

# Churning the Ocean: Time variable gravity for ocean applications



[Samudra Manthan, CC BY 3.0](#)

Roelof Rietbroek, 28 Sept. 2022



# Analogies with today's talk



Find this presentation on <https://github.com/strawpants/grace-hackweek-ocean>



# Analogy's with today's talk

- Mount Mandara: Adding mass to the ocean (e.g. melt water)



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- Snake Vasuki: set the ocean in motion (e.g. forcing from wind stress)



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# Analogy's with today's talk

- Mount Mandara: Adding mass to the ocean (e.g. melt water)
- Snake Vasuki: set the ocean in motion (e.g. forcing from wind stress)
- Central Question: How can we use time variable gravity to observe ocean signals?



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# Changing the mass to the oceans



# Changing the mass to the oceans

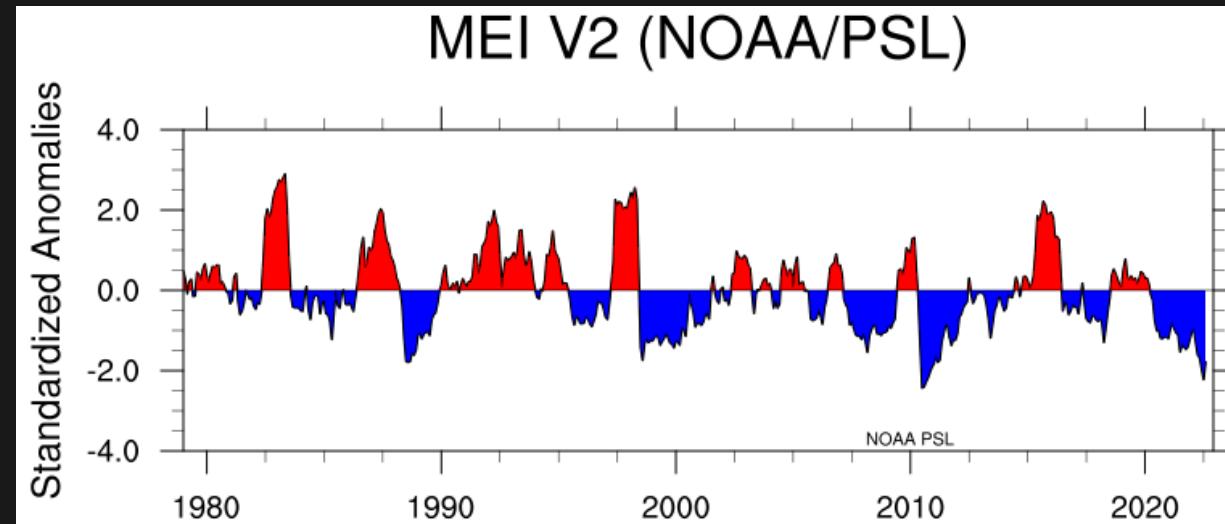
## (or removing it)



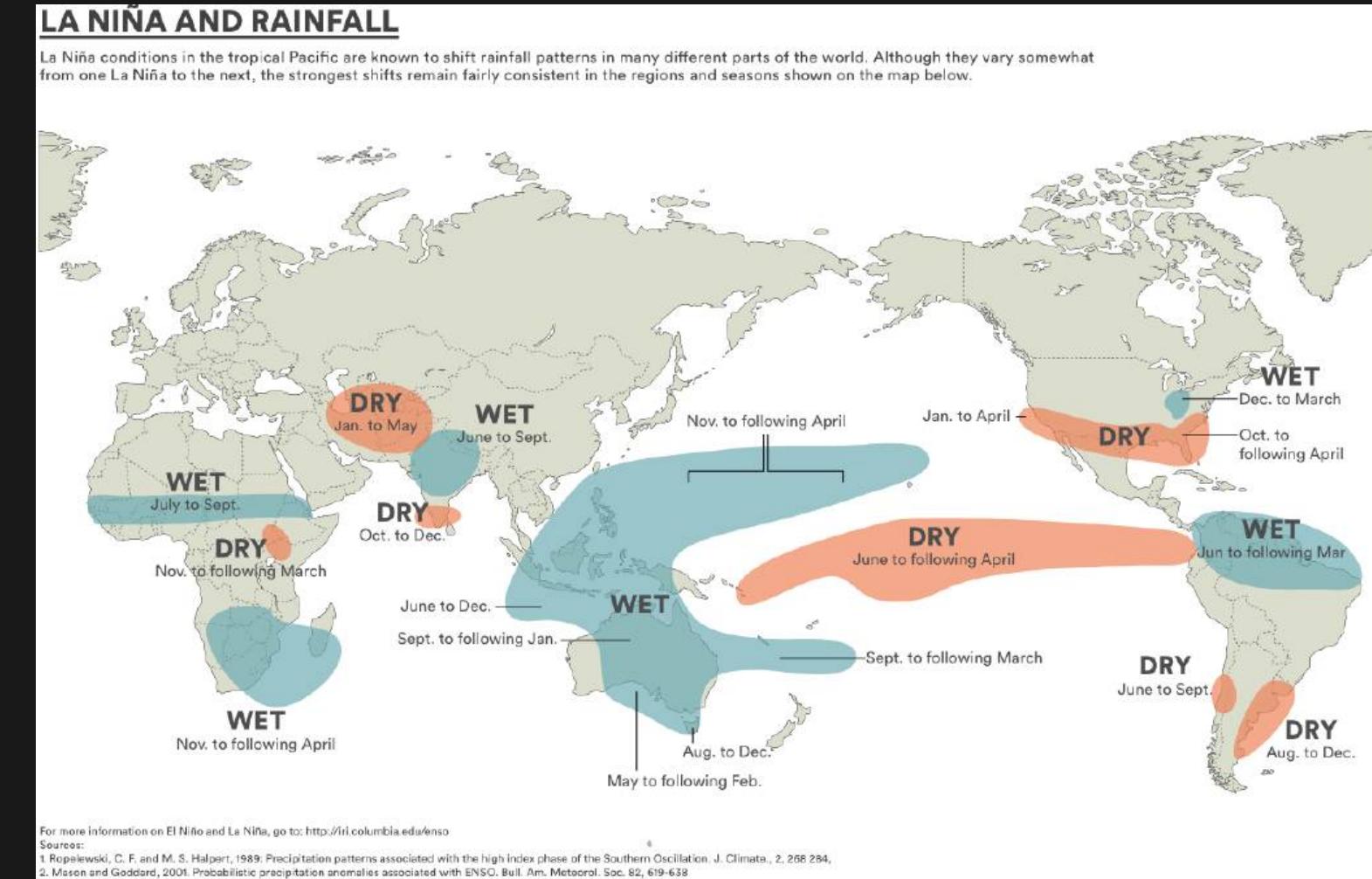
2022 Floods in Pakistan, image: AFP



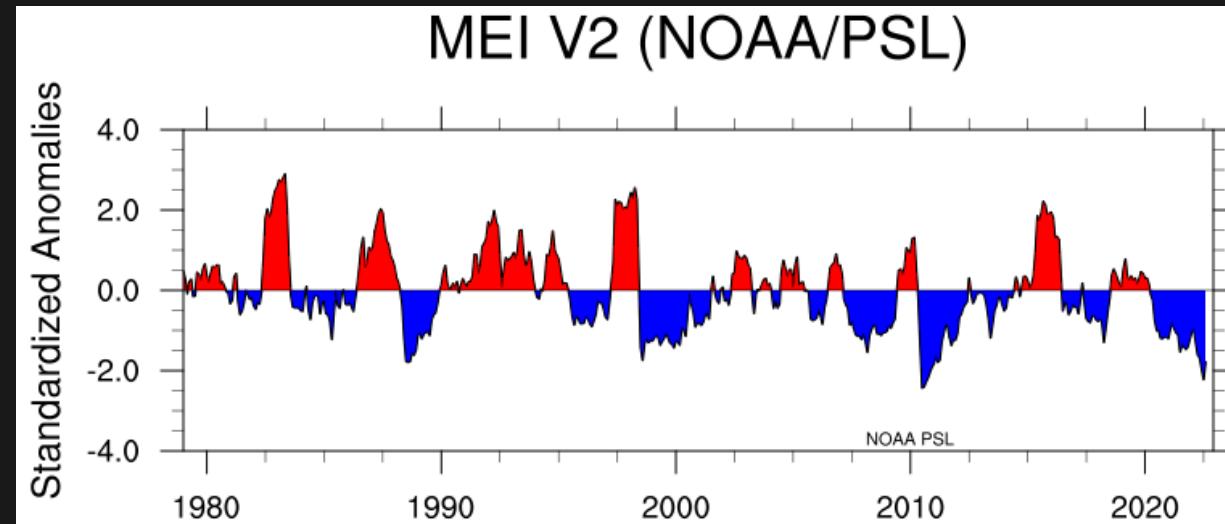
# Does La Niña affect sea level?



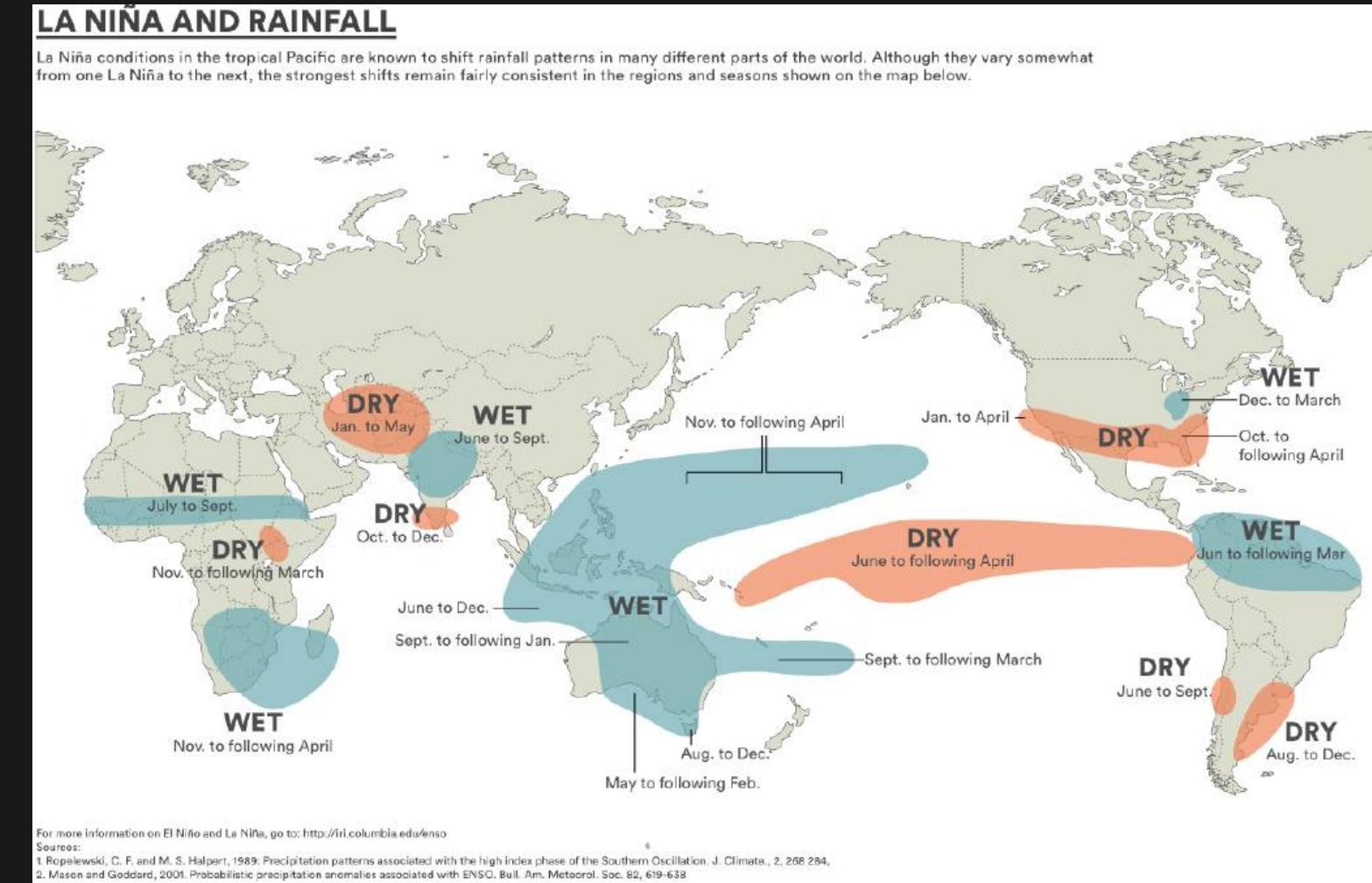
Multivariate ENSO index, <https://psl.noaa.gov/enso>



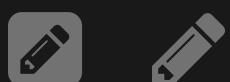
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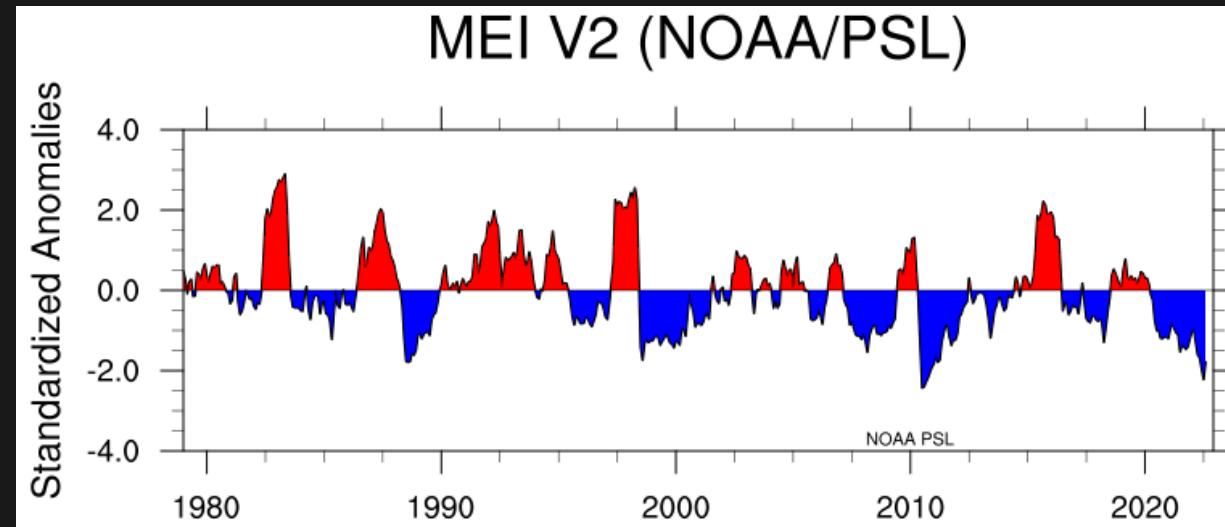
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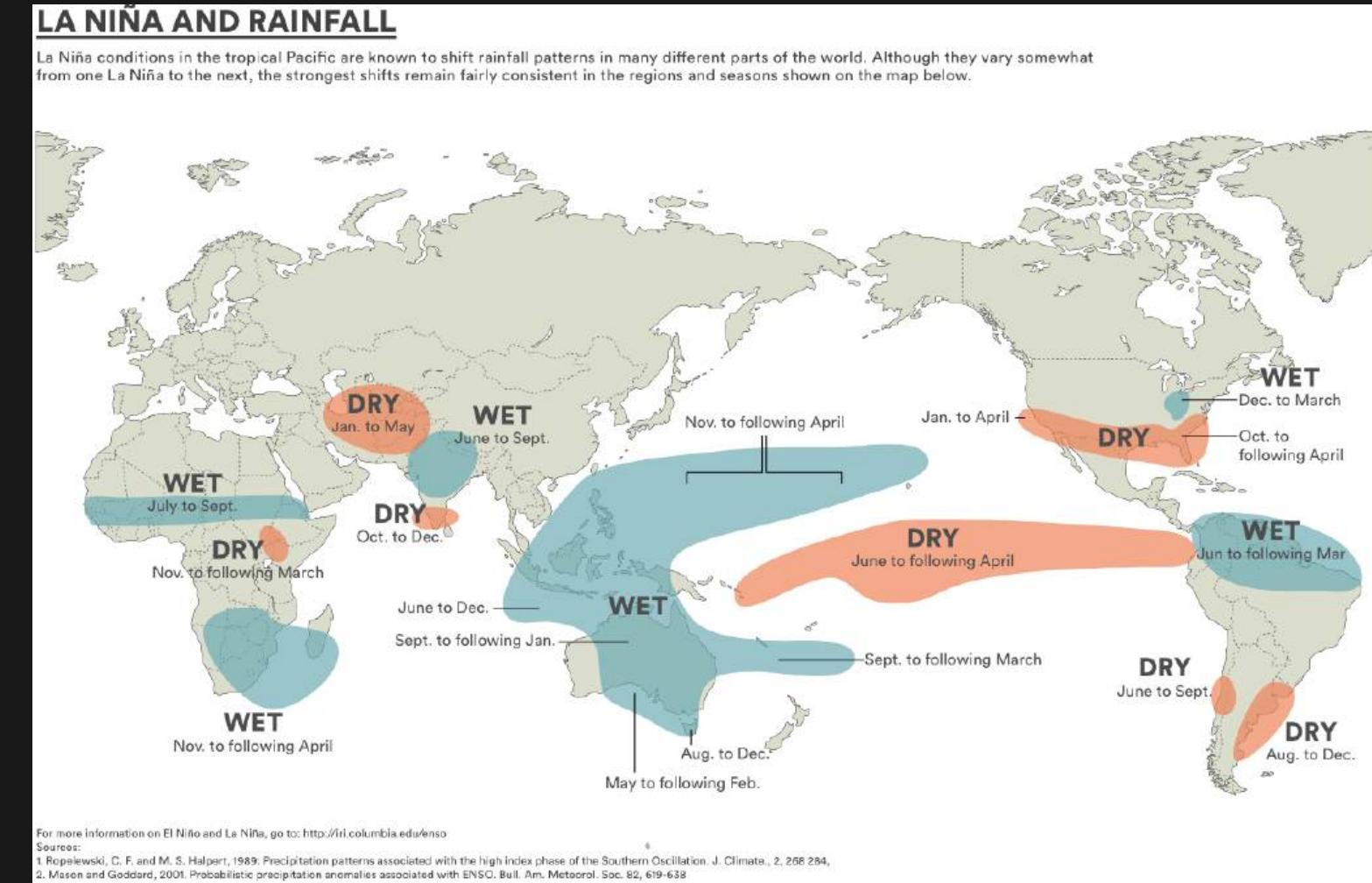
- Stronger trade winds -> warm/wet ocean blob in the western Pacific



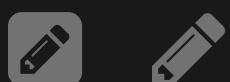
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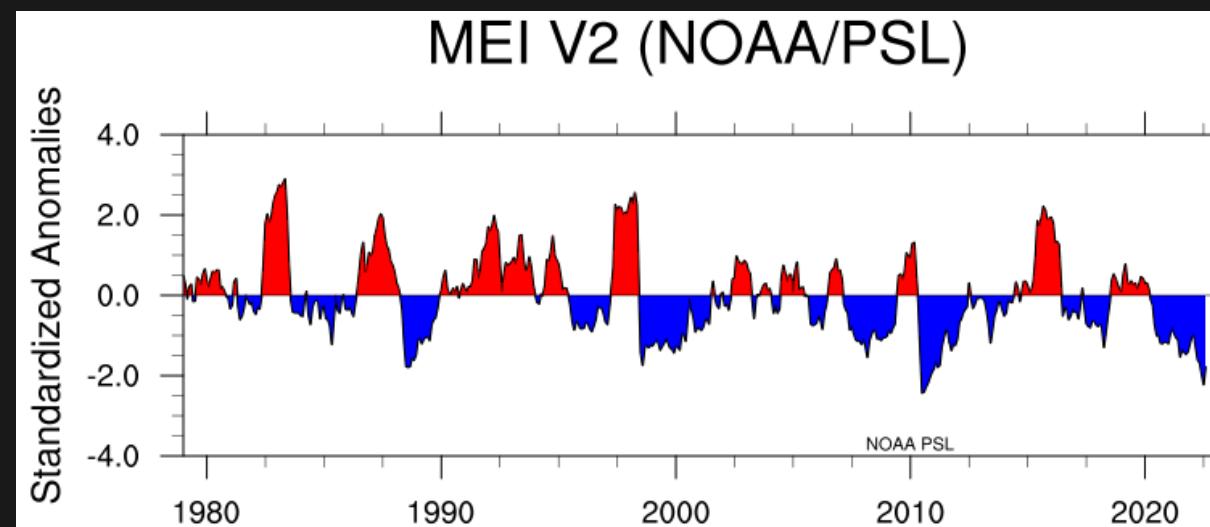
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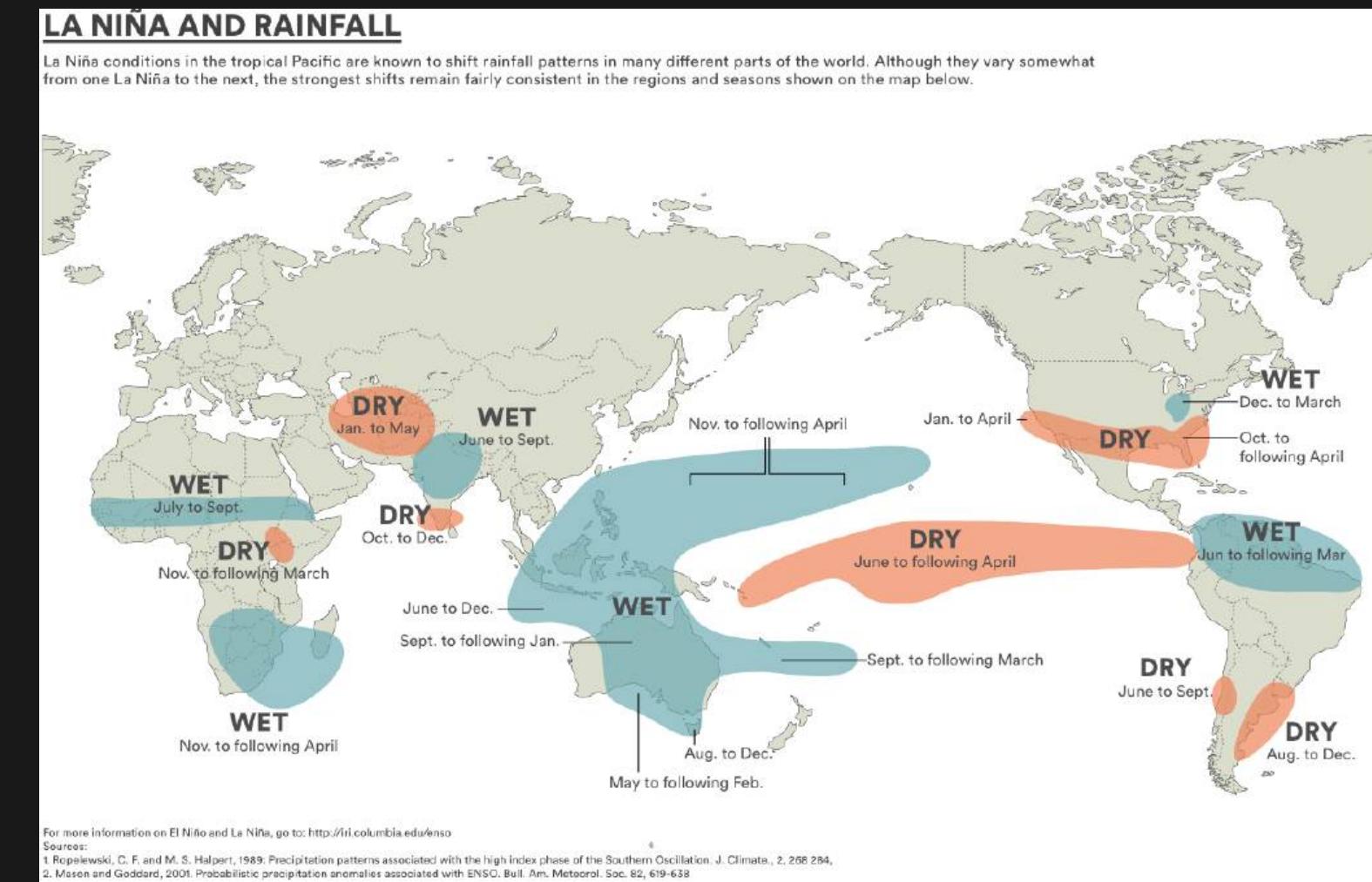
- Stronger trade winds -> warm/wet ocean blob in the western Pacific
- Wet conditions in the West Pacific cause extreme precipitation



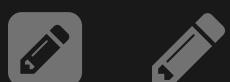
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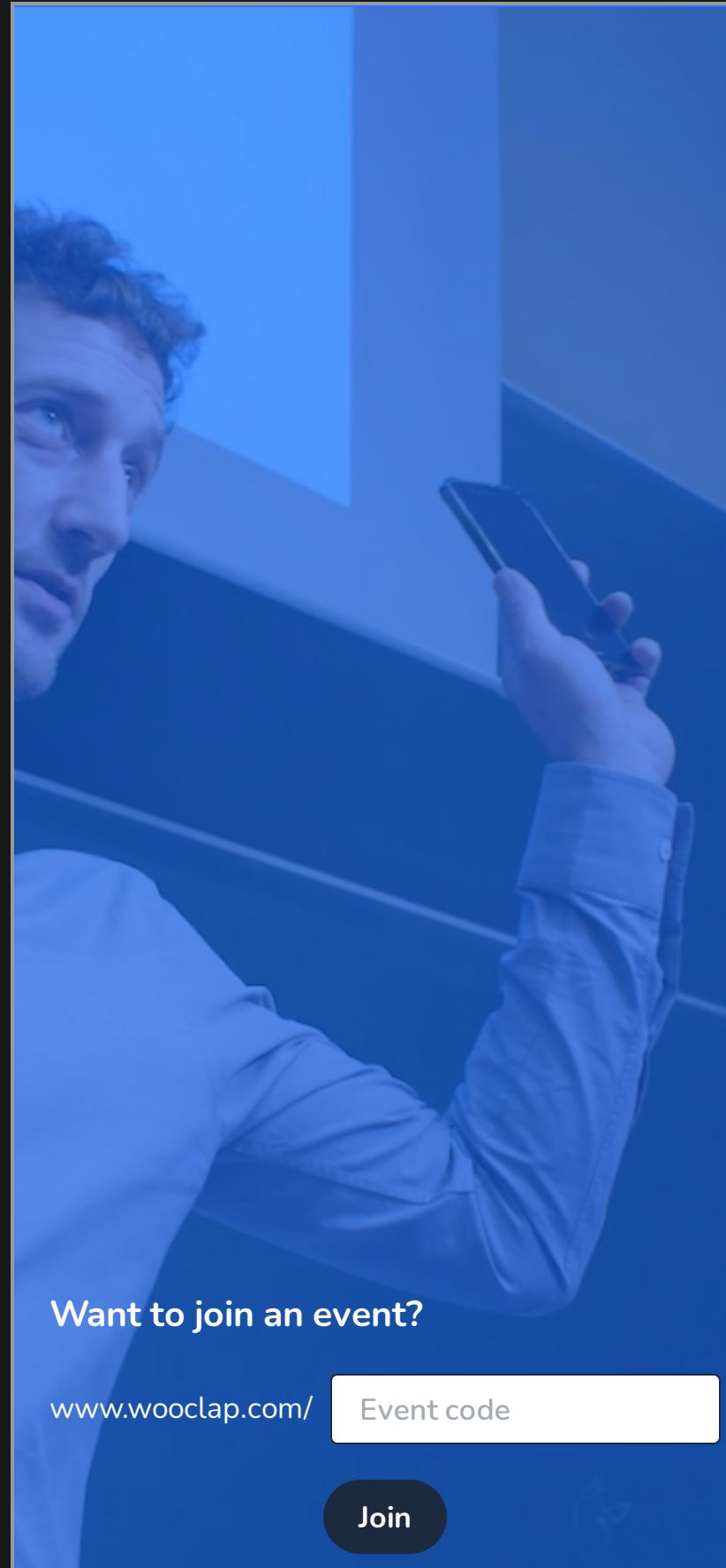
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- Stronger trade winds -> warm/wet ocean blob in the western Pacific
- Wet conditions in the West Pacific cause extreme precipitation
- Teleconnections with Monsoon, Africa..



