

QUESTION 4 [6 marks] Given

$$F(A, B, C, D) = \Sigma m(1, 2, 4, 6, 8, 9, 11, 14) + d(3, 10, 12)$$

Use Karnaugh maps to find a minimal **POS** and **SOP** of F.

CD \ AB	00	01	11	10
00	0	1	X	1
01	1	0	0	1
11	X	0	0	1
10	1	1	1	X

CD \ AB	00	01	11	10
00	0	1	X	1
01	1	0	0	1
11	X	0	0	1
10	1	1	1	X

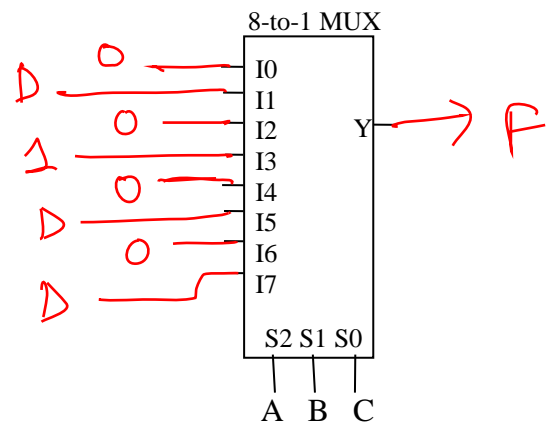
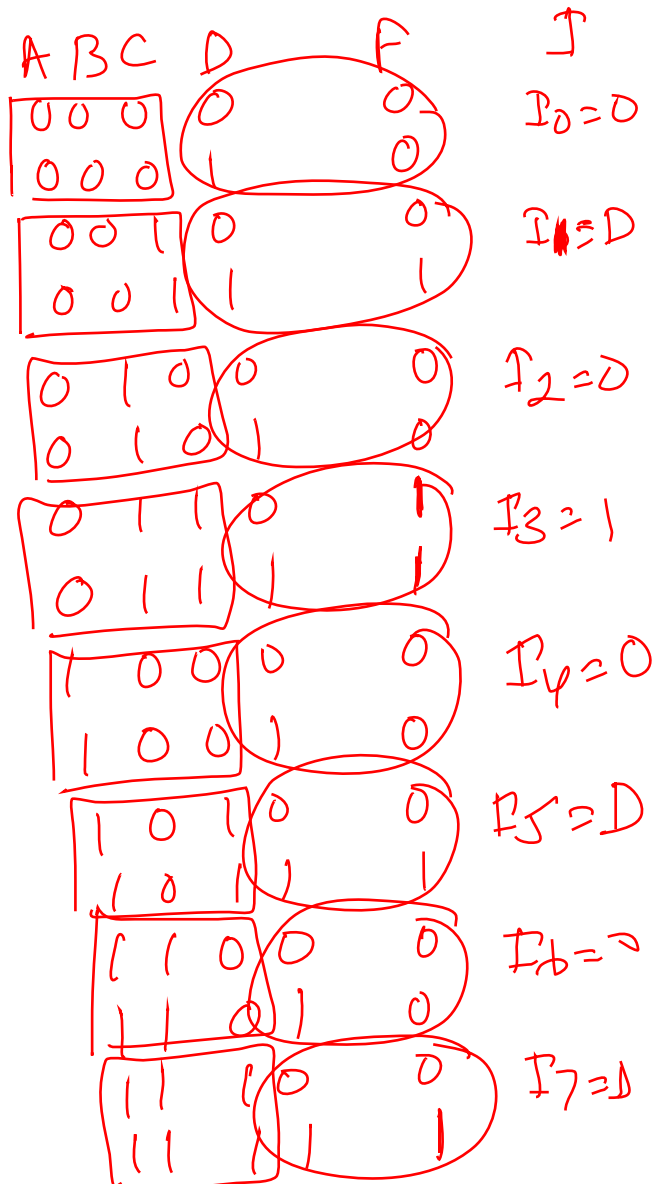
$$F(A, B, C, D) = \underline{B\bar{D} + A\bar{B} + C\bar{D} + \bar{B}D} \quad \text{(Sum-of-Products)}$$

$$F(A, B, C, D) = \underline{(A+B+C+D) \cdot (\bar{A} + \bar{D})} \quad \text{(Product-of-Sums)}$$

**QUESTION 5 [8 marks]** You are given the following Karnaugh map:

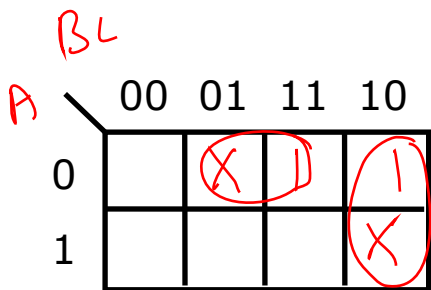
AB \ CD	CD			
	00	01	11	10
00			1	
01			1	1
11			1	
10			1	

Realize the function above (i.e., draw a circuit) using one 8-to-1 multiplexer and any number of 2-input gates and inverters. Observe that A, B and C are connected to the select inputs. Show your work.

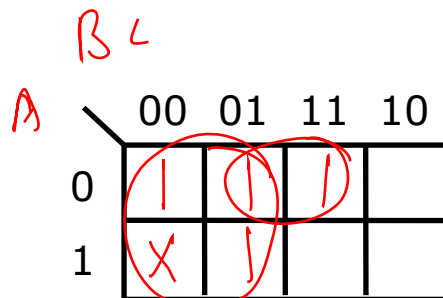


**QUESTION 6 [6 marks]** Design a multi-output digital circuit that maps the 3-bit input to a 3-bit output as follows:

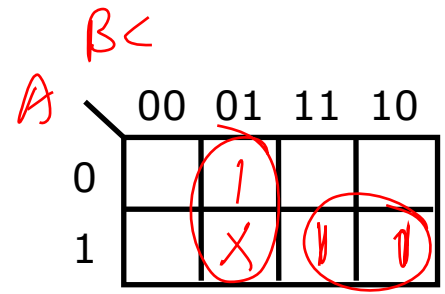
INPUT			OUTPUT		
A	B	C	X	Y	Z
0	0	0	0	1	0
0	0	1	X	1	1
0	1	0	1	0	0
0	1	1	1	1	0
1	0	0	0	X	0
1	0	1	0	1	X
1	1	0	X	0	1
1	1	1	0	0	1



$$X = \bar{A}B + B\bar{C}$$



$$Y = \bar{B} + \bar{A}C$$



$$Z = \bar{B}C + AB$$

