

Exercise 4

Implementing a centralized agent

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1 Solution Representation

Unless noted otherwise, values that are not defined explicitly here use the definitions provided in the reference paper.

1.1 Variables

The following variables are used to define the CSP:

- P - a set of plans, one for each vehicle.

$$P = \{p_1, p_2, \dots, p_{N_V}\}$$

- p_i - a doubly linked list representing the sequence of actions in a particular plan i.e. the deliveries and pickups that the vehicle should execute.

$$p_i = (u_1 \rightarrow u_2 \rightarrow d_2 \rightarrow \dots | u_i \in U \wedge d_i \in D)$$

- U - the set of pickups associated to each task.

$$U = \{u_1, u_2, \dots, u_{N_T}\}$$

- D - the set of deliveries associated to each task.

$$D = \{d_1, d_2, \dots, d_{N_T}\}$$

1.2 Constraints

1. All tasks must be delivered i.e. $p_1 \cup p_2 \cup \dots \cup p_{N_V} = U \cup D$
2. Max load of a given plan must be under the carrying capacity of the vehicle i.e. $maxLoad(p_i) \leq maxCapacity(v_i) \forall p_i \in P$
3. A plan can only deliver a task it has previously picked up i.e. $u_i \in predecessors(d_i) \forall u_i, d_i \in p_i$
4. A given action can only appear once in the set of all the plans.
5. If there is a pickup action in a plan then there is a corresponding delivery action in the same plan and vice-versa. i.e. $u_i \in p_i \leftrightarrow d_i \in p_i \forall p_i \in P, u_i \in p_i, d_i \in p_i$

1.3 Objective function

Let us first define the total cost of a vehicle v with a given plan.

$$c_v = \sum_{a_i \in p_v} (dist(a_i)) \cdot cost(v)$$

The total cost of the company is then defined by the sum of the costs of each vehicle in the company i.e.

$$\sum_{v_i \in V} c_{v_i}$$

2 Stochastic optimization

2.1 Initial solution

The initial solution is generated simply by giving all the tasks to the biggest vehicle.

2.2 Generating neighbours

Two operators are used to generate neighbours:

- *Changing vehicle*: give a pair of delivery and pickup tasks to another vehicle by appending them to the plan of the other vehicle. Weight constraints should not be violated by this change.
- *Changing task order*: change the order of two tasks in the plan of a vehicle while making sure that the order does not violate constraint 3; namely the fact that a delivery task cannot come before the associated pickup task.

2.3 Stochastic optimization algorithm

The algorithm works by first generating an initial solution that satisfies all the constraints. Then locally similar solutions are generated and the best one among them is chosen. This is repeated until a given number of iterations is reached. Since it uses a hill climbing heuristic, the algorithm is susceptible to getting stuck in a local minima and thus there is no guarantee of finding an optimal solution. To reduce the chances of getting stuck in a local minima, local improvements are only chosen with a certain probability.

3 Results

3.1 Experiment 1: Model parameters

3.1.1 Setting

3.1.2 Observations

3.2 Experiment 2: Different configurations

3.2.1 Setting

3.2.2 Observations