# Quiz time!



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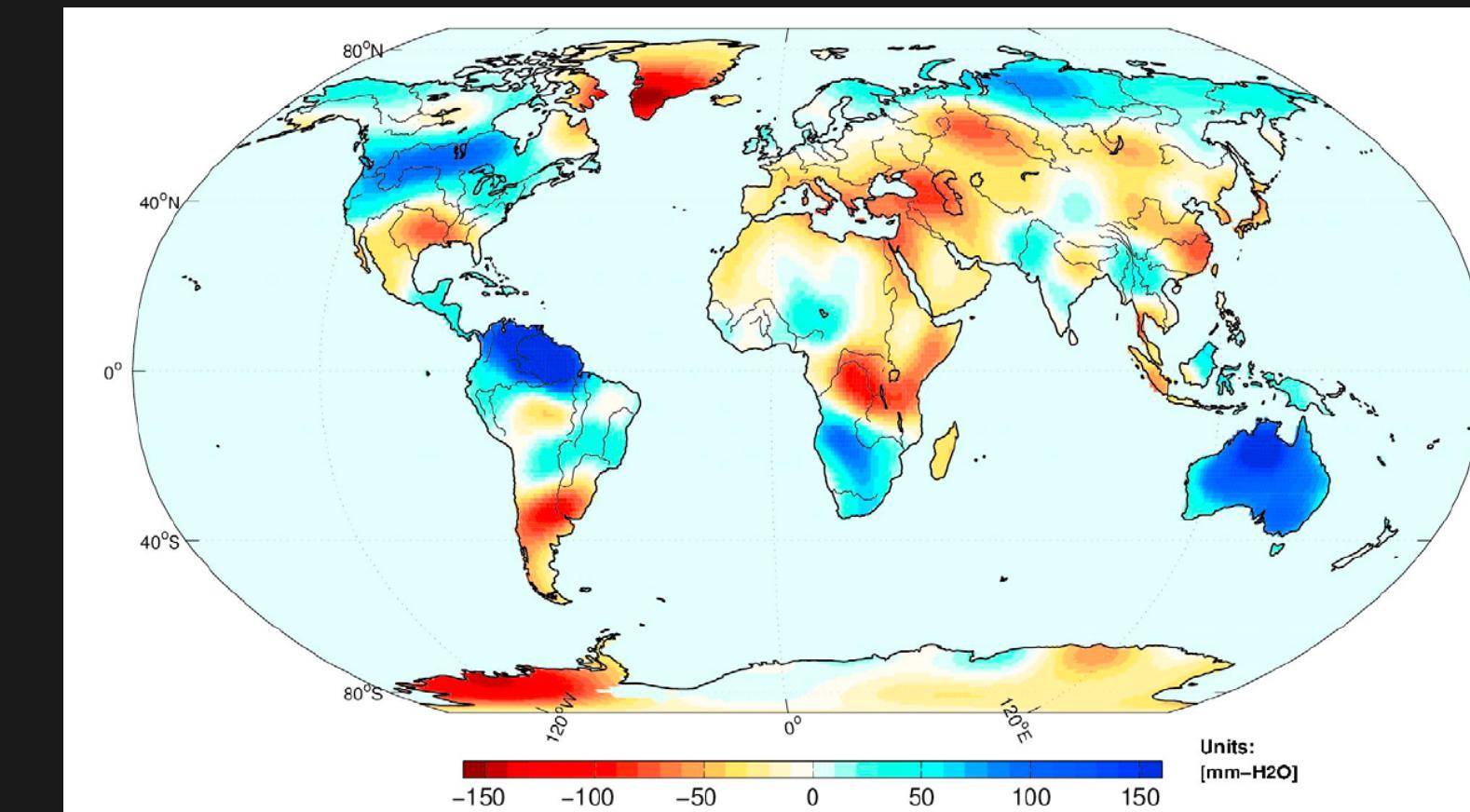
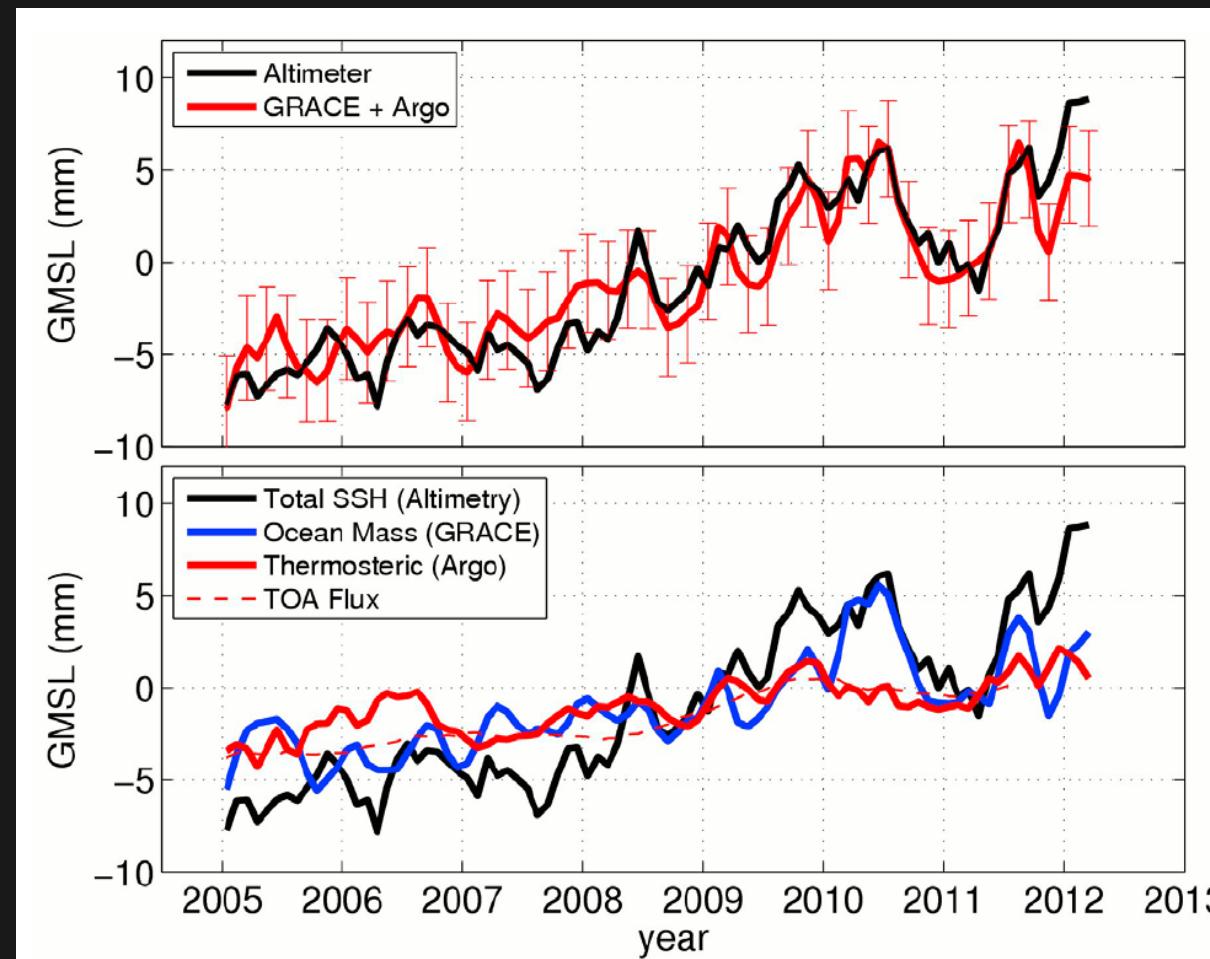
**Accept all**

**Reject All**

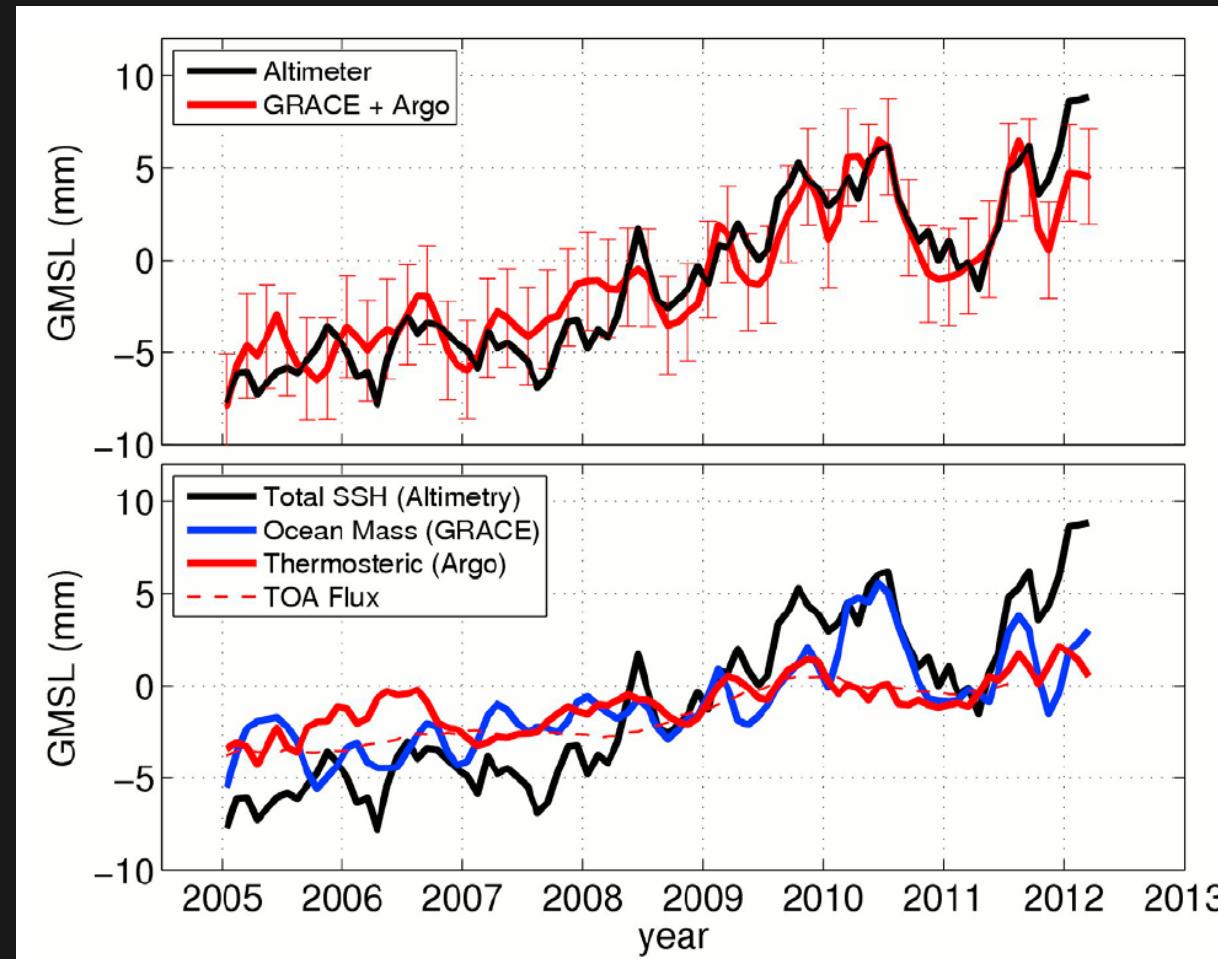
**Customise**



# 2010-2011 La Nina event

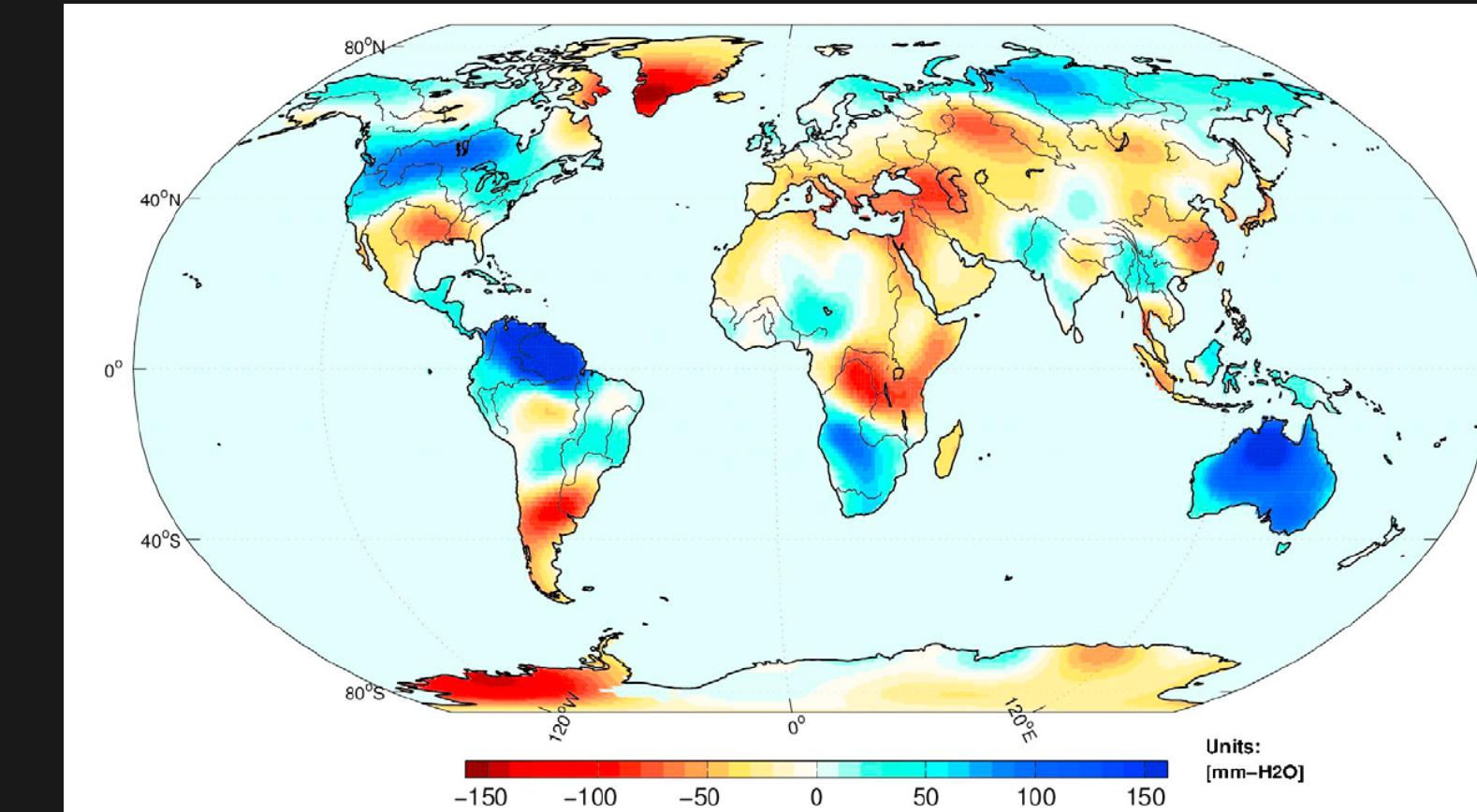


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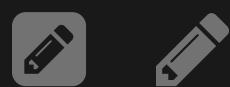


Global mean sea level variations (total, mass driven and 'steric'),  
From Böning et al. 2012

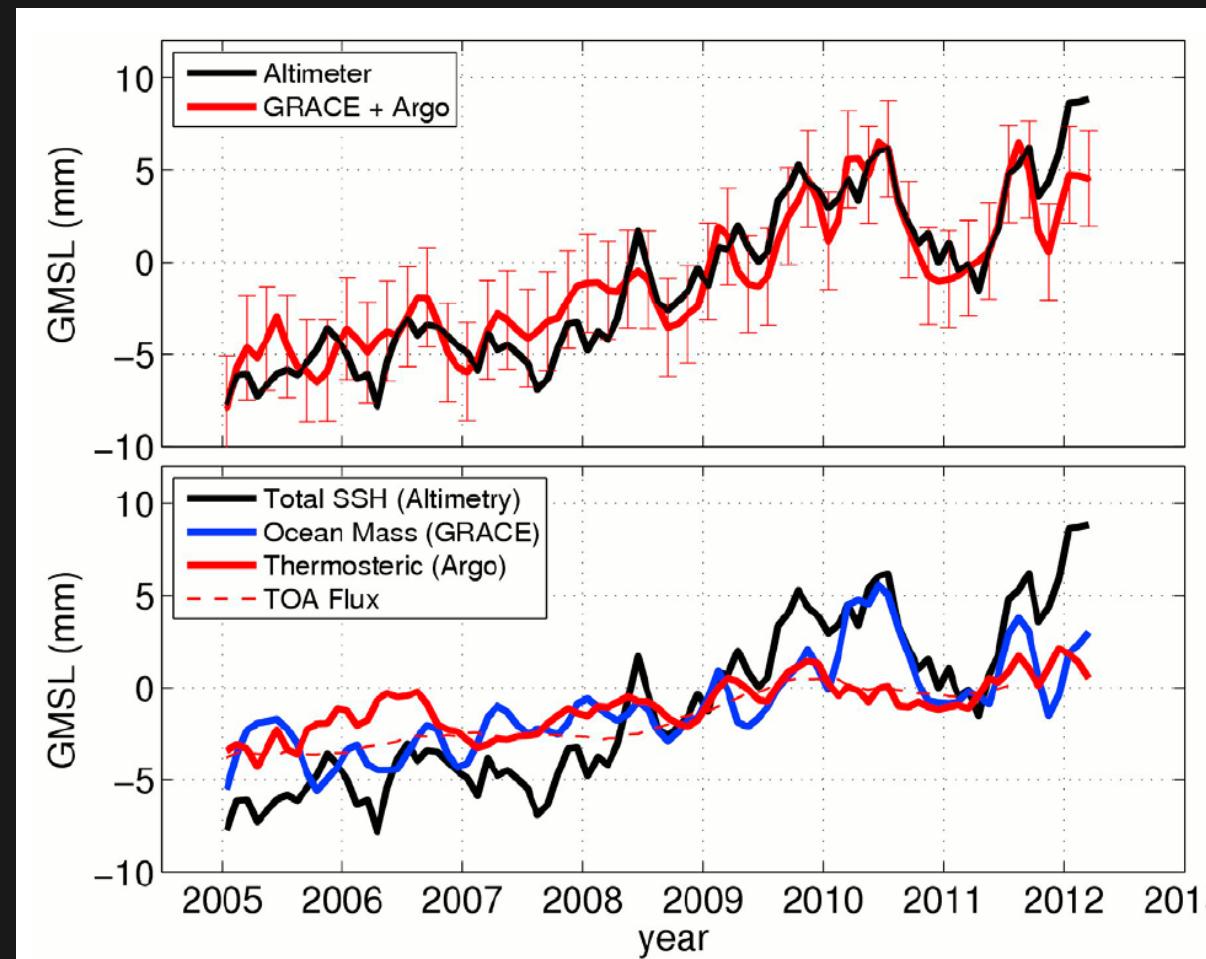
- Detectable with radar altimetry



Terrestrial water storage change (2010-2011) from GRACE, From Böning et al. 2012

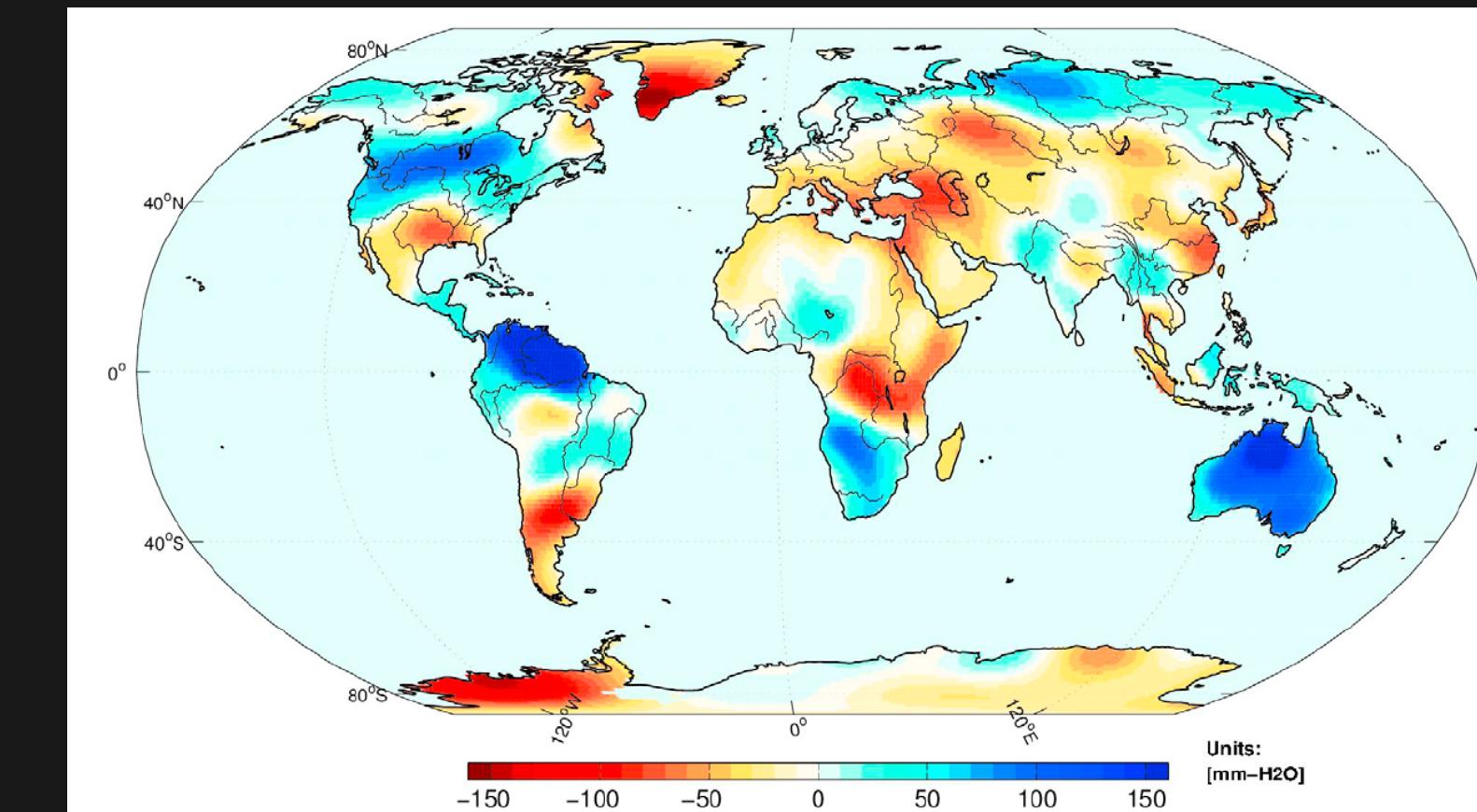


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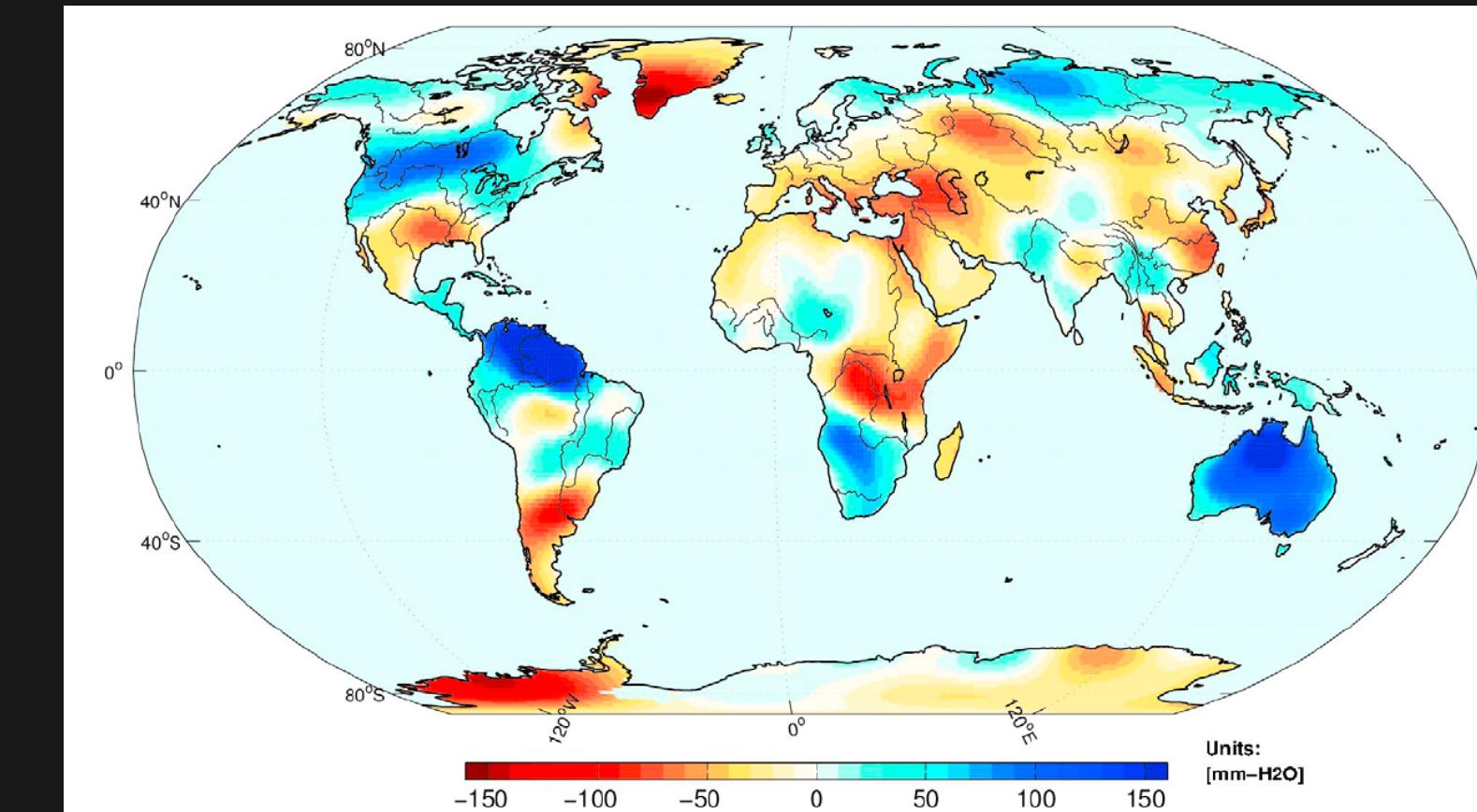
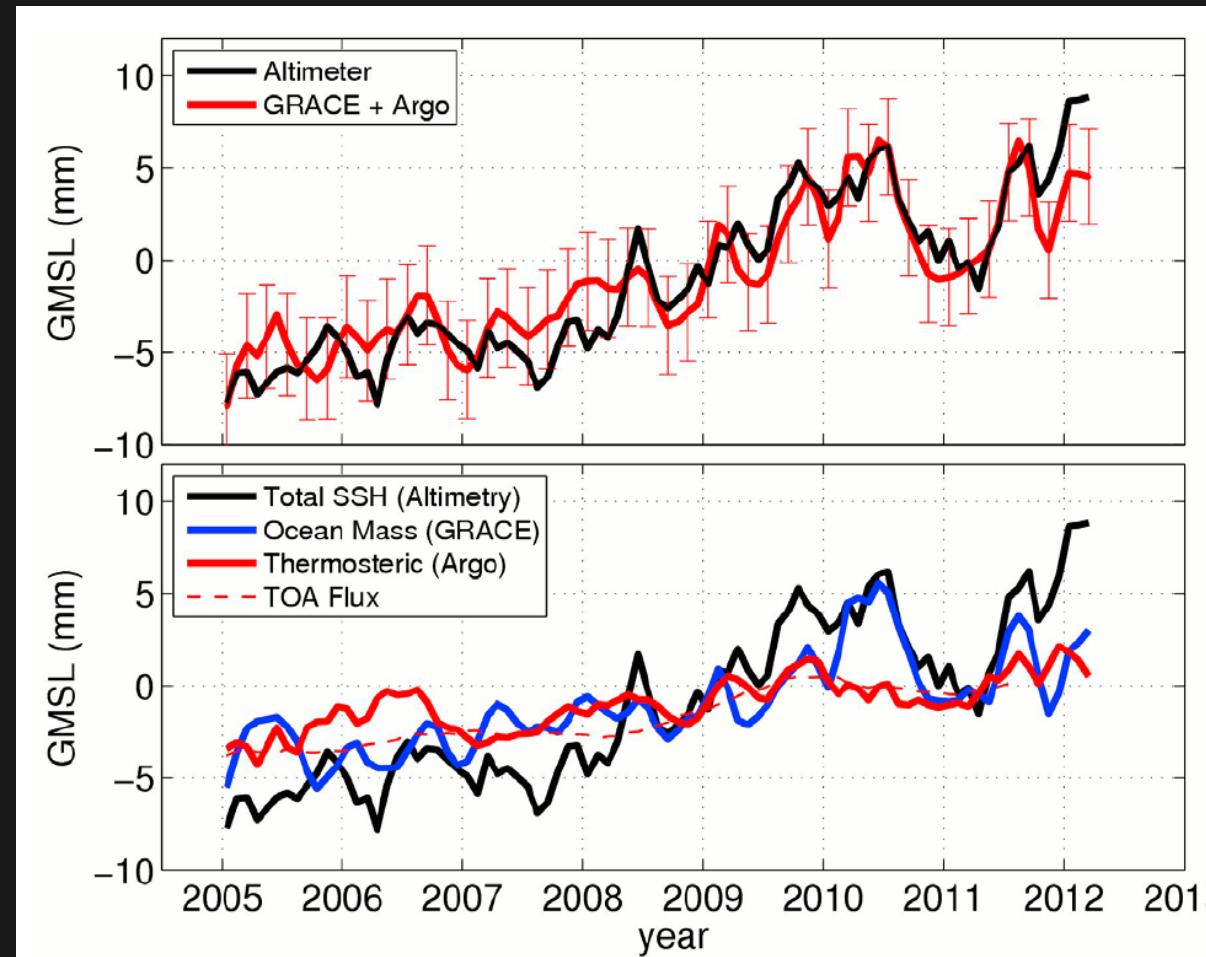
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- Can be explained by mass-driven sea level (GRACE)



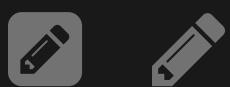
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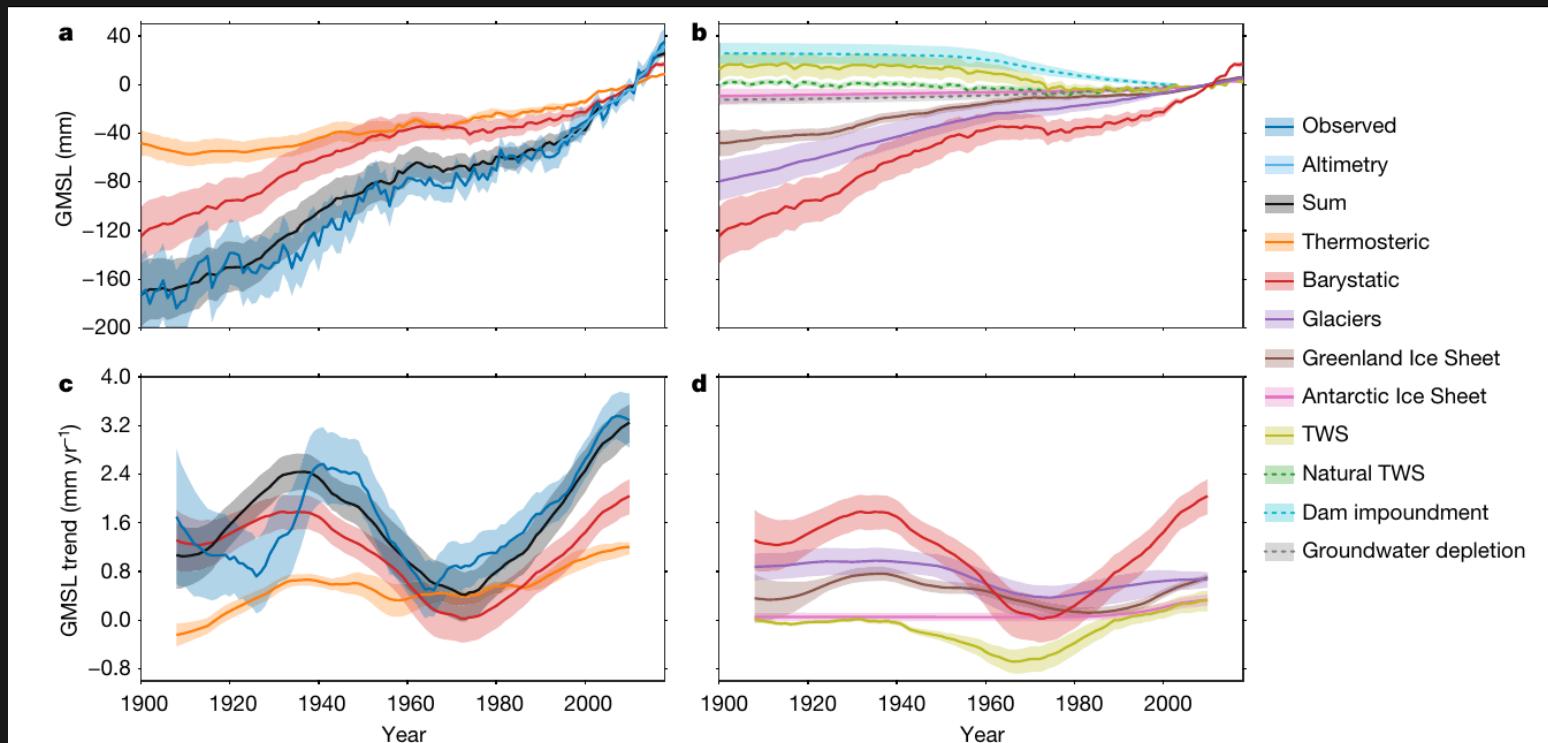
# 2010-2011 La Nina event



- Detectable with radar altimetry
- Can be explained by mass-driven sea level (GRACE)
- Hotspot: Australia



