UNN(A) = $\sum_{i=1}^{n} a_i \sigma(wix + bi)$ shallow learnable coeff. Step 1 a = (ai) i=1,-n 1. $\angle (a) = \int_{a}^{a} (u_{NN}(x) - f)^{2} dx \rightarrow function approx$ Sel 71 € 2 $\mathcal{L}(2) = \frac{1}{2} \int_{0}^{1} (4 \sin^{2})^{2} dx - \int_{0}^{1} u_{NN}(x) f(x) dx$, FNA $\int_{0}^{1} -u''(x) = f(x)$ 3. $L(9) = \int_{0}^{1} (u_{NN}^{11} + f)^{2} dx$ PINNS Apply gradient dealent to L , wi, Si rendomised ain = an- proalle) stert wik]=2 Step up (4) = \(\for \text{prind}\) book functions

Step up (4) = \(\frac{1}{2} \text{ with } \frac{1}{2} \)

Step up (4) = \(\frac{1}{2} \text{ with } \frac{1}{2} \)

Step up (5) \(\frac{1}{2} \)

Step up up (4) = \(\frac{1}{2} \)

Window functions Repeat the Love Rendomis cui, bi, one-level FPBINN -> RTM milhoud = coarge network $\frac{1}{m_1} = \frac{1}{2} a_i \sigma(w_i \pi + \delta_i) w_1(\pi)$ $\frac{1}{m_2} = \frac{1}{2} a_i \sigma(w_i \pi + \delta_i) w_2(\pi)$ $\frac{1}{m_1} = \frac{1}{2} a_i \sigma(w_i \pi + \delta_i) w_2(\pi)$ ò 42-8 42+8 $L(a) = \frac{1}{2} \int_{0}^{1} (f(x) - u_{NN}(x))^{2} dx = \frac{1}{2} \int_{0}^{1} (f(x) - u_{NN}(x))^{2} dx + \frac{1}{2} \int_{0}^{1} (f(x) - u_{NN}(x))^{2} dx$ +15 (+(x) - 4NN (x) 2 dx = -5, a, + 1 a, m, a, - (5, 5,] [a, a2] - 52 az + 1 2 az 4 az + 1 [a, az] Tr [a, az] (M2)ij= [(Wints) (Wints) dx (M2); come with w, b,

$$= -5^{T}_{1}\alpha_{1} + \frac{1}{2}a_{1}^{T}H_{1}\alpha_{1} - (5^{T}_{1}5_{1})^{T}_{1}[\alpha_{1}\alpha_{2}] \qquad \qquad \widetilde{H} = \begin{bmatrix} \widetilde{H}_{1} & H_{12} \\ H_{21} & \overline{H}_{2} \end{bmatrix} \qquad H_{12} = H_{21}^{T}_{21} \\ -5^{T}_{1}\alpha_{1} + \frac{1}{2}a_{2}^{T}H_{1}\alpha_{2} + \frac{1}{2}[\alpha_{1}\alpha_{2}]^{T}\widetilde{H}[\alpha_{1}\alpha_{2}] \qquad \qquad \widetilde{H} = \begin{bmatrix} \widetilde{H}_{1} & H_{12} \\ H_{21} & \overline{H}_{2} \end{bmatrix} \qquad H_{12} = H_{21}^{T}_{21}$$

$$\nabla_{\mathbf{q}} \langle \mathbf{l} \mathbf{q} \rangle = - + \left(\begin{array}{ccc} \eta_{1} + \widetilde{\mathbf{H}}_{1} & \eta_{1} \\ \eta_{1} & \eta_{1} + \widetilde{\eta}_{1} \end{array} \right) \left(\begin{array}{c} \mathbf{q}_{1} \\ \mathbf{q}_{2} \end{array} \right)$$

$$H = \begin{cases} n_1 + \tilde{n}_1 & n_{12} \\ n_{21} & n_{12} \end{cases} \text{ is this make:} \qquad \begin{aligned} w_{1(1)} &= \frac{42+\delta-2}{8} & \text{ on } (42-\delta_1 44+\delta_2) \\ w_{2(1)} &= \frac{2-(41-\delta)}{8} & \text{ on } (42-\delta_1 44+\delta_2) \end{aligned}$$

Enhies of the matrix it are all computable

- A fow quehous: . arous the conditor number of this matrix
- . aven approximation proputes
- . cen sur havre a rough estimate of the condition number!

Raylish creft
$$x[H_1 + H_1]x + y^T(H_1 + H_2)y + 2x^TH_{12}y = \frac{\lambda_1 \|x\|^2 + \lambda_2 \|y\|^2 + 2x^TH_{12}y}{(x y)^T(x,y)}$$

λ = min (λ1, λ2), what do we need about 1912 to estimate

zt my z n xiy? If we suppose so and y are of the same rise boam number of weights for each

=) M12 is equare (also symmetric i) we us the same achirchen junction)

. mugh compark everything numerically the by to get some therity.

no would expect the H & teller conditioned then just working on the whole interval rook larger methods