

Tackling Concurrency Bugs with TLA+

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Hi a plus

Hillel Wayne

ESPARK LEARNING

[Speaker site](#)

 [@hillelogram](#)

 [hwayne](#)

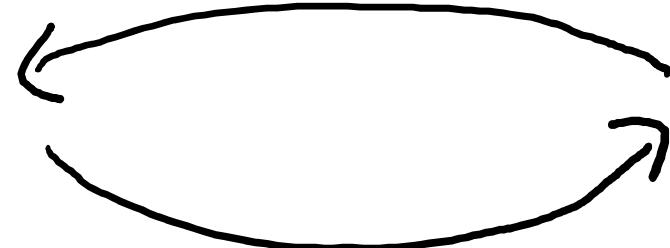
Hillel is a senior software engineer at eSpark Learning. He enjoys technical writing and is the author of Learn TLA+ (<https://learntla.com>). In his free time he juggles and makes chocolates. He _probably_ brought enough for everyone.



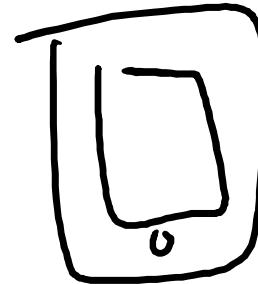
@hillelogram

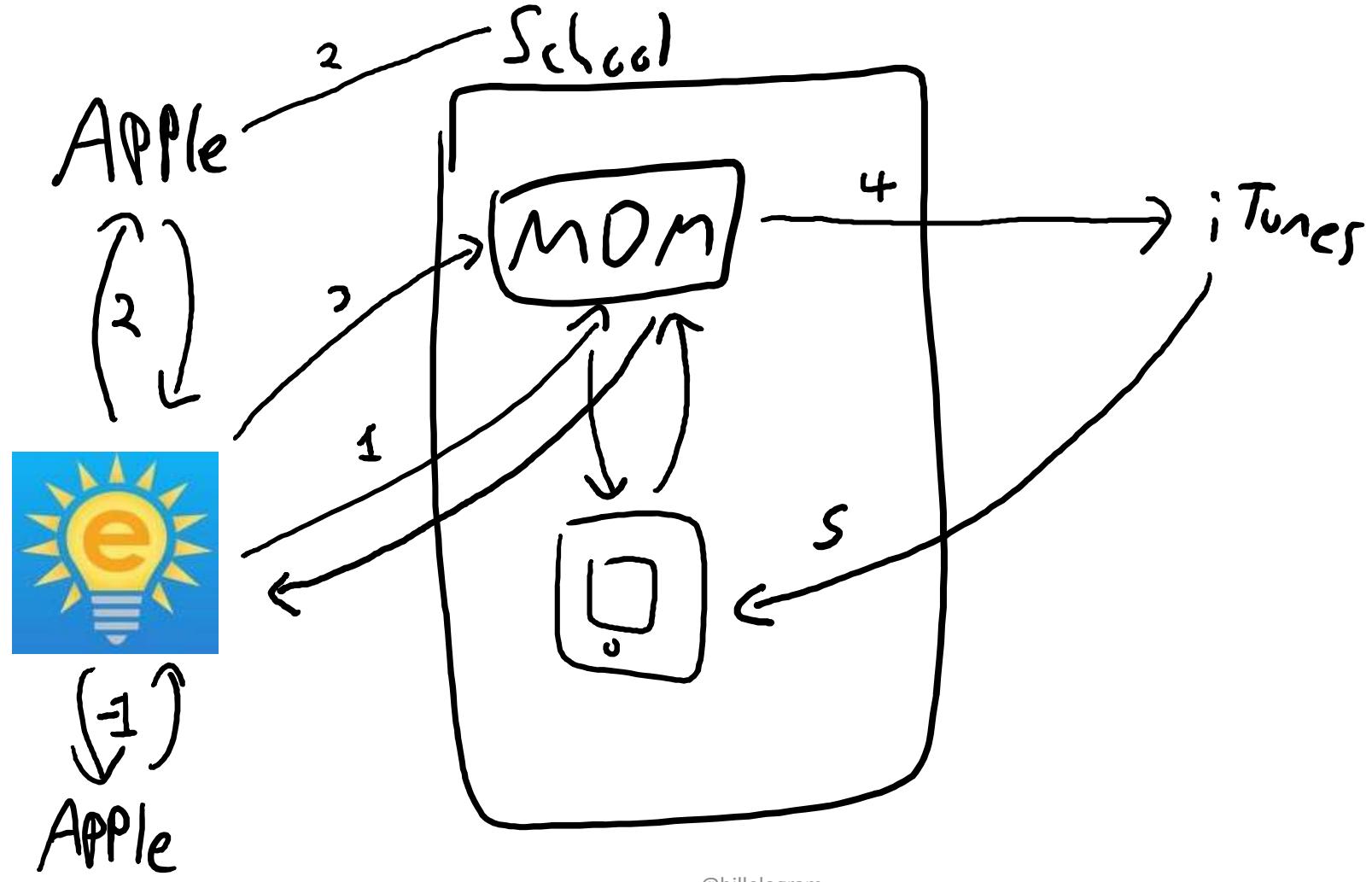


Student Data



Apps to install



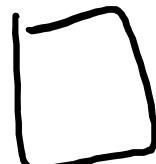
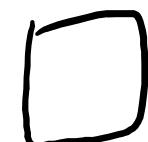
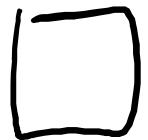


@hilleogram

Concurrency

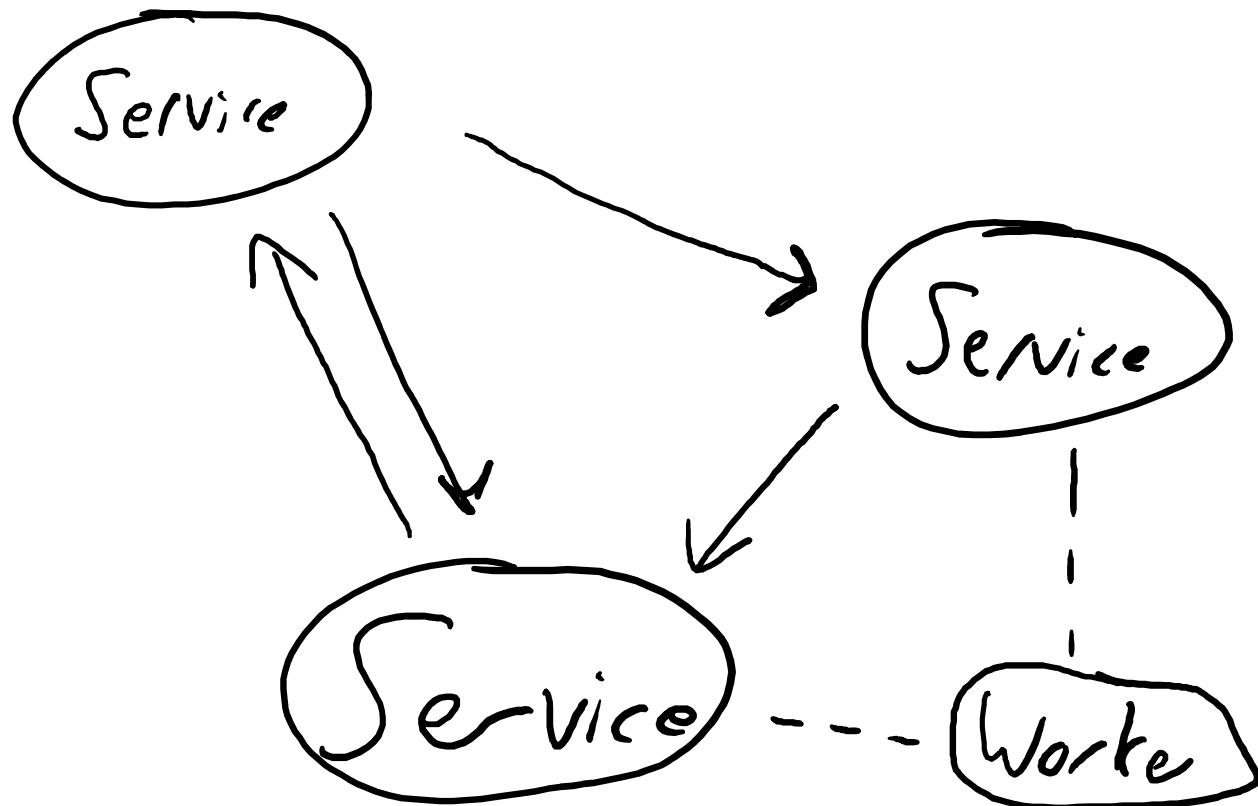
- Multiple Systems
- Running Independently
- With some global state
- **Nondeterministic**

Writers



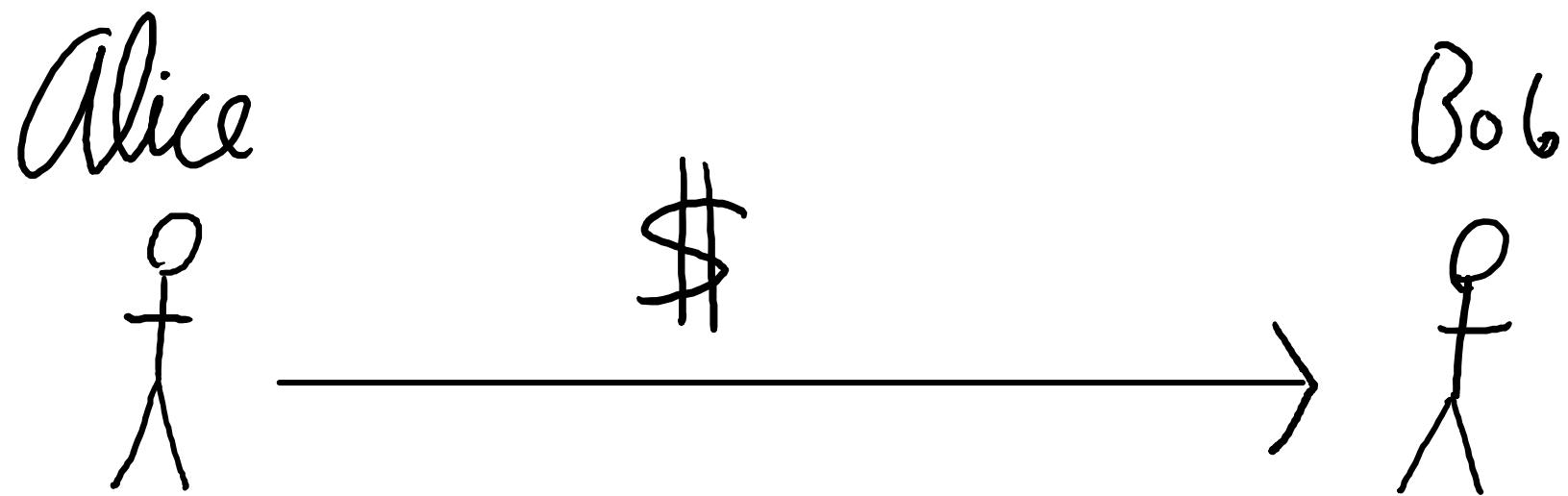
Readers



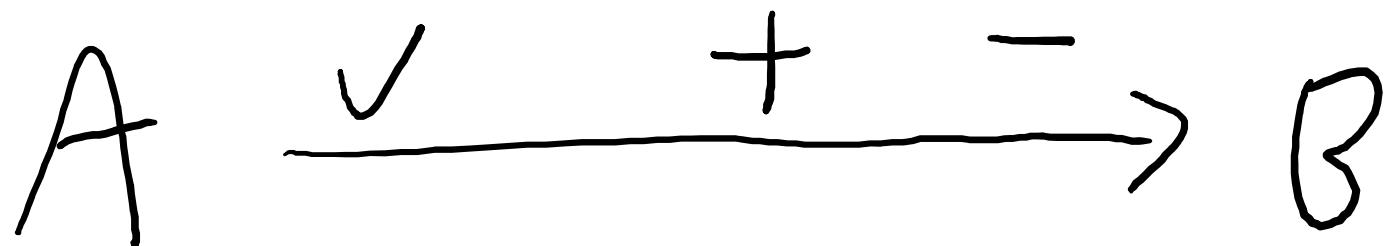


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Example



```
def transfer(amount, to)
    raise if self.balance < amount
    to.balance += amount
    self.balance -= amount
end
```