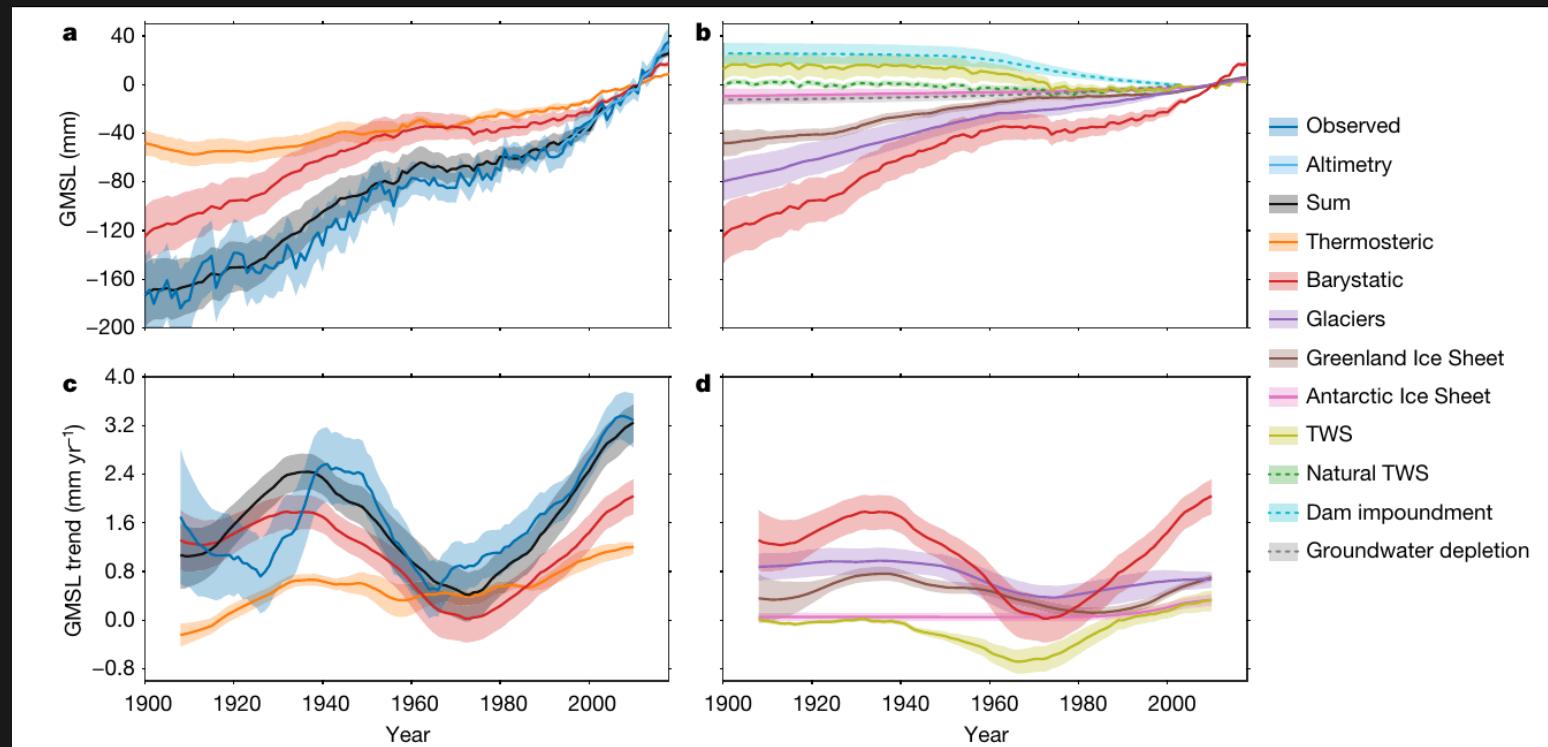
# Sea level contributions since 1900



Historic sea level can be largely explained with different (modelled) sea level contributions. From Frederikse et al. 2020



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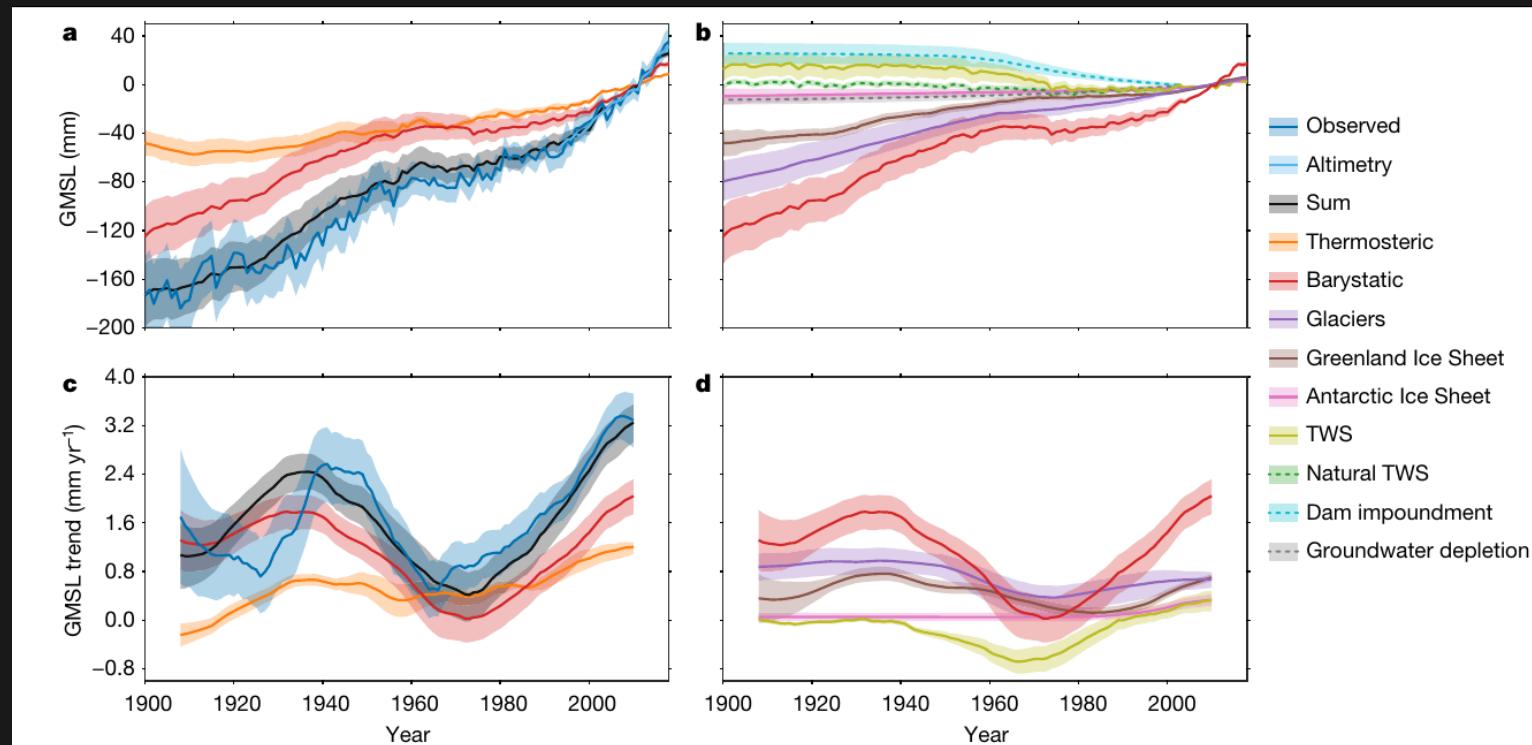


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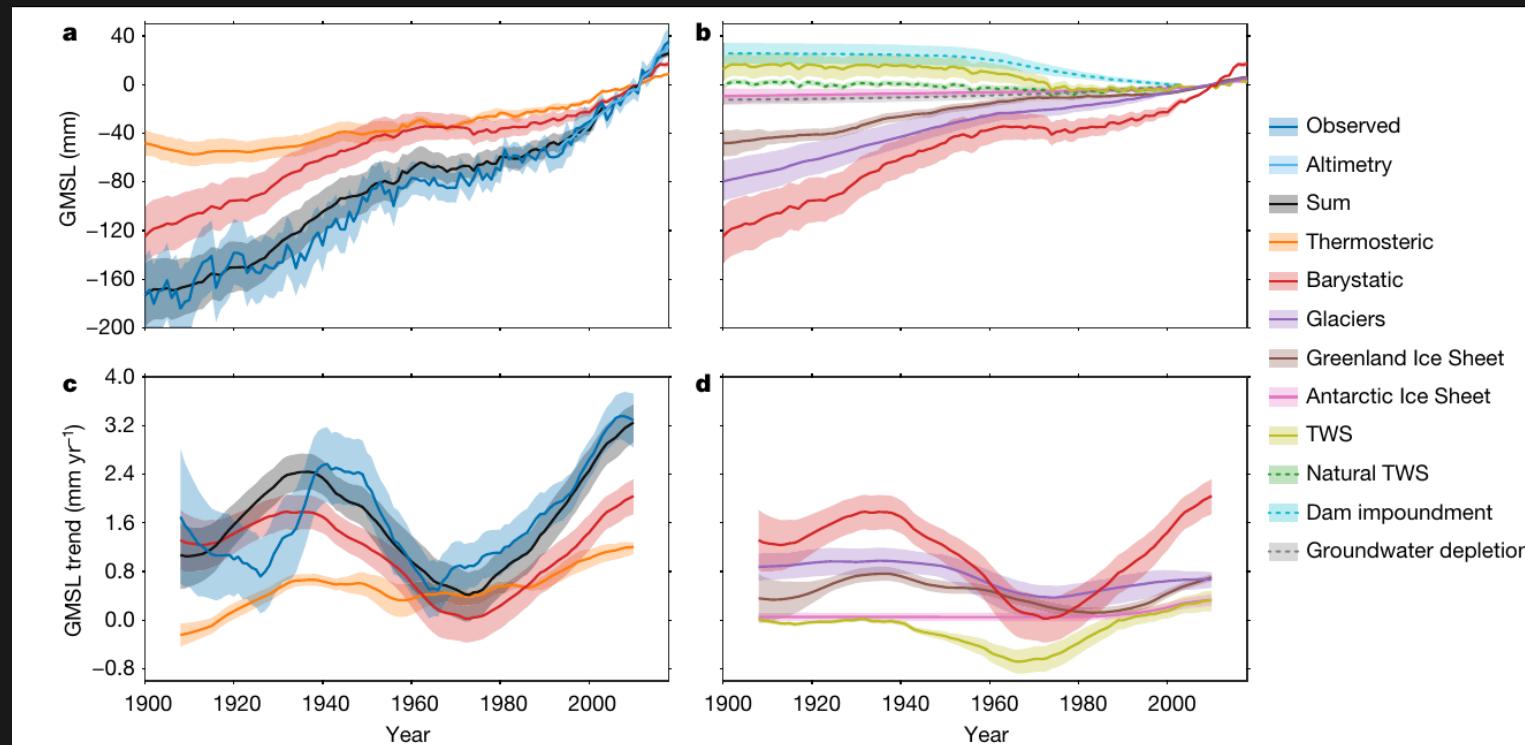


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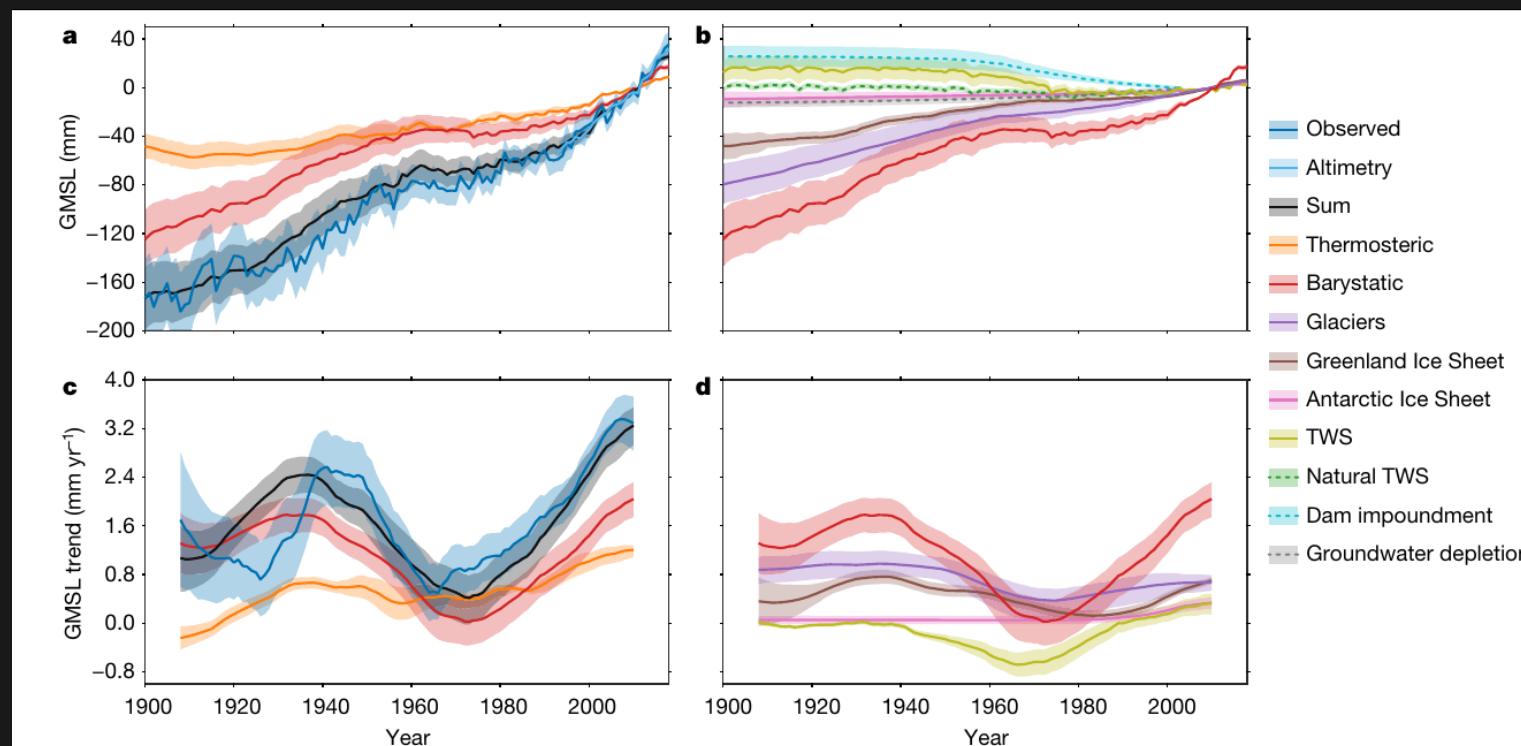


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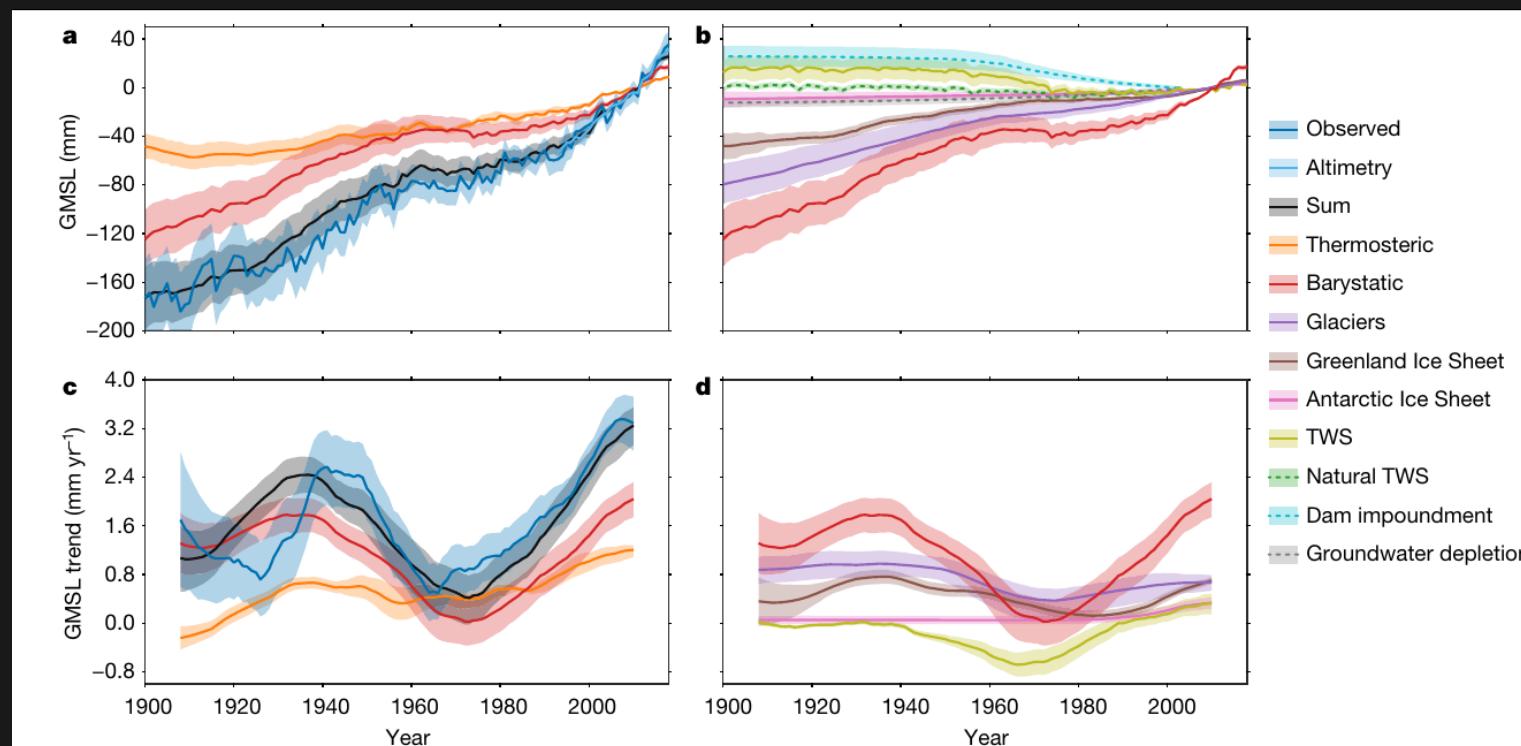


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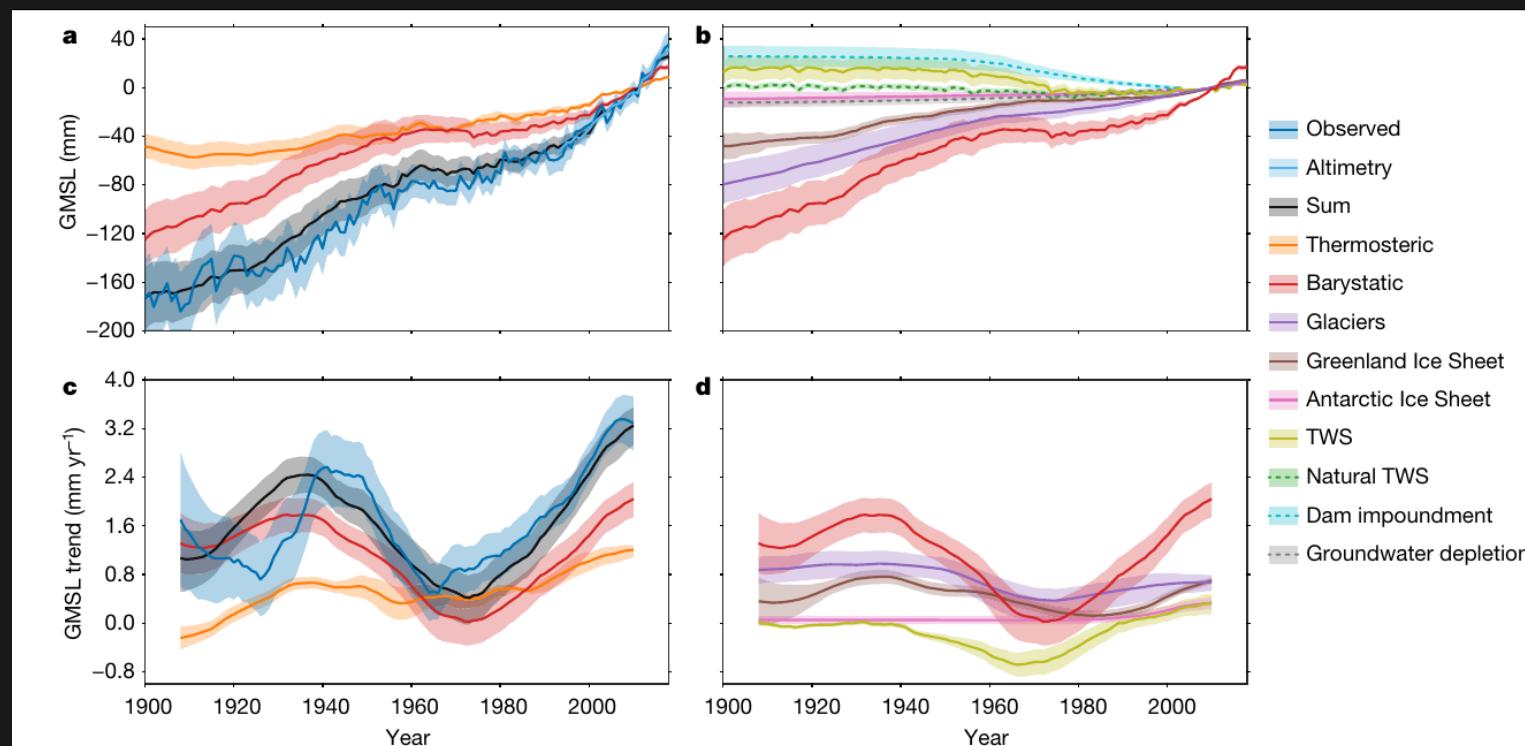


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- Recent accelerations from icesheets and glaciers -> (observable by GRACE since 2002)



# Ocean mass from GRACE (Theory)

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**Methods for inferring regional surface-mass anomalies from Gravity Recovery and Climate Experiment (GRACE) measurements of time-variable gravity**

Sean Swenson and John Wahr

Department of Physics and Cooperative Institute for Research in Environmental Sciences, University of Colorado, Boulder, USA

Received 8 May 2001; revised 9 March 2002; accepted 14 March 2002; published 19 September 2002.

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$$\widetilde{\Delta\sigma}_{\text{region}} = \sum_{l,m} \frac{K_l}{\Omega_{\text{region}}} (W_{lm}^c \Delta C_{lm} + W_{lm}^s \Delta S_{lm}). \quad (27)$$



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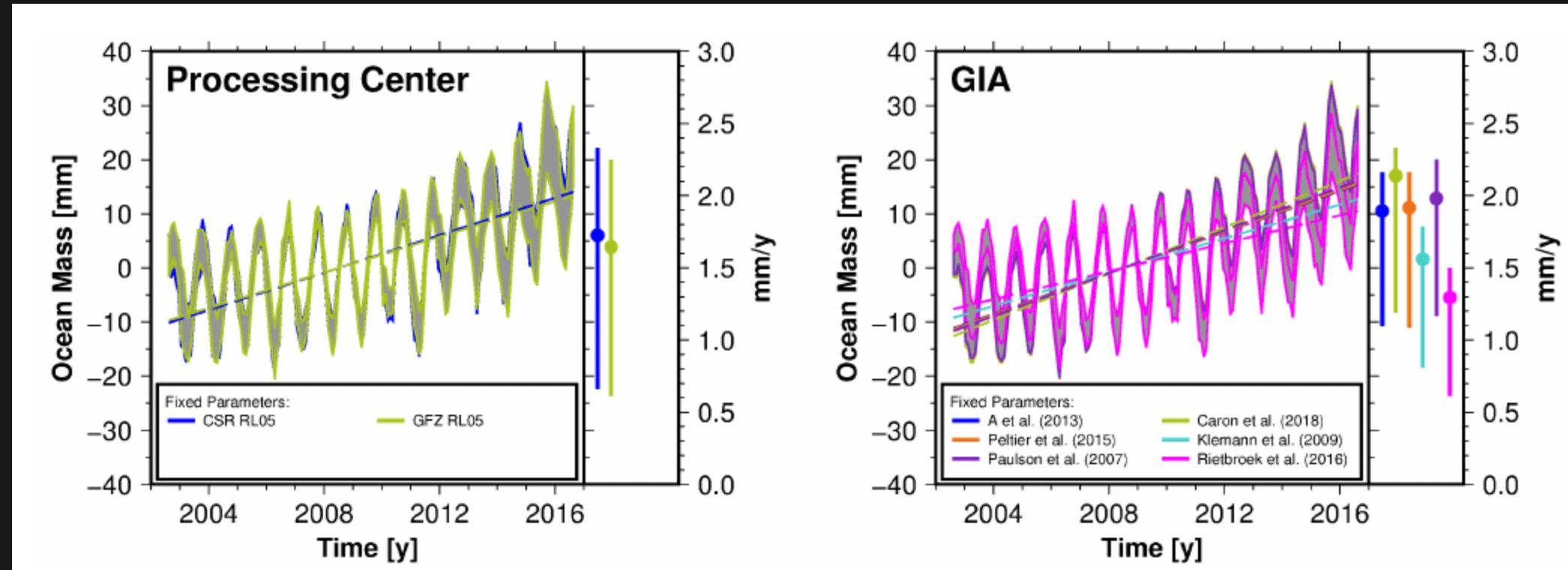
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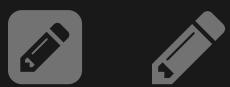
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  - dot product of smoothed basin coefficients with GRACE-TWS coefficients



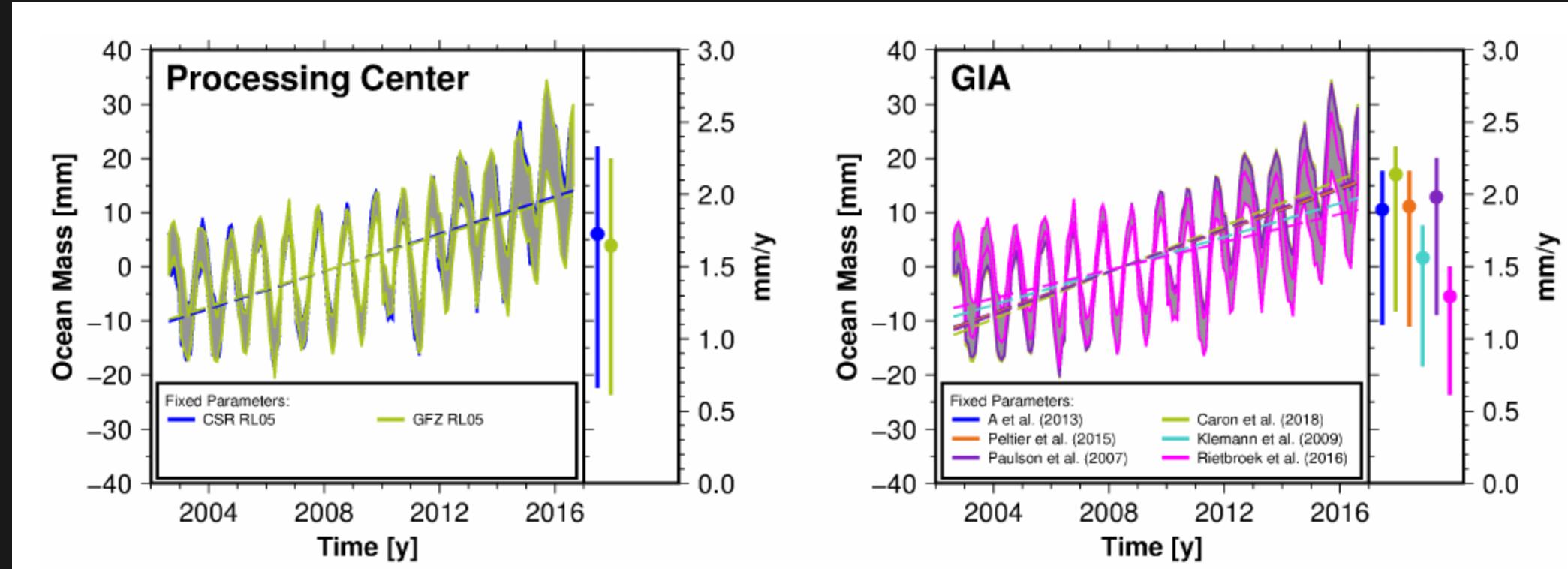
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Effect of different processing choices on ocean mass estimates, from Uebbing et al. 2019

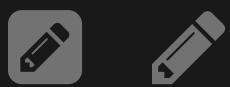


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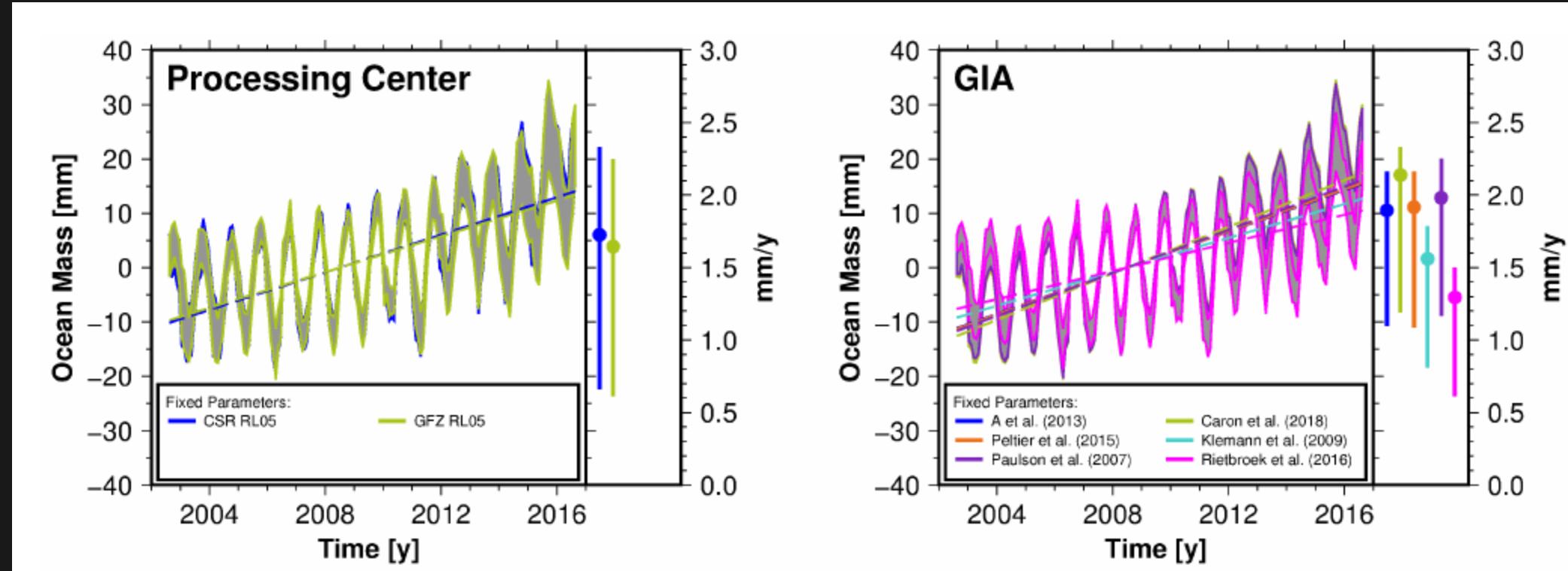


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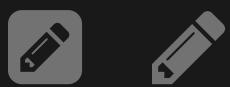


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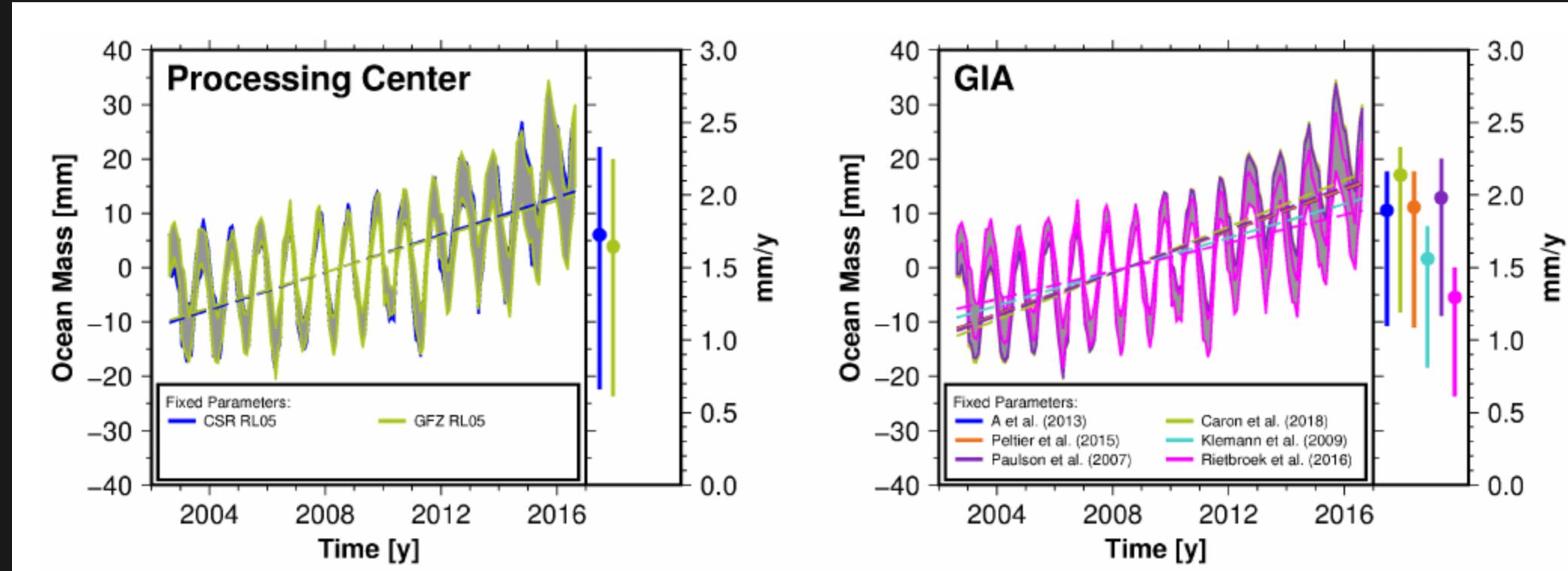


