

Expectimax Search

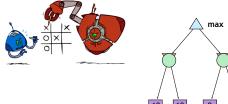
CSE 415: Introduction to Artificial Intelligence University of Washington Winter, 2018

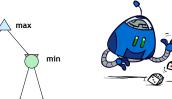
Credit goes to Dan Klein and Pieter Abbeel, Univ. of California, for the slides of this lecture.

Uncertain Outcomes



Worst-Case vs. Average Case





Idea: Uncertain outcomes controlled by chance, not an adversary!

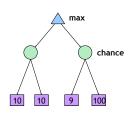
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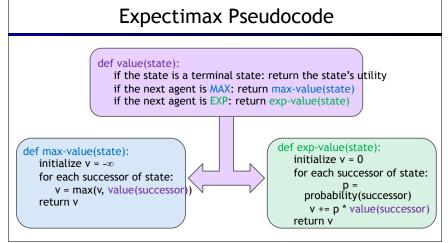
Expectimax Search

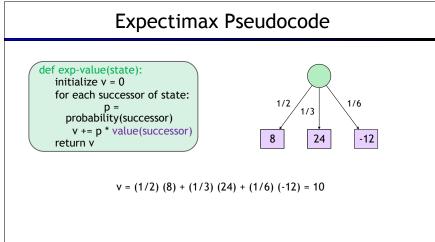
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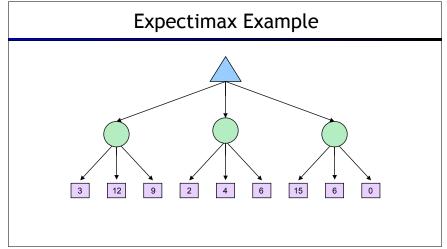
- Why wouldn't we know what the result of an action will

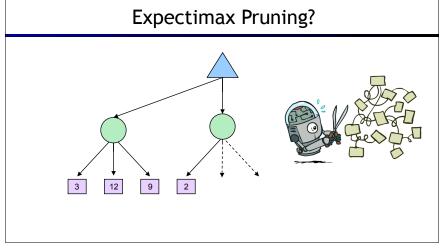
 - Explicit randomness: rolling dice
 Unpredictable opponents: the ghosts respond randomly
 Actions can fail: when moving a robot, wheels might slip
- Values should now reflect average-case (expectimax) outcomes, not worst-case (minimax) outcomes
- Expectimax search: compute the average score under
- Max nodes as in minimax search
 Chance nodes are like min nodes but the outcome is
- Calculate their expected utilities
 I.e. take weighted average (expectation) of children
- Later, we'll learn how to formalize the underlying uncertain-result problems as Markov Decision Processes

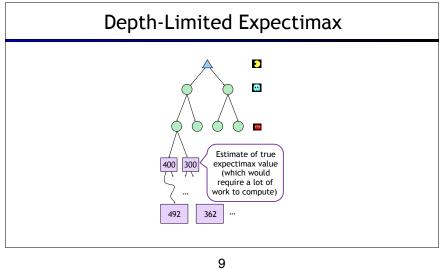


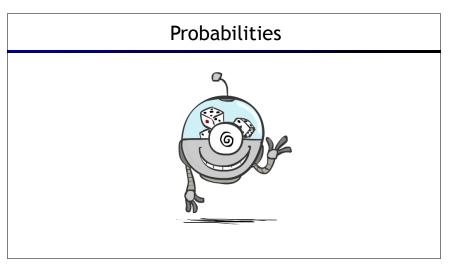


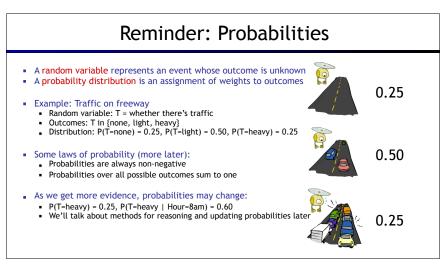


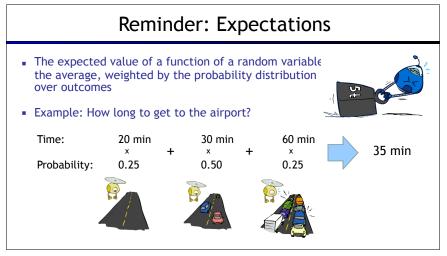












What Probabilities to Use?

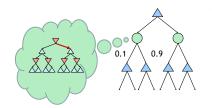
- In expectimax search, we have a probability model of how the opponent (or environment behave in any state
 - Model could be a simple uniform distribution (roll a
 - Model could be sophisticated and require a great dea of computation
 - We have a chance node for any outcome out of our control: opponent or environment
 - The model might say that adversarial actions are likely!
- For now, assume each chance node magically comes along with probabilities that specify the distribution over its outcomes

Having a probabilistic belief about

Having a probabilistic belief about another agent's action does not mean that the agent is flipping any coins!

Quiz: Informed Probabilities

- Let's say you know that your opponent is actually running a depth 2 minimax, using the result 80% of the time, and moving randomly otherwise
- Question: What tree search should you use?



- Answer: Expectimax!
 - To figure out EACH chance node's probabilities, you have to run a simulation of your opponent
 - This kind of thing gets very slow very quickly
 - Even worse if you have to simulate your opponent simulating you...
 - ... except for minimax, which has the nice property that it all collapses into one game tree

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Modeling Assumptions



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The Dangers of Optimism and Pessimism

Dangerous Optimism
Assuming chance when the world is adversarial

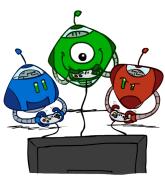


Dangerous Pessimism
Assuming the worst case when it's not likely





Other Game Types

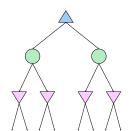


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Mixed Layer Types

- E.g. Backgammon
- Expectiminimax
 - Environment is an extra "random agent" player that moves after each min/max agent
 - Each node computes the appropriate combination of its children









Example: Backgammon

- Dice rolls increase b: 21 possible rolls with 2 dice
 - Backgammon ≈ 20 legal moves
 - Depth 2 = $20 \times (21 \times 20)^3 = 1.2 \times 10^9$
- As depth increases, probability of reaching a given search node shrinks
 - So usefulness of search is diminished
 - So limiting depth is less damaging
 - But pruning is trickier...
- Historic AI: TDGammon uses depth-2 search + very good evaluation function + reinforcement learning: world-champion level play
- 1st Al world champion in any game!





Image: Wikipedia

Multi-Agent Utilities • What if the game is not zero-sum, or has multiple players? Generalization of minimax: Terminals have utility tuples Node values are also utility tuples • Each player maximizes its own component Can give rise to cooperation and competition dynamically... 6,1,2 7,2,1

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