Lecture Introduction to Network Science Prof. Dr. David B. Blumenthal Dr. Anne Hartebrodt Fabian Woller



## SOLUTION 9

Exercise Session: 4.7.2024

## **Question 1**

- a) Multiple clustering levels in dendrogram; parameter k in spectral clustering
- b) Modularity measures if the actual number of edges within clusters is higher than expected by chance. Measure is agnostic of number of clusters k.
- c) Use as criterion to obtain best clusters from dendrogram; directly optimize for modularity, as done in the Louvain algorithm
- d) Nodes are initially assigned to individual cluster each; nodes iteratively update their community memberships based on the most frequent label in their neighbourhood; run until convergence of labels
- e) Asynchronous vs. synchronous label update; different neighborhood structures; label update rule

## **Question 2**

a) The labels of the nodes after synchronous label update are A:1, B:1, C:3, D:3, E:3.

For parts b) and c) there is no unique solution due to randomized tiebreaks and asynchronous label update, we discuss possible solutions in the exercise session.

## **Question 3**

See exemplary implementation in girvan\_modularity.ipynb.