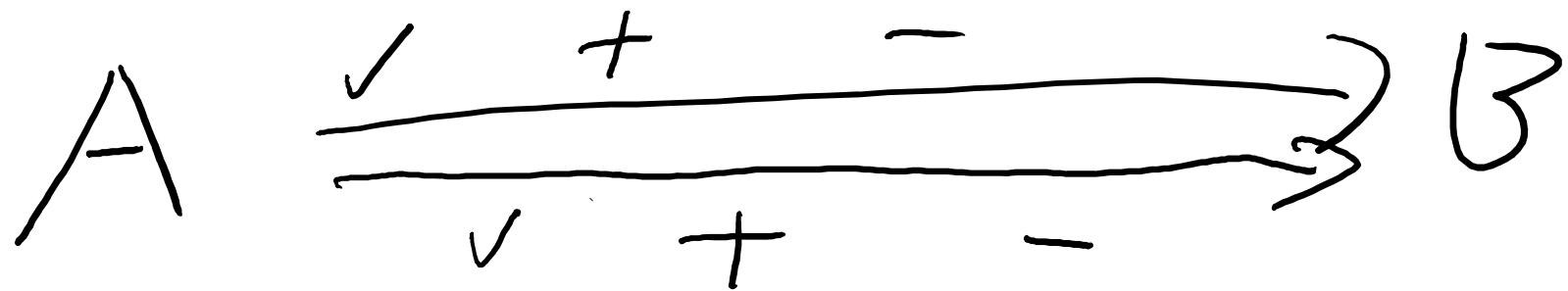


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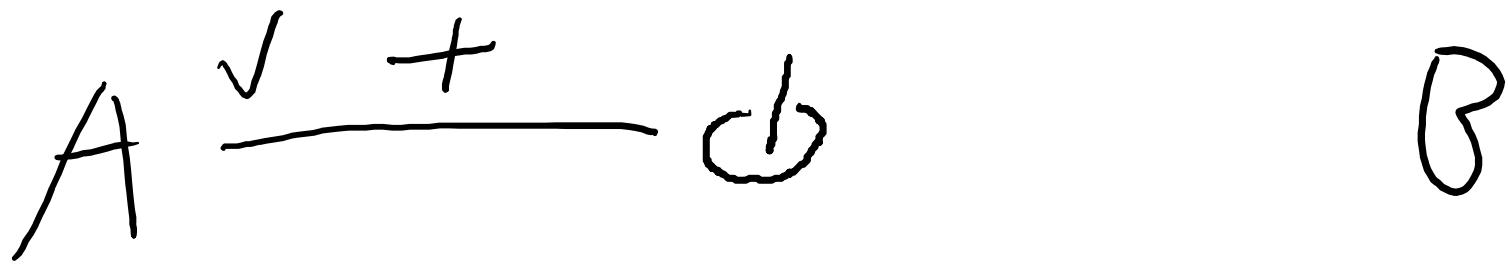
Carnival of Horrors

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Race Conditions



Crashes



Deadlocks



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H

a

P

Unit Tests

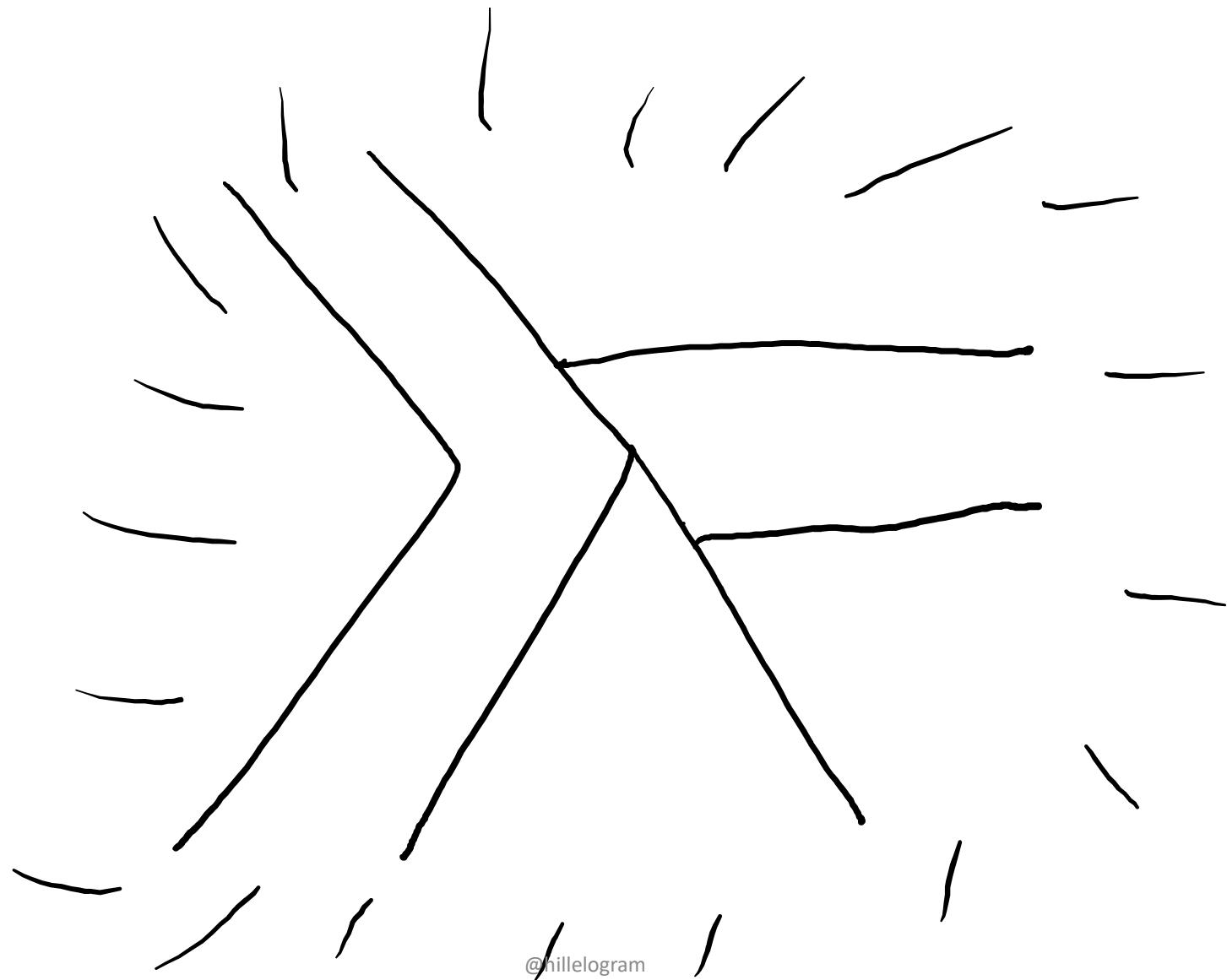
When "I receive a message"
Then "it sends an alert"

When "I receive a message"
And "the message queue duplicated
the message"
And "another worker receives the
copy later but finishes first"
And "Github is down"
Then "it sends an alert"

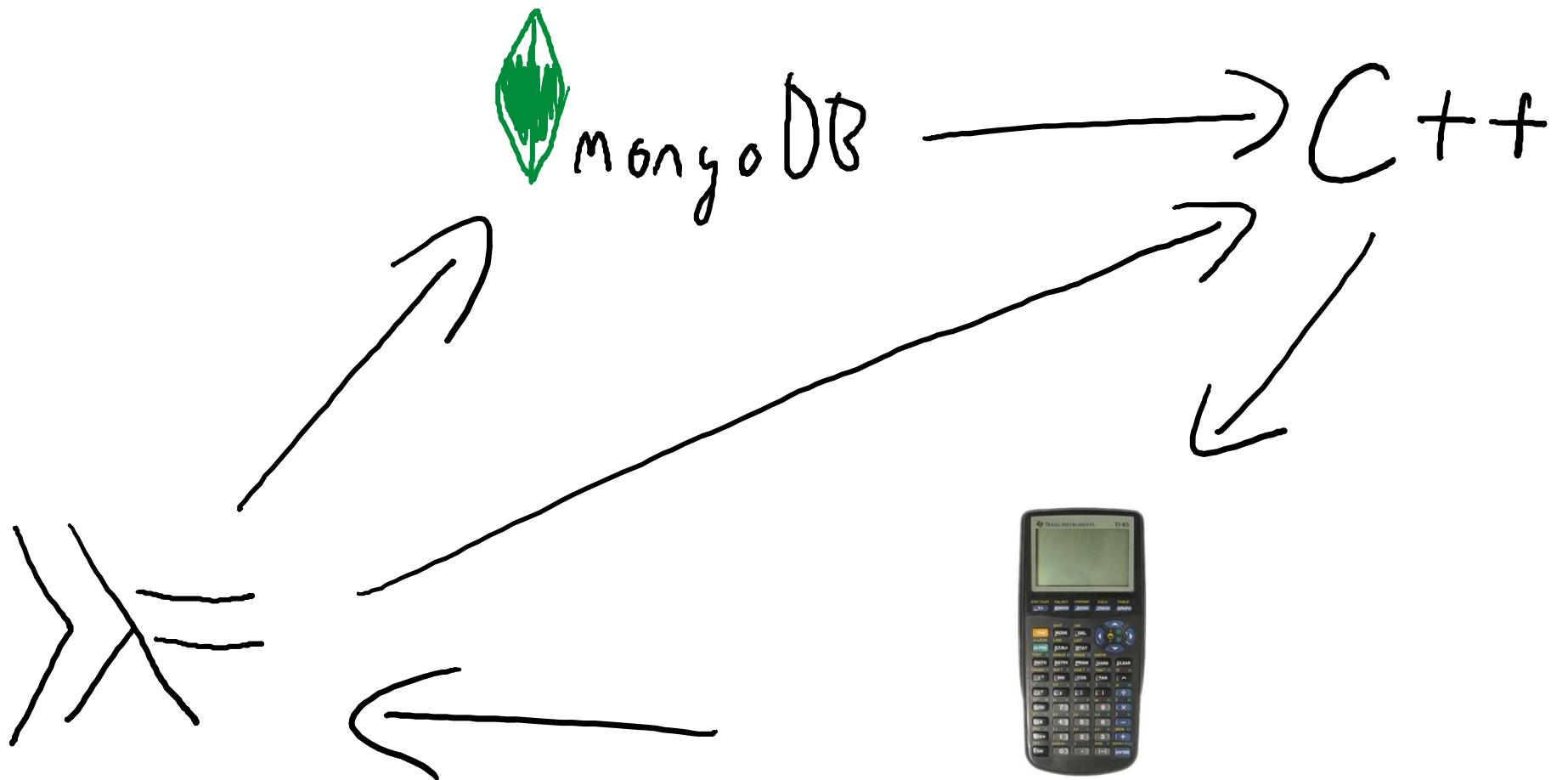
EN)