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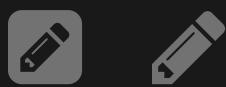


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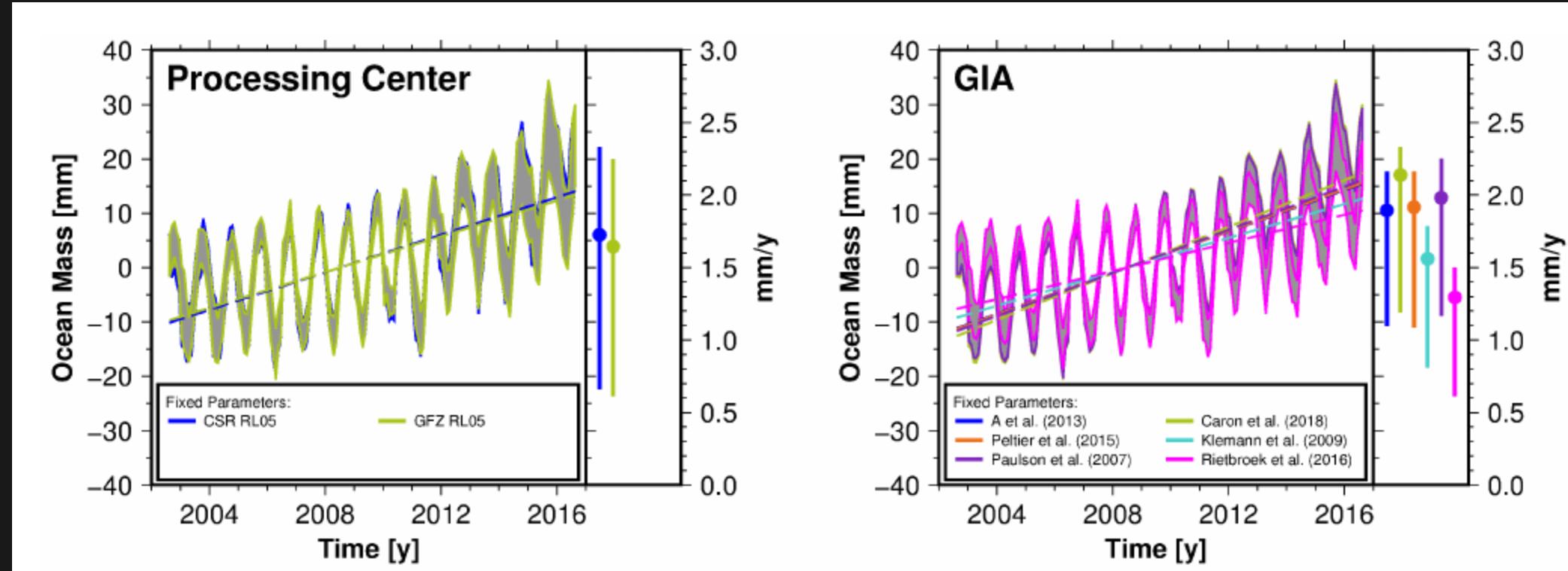


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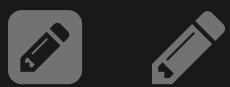


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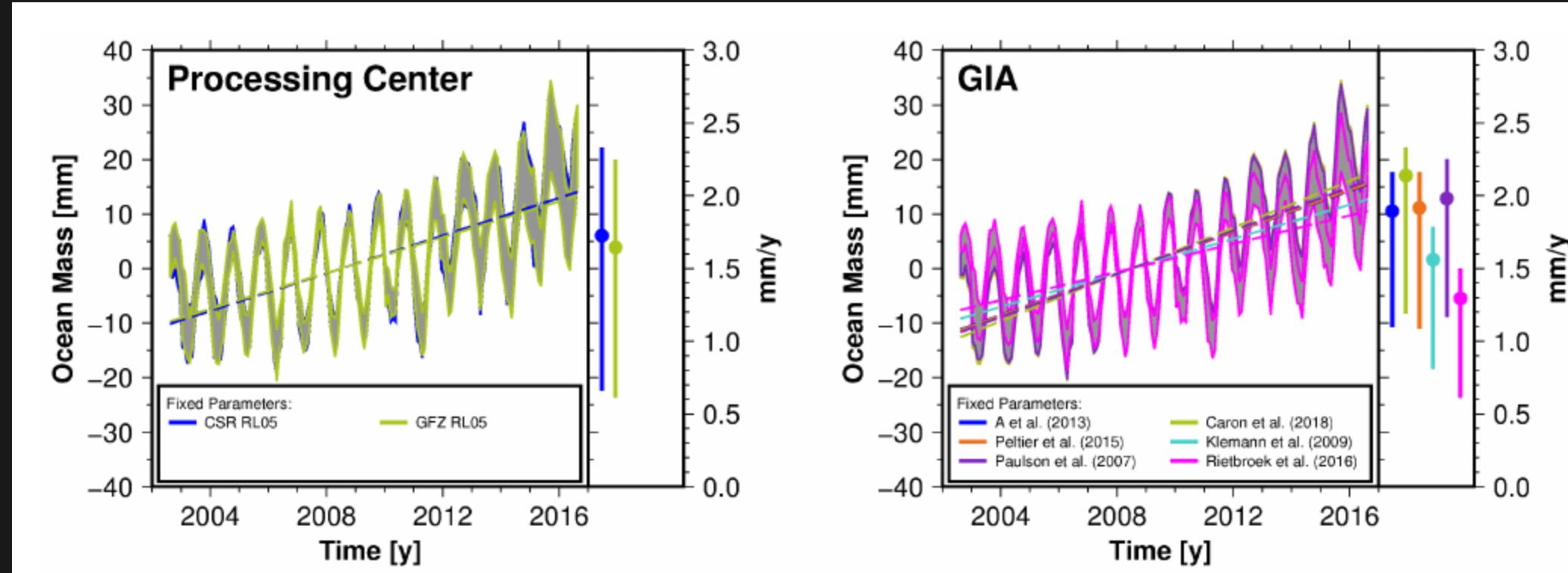


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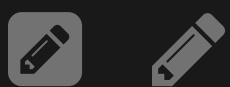


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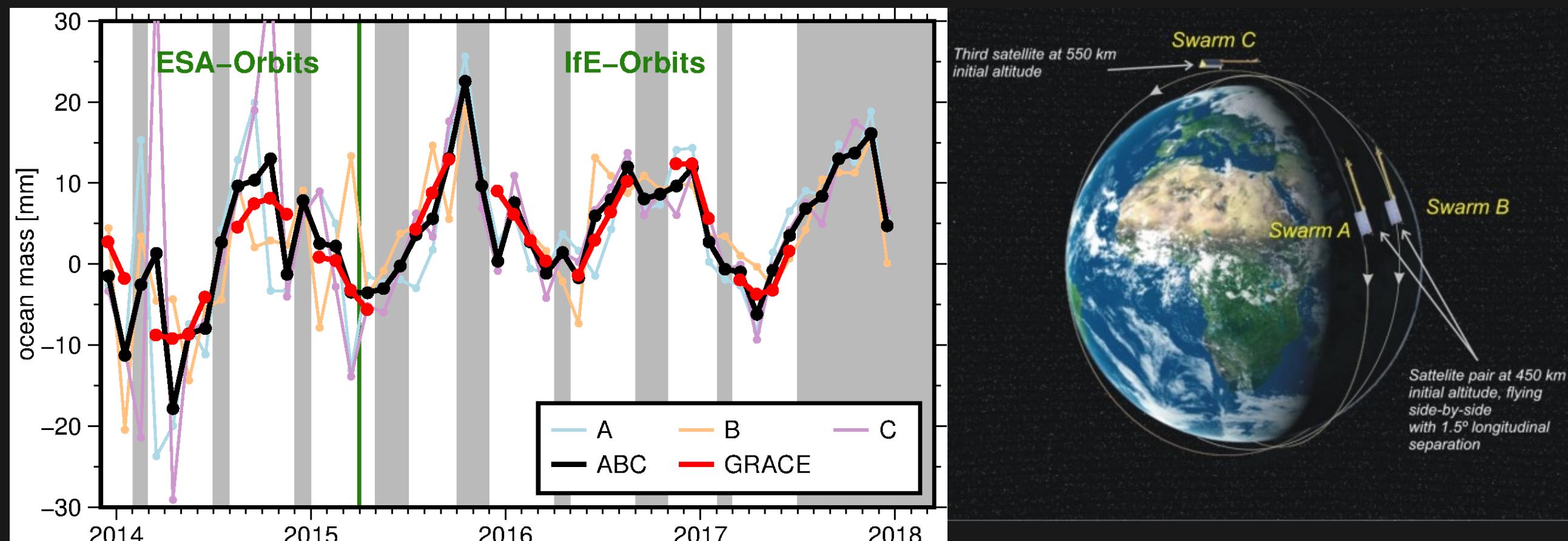


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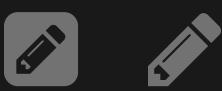
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  - Current mass trends  $\sim$ 1.5-2mm/yr (c.f. total trend  $\sim$ 3.3 mm/yr)



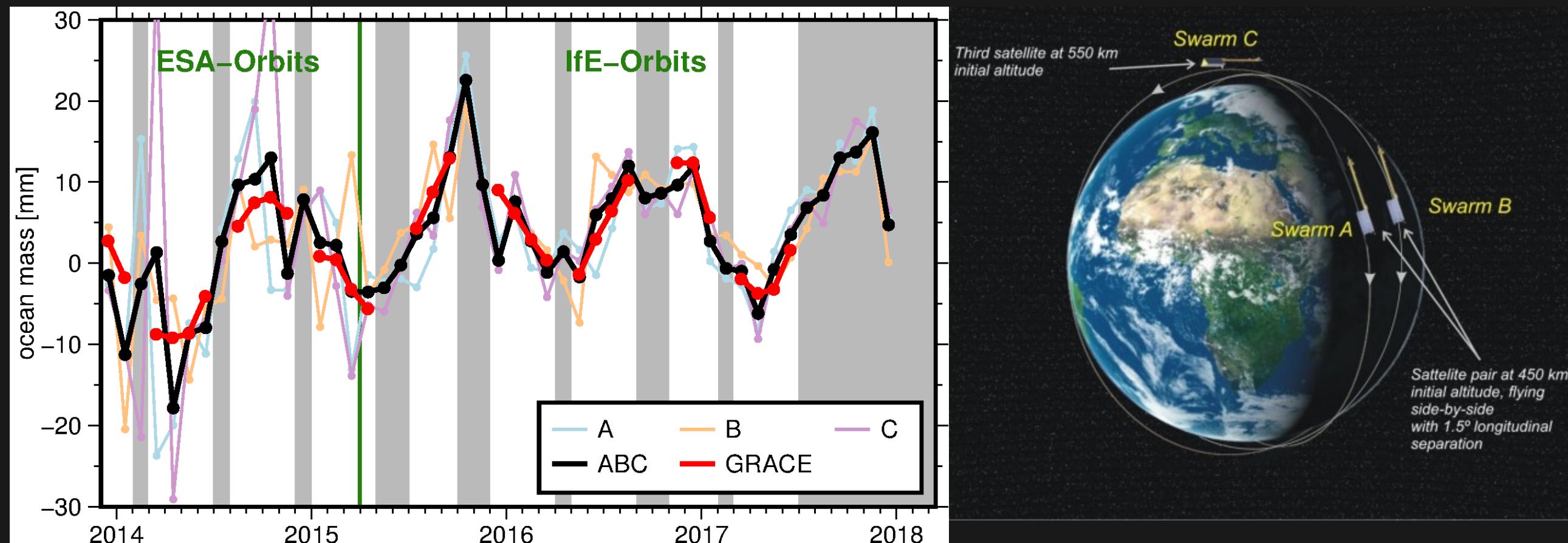
# Ocean mass from the SWARM Mission



Comparison of ocean mass from GRACE and the SWARM (A,B,C satellites). Update of Luck et al. 2018

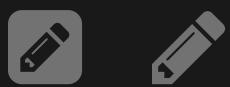


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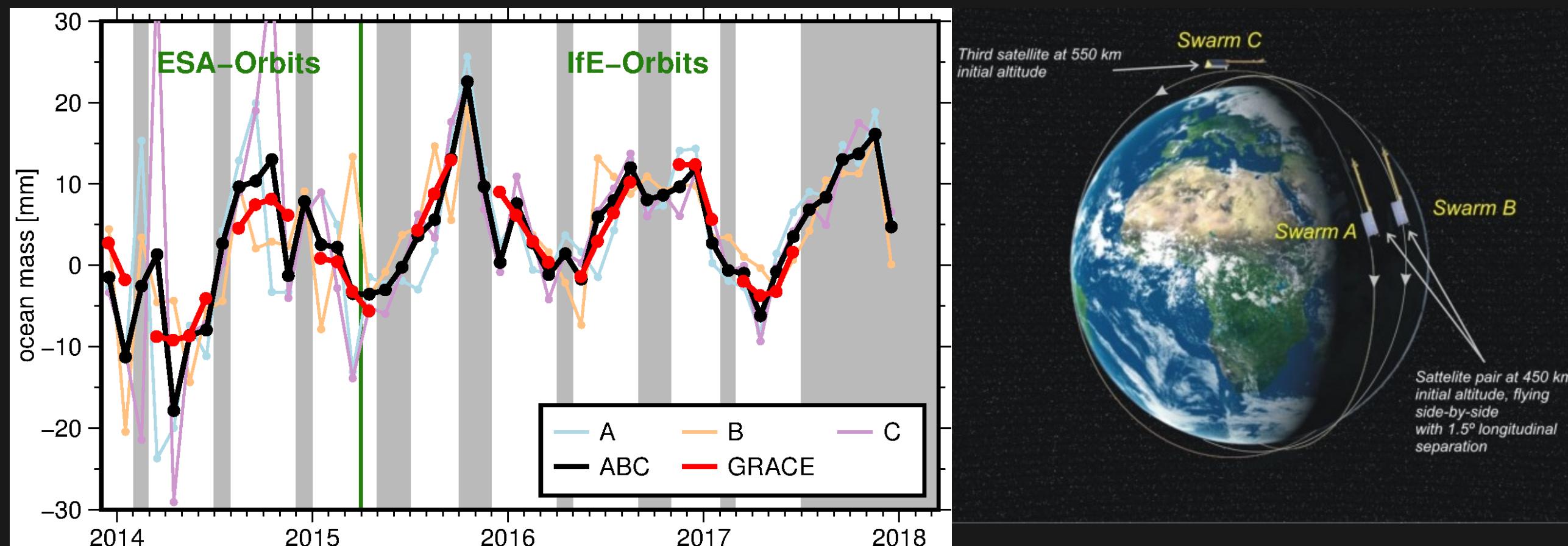


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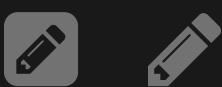


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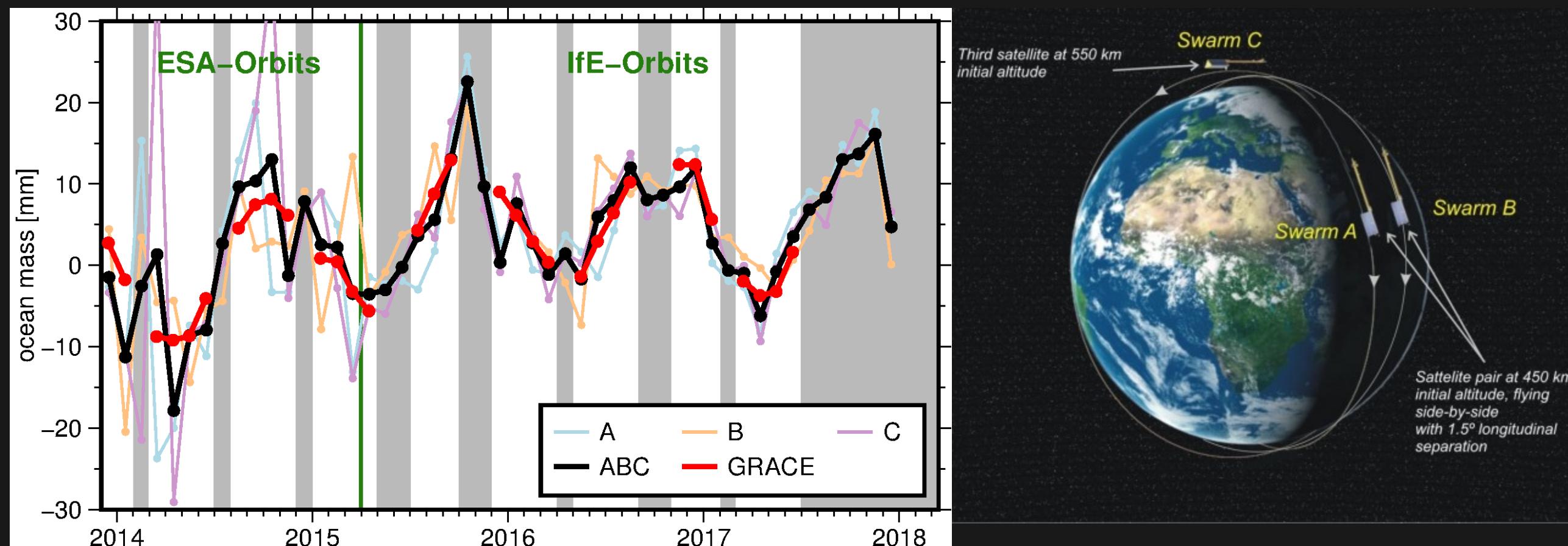


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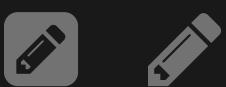


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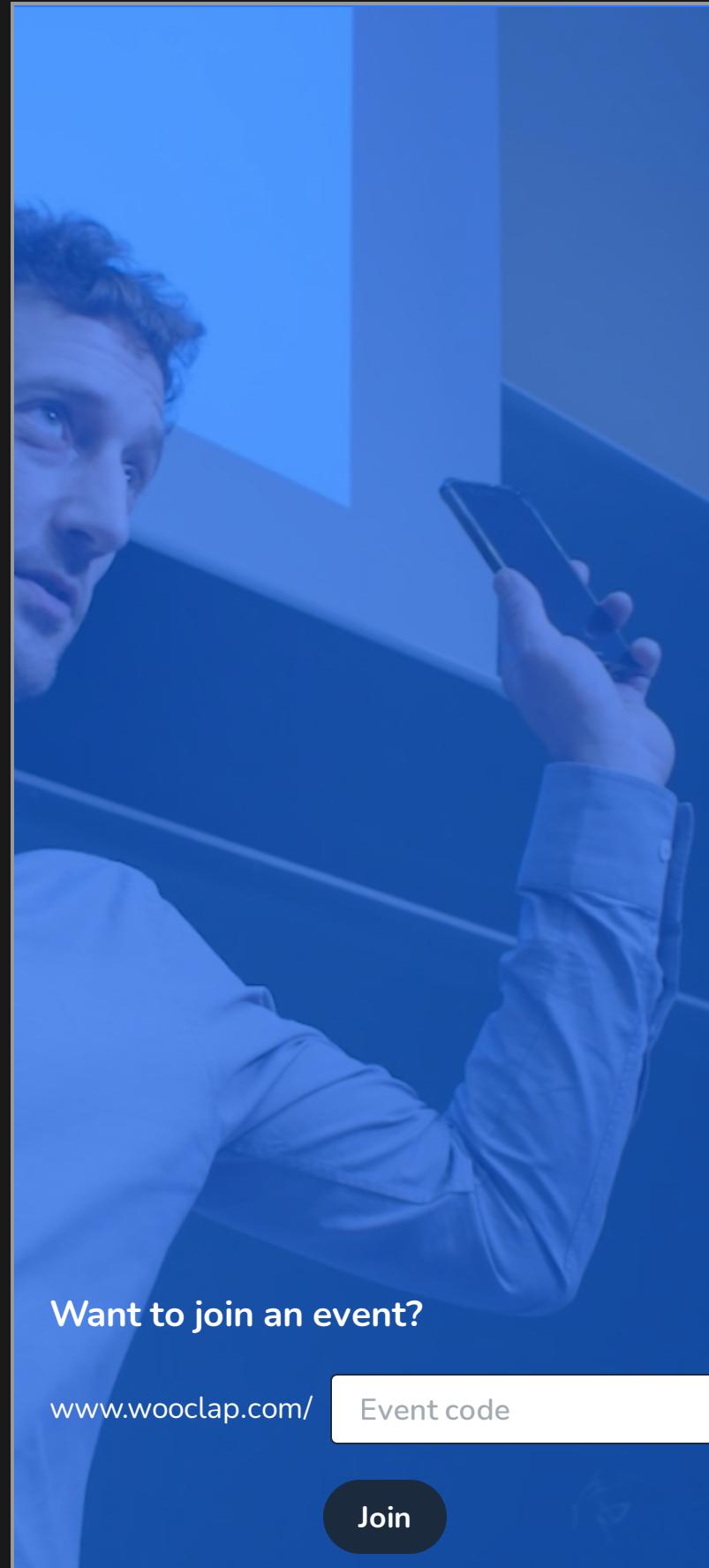


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- Precise (kinematic) orbits contain information on low-resolution gravity changes -> ocean scales
- Principle is useful for filling gaps and potentially pre-GRACE era



# Does Greenland induce regional sea level changes?



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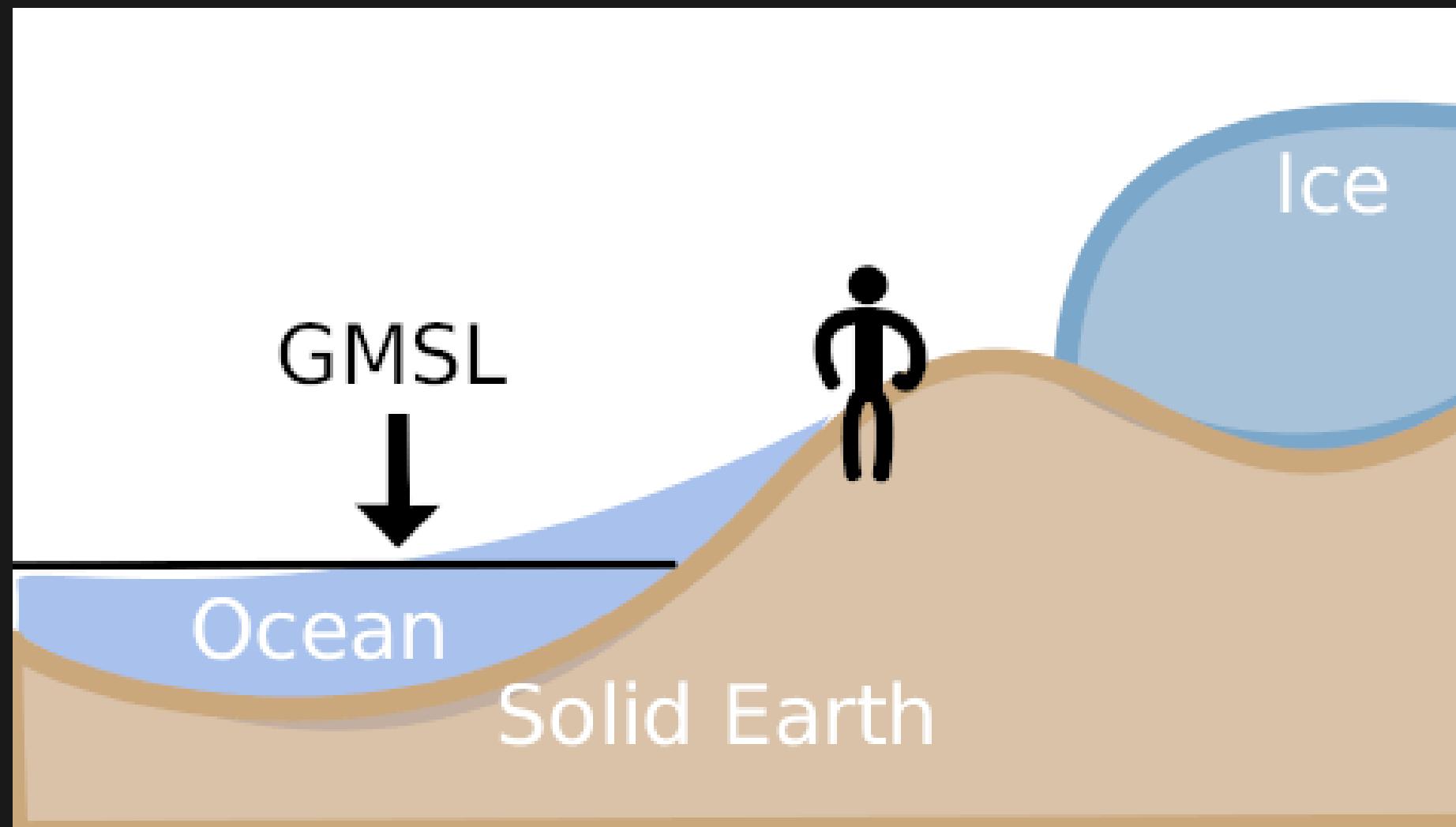
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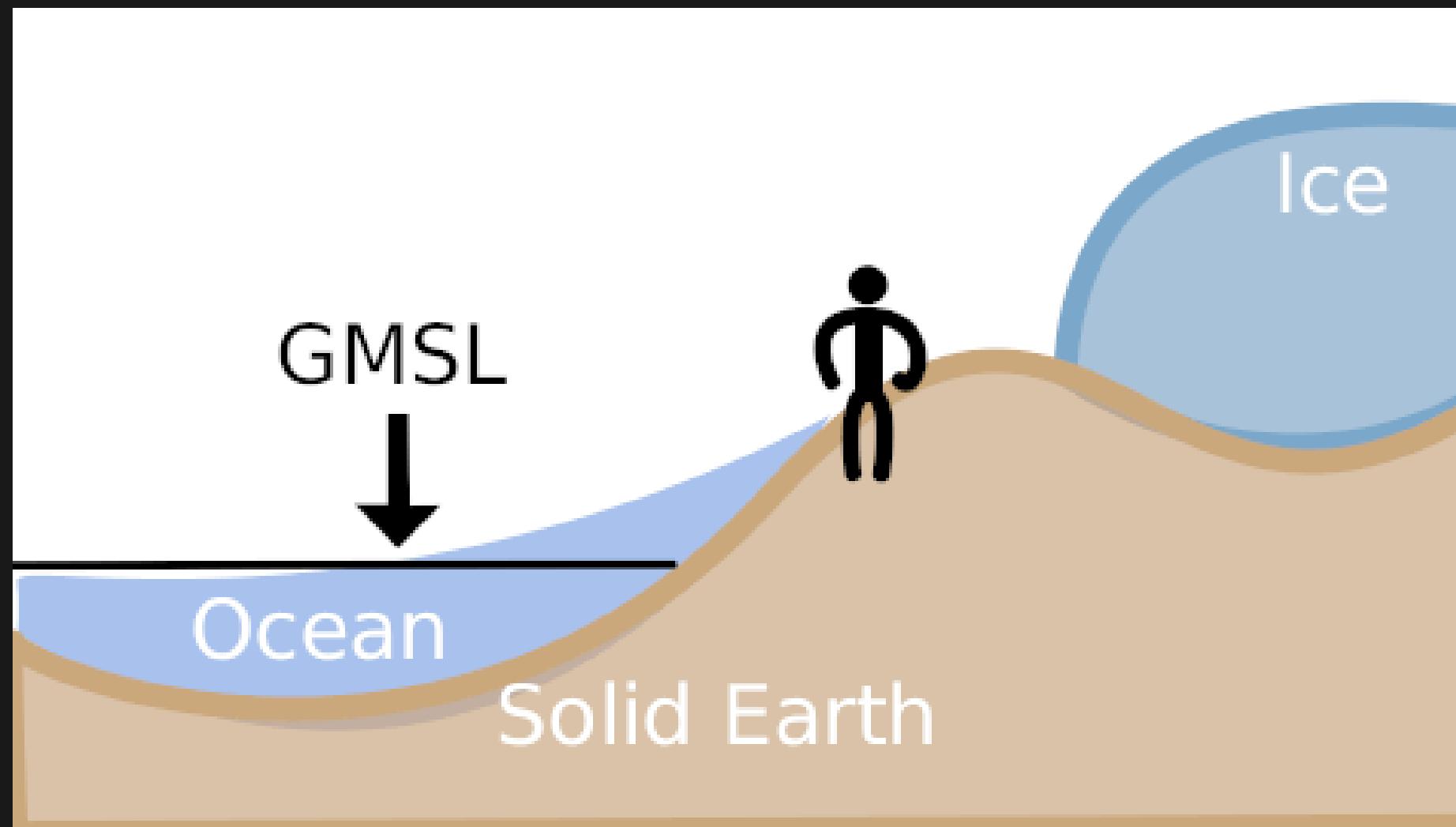
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Relative sea level is affected by self attraction and loading (SAL)..

