Lecture Introduction to Network Science Prof. Dr. David B. Blumenthal Dr. Anne Hartebrodt Fabian Woller



## SOLUTION 1

Exercise Session: 2.5.2024

## **Question 2**

BFS: 
$$1-5-6-2-4-7-8-3-9$$
  
DFS:  $1-2-3-4-5-6-7-8-9$ 

## **Question 3**

- a) You can find an examplary implementation in the jupyter notebook traversal.ipynb.
- b) See a).
- c) Both DFS and BFS have runtime complexity  $\mathcal{O}(|V|+|E|)$ . With both DFS and BFS the total of number of taken "steps", i.e. analyzed entities equals  $v_1+E(v_1)+v_2+E(v_2)+\cdots+v_n+E(v_n)=(v_1+\cdots+v_n)+(E(v_1)+\cdots+E(v_n))$ , where  $v_i$  are the nodes of the given graph and  $E(v_i)$  denotes the set of incident edges of node  $v_i$ . The first part of the sum is in  $\mathcal{O}(|V|)$  and the second one in  $\mathcal{O}(2|E|)=\mathcal{O}(|E|)$ .