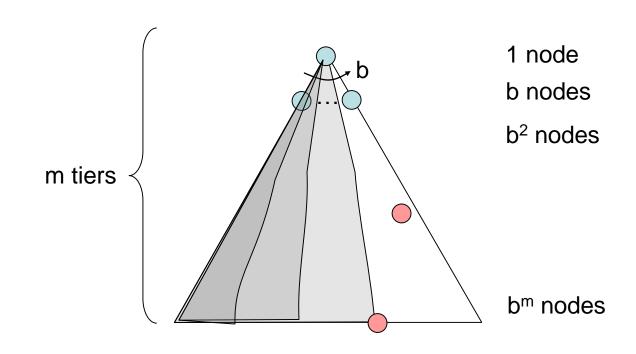
Only has siblings on path to root, so O(bm)

#### Is it complete?

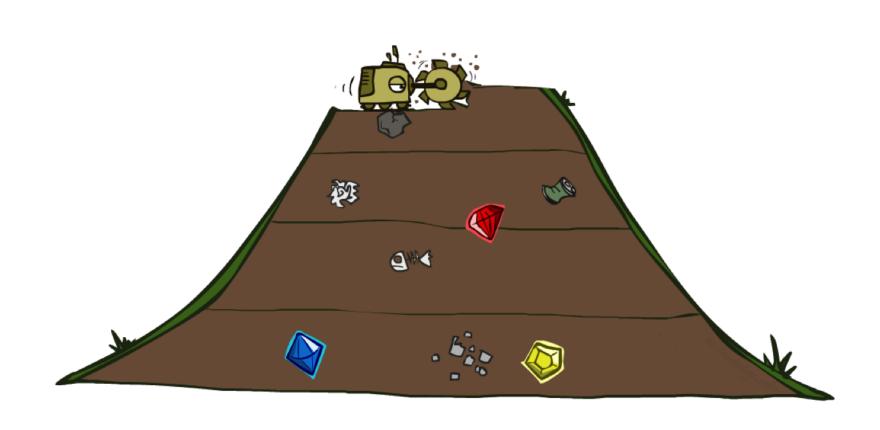
 m could be infinite, so only if we prevent cycles (more later)