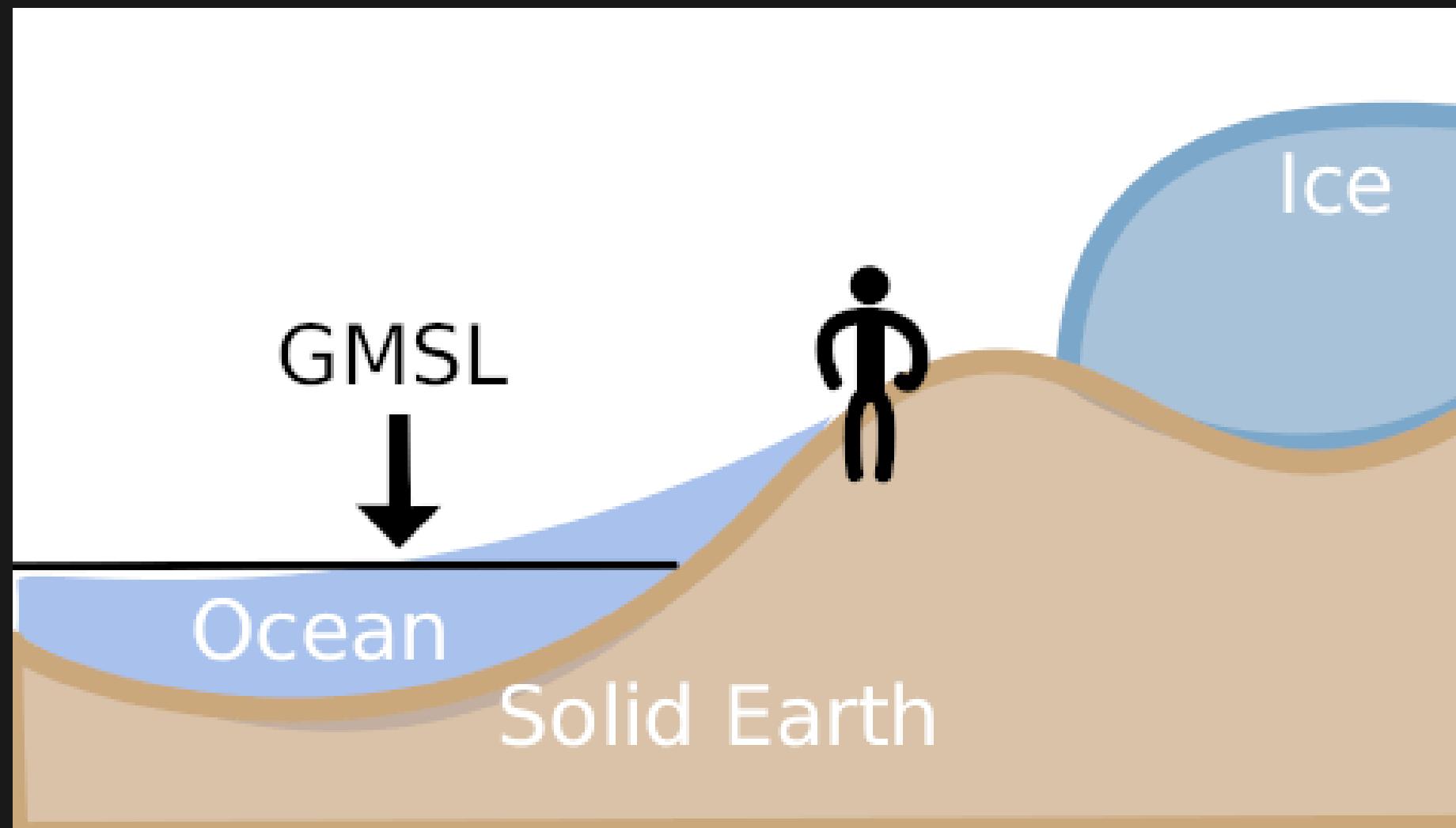


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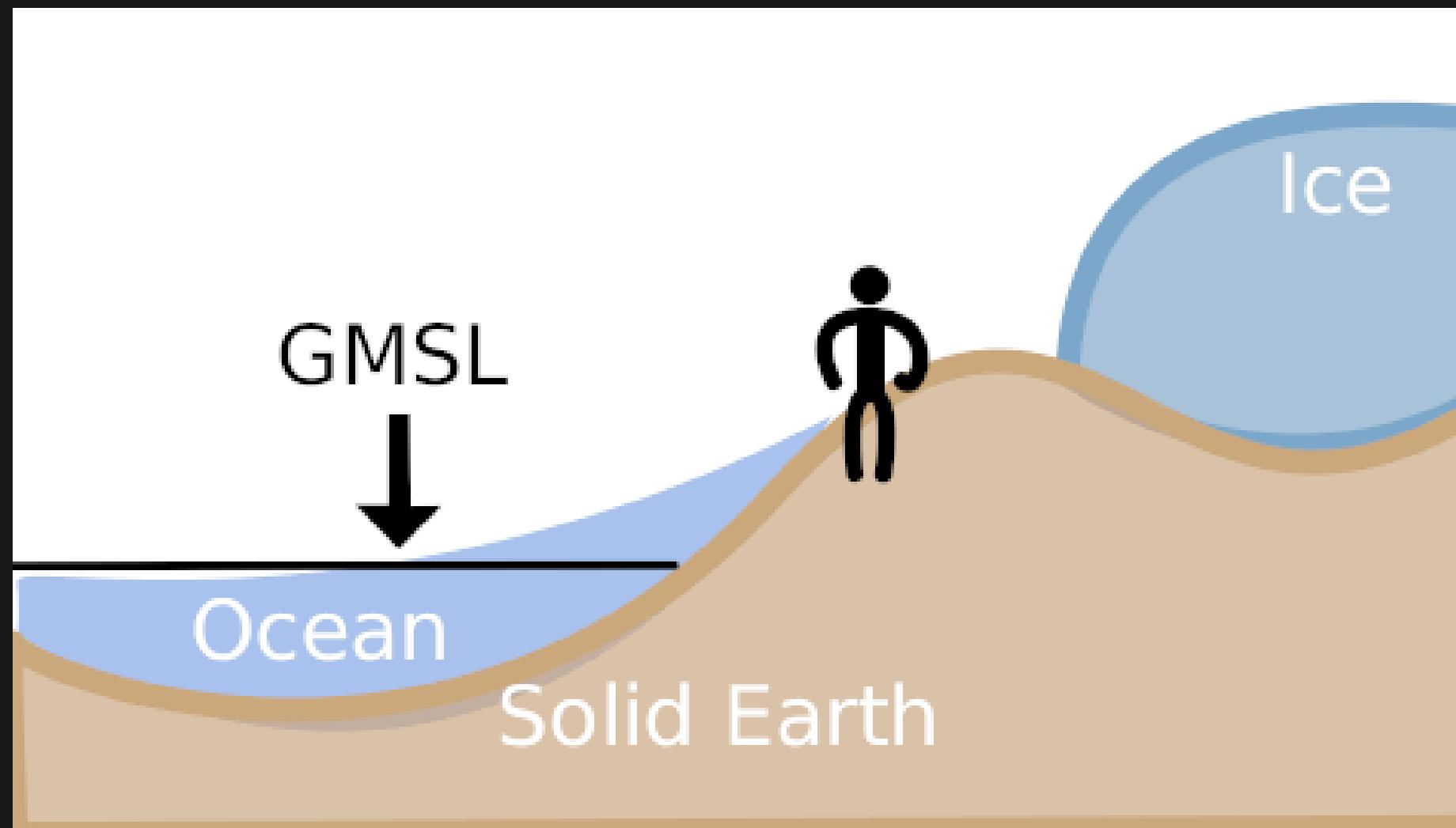
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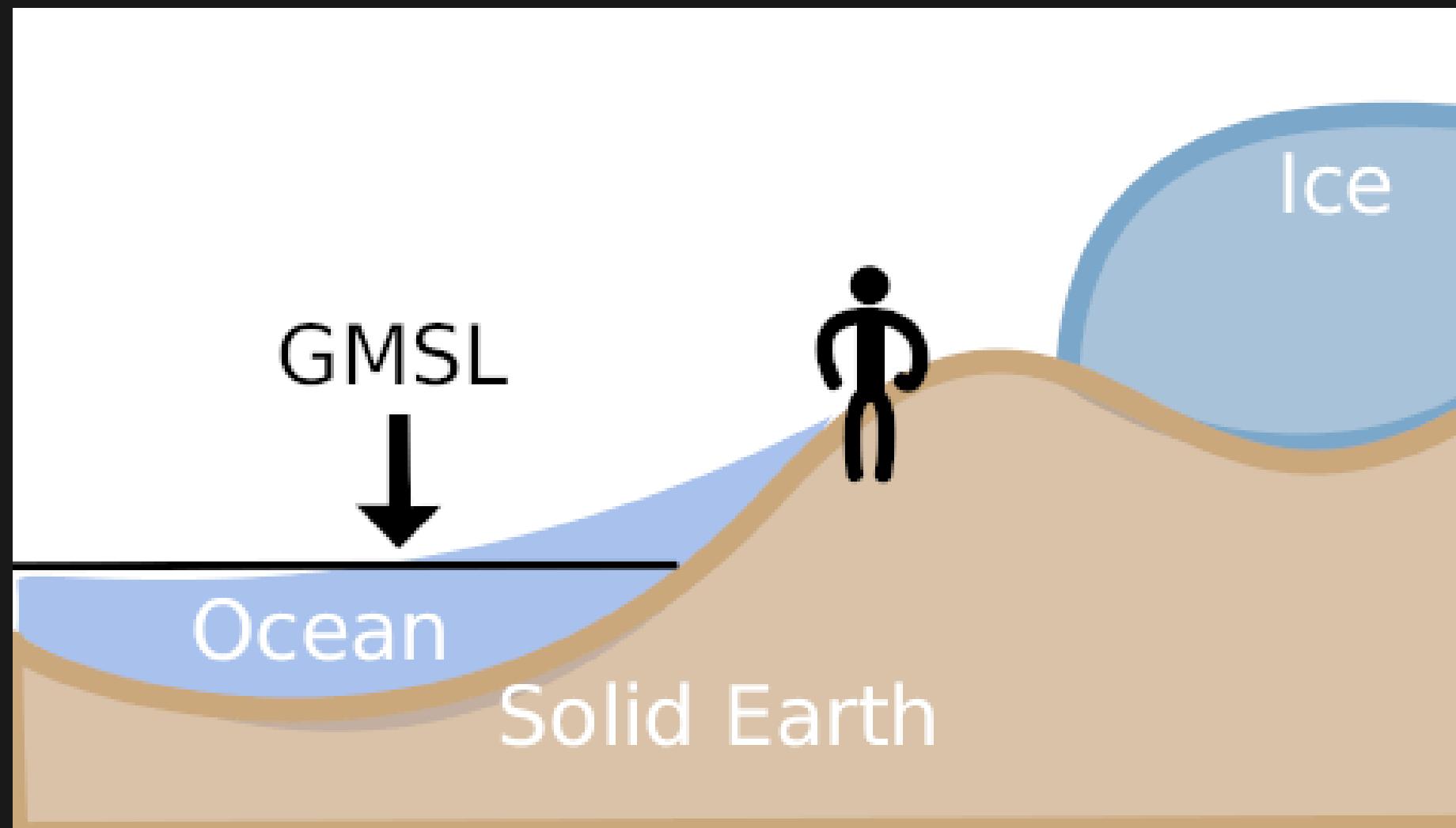
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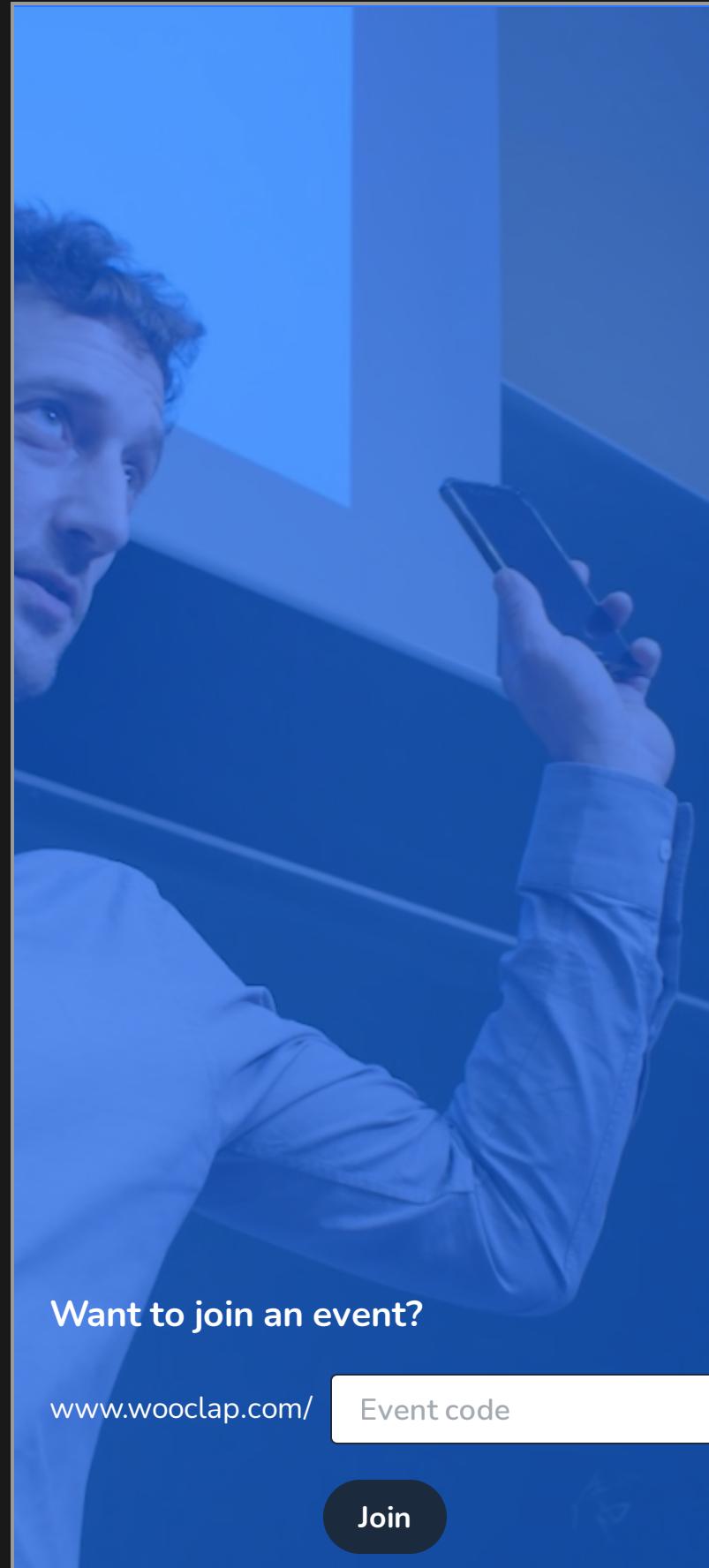
- Theory goes back to 1888 (Woodward)
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- mass conserving

# Relative sea level is affected by self attraction and loading (SAL)..



- Theory goes back to 1888 (Woodward)
- Modelled as a passive ocean response (no currents)
- mass conserving
- Takes into account the deformation of the Earth

# Other factors affecting relative sea level?



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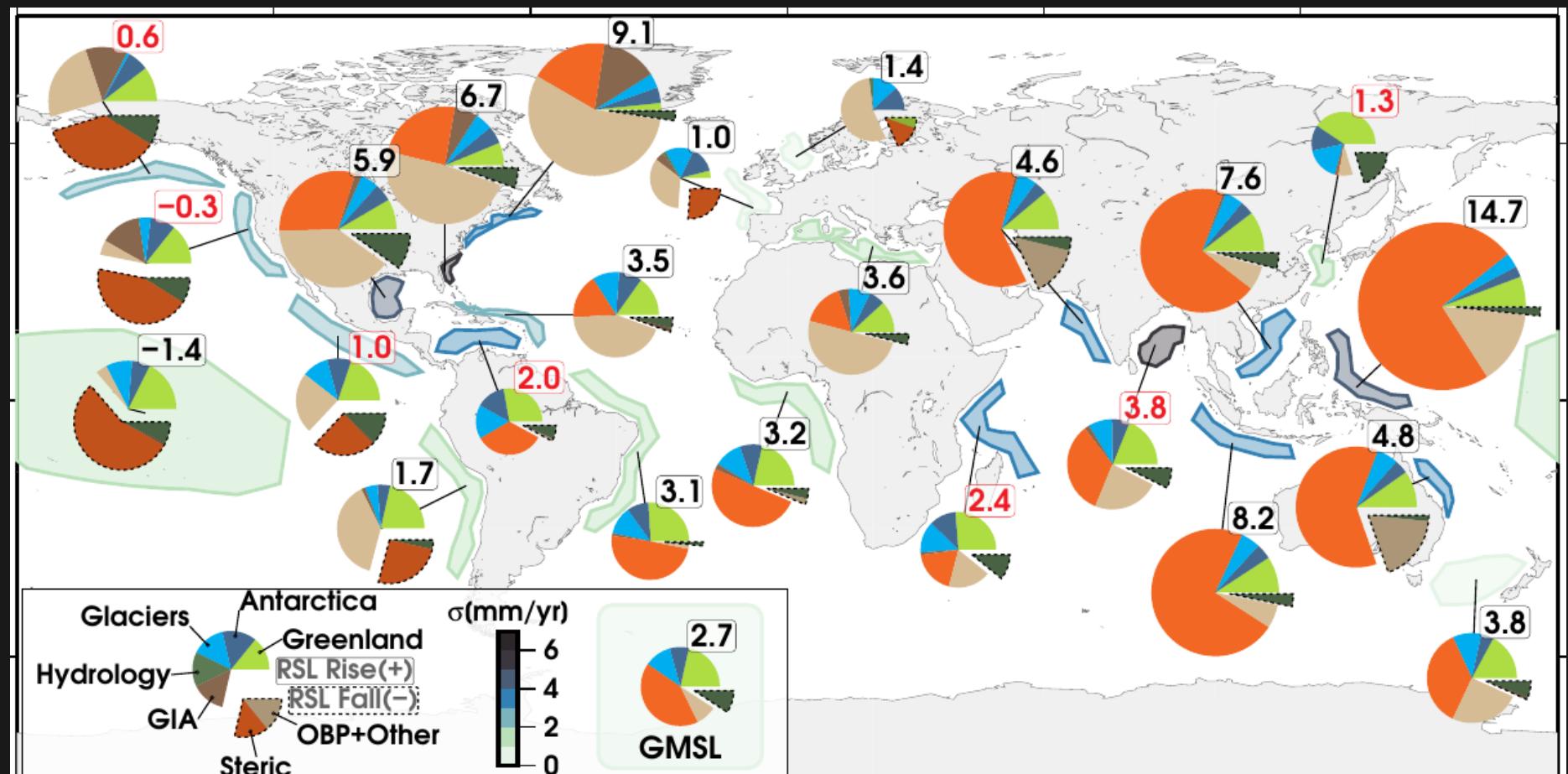
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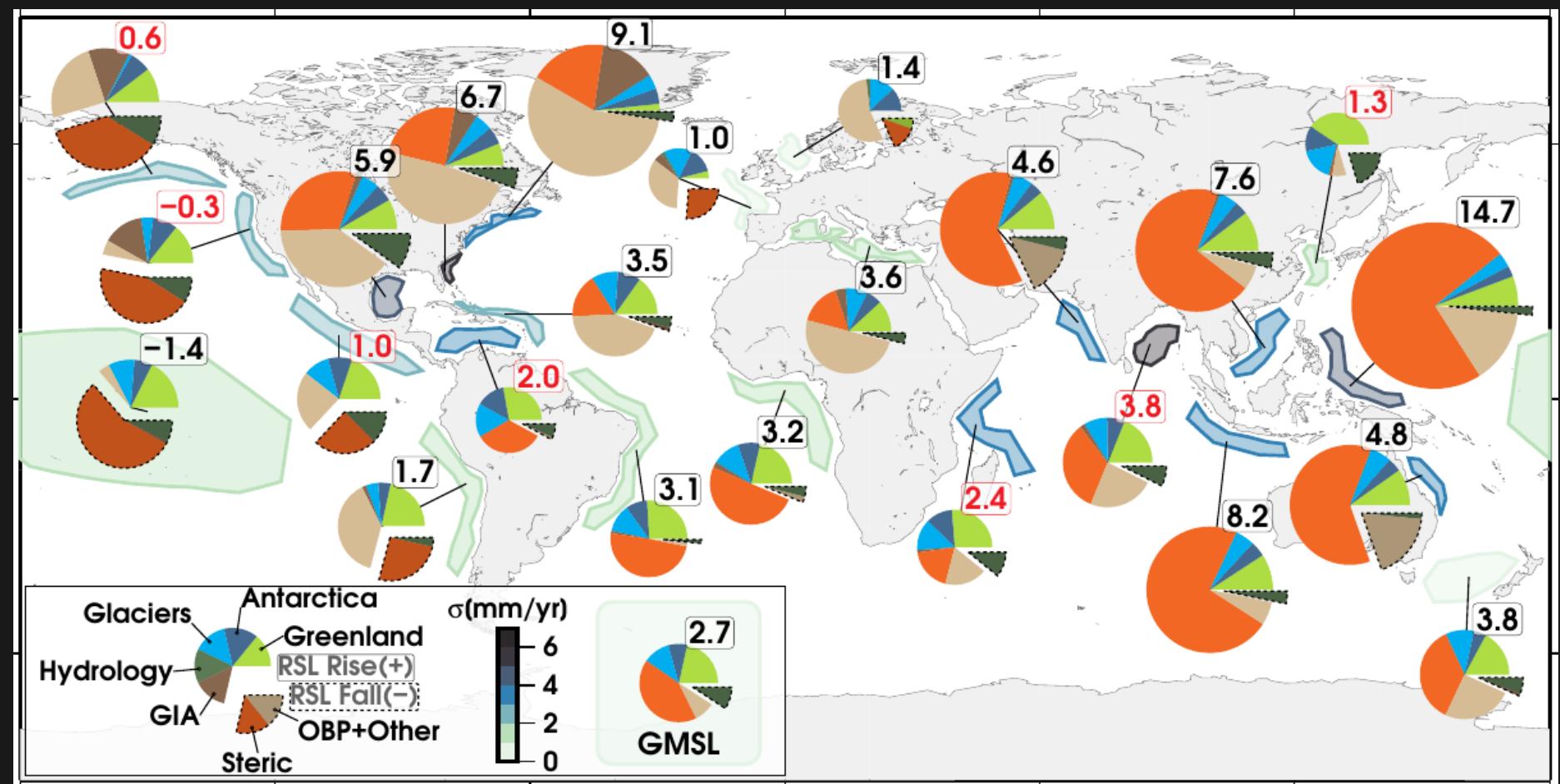
# Regional sea level budgets



Regional sea level budgets from Rietbroek et al. 2016

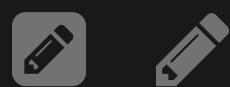


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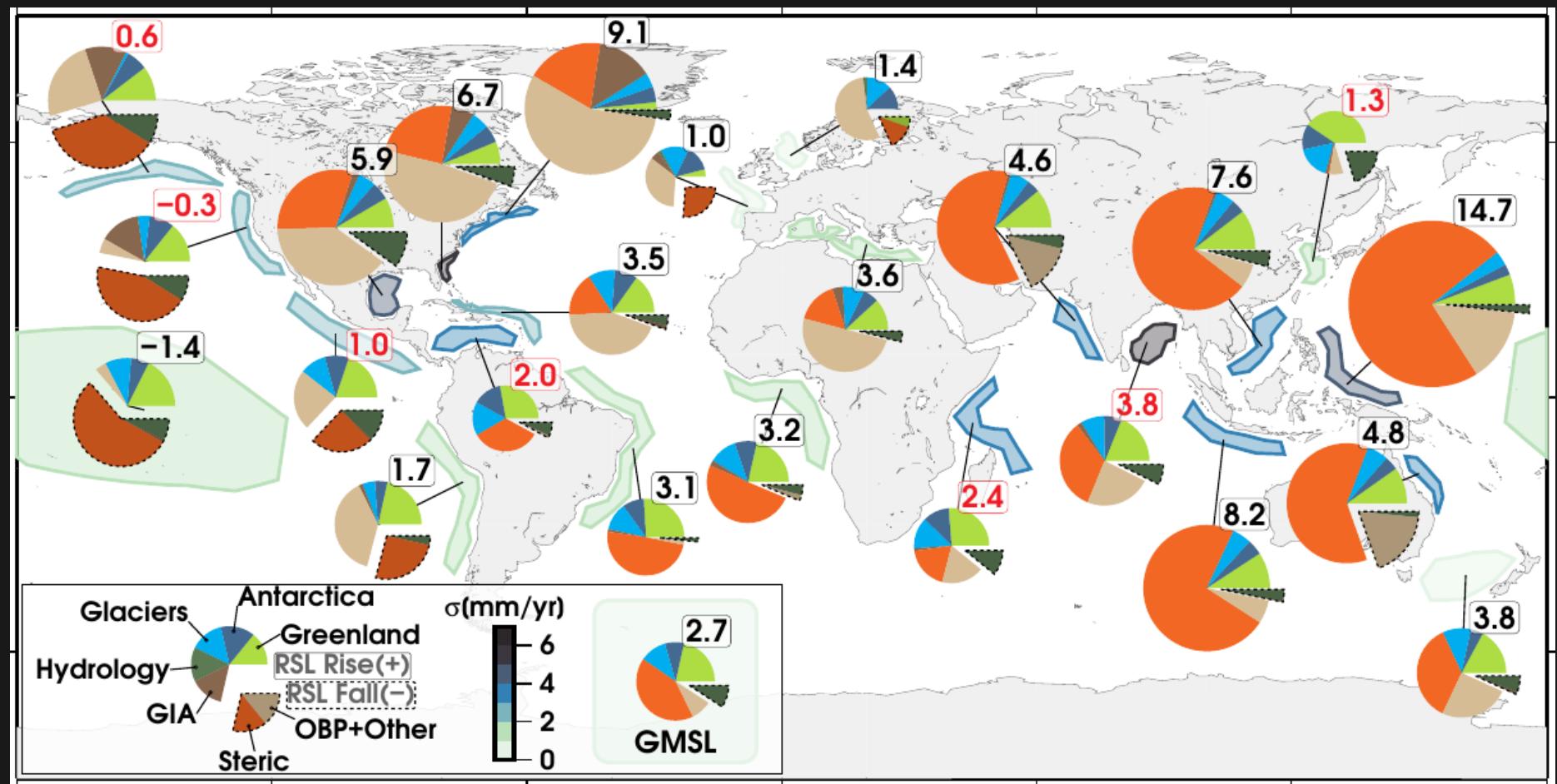


Regional sea level budgets from Rietbroek et al. 2016

- Sea level rise is not uniform

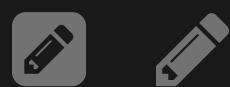


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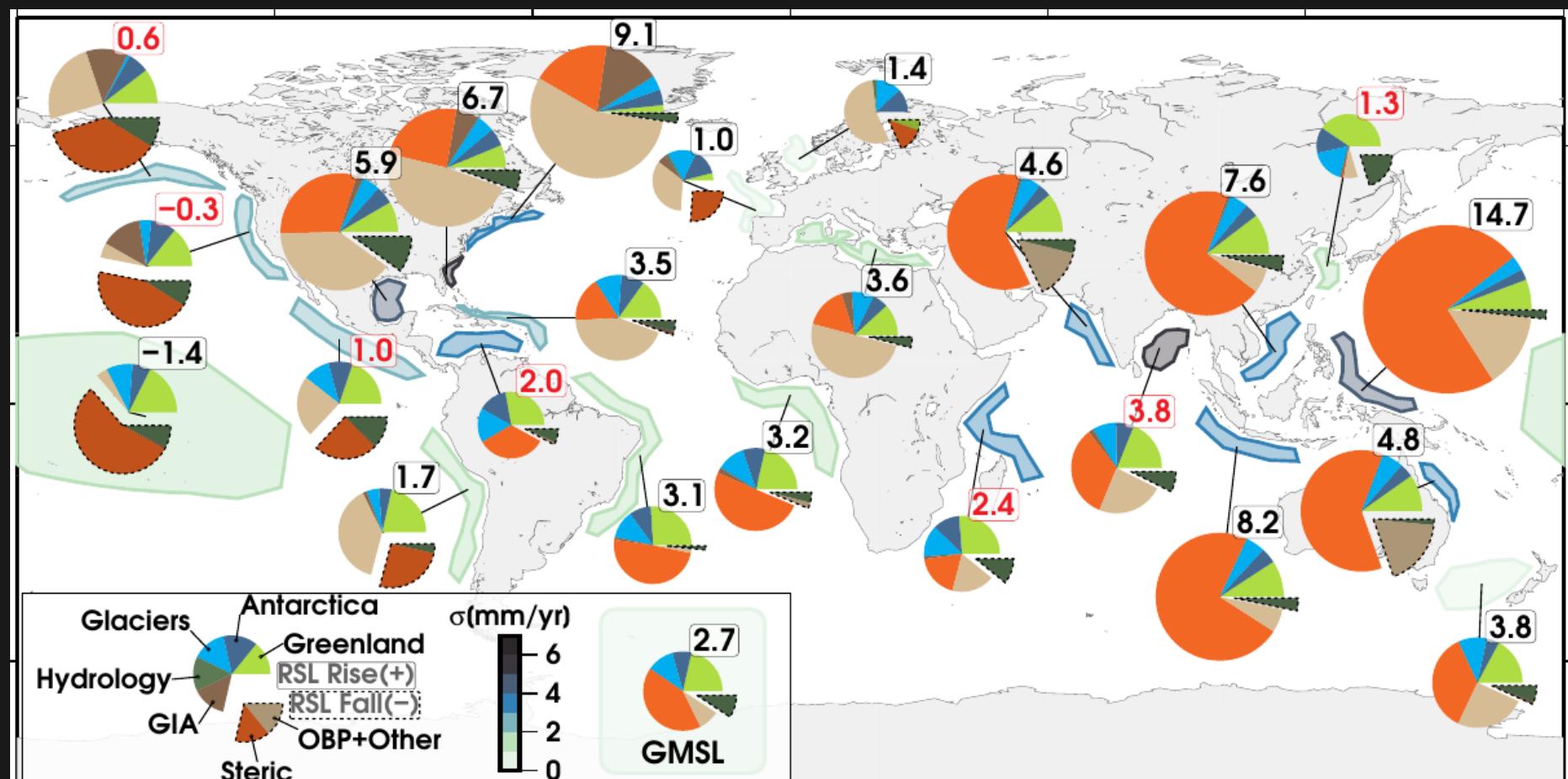


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- Sea level rise is not uniform
- SAL effects

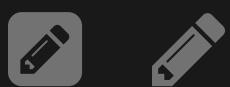


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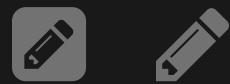
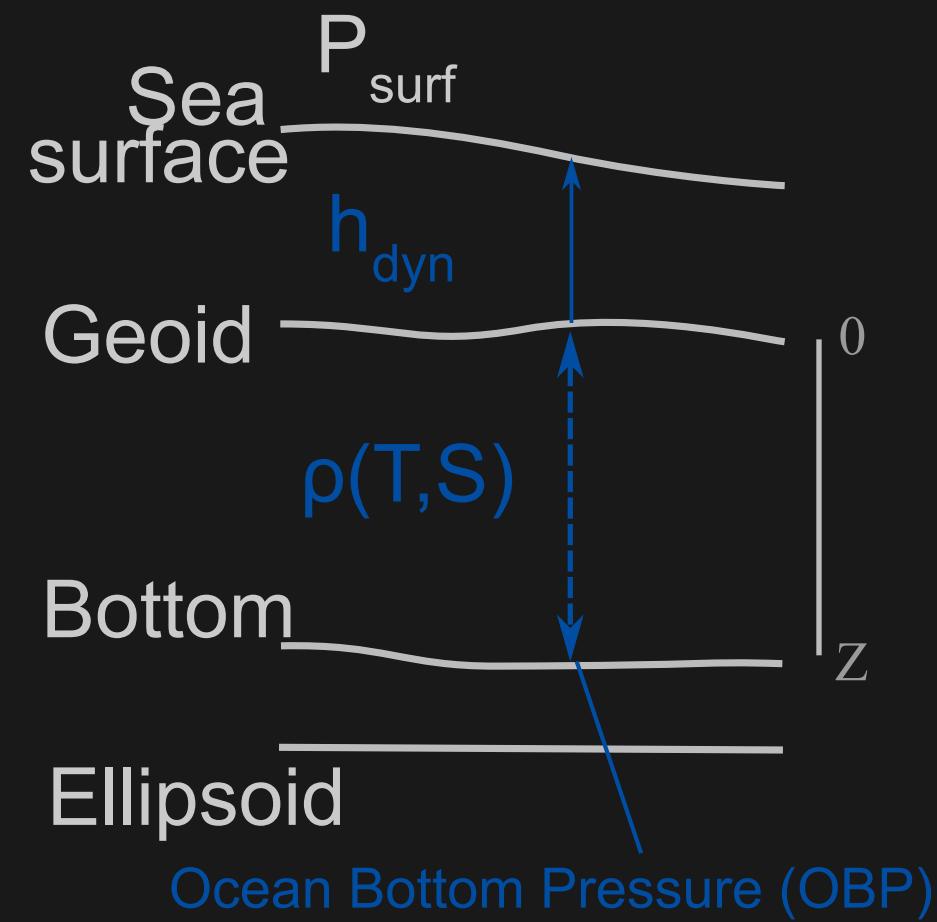
- Sea level rise is not uniform
- SAL effects
- Thermosteric and ocean bottom pressure changes play a larger role in the regional budgets



