Matrici si determinanti

Motrice de tipul m x n (m-linir n' n-colorne) au conficienti in K, unde K str Q, R, C (see chair Z, Zm):

$$A = \begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{2m} \\ a_{i1} & a_{i2} & a_{ij} & a_{im} \end{pmatrix} = \begin{pmatrix} a_{ij} \\ a_{ij} \end{pmatrix}_{1 \leq i \leq m}$$

$$\begin{pmatrix} a_{i1} & a_{i2} & a_{ij} & a_{im} \\ a_{m1} & a_{m2} & a_{mj} & a_{mn} \end{pmatrix} \qquad a_{ij} \in K, \ t i, j.$$

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- adu narea: $(O_{ij}) + (b_{ij}) = (C_{ij})_{...}$, $C_{ij} = O_{ij} + b_{ij}$. $I = j \in M$

$$\left(\begin{array}{cc} x & y \\ \overline{z} & \overline{t} \end{array}\right) + \left(\begin{array}{cc} x & \beta \\ \overline{z} & \overline{z} \end{array}\right) = \left(\begin{array}{cc} x + x & y + \beta \\ \overline{z} + \overline{y} & \overline{t} + \overline{z} \end{array}\right)$$

- in multine: (0;;) (b;;) = (d;;) - r de colone pt (9;)

d. - Q. h. + Q. h. + + Q. b. = r de lini din (b;;) dij = ai, b, + ai, bzj + ... + aip bpj

d₁₃ = 0,1. b₁₃ + a₁₂. b₂₃ + 0,3 b₃₃

I Cumultirea motricilos mu este comobbira doci -) AB ni BA m stim ce AB = BA

1. Fix X o motrie en conficient rede a.i.: $\begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix} X = X \begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix}. \qquad \begin{pmatrix} 4 \end{pmatrix} \begin{array}{c} 26 \\ 5 \\ 7 \end{array}$ $(x^2=1)$ Aleysti vorientels coxcet din cele de mai jos:

A) $X = \begin{pmatrix} 0 & 2 \\ 3 & 0 \end{pmatrix}$ $X = \begin{pmatrix} \times & \beta \\ 3p \\ 2 \end{pmatrix}$ X = R(c) $X = \begin{pmatrix} a & 25 \\ 35 & a \end{pmatrix}$, $a = \begin{pmatrix} a & 25 \\ a & b \end{pmatrix}$, $a = \begin{pmatrix} a & 2$ 1 D) Oriv motive din Mz (R) verifice egalitotee de mai sus. $X = \begin{pmatrix} m & m \\ p & g \end{pmatrix} \Rightarrow \begin{pmatrix} 1 & 2 \\ 3 & l \end{pmatrix} \begin{pmatrix} m & m \\ p & g \end{pmatrix} = \begin{pmatrix} m & m \\ p & g \end{pmatrix} \cdot \begin{pmatrix} 3 & 1 \\ 3 & 1 \end{pmatrix}$ $\left(\frac{m+2p}{3m+p}, \frac{m+2q}{3m+q}\right) = \left(\frac{m+3m}{2m+3m}, \frac{2m+m}{2p+q}\right)$ $\begin{cases} \frac{2p = 3m}{22 = 2m} \\ \frac{3m = 32}{3m = 2p} \end{cases} = \begin{cases} 1 & 2p = 3m \\ m = 9 \end{cases}$ m = 9 m = 9

2. Fix
$$A = \begin{pmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$
 or $P, Q \in \mathbb{R}$ $Q. P.$

$$A^{2021} = P A^2 + Q A.$$

A) $PQ < 0$ B) P proportion of P constants P and P constants P cons

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$$\begin{cases}
2^{220} = p \cdot 2 + 9 \\
1 = p + 9
\end{cases} =) / p = 2^{2020} < 0$$

$$\begin{cases}
r_2 < 0 & \text{oh} \quad A \\
r_1 = r_1 = r_2
\end{cases} =) / p = 2^{2020} < 0$$

$$\begin{cases}
r_2 < 0 & \text{oh} \quad A \\
r_2 = 1
\end{cases} = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{100} + 1) = (2^{50} - 1)(2^{50} + 1)(2^{50} + 1) = (2^{50} - 1)(2^{50} + 1)(2^{$$

vorg A = cle moi mor dimersiane a unui minor ment of lui A. et colal: nylocó de la minor mici menti con se bor des to 3. $A = \begin{pmatrix} 1 & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & | & -2 & |$ Daco A mi 13 au ambele rongel 2, otunci (A) det(A) = det(B) = 0 [A-NV = CORECT 11] (B) 975 (C) 960, 50 (c) 9 <0, 6>0 (D) a>0, b>0. 3 1 = 7 70 rog A = 2 = $\begin{vmatrix} 1 & -2 & -2 \\ 3 & 4 & 0 \\ 3 & -1 & 1 \end{vmatrix} = 0 = 2 = 19/5$ rong B = ? =) ----1/ 1 -2 4 | = 0 => 6 = 44 3 -1 6 | = 0 => 6 = 7 1) Colculos. A $\frac{1}{4}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 4 & 1 \end{pmatrix}$

2.
$$D(0,1) = \begin{cases} 5 & 5a-3b & 5a^2+b^2-2ab \\ 5 & 5a-3b & 5a^2+b^2-2ab \end{cases}$$

(A) $D(a,b)$ on dyinh dx a.

(B) $\forall a \in \mathbb{R}$, $\int_{a} : \mathbb{R} \to \mathbb{R}$, $\int_{a}(x) = \mathcal{N}(a,x)$ is the impariance of the second o