#### Is it optimal?

 No, it finds the "leftmost" solution, regardless of depth or cost



# **Breadth-First Search**

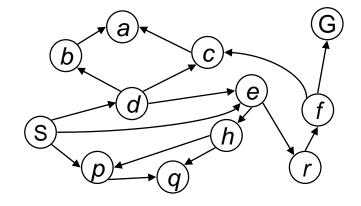


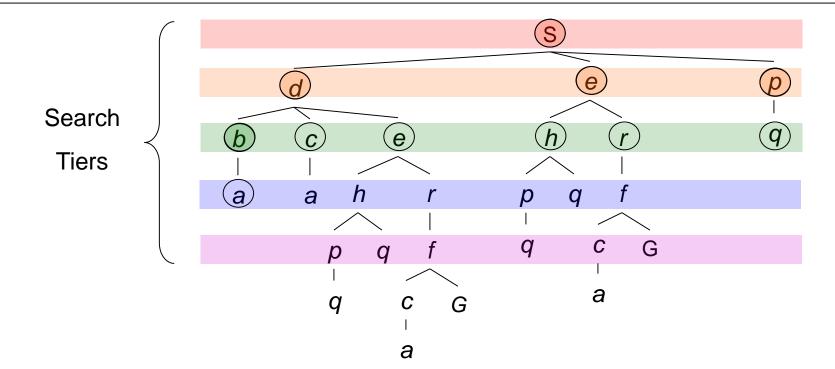
### **Breadth-First Search**

Strategy: expand a shallowest node first

*Implementation: Fringe* 

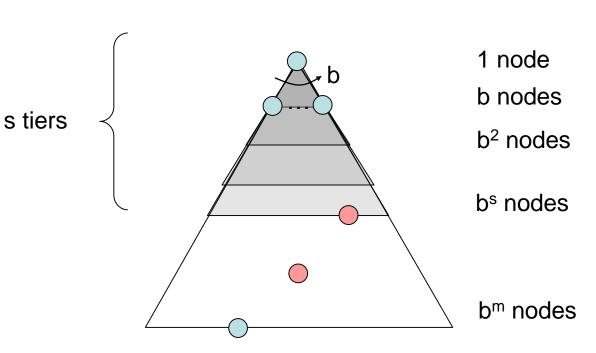
is a FIFO queue



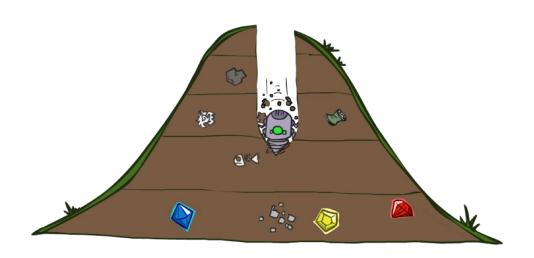


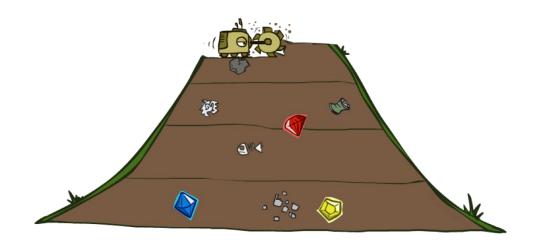
## Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
  - Processes all nodes above shallowest solution
  - Let depth of shallowest solution be s
  - Search takes time O(b<sup>s</sup>)
- How much space does the fringe take?
  - Has roughly the last tier, so O(b<sup>s</sup>)
- Is it complete?
  - s must be finite if a solution exists, so yes!
- Is it optimal?
  - Only if costs are all 1 (more on costs later)



# Quiz: DFS vs BFS



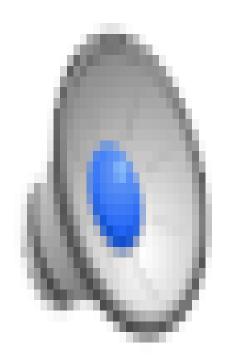


### Quiz: DFS vs BFS

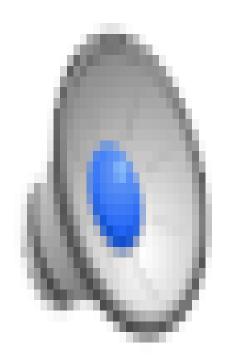
When will BFS outperform DFS?

When will DFS outperform BFS?