# Churning the ocean (forcing from wind stress, density contrasts)

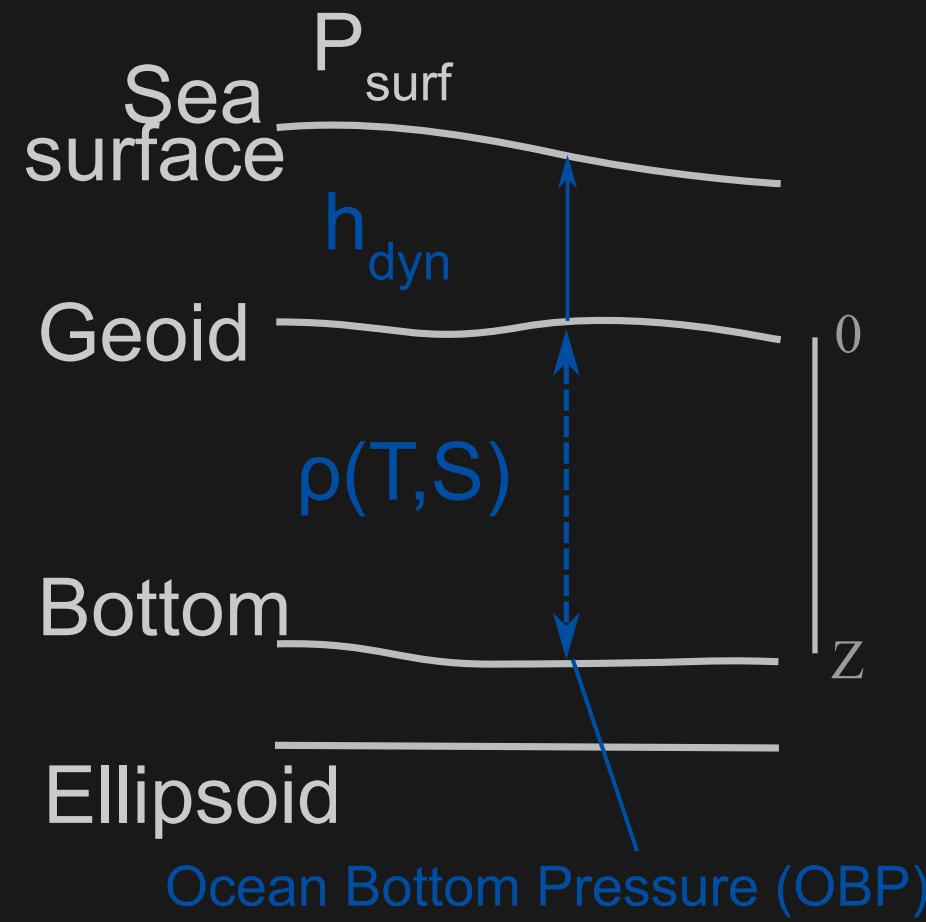


# Integrating the water column to obtain ocean bottom pressure

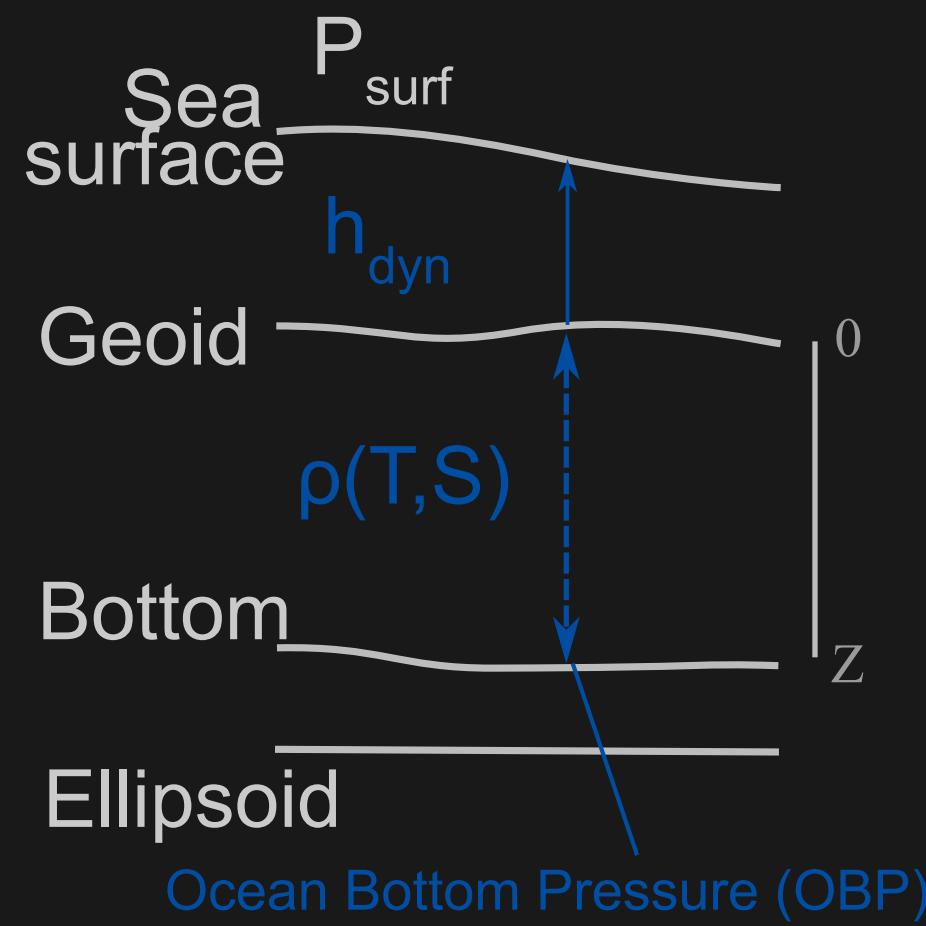


# Integrating the water column to obtain ocean bottom pressure

$$P_{OBP} = P_{surf} + g \int_{-Z}^0 \rho(z) dz \\ + g\rho_{sea} h_{dyn}$$



# Integrating the water column to obtain ocean bottom pressure

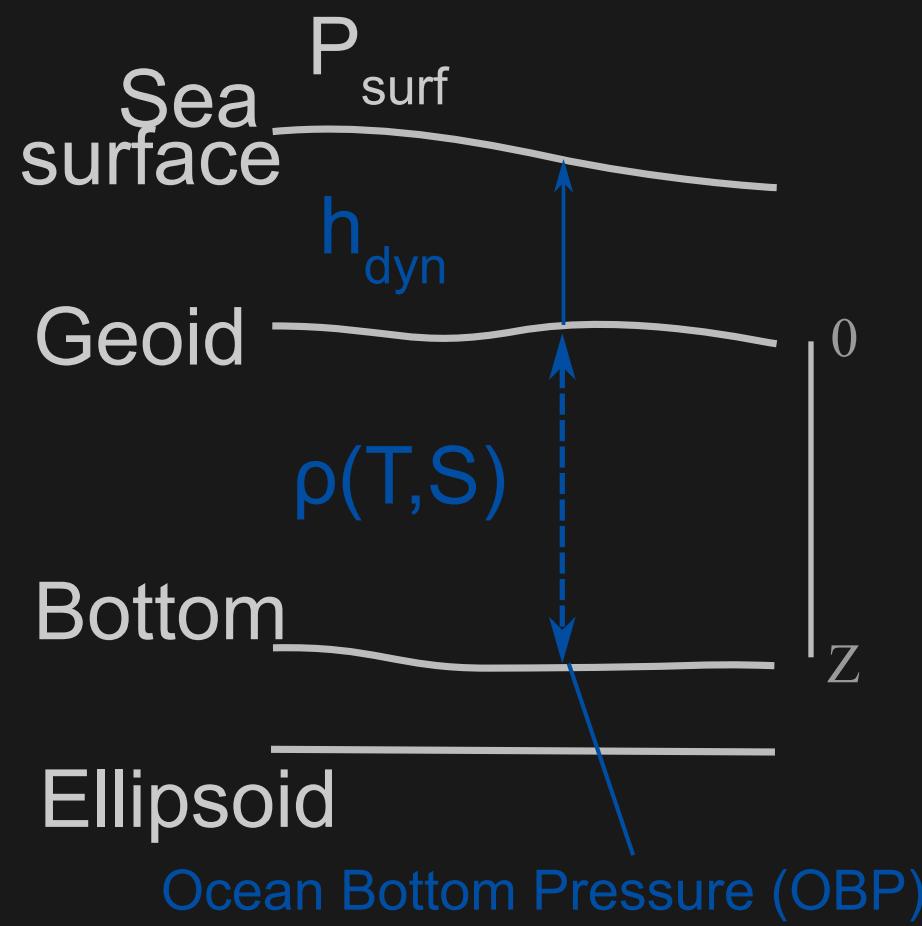


$$P_{OBP} = P_{surf} + g \int_{-Z}^0 \rho(z) dz + g \rho_{sea} h_{dyn}$$

No OBP change  $\rightarrow$  Steric change ( $h_{dyn} = h_{ster}$ )

$$0 = g \int_{-Z}^0 \delta \rho(z, T, S) dz + g \rho_{sea} h_{ster}$$

# Integrating the water column to obtain ocean bottom pressure



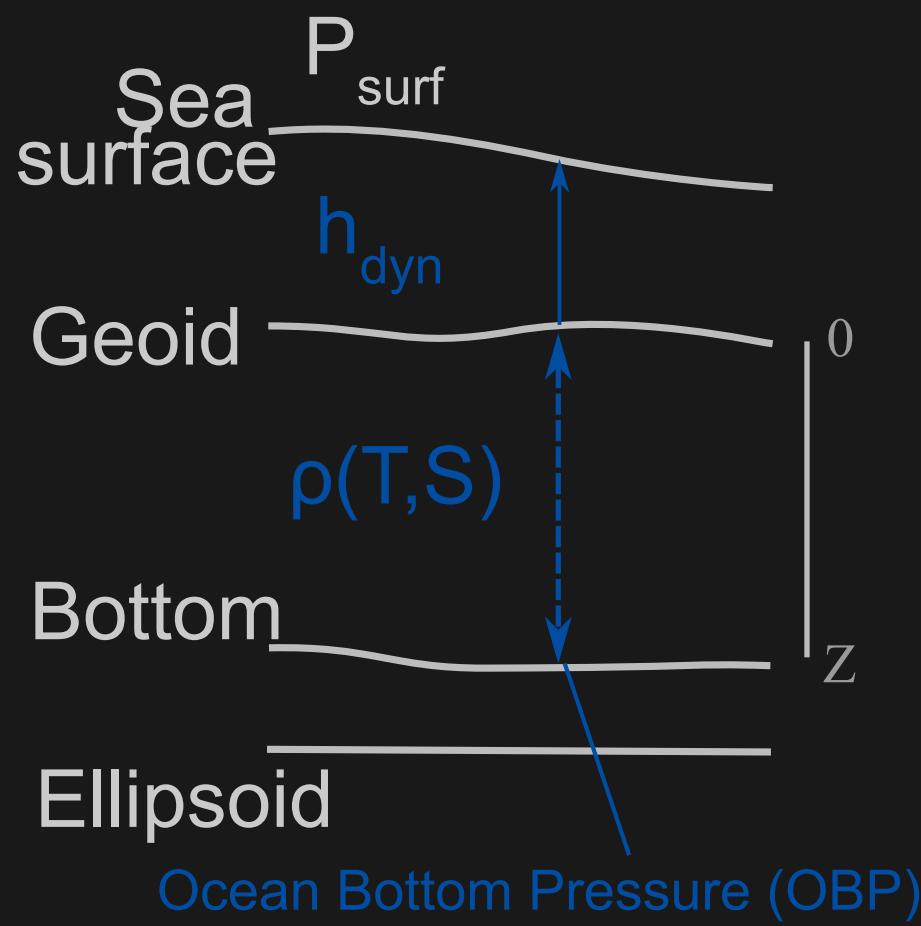
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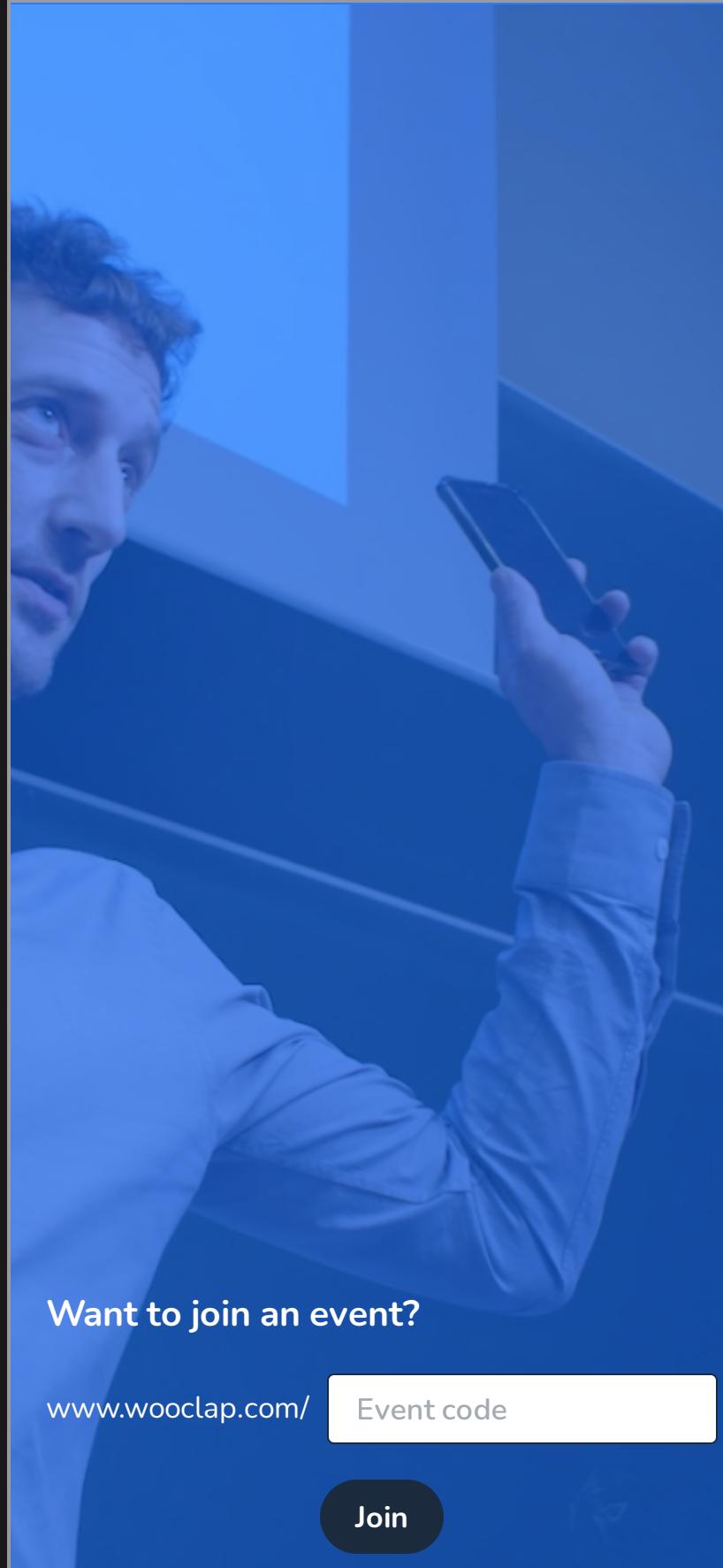
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$$h_{ster} = -\frac{1}{\rho_{sea}} \int_{-Z}^0 \delta \rho(z, T, S) dz$$

- ~~$h_{ster}$~~  invisible to GRACE! ( $P_{OBP} = 0$ )
- ~~$h_{ster}$~~  visible by radar altimetry!
- Density  $\uparrow$  results in  $\downarrow$  of sea level
- Wind driven (quick)  $\rightarrow$  change in  $h_{dyn}$
- Density driven (slow)  $\rightarrow h_{dyn} \approx h_{ster}$

# Quiz time! (again)



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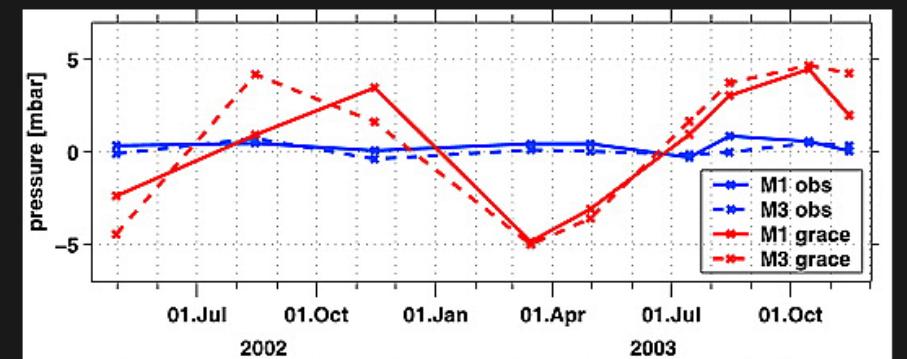
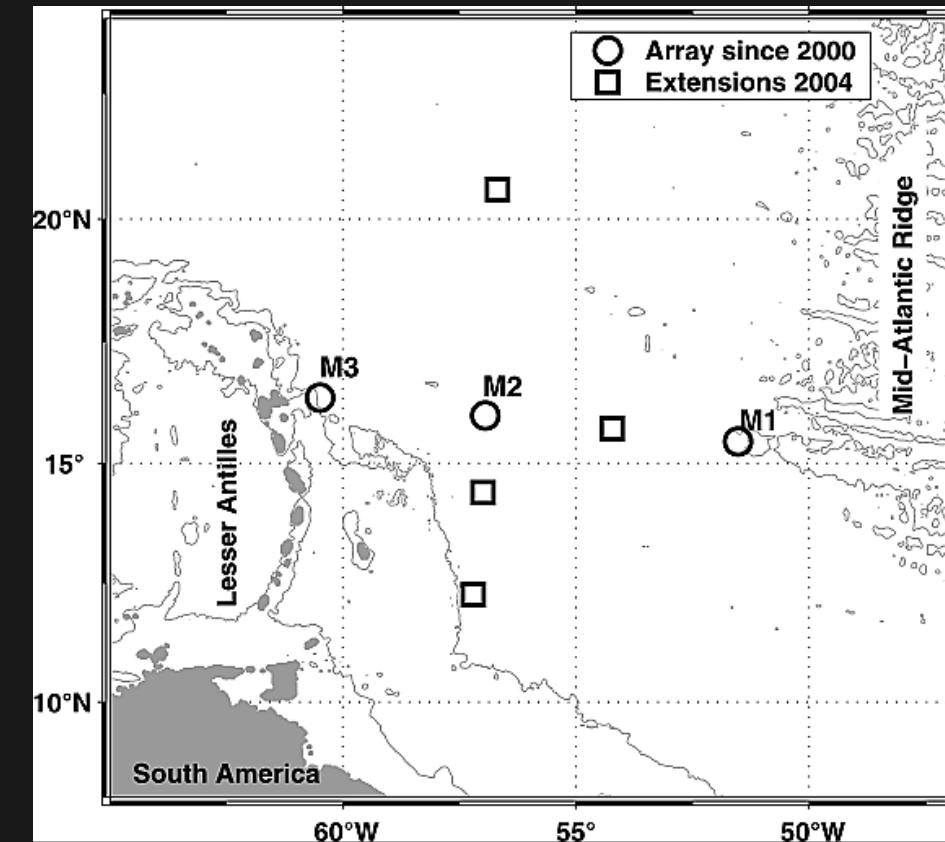
**Accept all**

**Reject All**

**Customise**

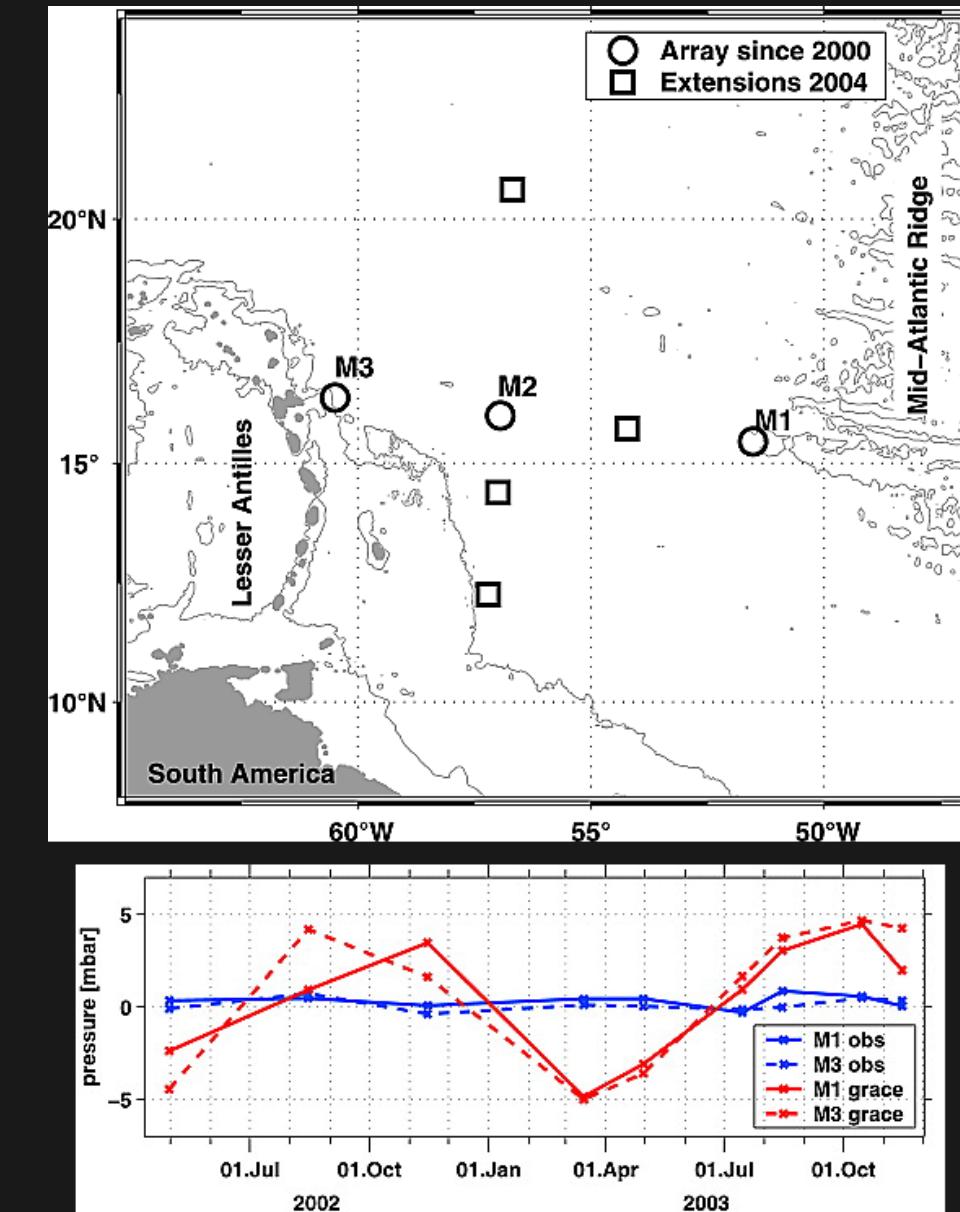


# Early GRACE validation of ocean bottom pressure changes (Kanzow et al. 2005)



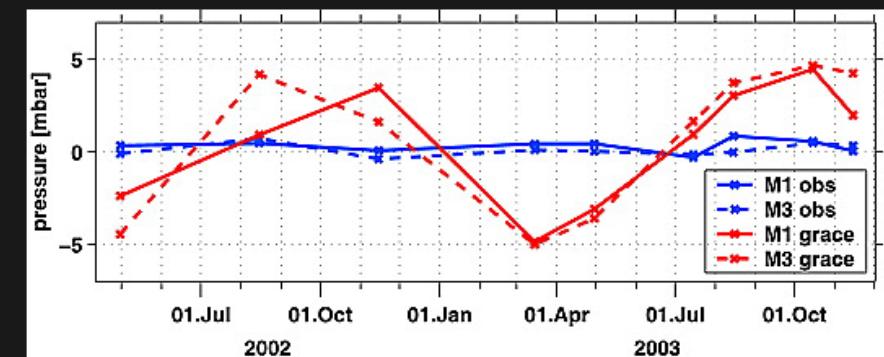
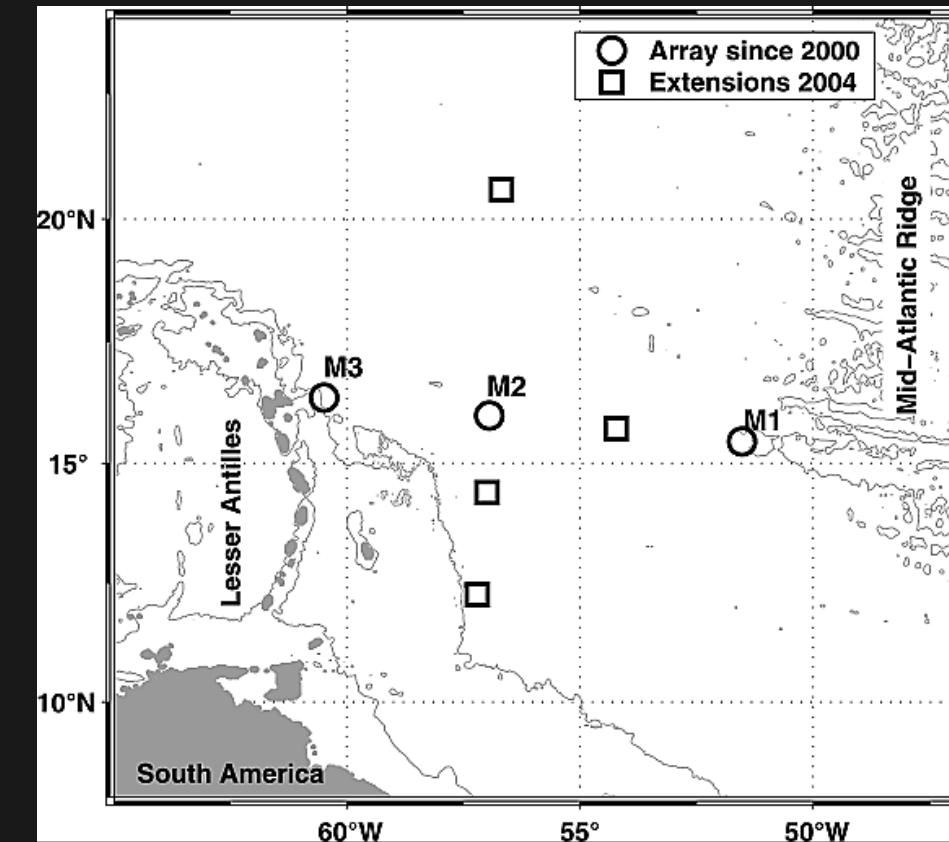
# Early GRACE validation of ocean bottom pressure changes (Kanzow et al. 2005)

- In situ validation with pressure sensors



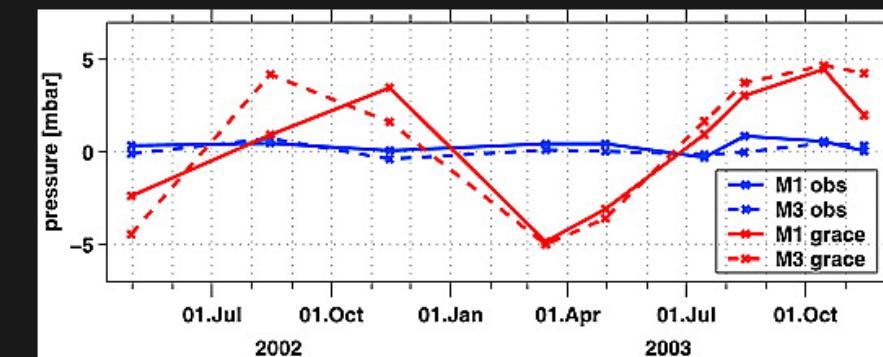
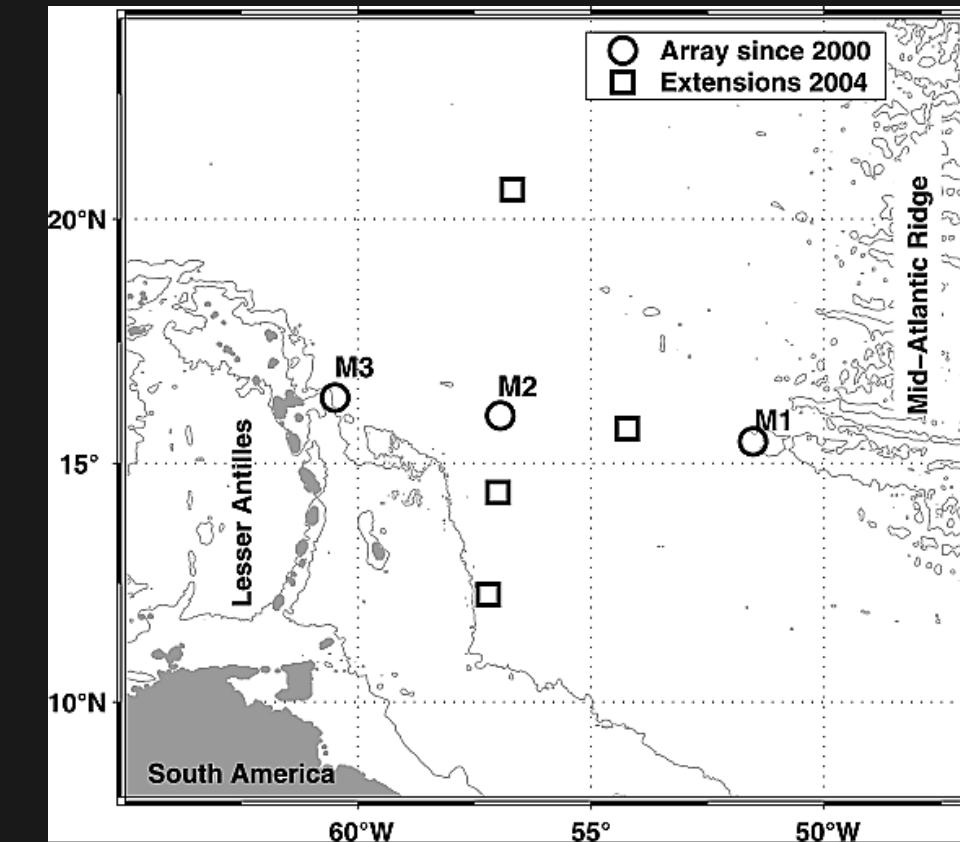
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- In situ validation with pressure sensors
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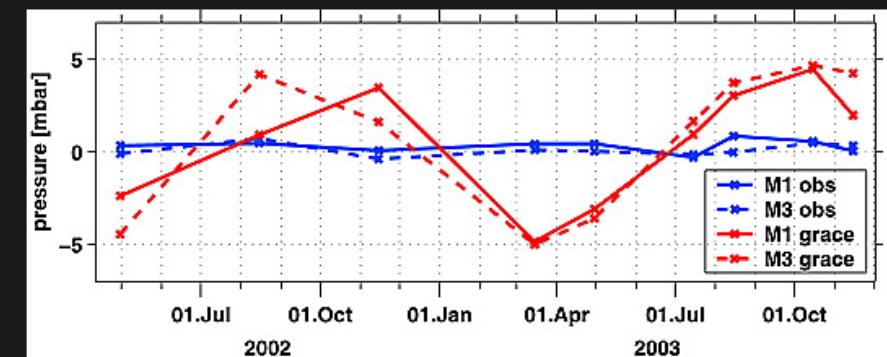
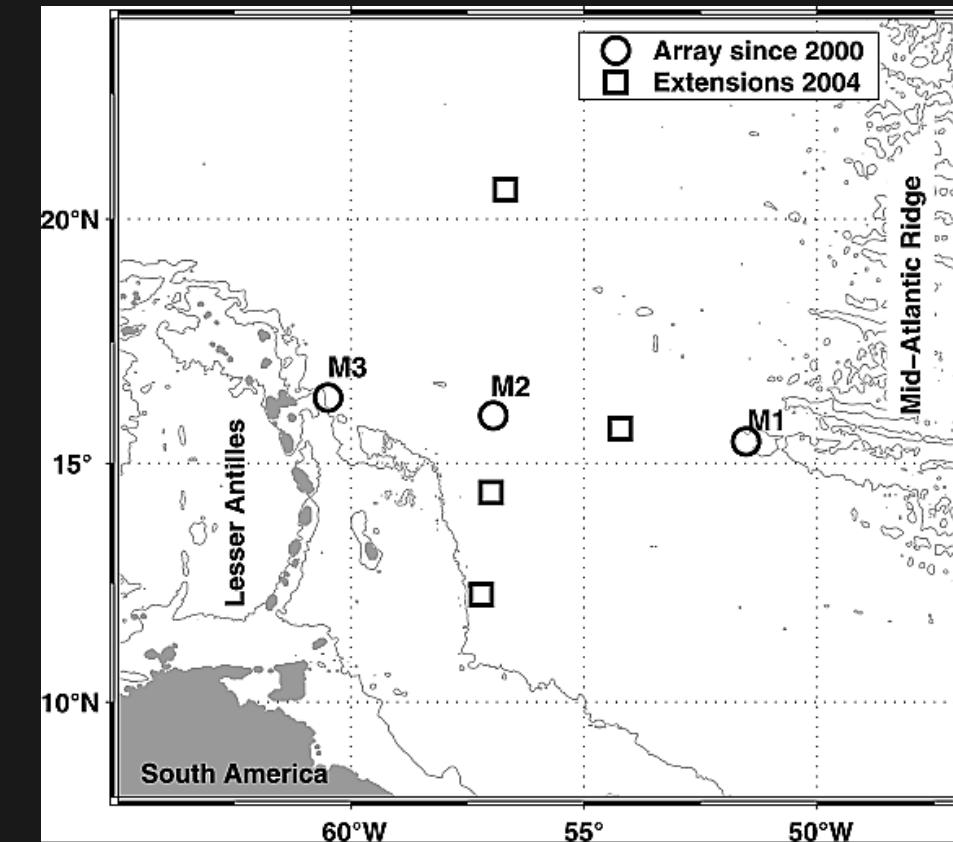
# Early GRACE validation of ocean bottom pressure changes (Kanzow et al. 2005)

