

# Churning the Ocean: Time variable gravity for ocean applications



[Samudra Manthan, CC BY 3.0](#)

Roelof Rietbroek, 28 Sept. 2022



# Analogies with today's talk



Find this presentation on <https://github.com/strawpants/grace-hackweek-ocean>



# Analogy's with today's talk

- Mount Mandara: Adding mass to the ocean (e.g. melt water)



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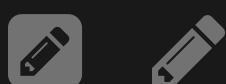


# Analogy with today's talk

- Mount Mandara: Adding mass to the ocean (e.g. melt water)
- Snake Vasuki: set the ocean in motion (e.g. forcing from wind stress)
- Central Question: How can we use time variable gravity to observe ocean signals?



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# Adding mass to the oceans



# Adding mass to the oceans

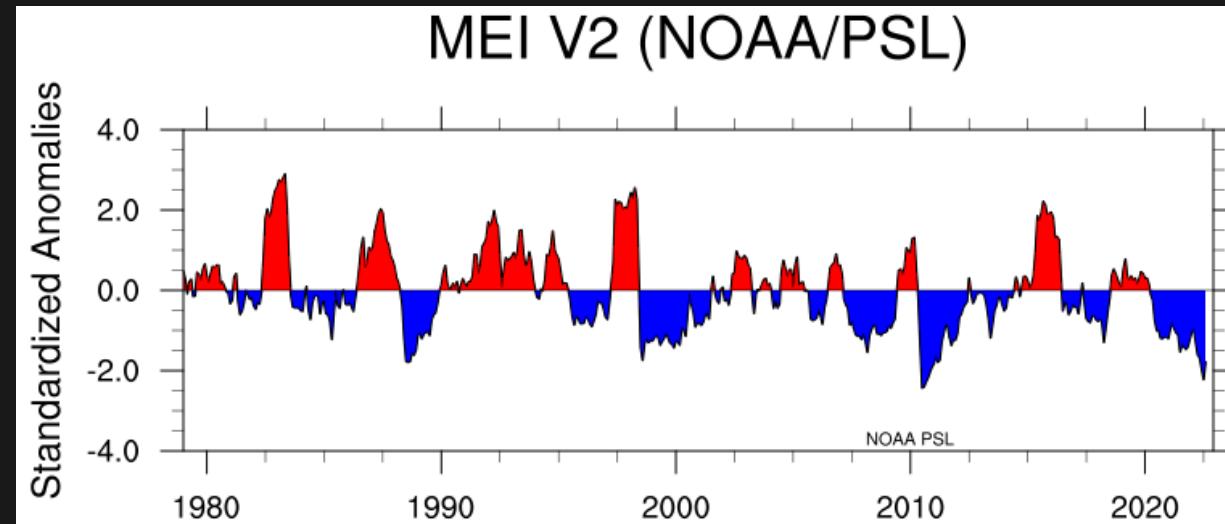
(or removing it)