— N
31

Static Typing



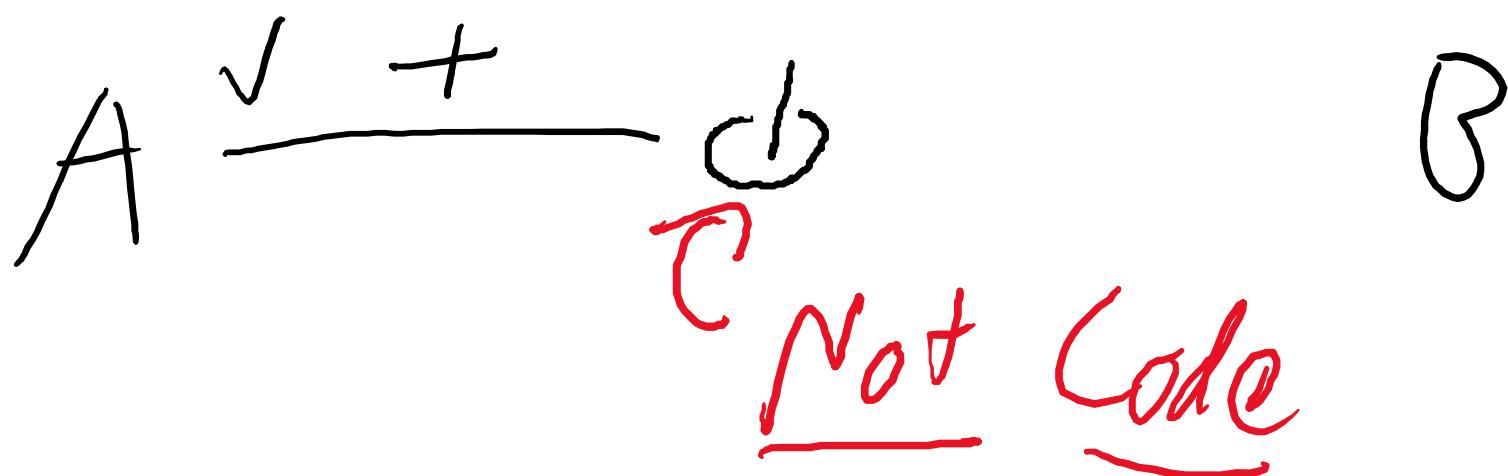
@nilleogram



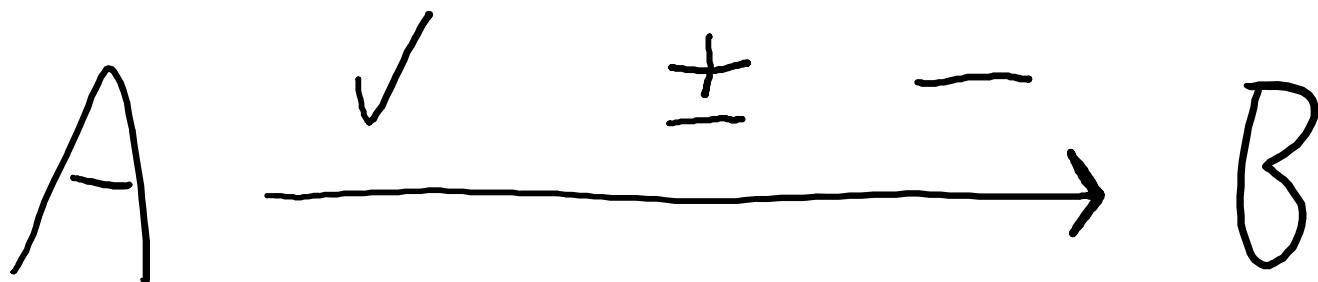
@hilleogram

We don't get
Purity

@hilleogram



```
def transfer(amount, to)
1 raise if self.balance < amount
2 { to.balance += amount
  self.balance -= amount
end
```



$$A \xleftarrow{\checkmark \pm} B$$

$$A \xleftarrow{\checkmark \circlearrowleft} B$$

$$A - \circlearrowleft B$$

$$A \xleftarrow{\checkmark \pm \circlearrowright} B$$

$$A \xrightarrow[\sqrt{\pm}]{\checkmark \pm} B$$

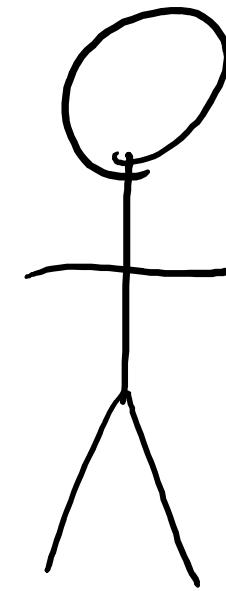
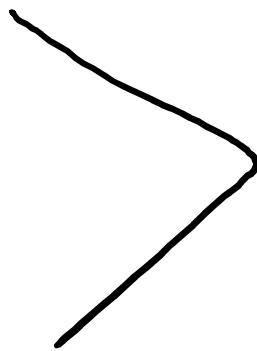
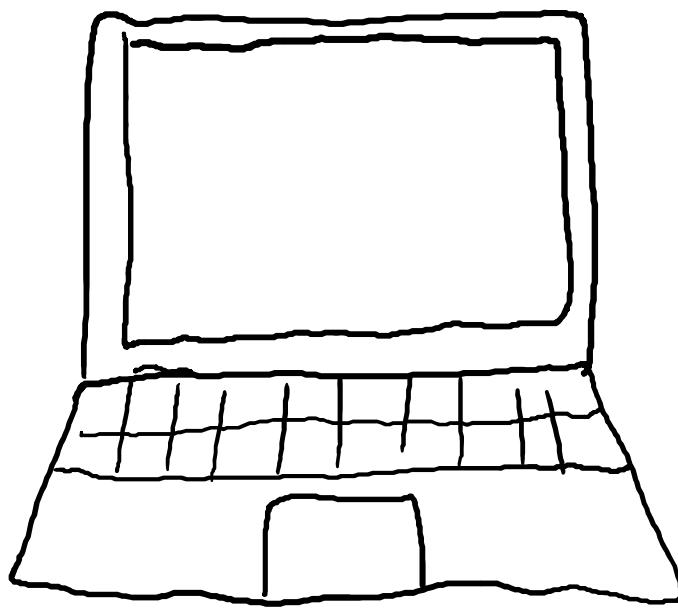
$$A \xrightarrow[\sqrt{\pm}]{\checkmark \pm} B$$

$$A \xrightarrow[\sqrt{\pm}]{\checkmark \pm} B$$

$$A \xrightarrow[\sqrt{\pm}]{\checkmark \pm} B$$



Chris Hastings, www.drmcninja.com



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Formal

specification

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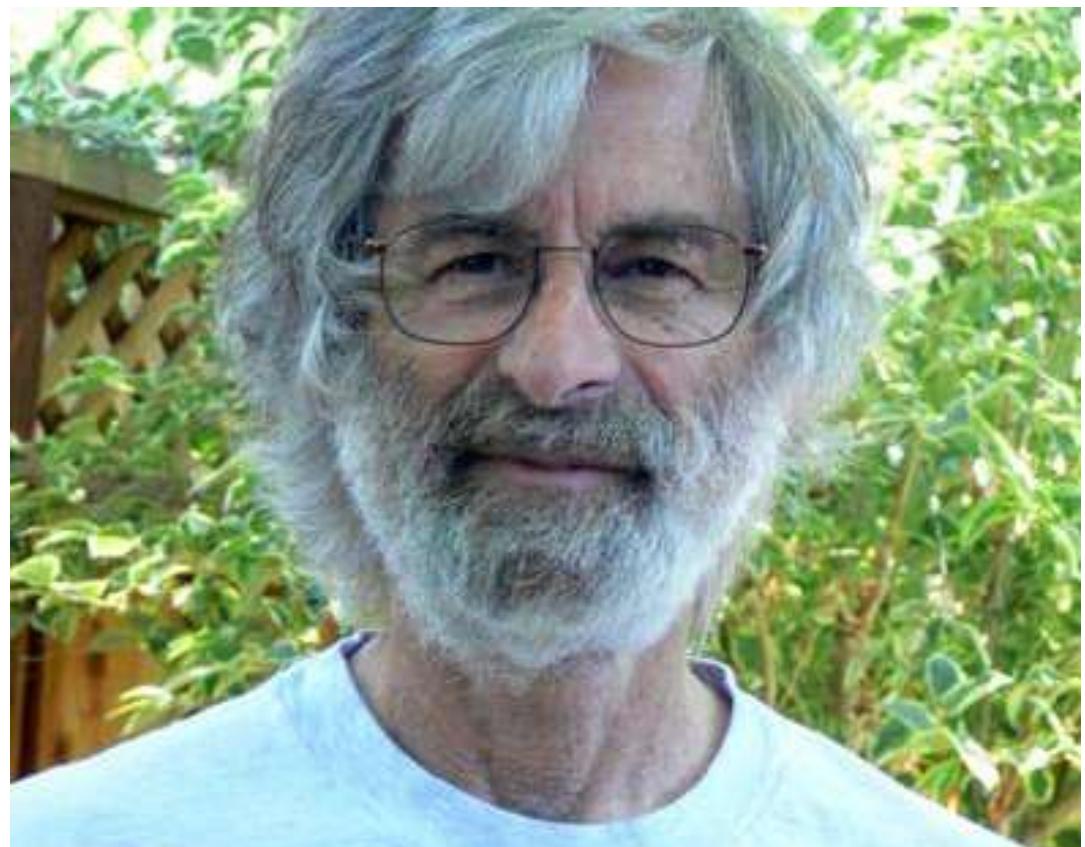
Specs do not
Check code



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Things Lamport did

- TLA+
- Paxos
- Byzantine Generals
- Digital signatures
- Sequential Consistency
- LaTeX



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Why TLA+ :

- Math
- Jargon
- Blah Blah Blah

```
variables alice_account = 10, bob_account = 10;
```