- In situ validation with pressure sensors
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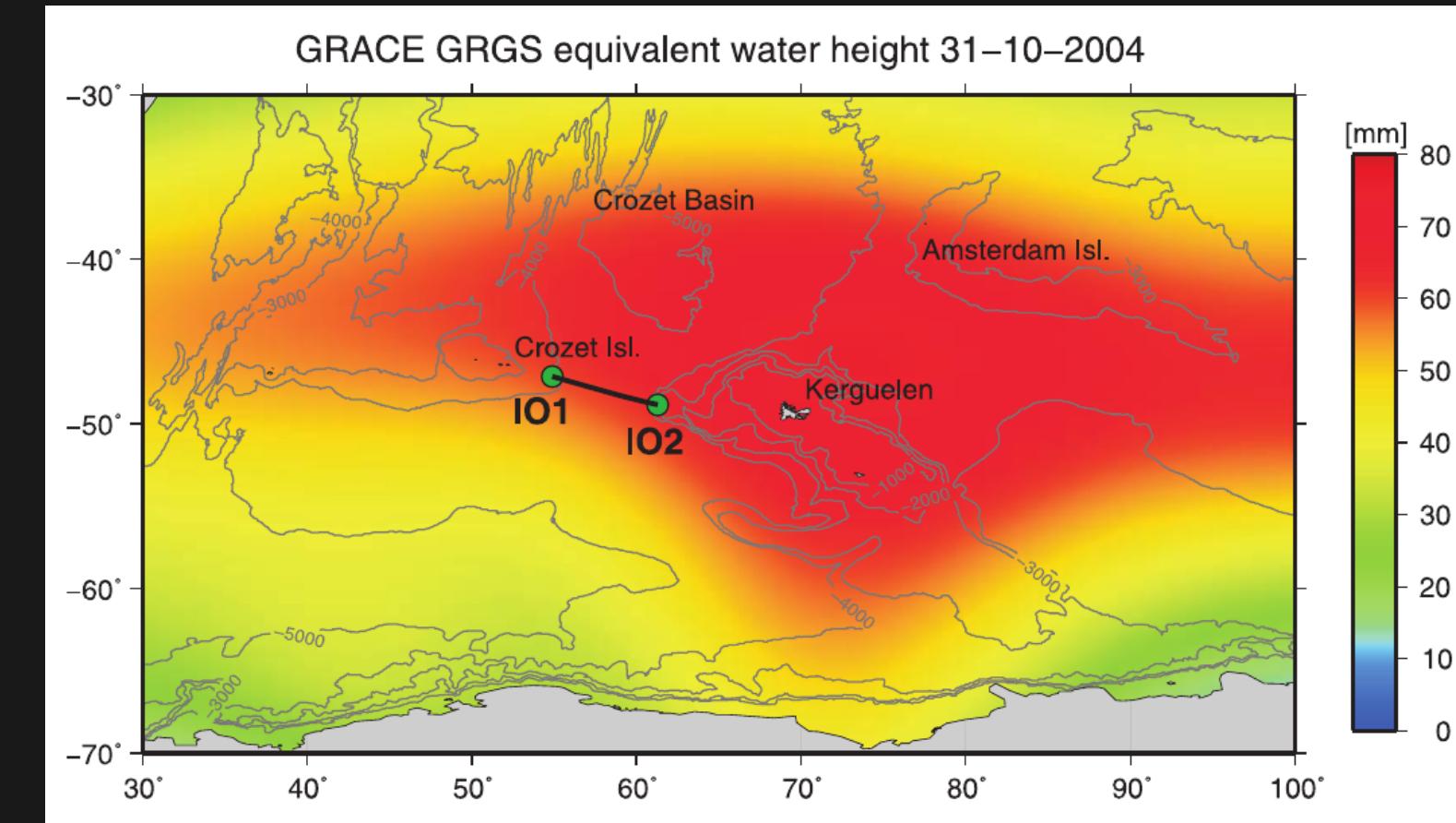
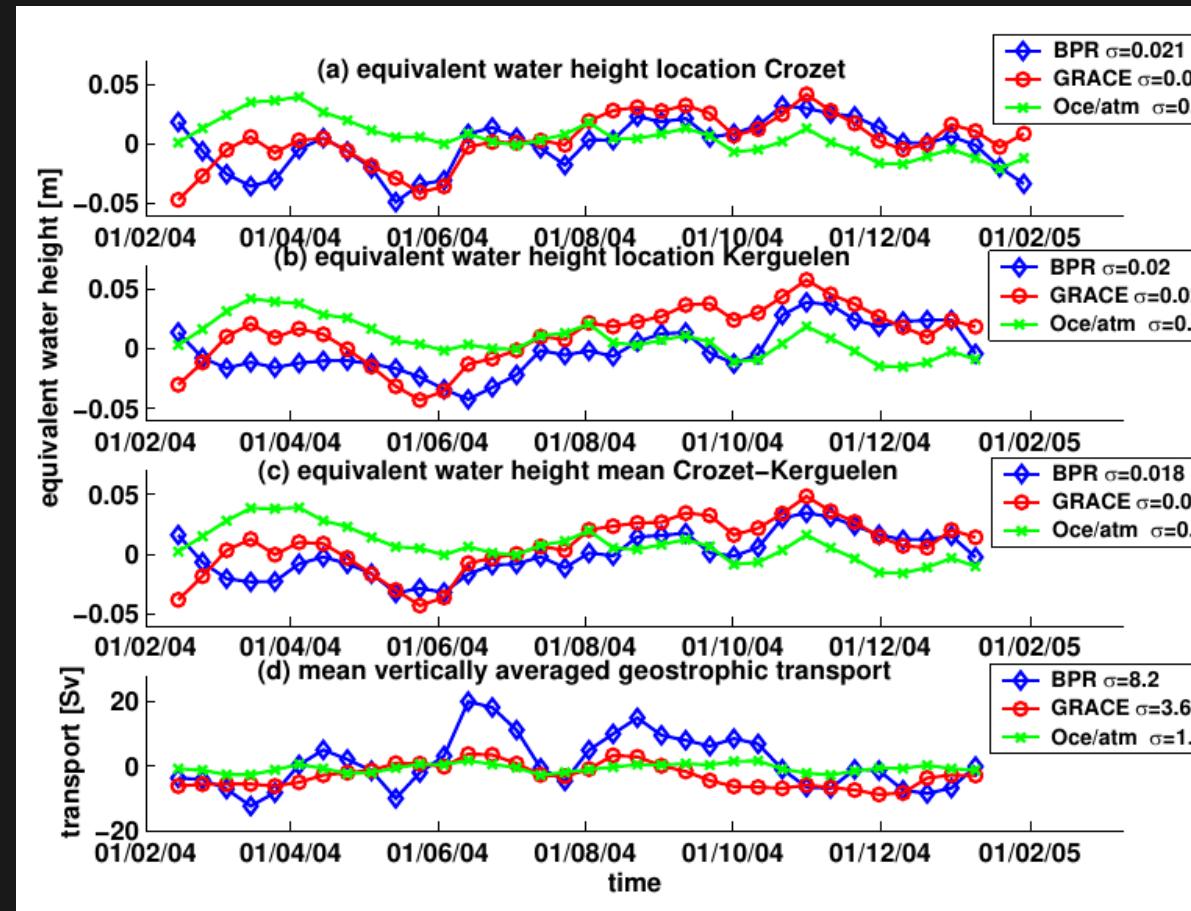


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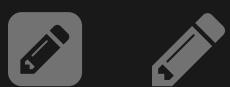
- In situ validation with pressure sensors
- GRACE fluctuations were too large
  - Signal leakage
  - Processing errors



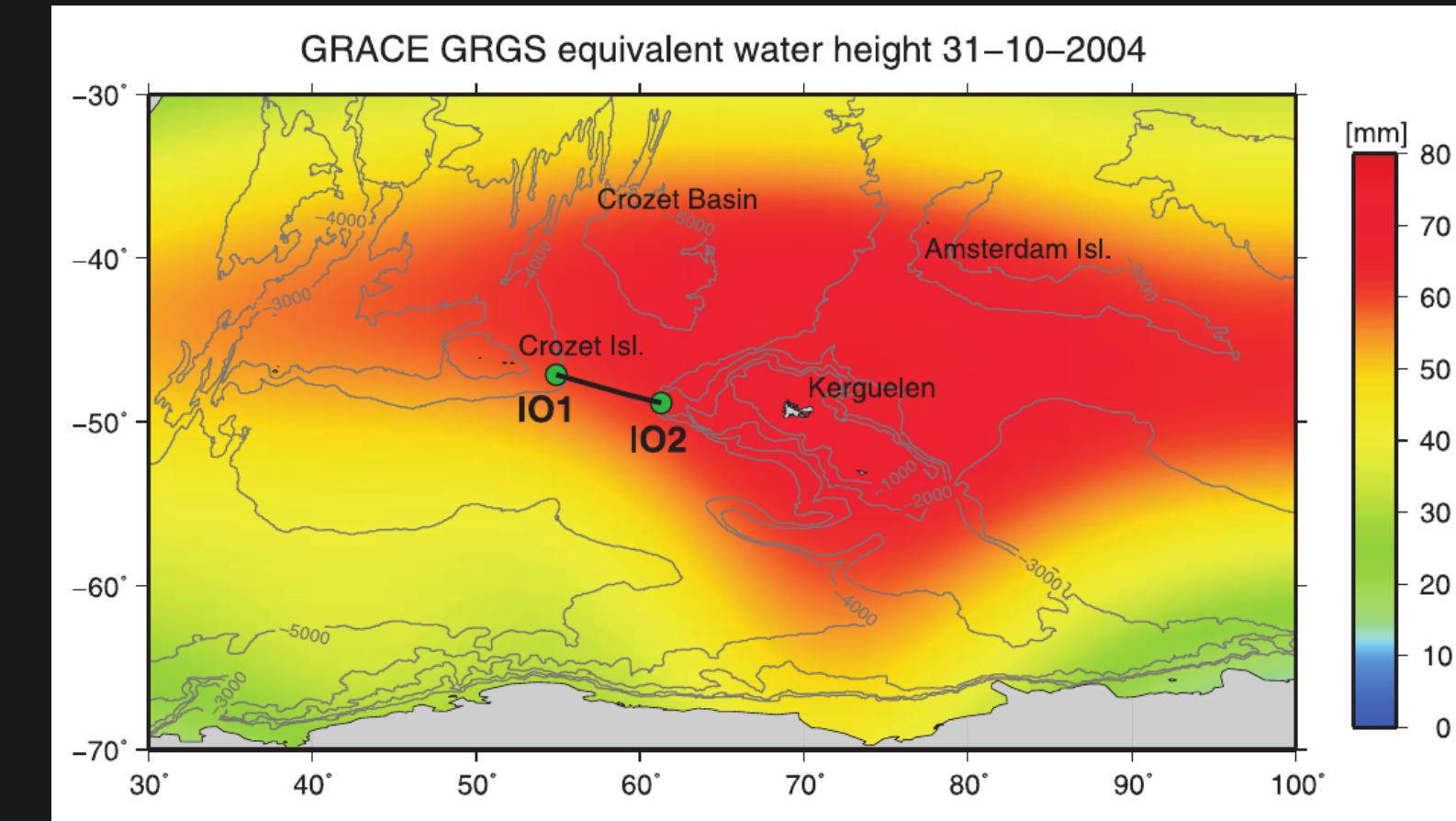
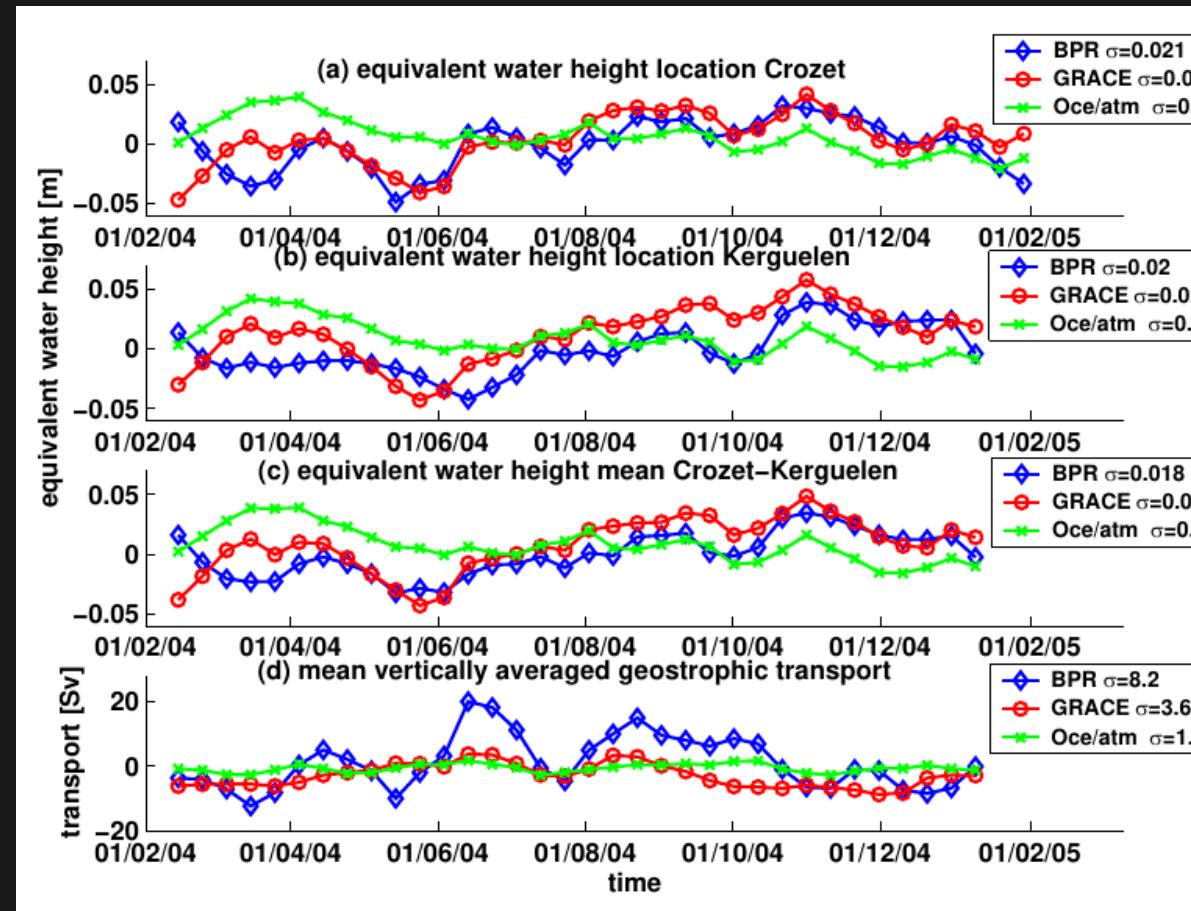
# Validation in the Southern Ocean



From Rietbroek et al. 2006



# Validation in the Southern Ocean

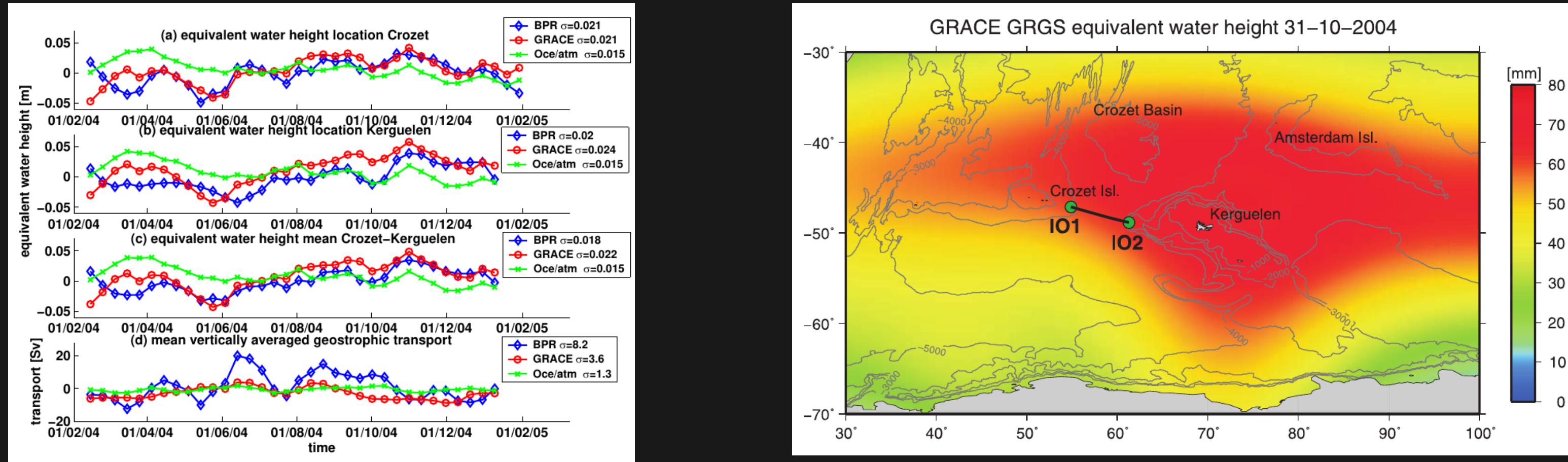


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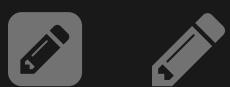


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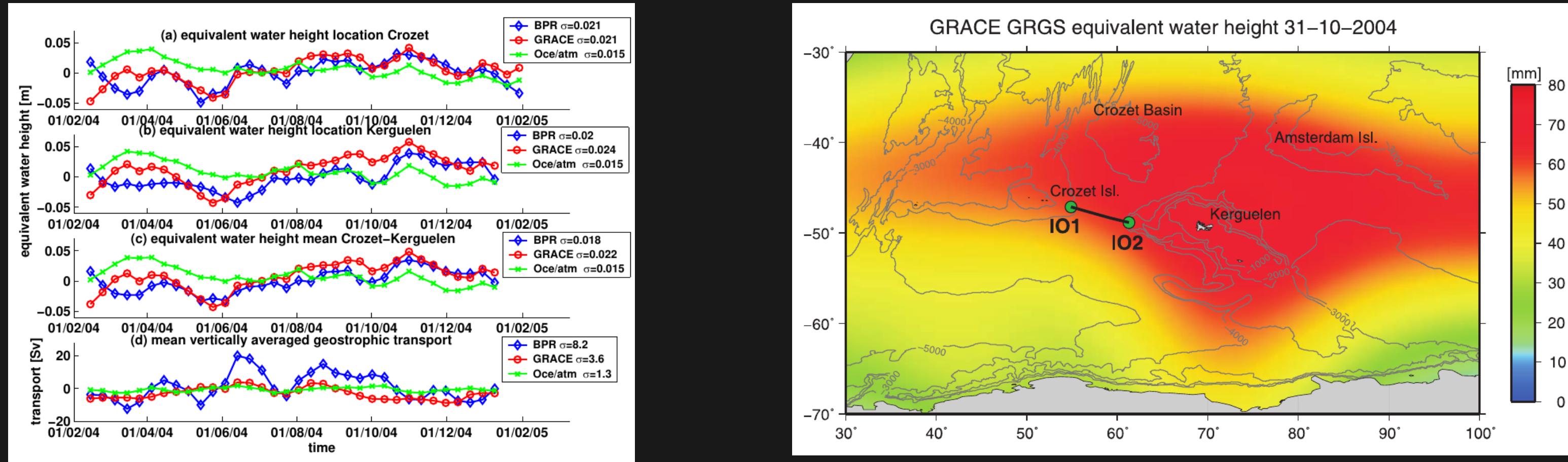


From Rietbroek et al. 2006

- In situ validation with pressure sensors
- 10-day GRACE solution was better than background model

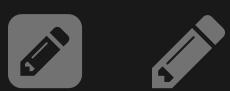


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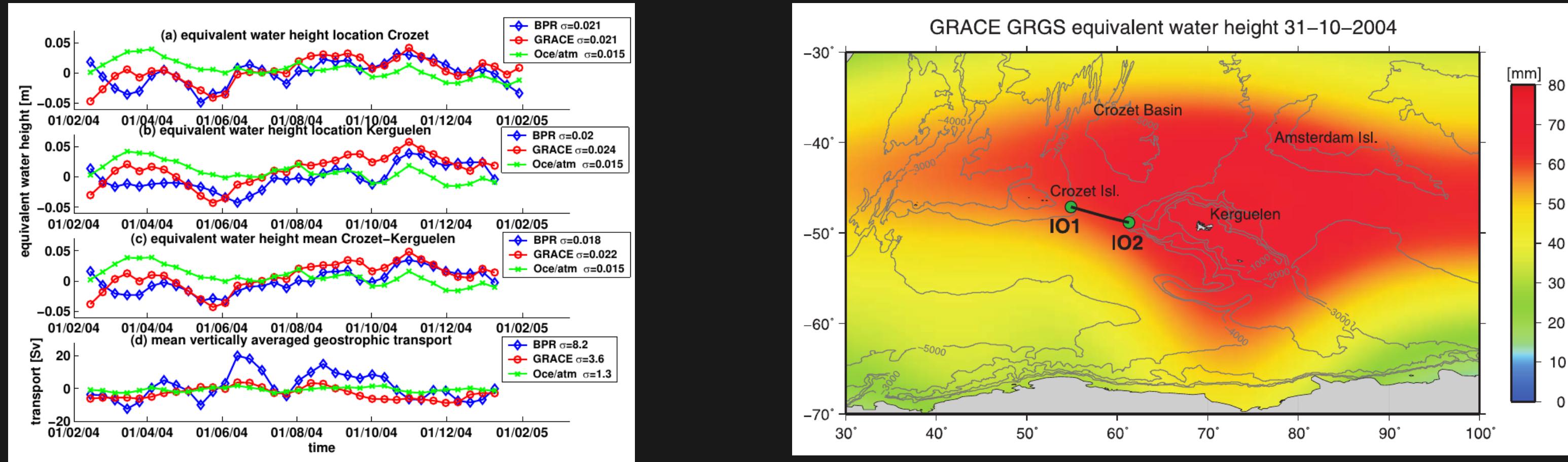


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- Large scale ocean signals picked up



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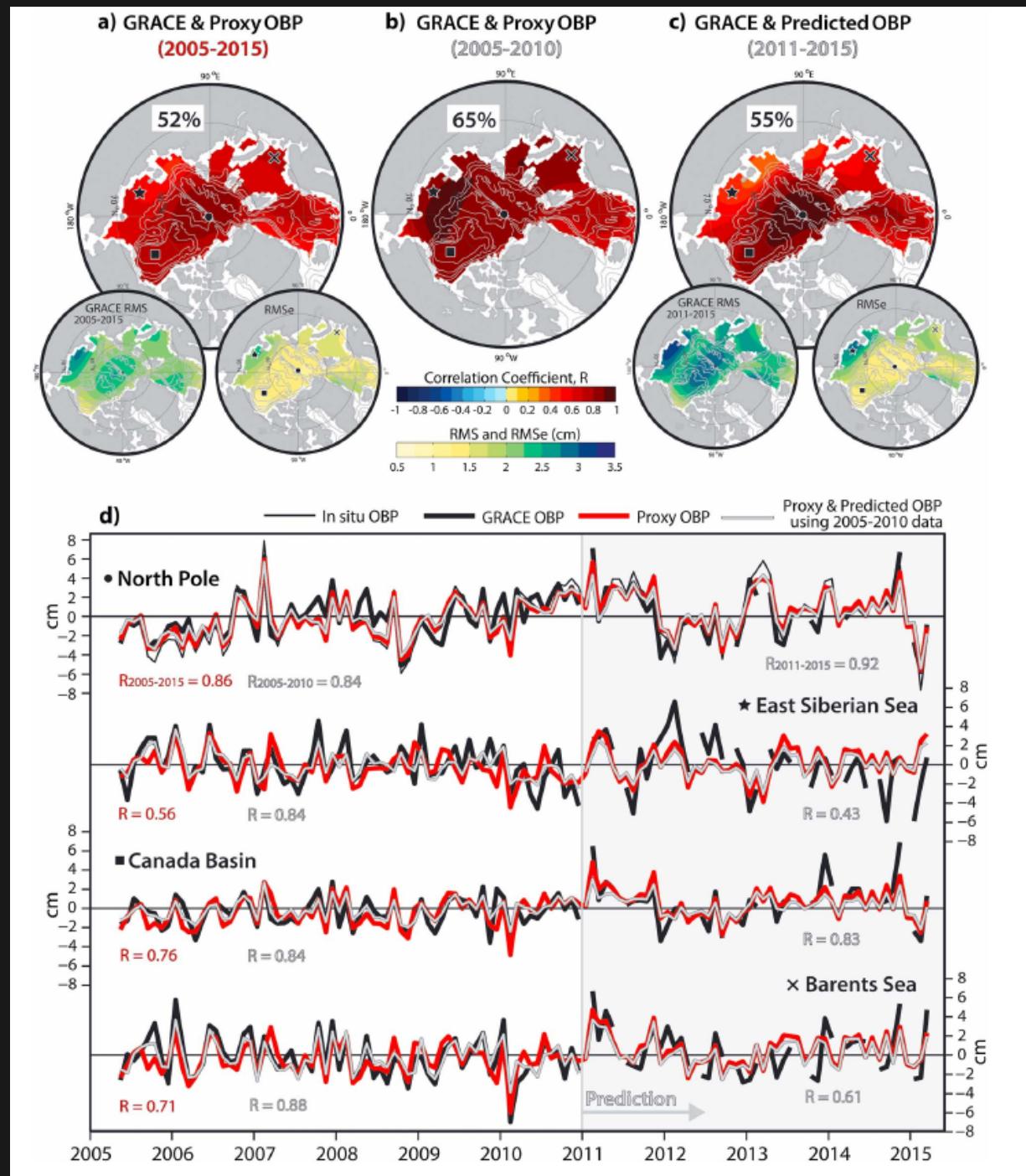


From Rietbroek et al. 2006

- In situ validation with pressure sensors
- 10-day GRACE solution was better than background model
- Large scale ocean signals picked up
- Due to smoothing geostrophic bottom currents not resolved



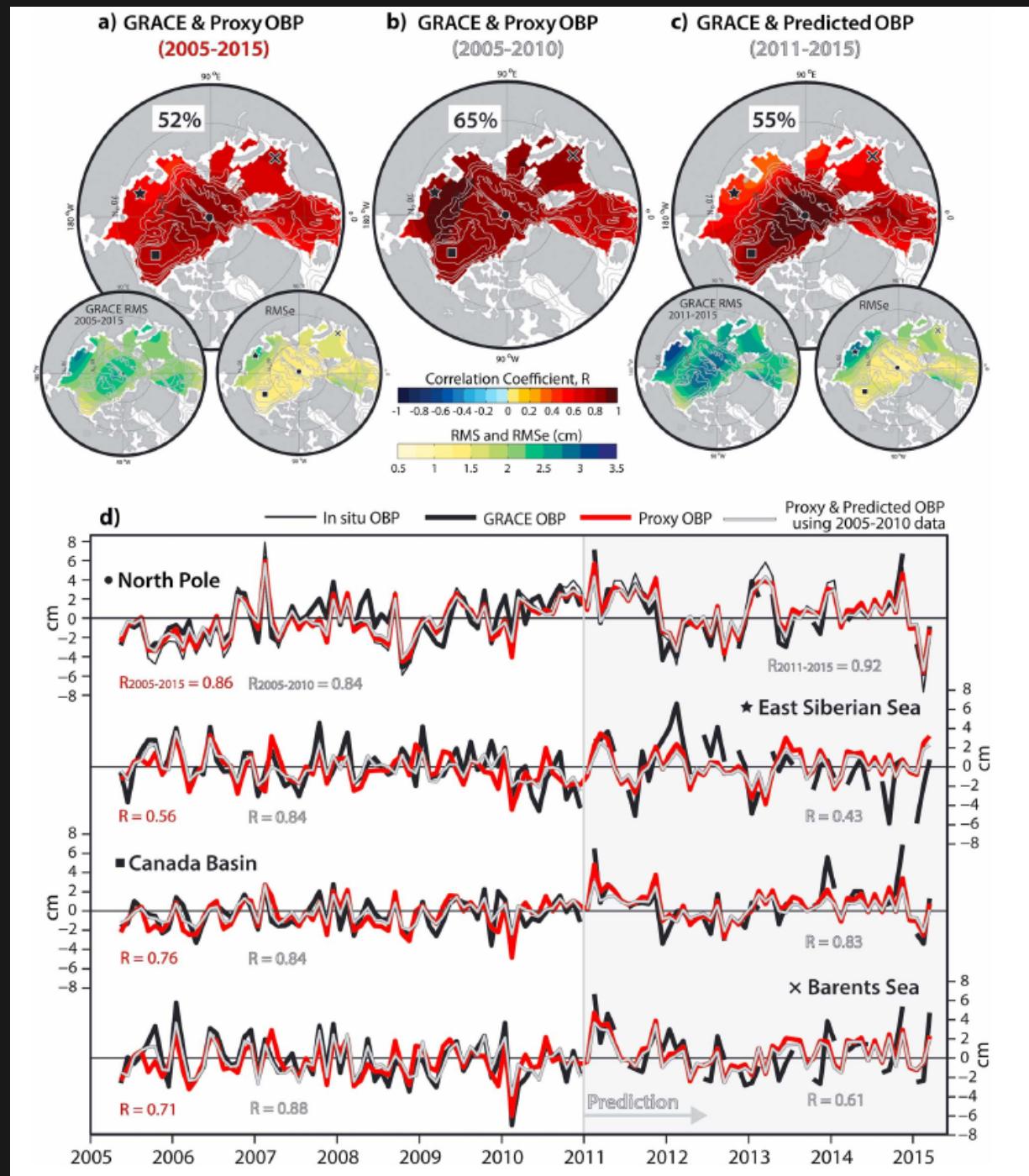
# Arctic Ocean Bottom pressure variations well captured by GRACE