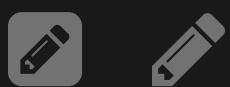
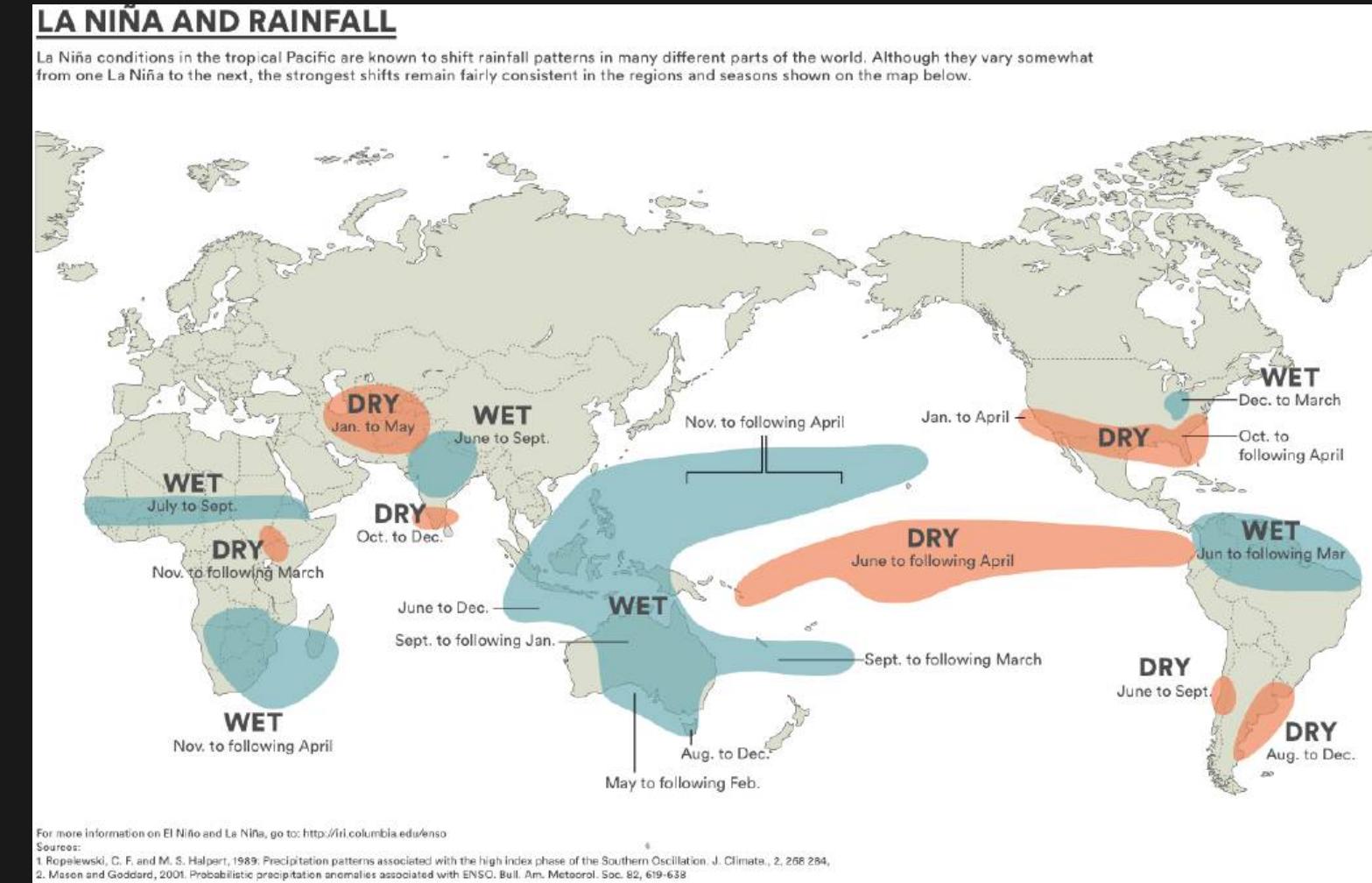
2022 Floods in Pakistan, image: AFP



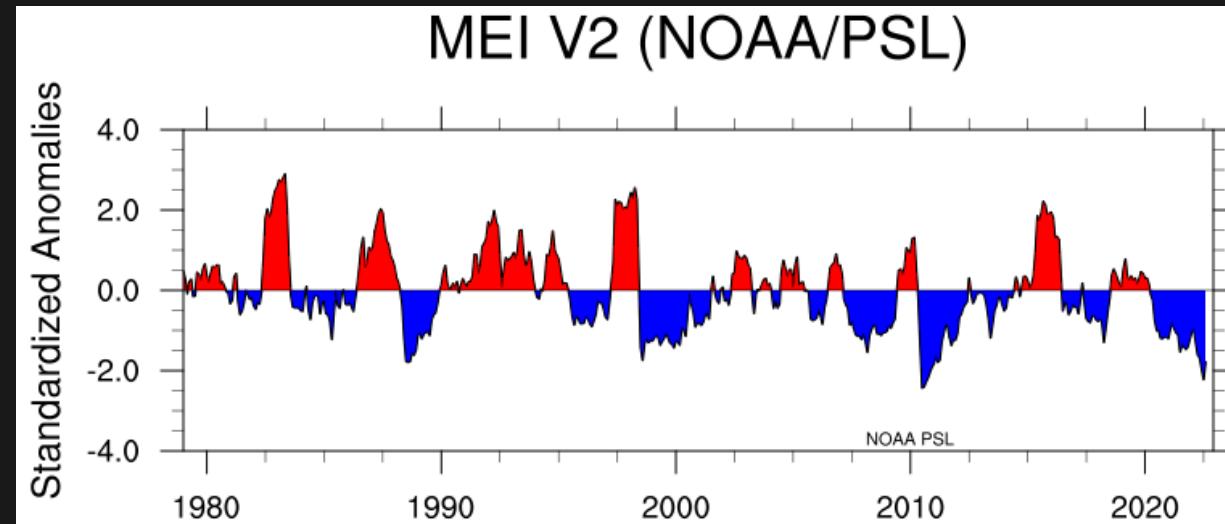
# Does La Niña affect sea level?