* Our algorithm goes here

```
NoOverdrafts == alice_account >= 0 /\ bob_account >= 0
```



defines

and

```
\* variables alice_account = 10, bob_account = 10;
variables people = {"alice", "bob"},  

    account = [p \in people |-> 10]  
  
\* account["alice"] = 10  
\* stuff goes here  
  
NoOverdrafts == \A p \in people: account[p] >= 0
```

```

variables people = {"alice", "bob"},  

    account = [p \in people | -> 10]  
  

process transfer = 1  

    variables amount = 1,  

        sender = "alice",  

        receiver = "bob";  
  

begin  

    Check: if account[sender] >= amount then  

        Add: account[receiver] := account[receiver] + amount;  

        Sub: account[sender] := account[sender] - amount;  

    end if;  

end process;

```

NoOverdrafts == \A p \in people: account[p] >= 0

TLA+ Toolbox

File Edit Window TLC Model Checker TLA Proof Manager Help

Transfer.tla Safety C:\Users\hwayn\OneDrive\TLA\Specs\guide\Transfer.tla

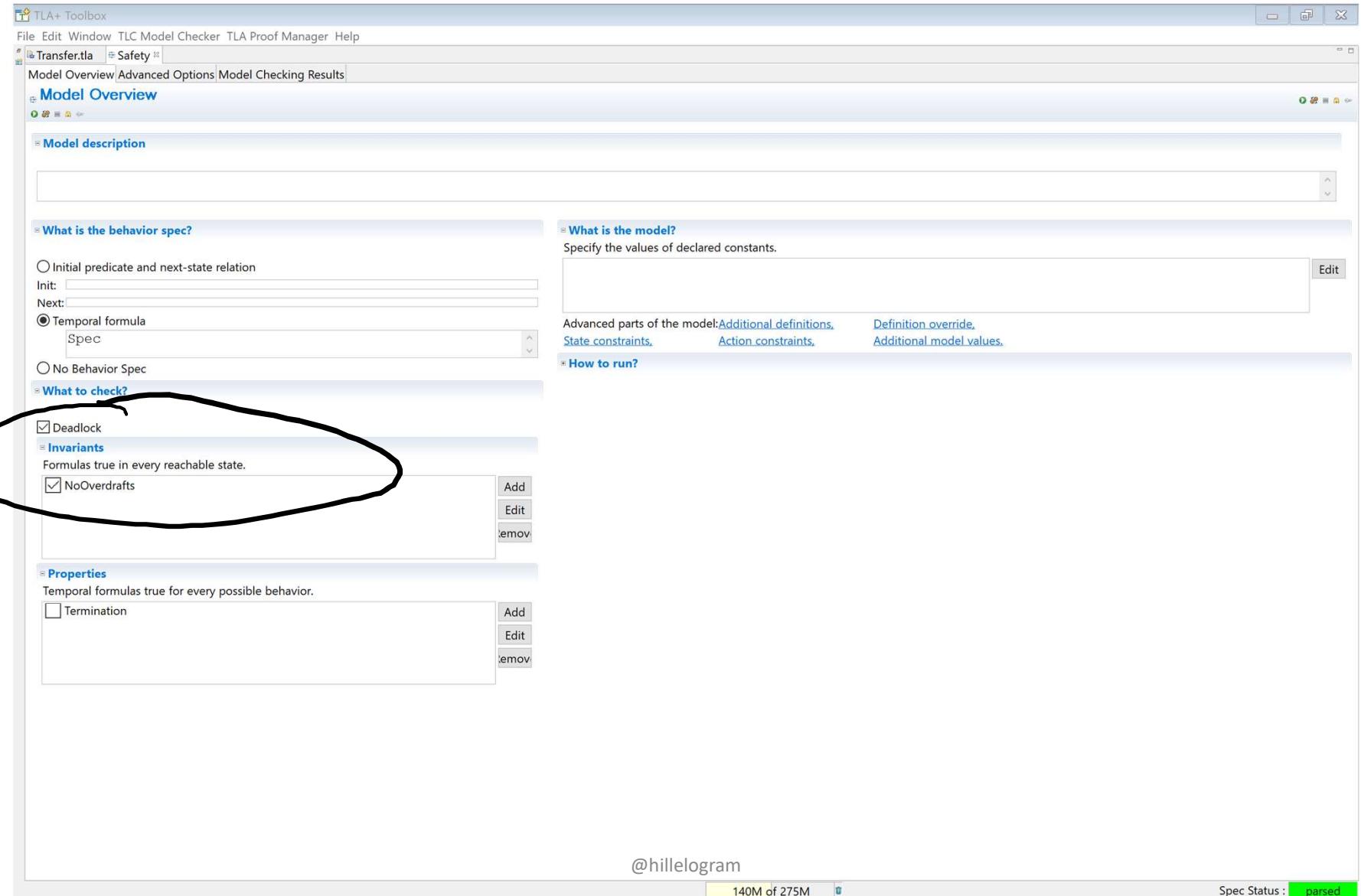
TLA Module

```

21 end algorithm; *)
22 /* BEGIN TRANSLATION
23 VARIABLES people, account, pc
24
25 (* define statement *)
26 NoOverdrafts == \A p \in people: account[p] >= 0
27
28 VARIABLES amount, sender, receiver
29
30 vars == << people, account, pc, amount, sender, receiver >>
31
32 ProcSet == {1}
33
34 Init == (* Global variables *)
35     /\ people = {"alice", "bob"}
36     /\ account = [p \in people |-> 10]
37     (* Process transfer *)
38     /\ amount = 1
39     /\ sender = "alice"
40     /\ receiver = "bob"
41     /\ pc = [self \in ProcSet |-> "Check"]
42
43 Check == /\ pc[1] = "Check"
44     /\ IF account[sender] >= amount
45         THEN /\ pc' = [pc EXCEPT !{1} = "Add"]
46         ELSE /\ pc' = [pc EXCEPT !{1} = "Done"]
47     /\ UNCHANGED << people, account, amount, sender, receiver >>
48
49 Add == /\ pc[1] = "Add"
50     /\ account' = [account EXCEPT ![receiver] = account[receiver] + amount]
51     /\ pc' = [pc EXCEPT !{1} = "Sub"]
52     /\ UNCHANGED << people, amount, sender, receiver >>
53
54 Sub == /\ pc[1] = "Sub"
55     /\ account' = [account EXCEPT ![sender] = account[sender] - amount]
56     /\ pc' = [pc EXCEPT !{1} = "Done"]
57     /\ UNCHANGED << people, amount, sender, receiver >>
58
59 transfer == Check \wedge Add \wedge Sub
60
61 Next == transfer
62     /\ (* Disjunct to prevent deadlock on termination *)
63     ((\A self \in ProcSet: pc[self] = "Done") \wedge UNCHANGED vars)
64
65 Spec == Init \wedge [] [Next]_vars
66
67 Termination == <>(\A self \in ProcSet: pc[self] = "Done")
68
69 /* END TRANSLATION
70
    
```

@hilleogram

20:13 83M of 275M Spec Status : parsed



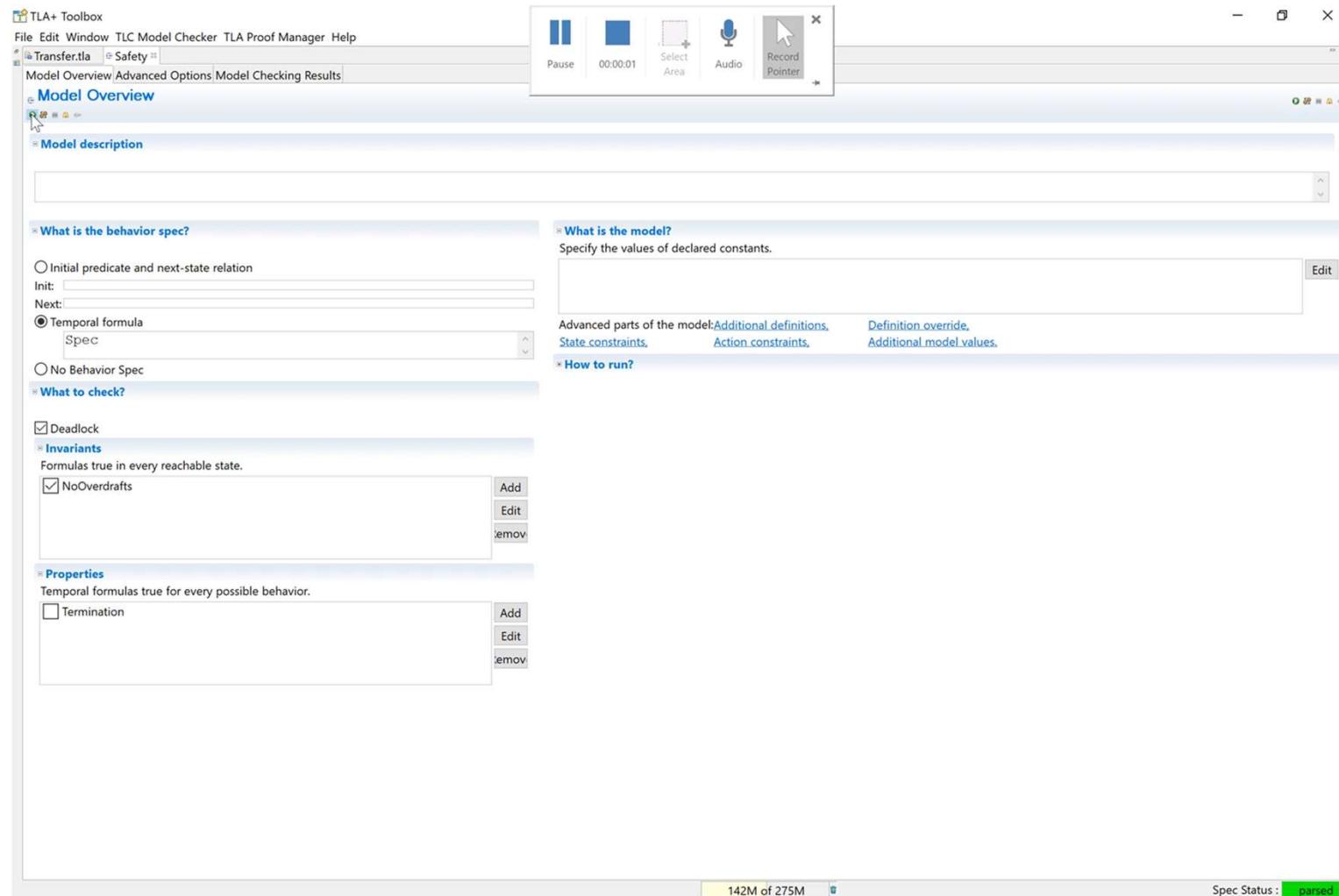
T

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C



@hilleogram



@hilleogram

```
variables people = {"alice", "bob"},  
    account = [p \in people | -> 10]  
  
process transfer = 1  
    variables amount = 1,  
        sender = "alice",  
        receiver = "bob";  
begin  
    Check: if account[sender] >= amount then  
        Add: account[receiver] := account[receiver] + amount;  
        Sub: account[sender] := account[sender] - amount;  
    end if;  
end process;  
  
NoOverdrafts == \A p \in people: account[p] >= 0
```

```

variables people = {"alice", "bob"},  

                  account = [p \in people | -> 10]  
  

process transfer = 1  

  variables amount \in 1..10,  

            sender = "alice",  

            receiver = "bob";  

begin  

  Check: if account[sender] >= amount then  

    Add: account[receiver] := account[receiver] + amount;  

    Sub: account[sender] := account[sender] - amount;  

  end if;  

end process;  
  

NoOverdrafts == \A p \in people: account[p] >= 0

