

## Problem 10.c

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1
2 /**
3  * Implementation of Prim's algorithm to build an MST
4  * Time Complexity:  $O(|E|. \log |V|)$ 
5  *
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7  */
8
9 #include <stdio.h>
10 #include <string.h>
11 #include <stdlib.h>
12 #include <limits.h>
13
14 #define GRAPH_SZ 50
15 typedef enum { FALSE, TRUE } BOOL;
16
17 /** Rudimentary Graph definition */
18 typedef struct _Graph Graph;
19 typedef struct _GraphNode GraphNode;
20
21 struct _Graph {
22     size_t size;
23     GraphNode *nodeList[GRAPH_SZ];
24     int adjList[GRAPH_SZ][GRAPH_SZ][2]; // [i][0] => adjNodeID; [i][1] => edgeWeight
25 };
26 struct _GraphNode {
27     int id; // Unique ID per node
28     int key; // To be used in Prim's algo
29     size_t adjSize;
30     BOOL heapCutSet;
31 };
32
33 /** Min-Heap implementation */
34 #define HEAP_DTYPE GraphNode
35
36 typedef int (*compare_func)(int, int);
37 typedef struct _MinHeap MinHeap;
38
39 struct _MinHeap {
40     size_t size;
41     HEAP_DTYPE *arr[GRAPH_SZ];
42     int idxMap[GRAPH_SZ]; // Internal mapping: GraphNode.id => Min-Heap.index
43 };
44
45 static inline void heap_swap_data(MinHeap *heap, size_t i1, size_t i2) {
46     // Update internal mappings
47     heap->idxMap[heap->arr[i1]->id] = i2;
48     heap->idxMap[heap->arr[i2]->id] = i1;
49
50     HEAP_DTYPE *temp;
51     temp = heap->arr[i1]; heap->arr[i1] = heap->arr[i2]; heap->arr[i2] = temp;
52 }
53
54 void heap_init(MinHeap *heap, HEAP_DTYPE **arr, size_t size) {
55     heap->size = size;
56     memcpy(heap->arr, arr, size * sizeof(HEAP_DTYPE *));
57
58     // Build internal index map
59     int i;
60     for (i = 0; i < heap->size; i++)
61         heap->idxMap[heap->arr[i]->id] = i;
62 }
63
64 /**
65  * Recursively min-heapify a node at index idx
66  * @heap: The heap to use
67  * @idx: Index of node to min-heapify
68  */
69 void min_heapify(MinHeap *heap, size_t idx) {
70     int lt = 2 * idx + 1;
71     int rt = 2 * (idx + 1);
72     int min;
73
74     if (lt < heap->size && heap->arr[idx]->key > heap->arr[lt]->key)
75         min = lt;
76     else
77         min = idx;
78     if (rt < heap->size && heap->arr[min]->key > heap->arr[rt]->key)
79         min = rt;
```

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80
81     if (idx != min) {
82         heap_swap_data(heap, idx, min);
83         min_heapify(heap, min);
84     }
85 }
86
87 /**
88  * Builds a min-heap out of the given heap
89  * @heap:      The heap to use
90  * @asz:      Size of the array
91  */
92 void build_min_heap(MinHeap *heap) {
93     int i;
94     for (i = heap->size / 2 - 1; i >= 0; i--)
95         min_heapify(heap, i);
96 }
97
98 HEAP_DTYPE * heap_extract_min(MinHeap *heap) {
99     if (heap->size == 0) return NULL;
100
101     HEAP_DTYPE *node = heap->arr[0];
102     heap_swap_data(heap, 0, heap->size - 1);
103     heap->size--; min_heapify(heap, 0);
104
105     return node;
106 }
107
108 /** Parent index */
109 #define PIDX(x) (((x)-1)/2)
110
111 void heap_decrease_key(MinHeap *heap, HEAP_DTYPE *node, int nkey) {
112     if (nkey > node->key) return;
113
114     node->key = nkey;
115     int i = heap->idxMap[node->id];
116
117     while (i > 0 && nkey < heap->arr[PIDX(i)]->key) {
118         heap_swap_data(heap, i, PIDX(i)); i = PIDX(i);
119     }
120 }
121
122 Graph * graph_create() {
123     Graph *graph = (Graph *) malloc(sizeof(Graph));
124     size_t i;
125     for (i = 0; i < GRAPH_SZ; ++i)
126         graph->nodeList[i] = NULL;
127     graph->size = 0; return graph;
128 }
129
130 void graph_destroy(Graph *graph) {
131     size_t i;
132     for (i = 0; i < graph->size; i++) {
133         free(graph->nodeList[i]);
134         graph->nodeList[i] = NULL;
135     }
136
137     graph->size = 0; free(graph);
138 }
139
140 GraphNode * graph_create_node(const int _id) {
141     GraphNode *node = (GraphNode *) malloc(sizeof(GraphNode));
142     node->id = _id; node->key = 0; node->adjSize = 0;
143     node->heapCutSet = FALSE; return node;
144 }
145
146 static void prim_init(Graph *graph, MinHeap *heap) {
147     if (graph == NULL || graph->size == 0)
148         return;
149
150     size_t i;
151     for (i = 0; i < graph->size; i++) {
152         // Emulate positive infinity
153         graph->nodeList[i]->key = INT_MAX;
154         graph->nodeList[i]->heapCutSet = FALSE;
155     }
156     graph->nodeList[0]->key = 0;
157
158     heap_init(heap, graph->nodeList, graph->size);

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159     build_min_heap(heap);
160 }
161
162 void prim_print_mst(Graph *graph, MinHeap *heap, void (*callback)(HEAP_DTYPE *)) {
163     prim_init(graph, heap);
164
165     size_t i, wt;
166     GraphNode *node, *adj_node;
167
168     while (heap->size) {
169         node = heap_extract_min(heap);
170         node->heapCutSet = TRUE; callback(node);
171
172         // Iterate through adjacent nodes
173         for (i = 0; i < node->adjSize; i++) {
174             adj_node = graph->nodeList[graph->adjList[node->id][i][0]];
175             wt = graph->adjList[node->id][i][1];
176
177             if (wt < adj_node->key && !adj_node->heapCutSet)
178                 heap_decrease_key(heap, adj_node, wt);
179         }
180     }
181 }
182
183 #define _scand(n) scanf("%d", &(n))
184 void graph_input(Graph *graph) {
185     int vs, asz, vi, i, j;
186
187     _scand(vs); // Number of vertices
188     graph->size = vs;
189     for (i = 0; i < vs; ++i) {
190         _scand(asz); // Adjacency list size
191         GraphNode *node = graph_create_node(i);
192         node->adjSize = asz;
193         for (j = 0; j < asz; ++j) {
194             _scand(vi); // Scan adjacent node's ID
195             graph->adjList[i][j][0] = vi;
196             _scand(vi); // Scan edge weight for the adjacent node
197             graph->adjList[i][j][1] = vi;
198         }
199         graph->nodeList[i] = node;
200     }
201 }
202
203 static void print_utility(HEAP_DTYPE *node) { printf("%d ", node->id); }
204
205 /** Driver function */
206 int main(int argc, char const *argv[]) {
207     Graph *graph = graph_create();
208     MinHeap heap;
209
210     printf("Enter graph data:\n");
211     graph_input(graph);
212
213     printf("\nMST result:\n");
214     prim_print_mst(graph, &heap, print_utility);
215     printf("\n"); graph_destroy(graph);
216
217     return 0;
218 }
219
220

```