Parts of strings 1 Substrings

# Parts of strings

# 1 Substrings

A **substring** is a continuous part of a string.

# Example 1.

The string *abcd* has 11 substrings:

- ε
- a
- b
- c
- d
- *ab*
- *bc*
- *cd*
- *abc*
- bcd
- abcd

Note that

- 1. the empty string is a substring of every string, and
- 2. every string is a substring of itself.

A substring u of v is a **proper** substring iff  $u \neq v$ .

## EXAMPLE 2.

All the strings listed above are proper substrings of abcd, except abcd itself.

#### Exercise 1.

For each one of the gaps below, enter  $\sqsubseteq$ ,  $\subsetneq$ , or  $\not\sqsubseteq$  depending on whether the first string is a substring of the second string, a proper substring, or neither:

- a\_aaaa
- a b
- ε\_b
- ε ε
- aa abbbca
- bc abbbca
- cb\_abbbca

Parts of strings 2 Subsequence

# 2 Subsequence

A **subsequence** is a discontinuous part of a string that preserves the order between the symbols.

### EXAMPLE 3.

The string *abcd* has subsequences:

- ε
- a
- b
- c
- d
- ab
- ac
- ad
- *bc*
- *bd*
- *cd*
- abc
- *abd*
- bcd
- abcd

Note that ca is not a subsequence of abcd, but it is a subsequence of abcda.

Just like substrings, a subsequence u of v is proper iff  $u \neq v$ .

#### Exercise 2.

For each one of the gaps below, enter  $\sqsubseteq$ ,  $\subsetneq$ , or  $\not\sqsubseteq$  depending on whether the first string is a subsequence of the second string, a proper subsequence, or neither:

- a aaaa
- a b
- ε b
- ε ε
- aa abbbca
- bc abbbca
- cb\_abbbca

### Exercise 3.

Say whether the following is True or False: Every substring of some string *s* is also

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a subsequence of s, but not the other way round. Justify your answer.