```

A $\xrightarrow{1}$ B

A $\xrightarrow{2}$ B

A $\xrightarrow{3}$ B

A $\xrightarrow{4}$ B

A $\xrightarrow{5}$ B

A $\xrightarrow{6}$ B

A $\xrightarrow{7}$ B

A $\xrightarrow{8}$ B

A $\xrightarrow{9}$ B

A $\xrightarrow{10}$ B

```

variables people = {"alice", "bob"},  

                  account = [p \in people | -> 10]  
  

process transfer = 1  

  variables amount \in 1..10,  

            sender = "alice",  

            receiver = "bob";  

begin  

  Check: if account[sender] >= amount then  

    Add: account[receiver] := account[receiver] + amount;  

    Sub: account[sender] := account[sender] - amount;  

  end if;  

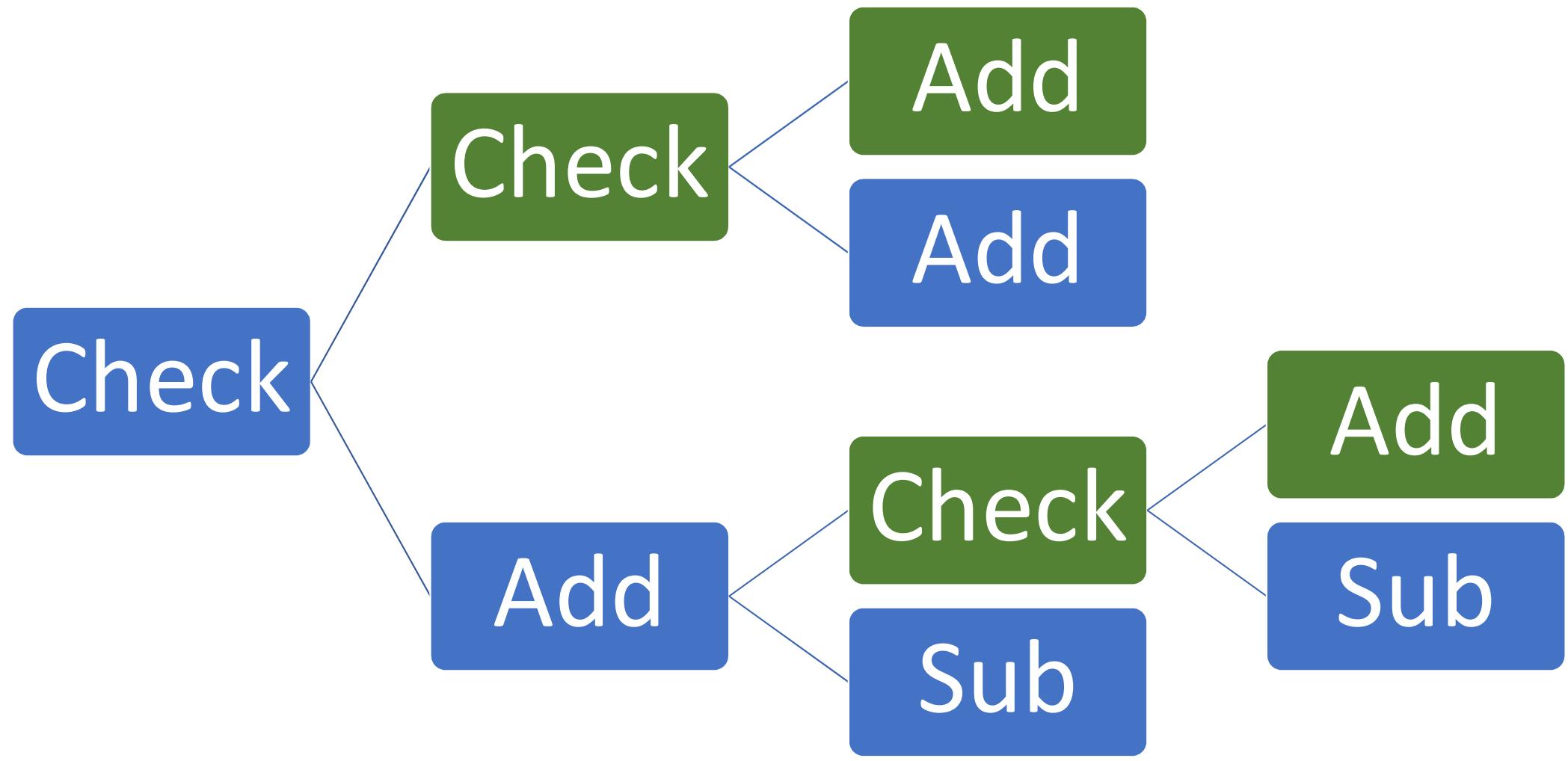
end process;  
  

NoOverdrafts == \A p \in people: account[p] >= 0

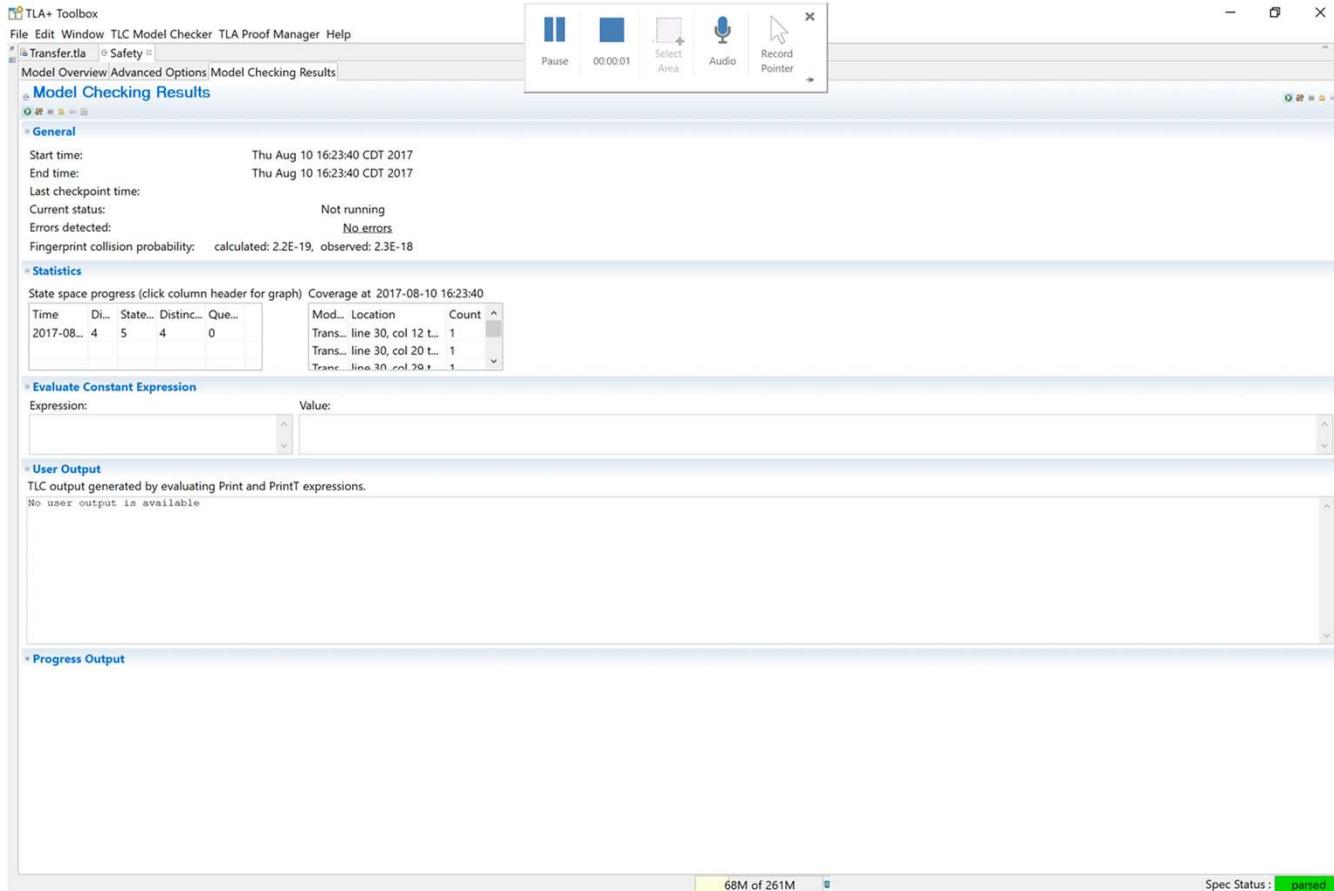
```

@hilleogram

```
variables people = {"alice", "bob"},  
                  account = [p \in people | -> 10]  
  
process transfer \in {"blue", "green"}  
variables amount \in 1..10,  
         sender = "alice",  
         receiver = "bob";  
  
begin  
  Check: if account[sender] >= amount then  
    Add: account[receiver] := account[receiver] + amount;  
    Sub: account[sender] := account[sender] - amount;  
  end if;  
end process;  
  
NoOverdrafts == \A p \in people: account[p] >= 0
```



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Transfer.tla Safety

Model Overview Advanced Options Model Checking Results

Model Checking Results 2 warnings detected

General

Start time: Thu Aug 10 16:18:49 CDT 2017
 End time: Thu Aug 10 16:18:50 CDT 2017
 Last checkpoint time:
 Current status: Not running
 Errors detected: 1 Error
 Fingerprint collision probability:

Statistics

State space progress (click column header for graph) Coverage at 2017-08-10 16:18:50

Time	Di...	State...	Distinct...	Que...	Mod...	Location	Count
2017-08...	7	2433	1620	186		Trans... line 30, col 12 t...	104
						Trans... line 30, col 20 t...	104
						Trans... line 30, col 20 t...	104

Evaluate Constant Expression

Expression: Value:

User Output

TLC output generated by evaluating Print and PrintT expressions.

No user output is available

Progress Output

TLC Errors 23

Safety

Invariant NoOverdrafts is violated.