## Video of Demo Maze Water DFS/BFS (part 1)

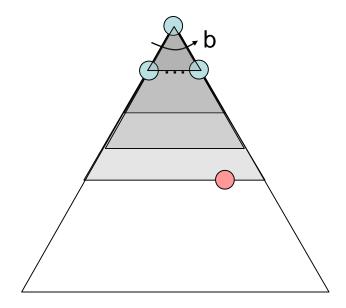


## Video of Demo Maze Water DFS/BFS (part 2)

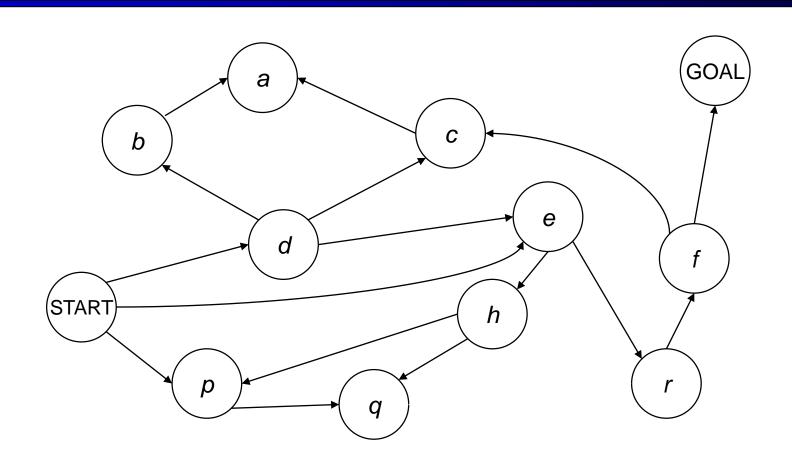


## Iterative Deepening

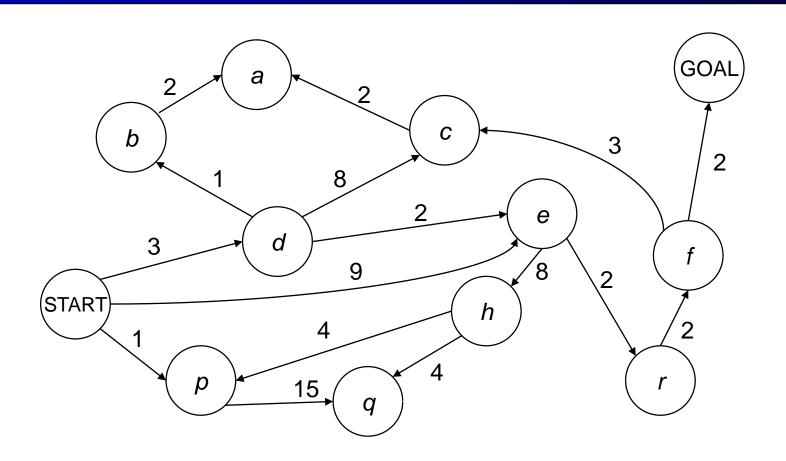
- Idea: get DFS's space advantage with BFS's time / shallow-solution advantages
  - Run a DFS with depth limit 1. If no solution...
  - Run a DFS with depth limit 2. If no solution...
  - Run a DFS with depth limit 3. .....
- Isn't that wastefully redundant?
  - Generally most work happens in the lowest level searched, so not so bad!



# **Iterative Deepening**

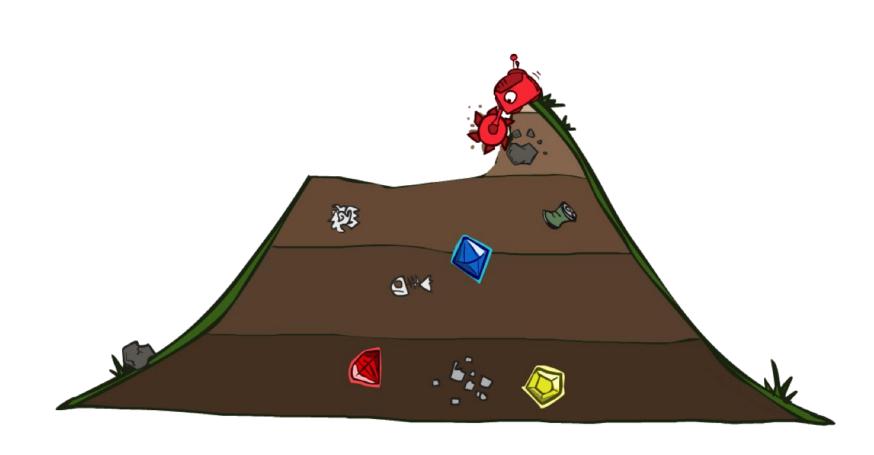


#### **Cost-Sensitive Search**



BFS finds the shortest path in terms of number of actions. It does not find the least-cost path. We will now cover a similar algorithm which does find the least-cost path.

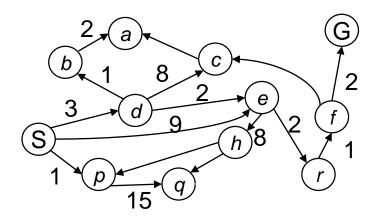
## **Uniform Cost Search**

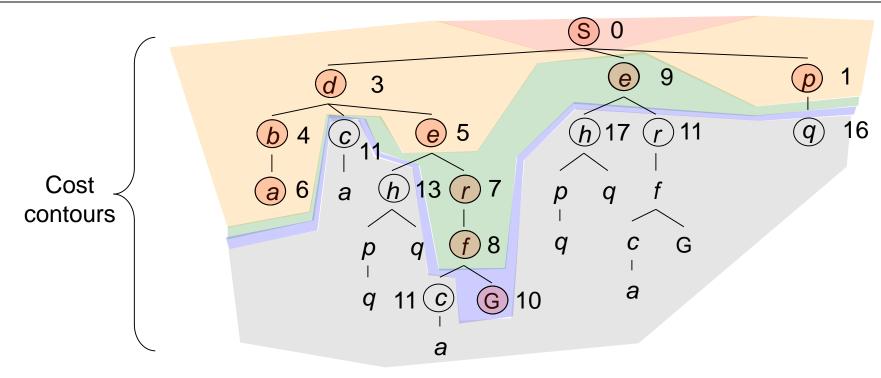


### **Uniform Cost Search**

Strategy: expand a cheapest node first:

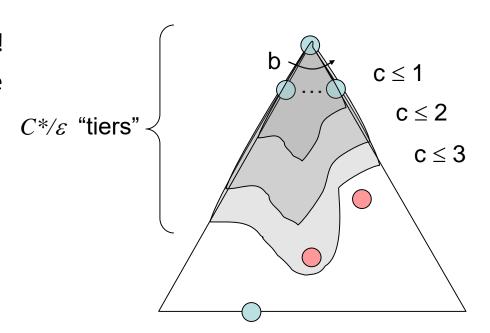
Fringe is a priority queue (priority: cumulative cost)