From Peralta-ferriz et al. 2016



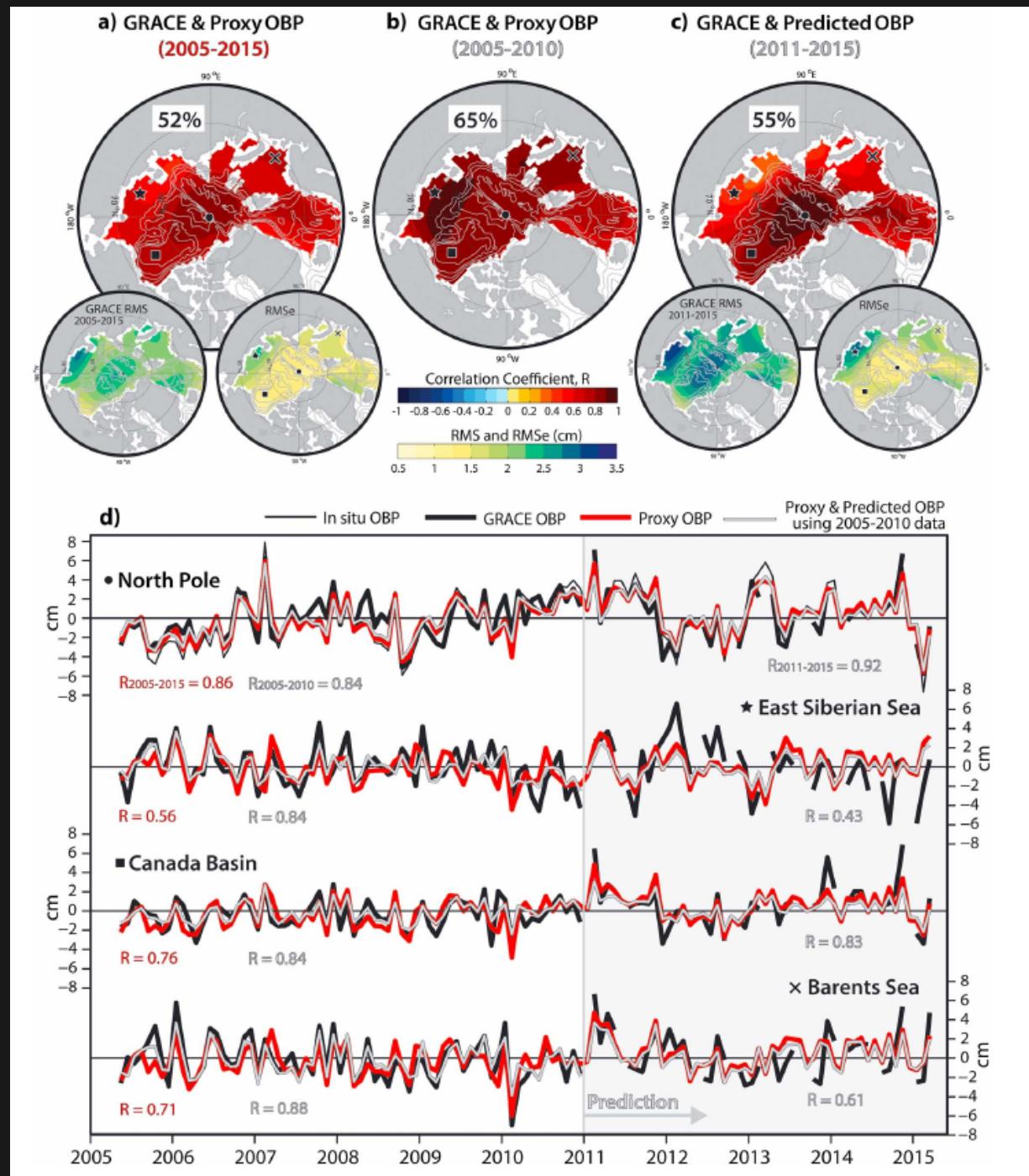
# Arctic Ocean Bottom pressure variations well captured by GRACE



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- In situ OBP well captured by GRACE

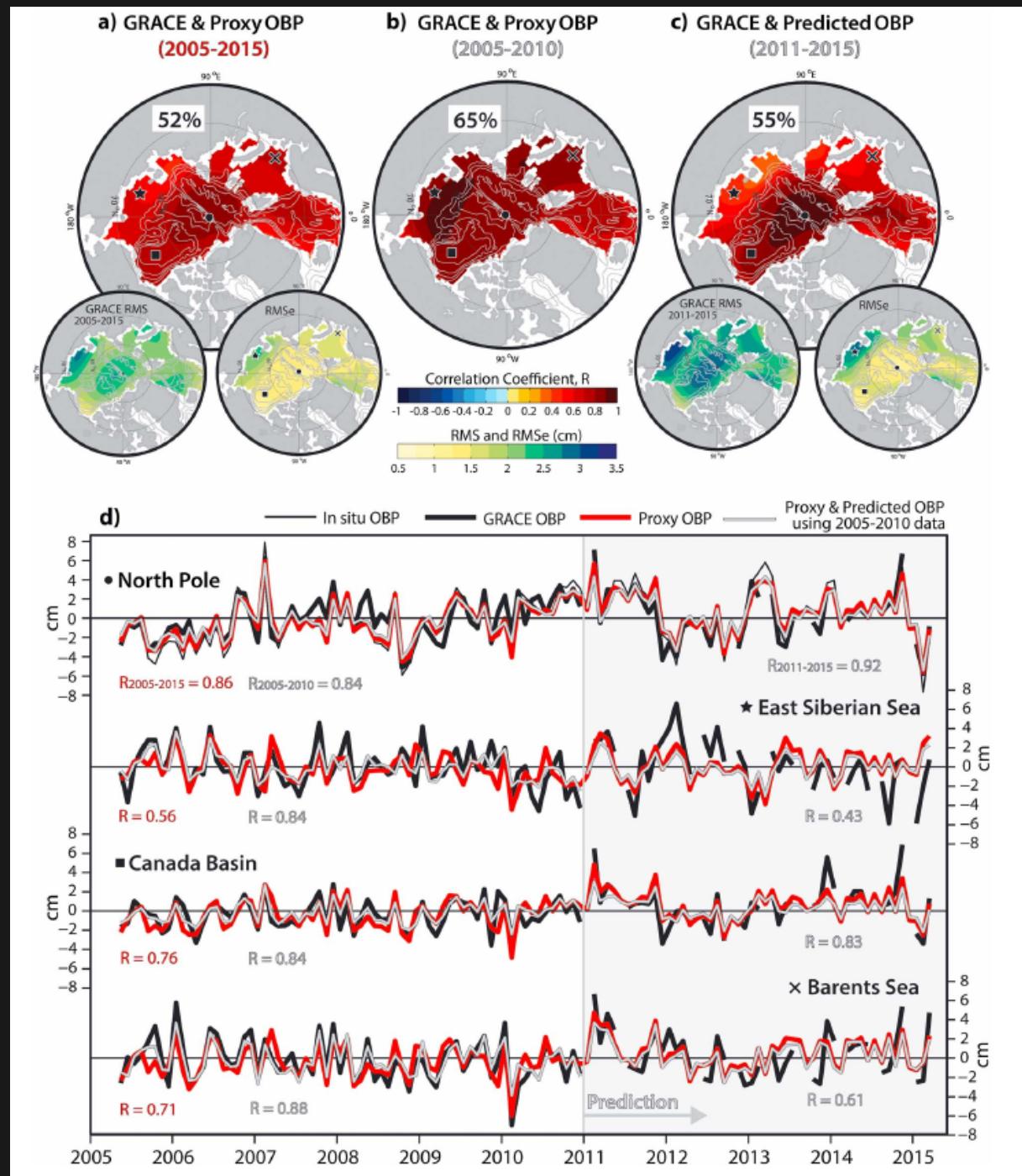
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- In situ OBP well captured by GRACE
- Coherent OBP signals in the Arctic

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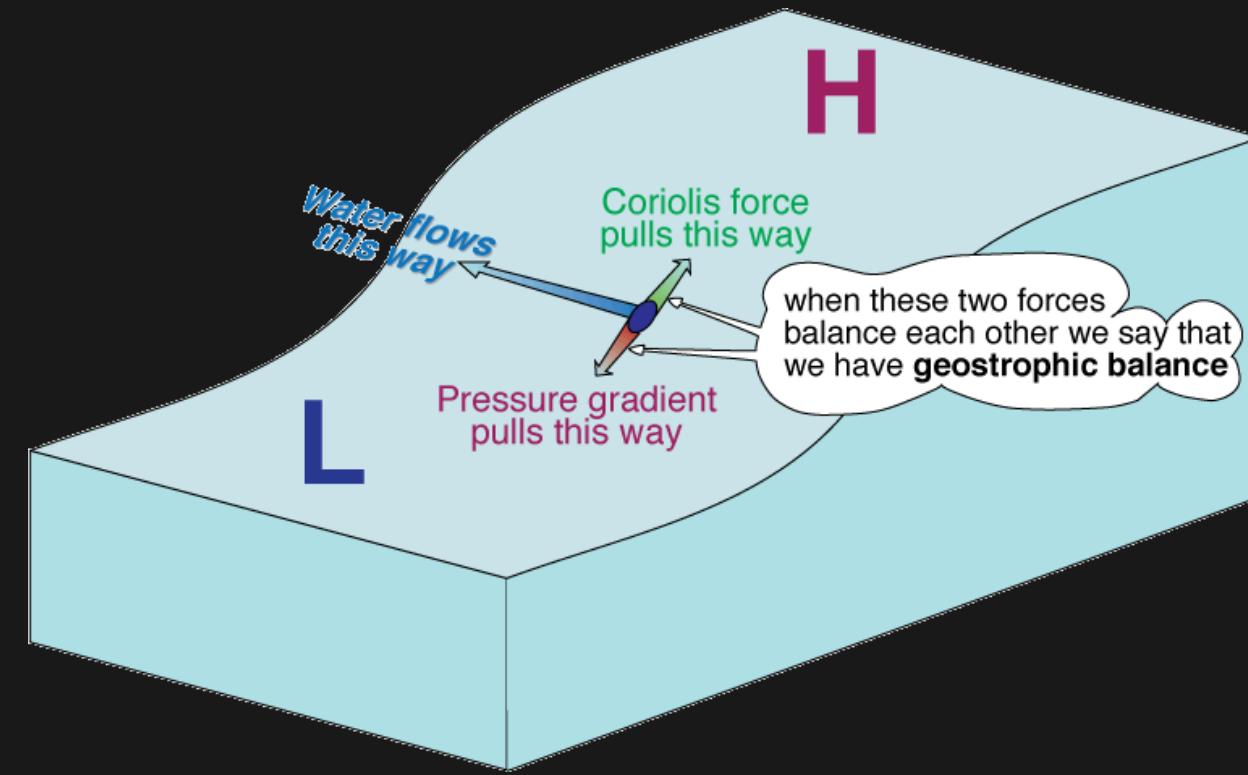
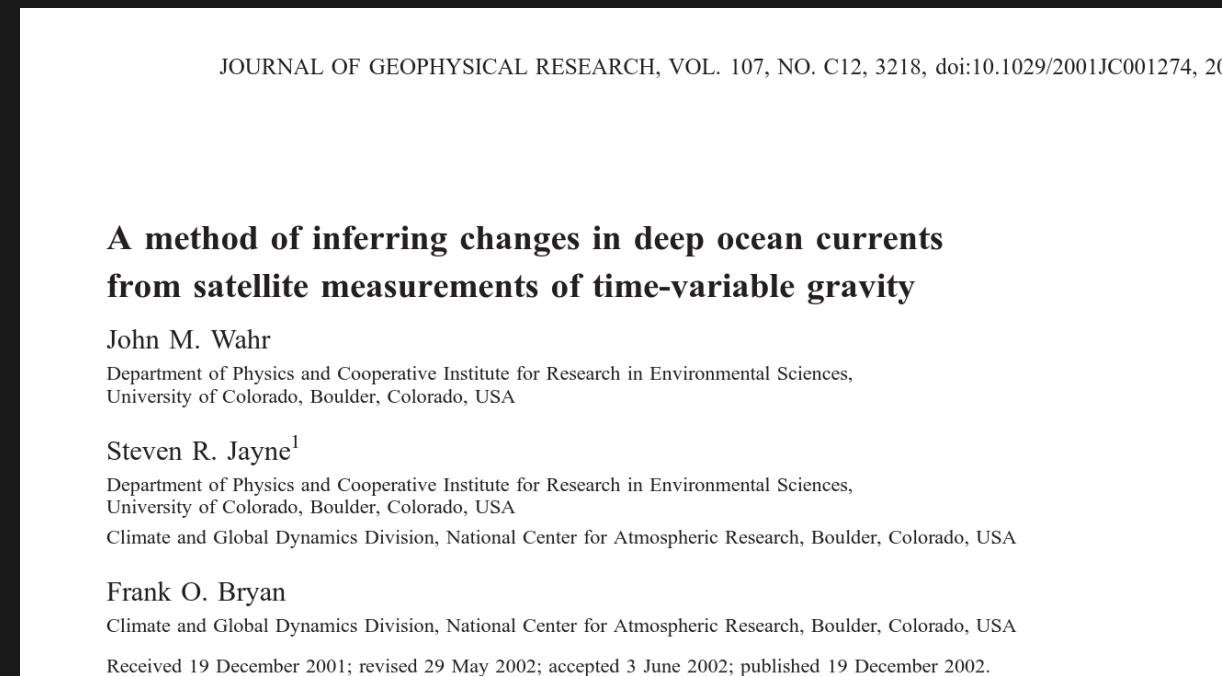


From Peralta-ferriz et al. 2016

- In situ OBP well captured by GRACE
- Coherent OBP signals in the Arctic
- Comparison showed that a single in situ OBP can serve as proxy for the entire Arctic



# Geostrophic currents from time variable gravity



CC-NC-SA, <https://www.seos-project.eu>

the effects of friction and external forcing are less important,  
(1) reduces to the geostrophic approximation:

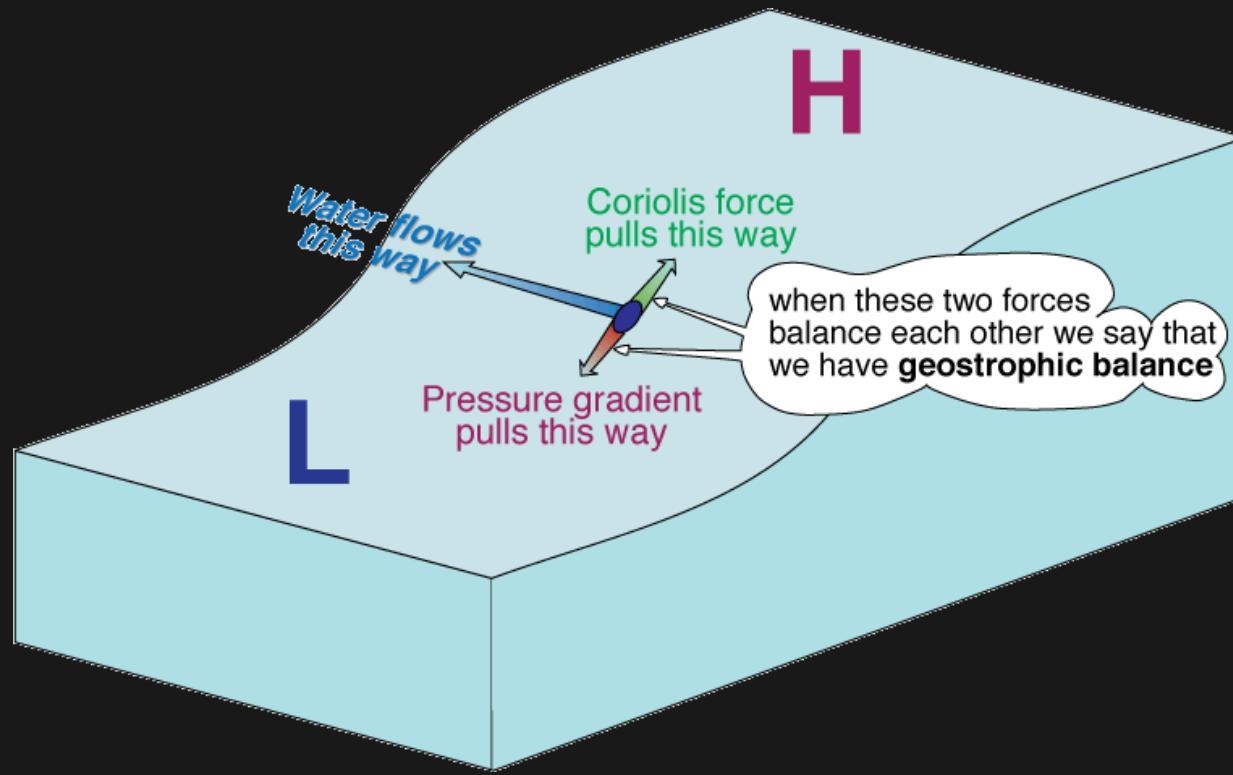
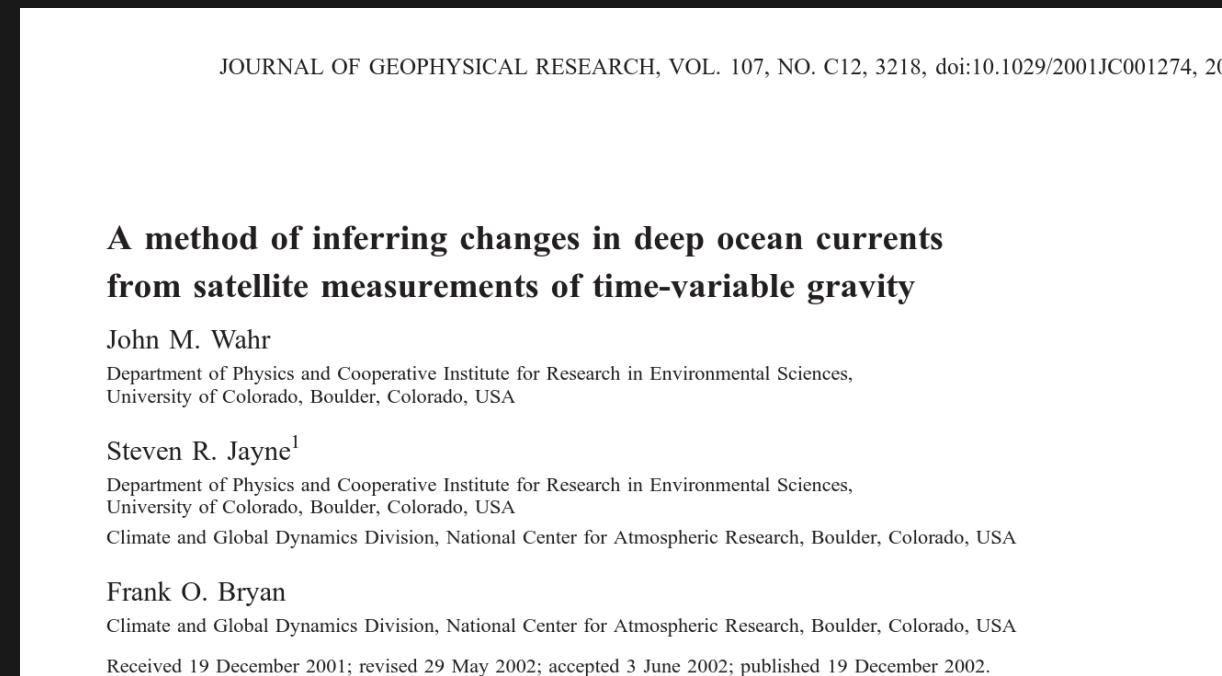
**Pressure gradient**

$$2\rho_0\Omega \times \mathbf{v} \approx -\nabla P \quad (2)$$

Earth rotation vector      ↑ velocity



# Geostrophic currents from time variable gravity



CC-NC-SA, <https://www.seos-project.eu>

- Assume no accelerations

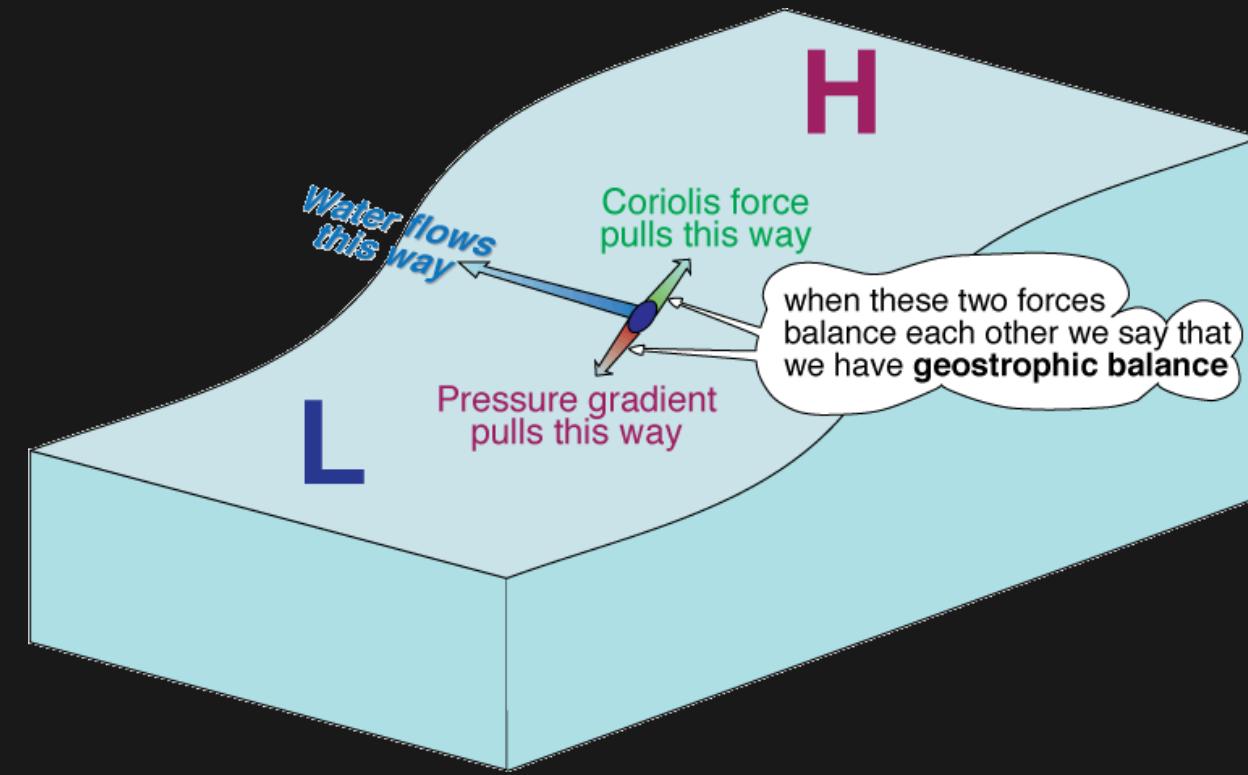
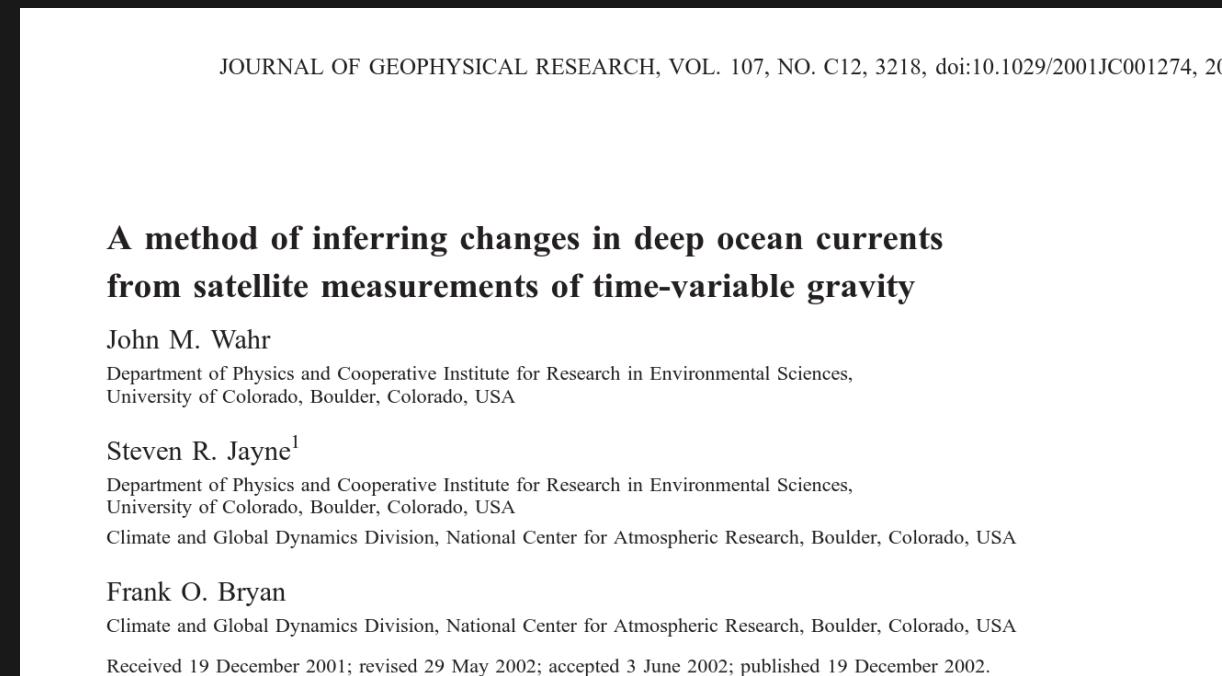
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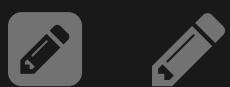
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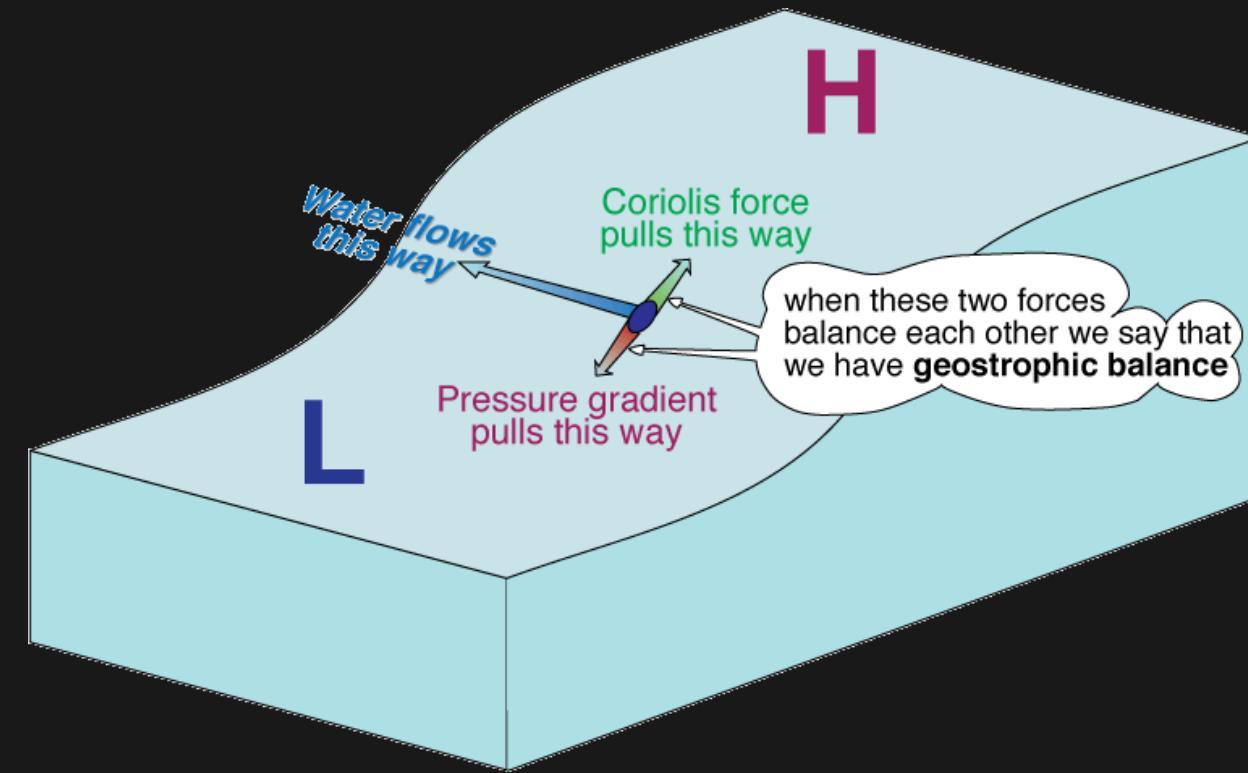
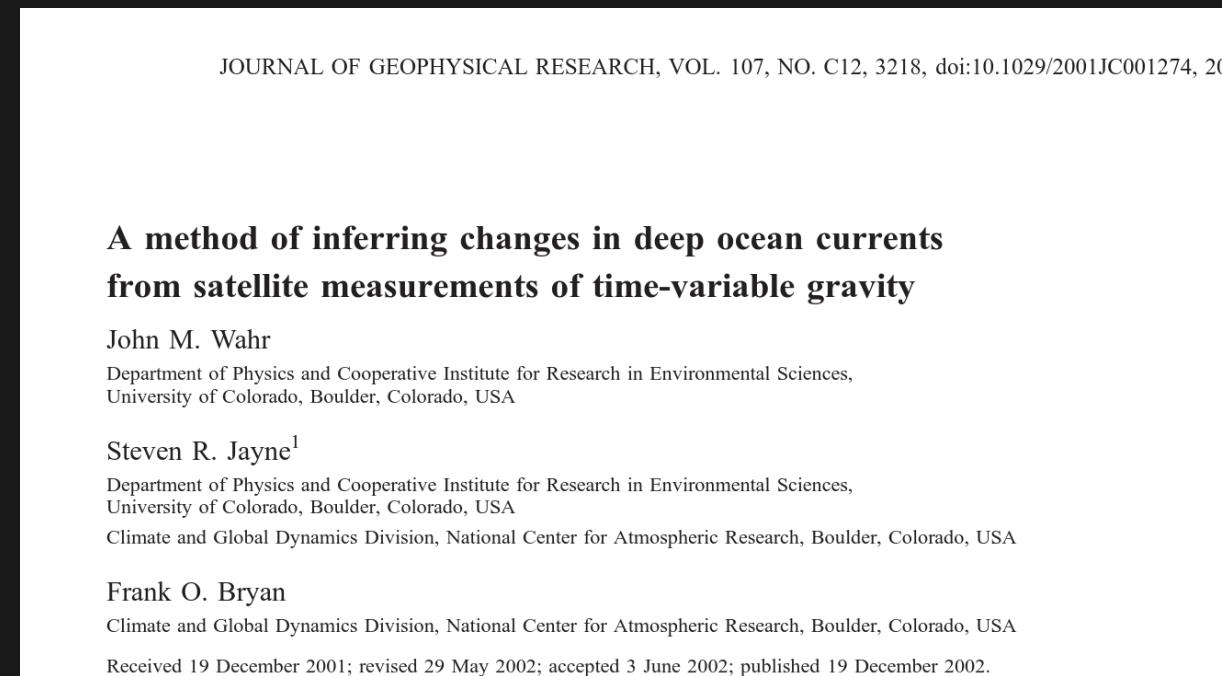
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Earth rotation vector      ↑ velocity

- Assume no accelerations
- cross-product -> latitude dependency



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CC-NC-SA, <https://www.seos-project.eu>

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Earth rotation vector



- Assume no accelerations
- cross-product  $\rightarrow$  latitude dependency
- Velocity is orthogonal to gradient!



# What have you learned?

- Adding mass to the ocean
  - Observable in time-variable gravity
  - GRACE (1.5 - 2 mm/yr global mean ocean mass change)
  - Different causes have non-uniform contributions (Ice sheets, hydrology, dam impoundment,..)
  - Regional sea level also influenced by: Self attraction and loading
- Churning the Ocean (currents and wind)
  - Integration of the water column -> OBP
  - OBP changes due to dynamic height differences and column density change
  - Steric sea level: density driven dynamic height changes under the assumption of no OBP change
  - Pressure gradients cause circulation (surface gradient may be different from bottom)



# Outlook

- Still many ocean applications unexplored (geostrophic currents!)
- Added value comes from combined data e.g. altimetry, Argo, etc.