Error-Trace Exploration

Error-Trace

Name	Value
<Initial predicate>	State (num = 1)
account	[alice -> 10, bob -> 10]
amount	[blue -> 1, green -> 10]
pc	[blue -> "Check", green -> "Check"]
people	{"alice", "bob"}
receiver	[blue -> "bob", green -> "bob"]
sender	[blue -> "alice", green -> "alice"]
<Action line 43, col 16 to line 47, col 75	State (num = 2)
account	[alice -> 10, bob -> 10]
amount	[blue -> 1, green -> 10]
pc	[blue -> "Add", green -> "Check"]
people	{"alice", "bob"}
receiver	[blue -> "bob", green -> "bob"]
sender	[blue -> "alice", green -> "alice"]
<Action line 49, col 14 to line 52, col 64	State (num = 3)
<Action line 43, col 16 to line 47, col 75	State (num = 4)
<Action line 49, col 14 to line 52, col 64	State (num = 5)
<Action line 54, col 14 to line 57, col 64	State (num = 6)
<Action line 54, col 14 to line 57, col 64	State (num = 7)
account	[alice -> -1, bob -> 21]
amount	[blue -> 1, green -> 10]
pc	[blue -> "Done", green -> "Done"]
/\ account = [alice -> 10, bob -> 10]	
/\ amount = [blue -> 1, green -> 10]	
/\ pc = [blue -> "Check", green -> "Check"]	
/\ people = {"alice", "bob"}	
/\ receiver = [blue -> "bob", green -> "bob"]	
/\ sender = [blue -> "alice", green -> "alice"]	

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60M of 275M
Spec Status : parsed

TLA+ Toolbox

File Edit Window TLC Model Checker TLA Proof Manager Help

TLC Errors

Safety

Invariant NoOverdrafts is violated.

Error-Trace Exploration

Error-Trace

Name	Value
<Initial predicate>	State (num = 1) [alice -> 10, bob -> 10] [blue -> 1, green -> 10] [blue -> "Check", green -> "Check"] {"alice", "bob"} [blue -> "bob", green -> "bob"] [blue -> "alice", green -> "alice"]
<Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 2)
<Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 3)
<Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 4)
<Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 5)
<Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 6)
<Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 7)

```

/\ account = [alice |-> 10, bob |-> 10]
/\ amount = [blue |-> 1, green |-> 10]
/\ pc = [blue |-> "Check", green |-> "Check"]
/\ people = {"alice", "bob"}
/\ receiver = [blue |-> "bob", green |-> "bob"]
/\ sender = [blue |-> "alice", green |-> "alice"]

```

Start!

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TLA+ Toolbox

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TLC Errors

Safety

Invariant NoOverdrafts is violated.

Error-Trace Exploration

Error-Trace

Name	Value
> ▲ <Initial predicate>	State (num = 1)
> ▲ <Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 2) [alice -> 10, bob -> 10] [blue -> 1, green -> 10] [blue -> "Add", green -> "Check"]
> □ account	{"alice", "bob"}
> □ amount	[blue -> "bob", green -> "bob"]
> □ pc	[blue -> "alice", green -> "alice"]
> □ people	
> □ receiver	
> □ sender	
▼ <Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 3) [alice -> 10, bob -> 11] [blue -> 1, green -> 10] [blue -> "Sub", green -> "Check"]
> □ account	{"alice", "bob"}
> □ amount	[blue -> "bob", green -> "bob"]
> □ pc	[blue -> "alice", green -> "alice"]
> □ people	
> □ receiver	
> □ sender	
> ▲ <Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 4)
> ▲ <Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 5)
> ▲ <Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 6)
> ▲ <Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 7)
/＼ account = [alice -> 10, bob -> 11]	
/＼ amount = [blue -> 1, green -> 10]	
/＼ pc = [blue -> "Sub", green -> "Check"]	
/＼ people = {"alice", "bob"}	
/＼ receiver = [blue -> "bob", green -> "bob"]	
/＼ sender = [blue -> "alice", green -> "alice"]	

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TLA+ Toolbox

File Edit Window TLC Model Checker TLA Proof Manager Help

TLC Errors

Safety

Invariant NoOverdrafts is violated.

Error-Trace Exploration

Error-Trace

Name	Value
<Initial predicate>	State (num = 1)
<Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 2)
<Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 3)
<Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 4)
account	[alice -> 10, bob -> 11]
amount	[blue -> 1, green -> 10]
pc	[blue -> "Sub", green -> "Add"]
people	{"alice", "bob"}
receiver	[blue -> "bob", green -> "bob"]
sender	[blue -> "alice", green -> "alice"]
<Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 5)
account	[alice -> 9, bob -> 11]
amount	[blue -> 1, green -> 10]
pc	[blue -> "Done", green -> "Add"]
people	{"alice", "bob"}
receiver	[blue -> "bob", green -> "bob"]
sender	[blue -> "alice", green -> "alice"]
<Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 6)
<Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 7)

```

/\ account = [alice |-> 9, bob |-> 11]
/\ amount = [blue |-> 1, green |-> 10]
/\ pc = [blue |-> "Done", green |-> "Add"]
/\ people = {"alice", "bob"}
/\ receiver = [blue |-> "bob", green |-> "bob"]
/\ sender = [blue |-> "alice", green |-> "alice"]

```

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TLA+ Toolbox

File Edit Window TLC Model Checker TLA Proof Manager Help

TLC Errors

Safety

Invariant NoOverdrafts is violated.

Error-Trace Exploration

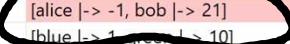
Error-Trace

Name	Value
> ▲ <Initial predicate>	State (num = 1)
> ▲ <Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 2)
> ▲ <Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 3)
> ▲ <Action line 43, col 16 to line 47, col 75 of module Transfer>	State (num = 4)
> ▲ <Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num = 5)
> ▲ <Action line 49, col 14 to line 52, col 64 of module Transfer>	State (num = 6)
> □ account	[alice -> 9, bob -> 21]
> □ amount	[blue -> 1, green -> 10]
> □ pc	[blue -> "Done", green -> "Sub"]
> □ people	{"alice", "bob"}
> □ receiver	[blue -> "bob", green -> "bob"]
> □ sender	[blue -> "alice", green -> "alice"]
▼ <Action line 54, col 14 to line 57, col 64 of module Transfer>	State (num =)
> □ account	[alice -> -1, bob -> 21]
> □ amount	[blue -> 1, green -> 10]
> □ pc	[blue -> "Done", green -> "Done"]
> □ people	{"alice", "bob"}
> □ receiver	[blue -> "bob", green -> "bob"]
> □ sender	[blue -> "alice", green -> "alice"]

```

/\ account = [alice |-> -1, bob |-> 21]
/\ amount = [blue |-> 1, green |-> 10]
/\ pc = [blue |-> "Done", green |-> "Done"]
/\ people = {"alice", "bob"}
/\ receiver = [blue |-> "bob", green |-> "bob"]
/\ sender = [blue |-> "alice", green |-> "alice"]

```



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```

variables people = {"alice", "bob"},  

    account = [p \in people |-> 10]  
  

process transfer \in {"blue", "green"}  

    variables amount \in 1..10,  

        sender = "alice",  

        receiver = "bob";  
  

begin  

Transfer:  

    if account[sender] >= amount then  

        account[receiver] := account[receiver] + amount ||  

        account[sender] := account[sender] - amount;  

    end if;  

end process;  
  

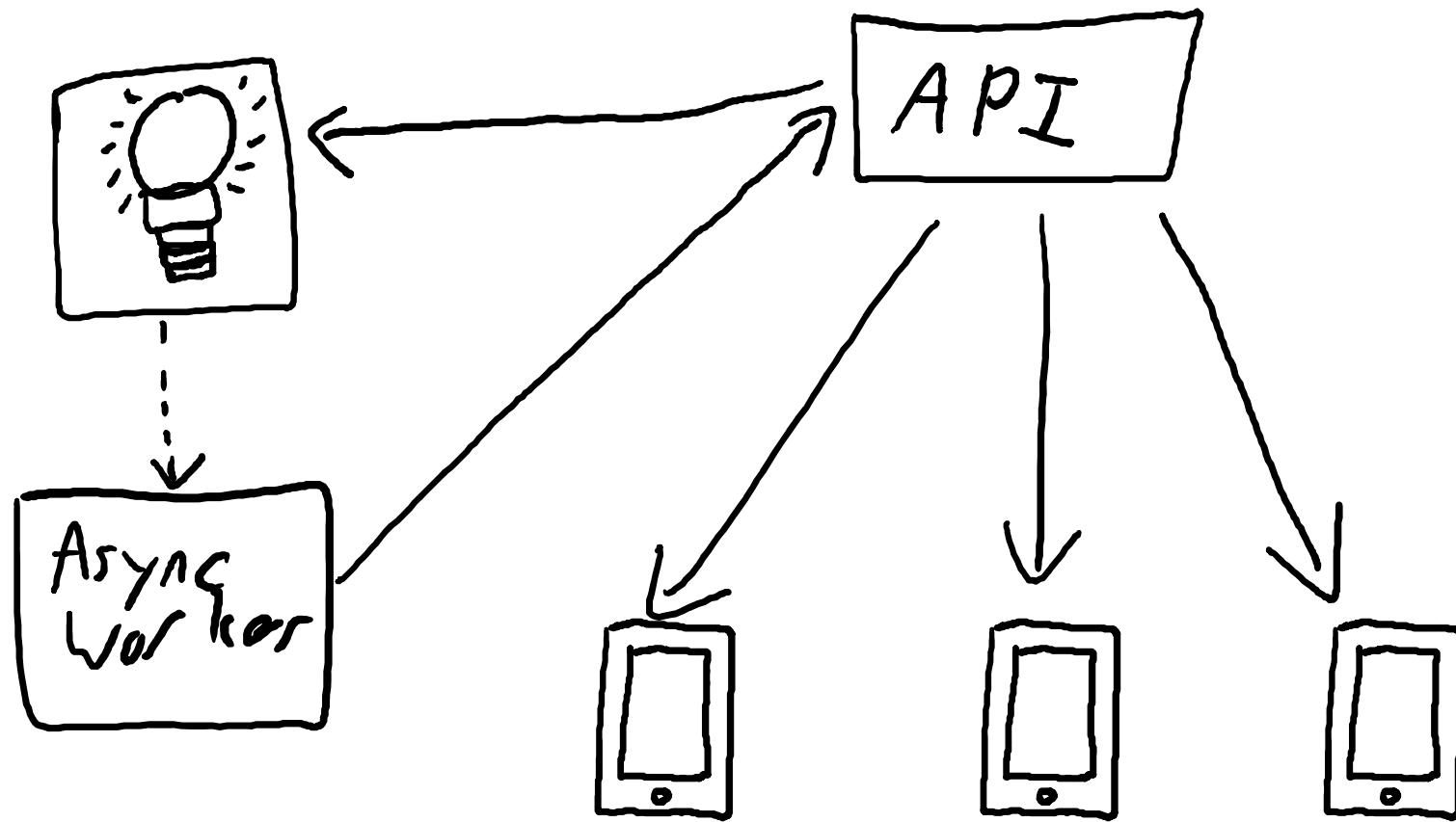
NoOverdrafts == \A p \in people: account[p] >= 0

```

W h o

C w e s t ,

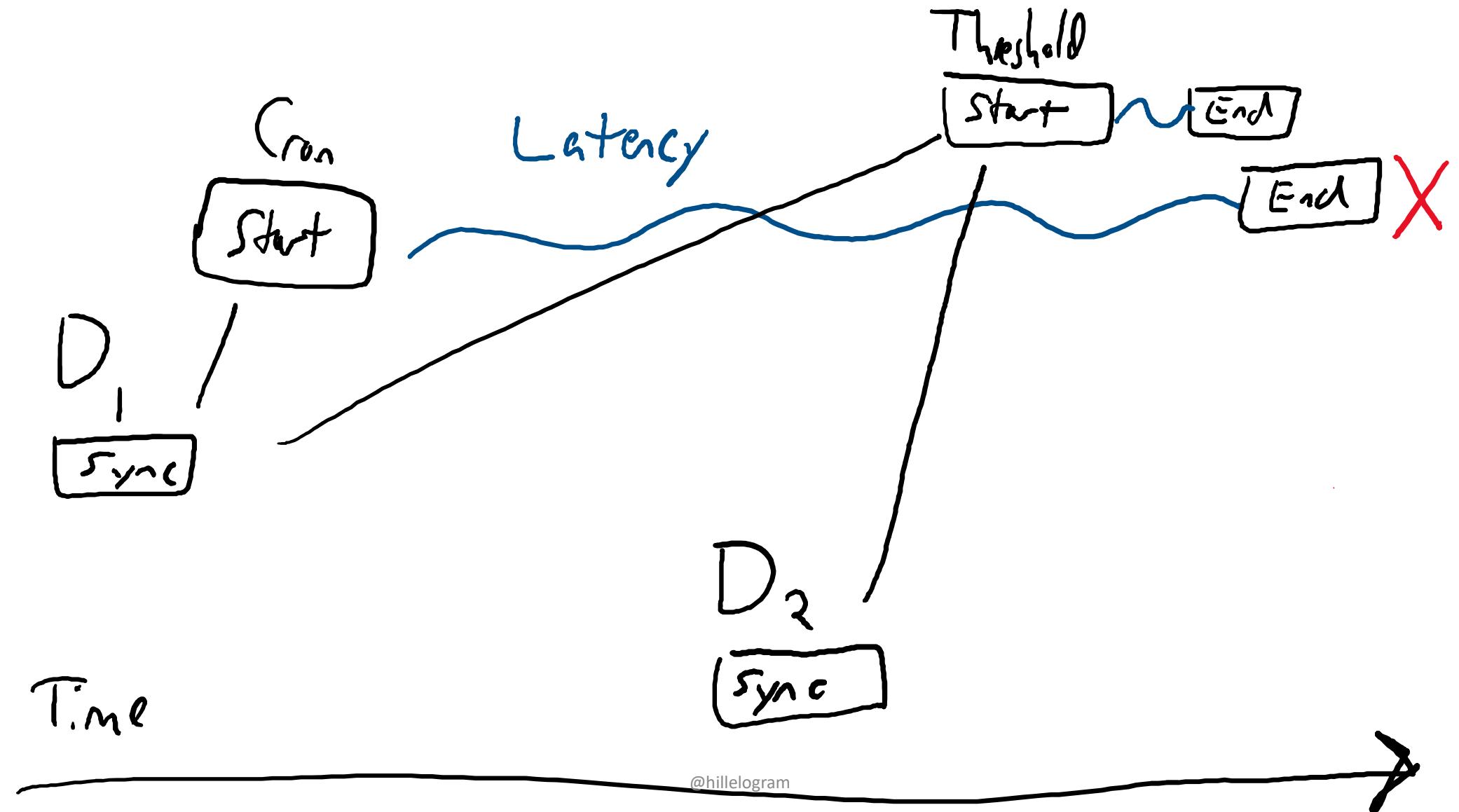
A P P Syncer



@hilleogram

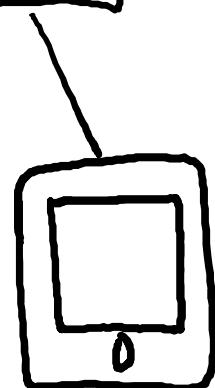
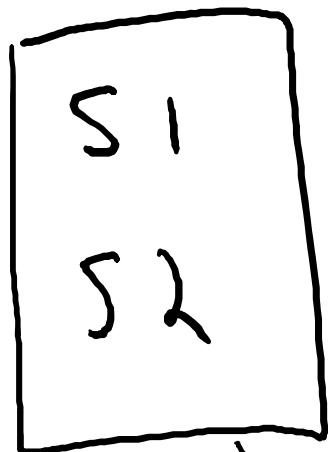
Never try to install an app that is
already installed