## Uniform Cost Search (UCS) Properties

- What nodes does UCS expand?
  - Processes all nodes with cost less than cheapest solution!
  - If that solution costs  $C^*$  and arcs cost at least  $\varepsilon$ , then the "effective depth" is roughly  $C^*/\varepsilon$
  - Takes time  $O(b^{C*/\varepsilon})$  (exponential in effective depth)
- How much space does the fringe take?
  - Has roughly the last tier, so  $O(b^{C*/\epsilon})$
- Is it complete?
  - Assuming best solution has a finite cost and minimum arc cost is positive, yes!
- Is it optimal?
  - Yes! (Proof next lecture via A\*)



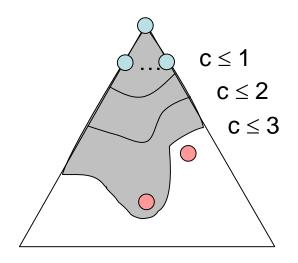
#### **Uniform Cost Issues**

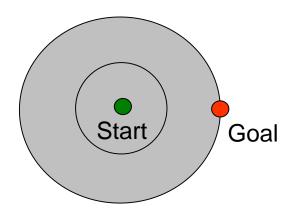
 Remember: UCS explores increasing cost contours

The good: UCS is complete and optimal!

- The bad:
  - Explores options in every "direction"
  - No information about goal location

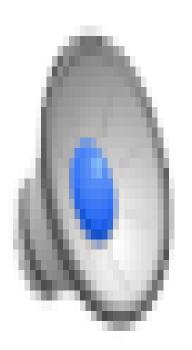
We'll fix that soon!



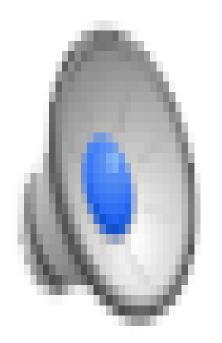


[Demo: empty grid UCS (L2D5)] [Demo: maze with deep/shallow water DFS/BFS/UCS (L2D7)]

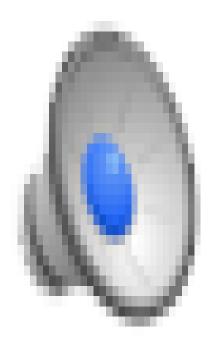
# Video of Demo Empty UCS



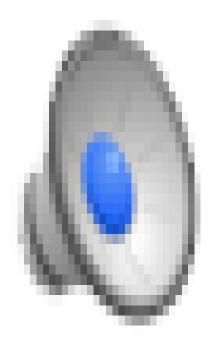
#### Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 1)



#### Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 2)



#### Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 3)



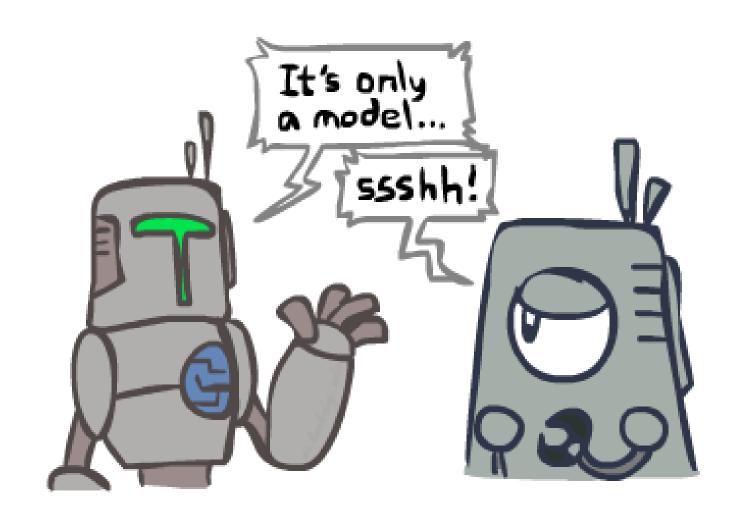
#### The One Queue

- All these search algorithms are the same except for fringe strategies
  - Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
  - Practically, for DFS and BFS, you can avoid the log(n) overhead from an actual priority queue, by using stacks and queues
  - Can even code one implementation that takes a variable queuing object



#### Search and Models

- Search operates over models of the world
  - The agent doesn't actually try all the plans out in the real world!
  - Planning is all "in simulation"
  - Your search is only as good as your models...



# Search Gone Wrong?