```
\A d \in Devices:  
InstallCount[d] \in {0, 1}
```

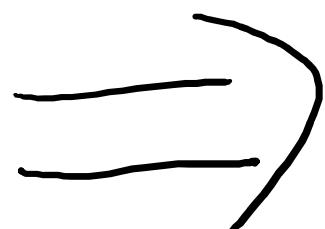
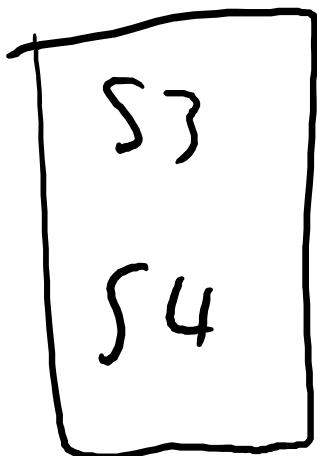


Zero Downtime
Deployments

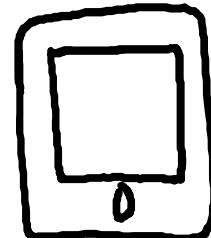
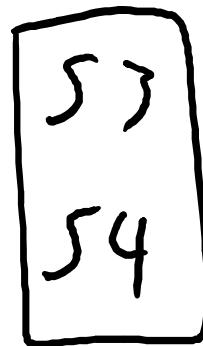
Load
Balancer



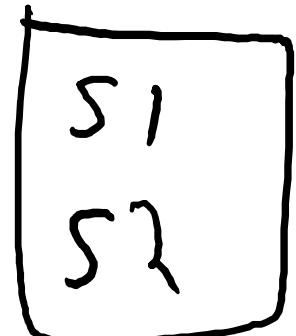
Updating



Load
Balancer



Updating



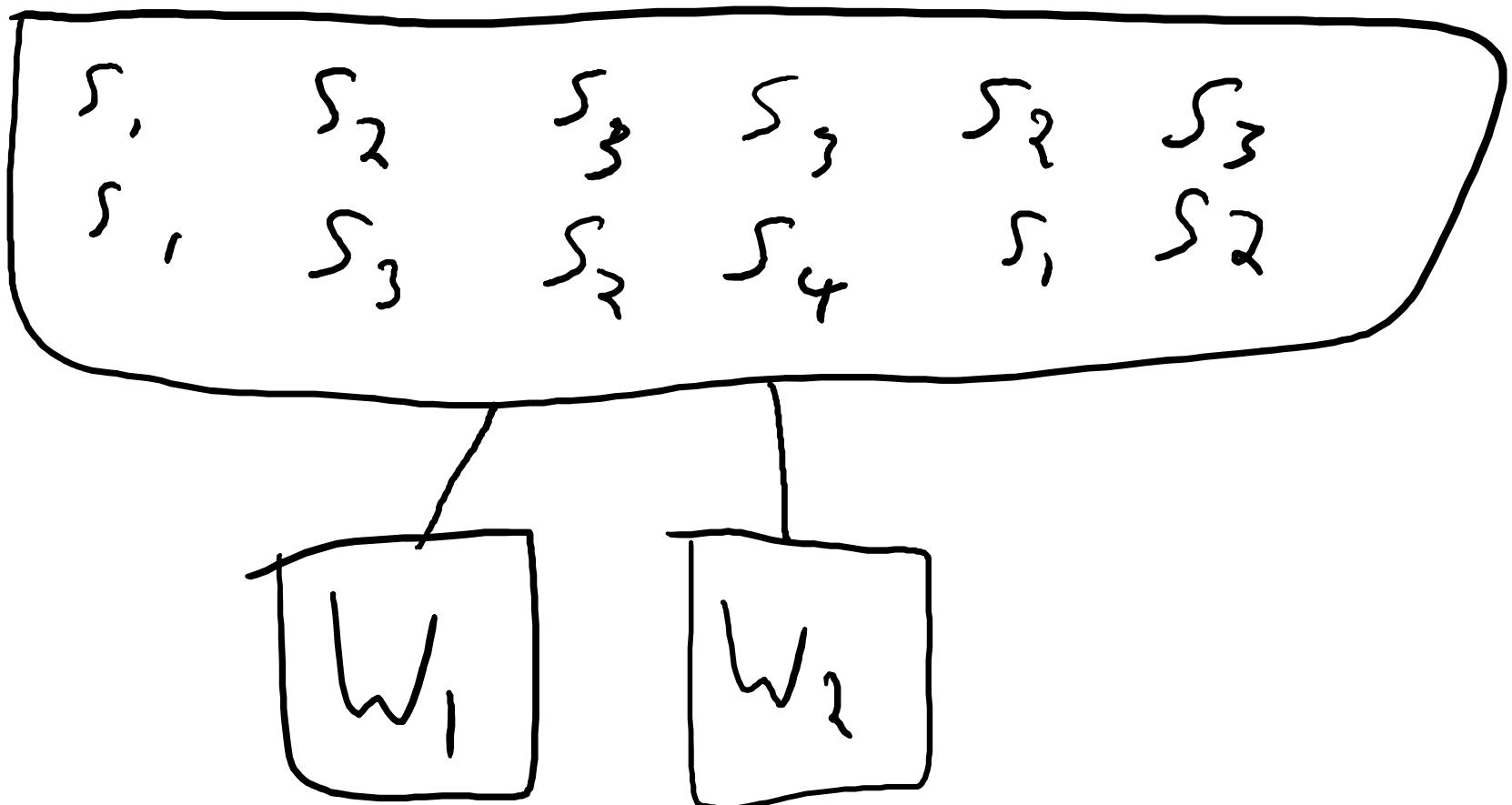
At least one server is available,
and all available servers on same
code

```
\E server \in load_balancer:  
  /\ status[server] /= UPDATING  
  /\ \A s \in load_balancer:  
    version[server] = version[s]
```

(actually worked pretty
well)

"Redacted"

P_{001}

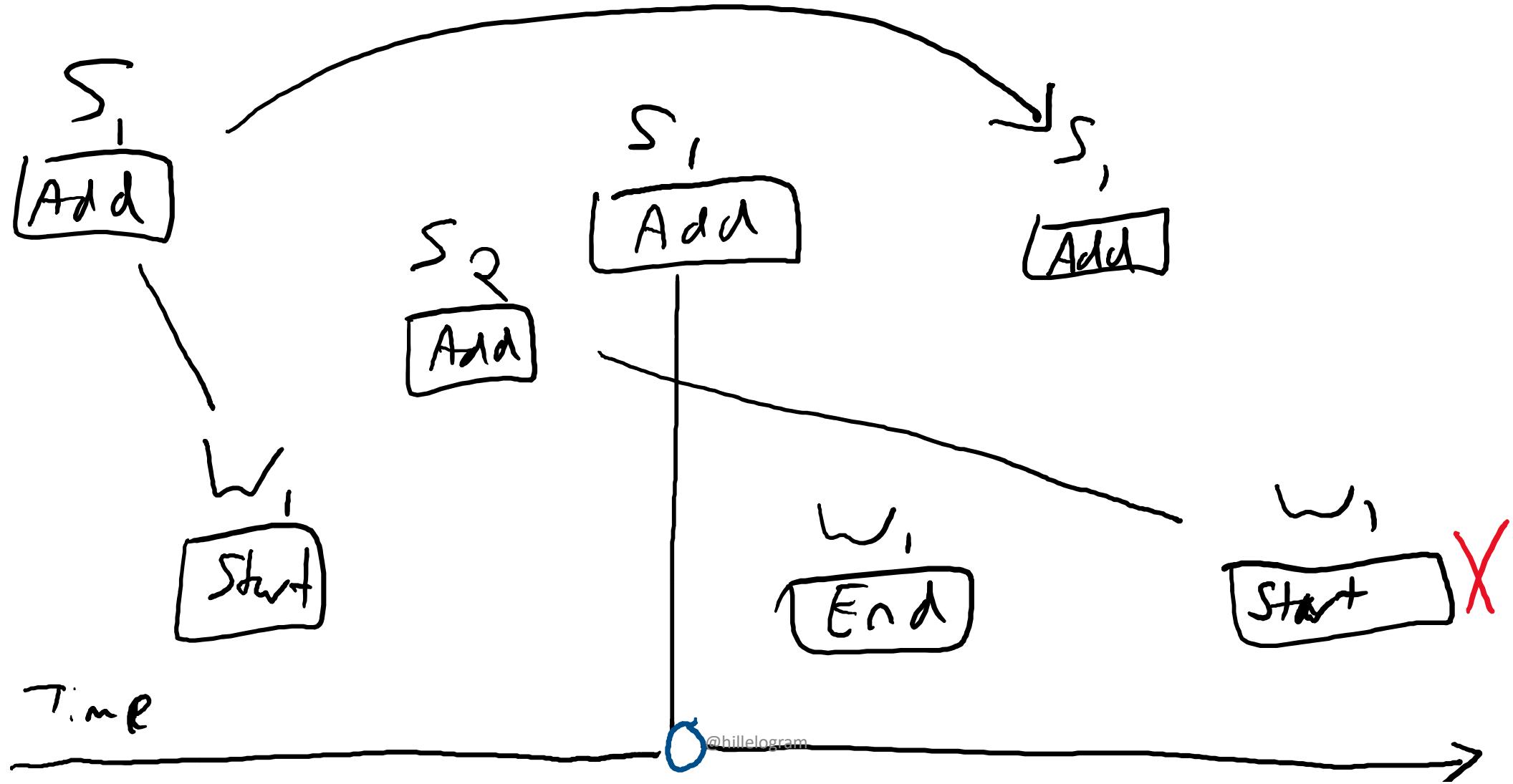


Workers

@hilleogram

When worker processes message source, does not switch sources until all messages processed

```
[ ] [ \A w \in Workers:  
      LET s == on_source[w] IN  
      messages_for[s] /= {}  
      => UNCHANGED s]_vars
```



TLC Errors X Model_1 ?

Temporal properties were violated.

Error-Trace Exploration

Error-Trace

Name	Value
► ▲ <Initial predicate>	State (num = 1)
► ▲ <Action line 111, col 18 to line...	State (num = 2)
► ▲ <Action line 111, col 18 to line...	State (num = 3)
► ▲ <Action line 111, col 18 to line...	State (num = 4)
► ▲ <Action line 111, col 18 to line...	State (num = 5)
► ▲ <Action line 111, col 18 to line...	State (num = 6)
► ▲ <Action line 111, col 18 to line...	State (num = 7)
► ▲ <Action line 119, col 20 to line...	State (num = 8)
► ▲ <Action line 128, col 24 to line...	State (num = 9)
► ▲ <Action line 128, col 24 to line...	State (num = 10)
► ▲ <Action line 128, col 24 to line...	State (num = 11)
► ▲ <Action line 119, col 20 to line...	State (num = 12)
► ▲ <Action line 128, col 24 to line...	State (num = 13)
► ▲ <Action line 111, col 18 to line...	State (num = 14)
► ▲ <Action line 128, col 24 to line...	State (num = 15)
► ▲ <Action line 111, col 18 to line...	State (num = 16)
► ▲ <Action line 111, col 18 to line...	State (num = 17)
▲ <Back to state 8>	State (num = 8)

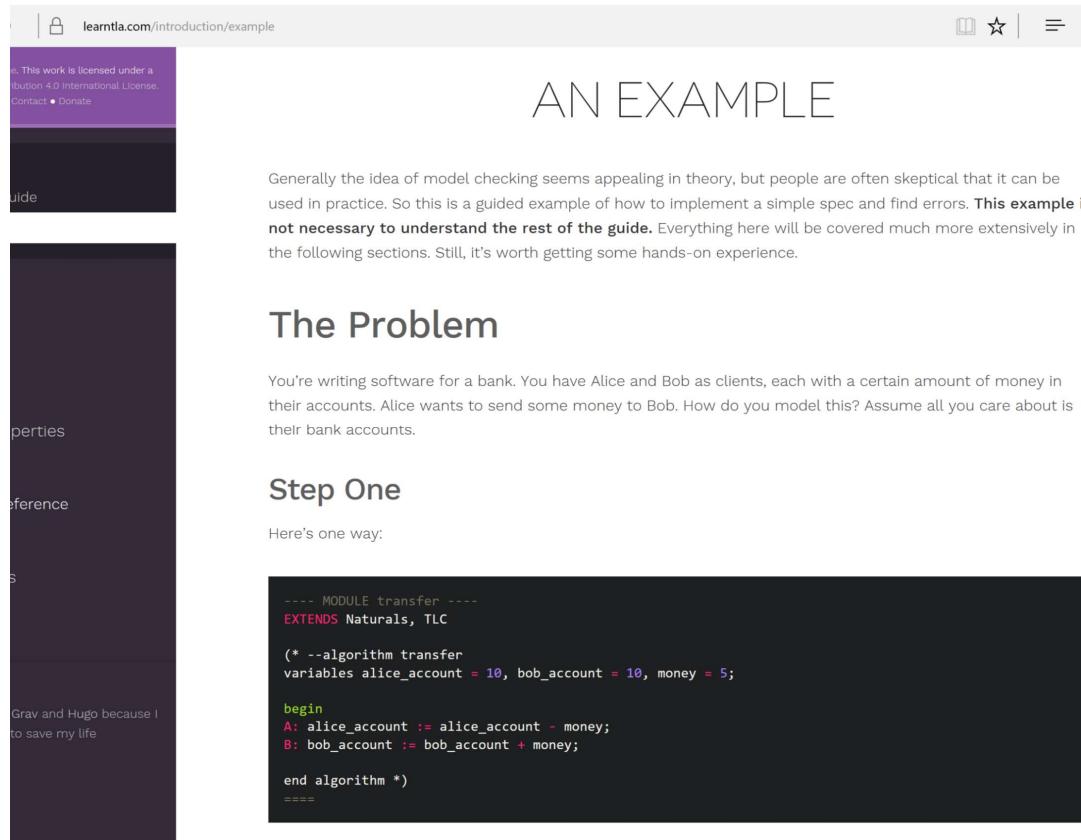
@hilleogram

Conclusions

- Concurrency is hard
- Specification is good
- TLA+ is cool
- Lamport is scary

www.learntla.com

- Me
- Beginner-level
- Uses PlusCal
- Lots of examples and exercises
- Easiest 30%



The screenshot shows a web browser window with the URL learntla.com/introduction/example. The page content is a PlusCal algorithm for a bank transfer. The algorithm defines a module named 'transfer' that extends 'Naturals' and 'TLC'. It has variables 'alice_account' (initially 10), 'bob_account' (initially 10), and 'money' (initially 5). The algorithm begins by subtracting 'money' from 'alice_account' and adding it to 'bob_account'. The code is annotated with comments: 'Grav and Hugo because I have to save my life'.

```
---- MODULE transfer ----
EXTENDS Naturals, TLC

(* --algorithm transfer
variables alice_account = 10, bob_account = 10, money = 5;

begin
A: alice_account := alice_account - money;
B: bob_account := bob_account + money;

end algorithm *)
=====
```

AN EXAMPLE

Generally the idea of model checking seems appealing in theory, but people are often skeptical that it can be used in practice. So this is a guided example of how to implement a simple spec and find errors. **This example is not necessary to understand the rest of the guide.** Everything here will be covered much more extensively in the following sections. Still, it's worth getting some hands-on experience.

The Problem

You're writing software for a bank. You have Alice and Bob as clients, each with a certain amount of money in their accounts. Alice wants to send some money to Bob. How do you model this? Assume all you care about is their bank accounts.

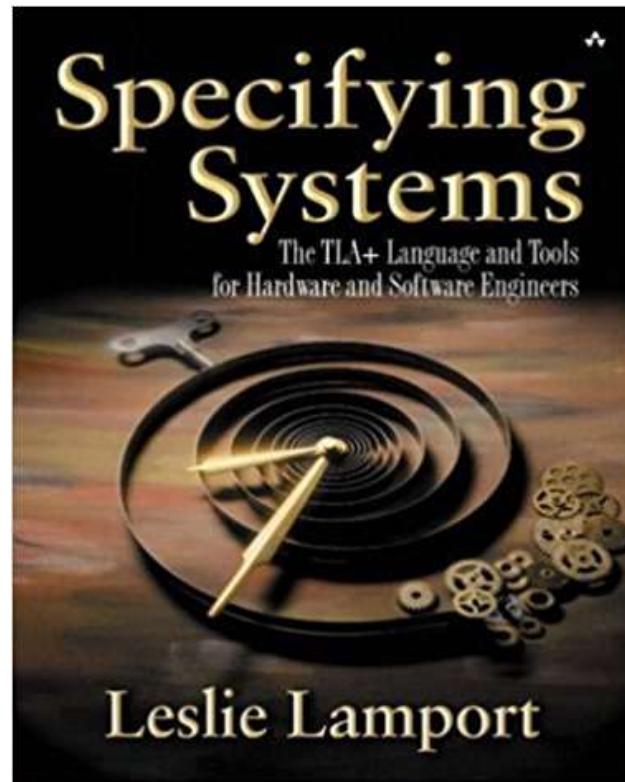
Step One

Here's one way:

@hilleogram

Specifying Systems

- Leslie Lamport
- Canonical text
- Covers theory
- No PlusCal
- Intermediate-level



@hilleogram

TLA+ in Practice and Theory (pron.github.io)

- Ron Pressler
- Covers history, theory, math
- More advanced, theoretical
- Wallace and Gromit avatar

pressron

TLA+ in Practice and Theory

Part 1: The Principles of TLA+

25 May 2017

This is the first installment in a four-part blog post series about TLA+. Part 2, Part 3, Part 4. A video of a 40-minute talk that covers parts of this series.

If you find TLA+ and formal methods in general interesting, I invite you to visit and participate in the new /r/tlaplus on Reddit.

Thinking doesn't guarantee that we won't make mistakes. But not thinking guarantees that we will.

Leslie Lamport, *Why We Should Build Software Like We Build Houses*

Thinking clearly is hard; we can use all the help we can get.

Leslie Lamport, *Specifying Systems*

@hilleogram

Thanks for coming!

@hillelogram

hillelwayne.com

learntla.com