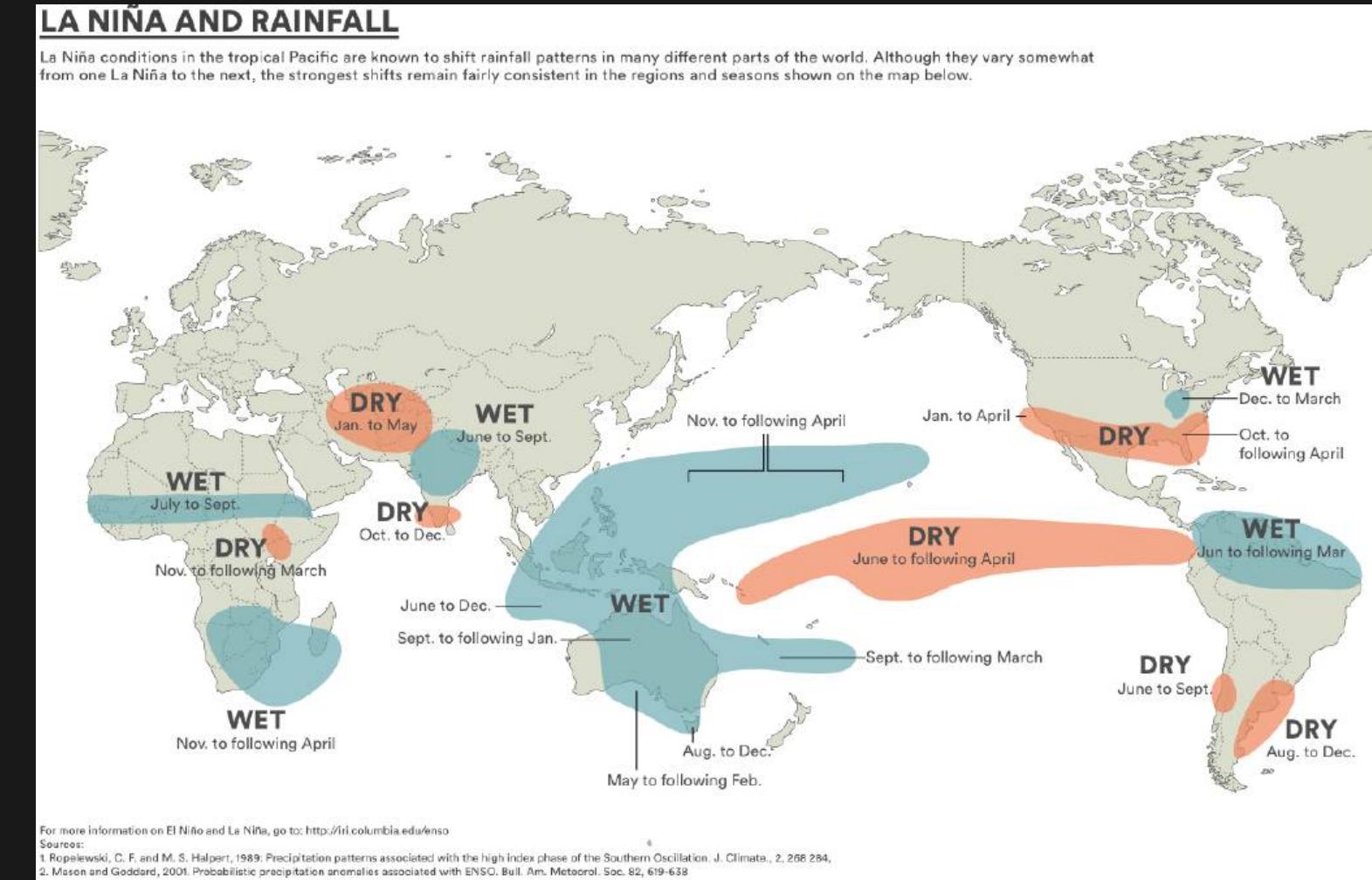
Multivariate ENSO index, <https://psl.noaa.gov/enso>



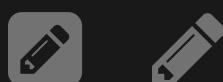
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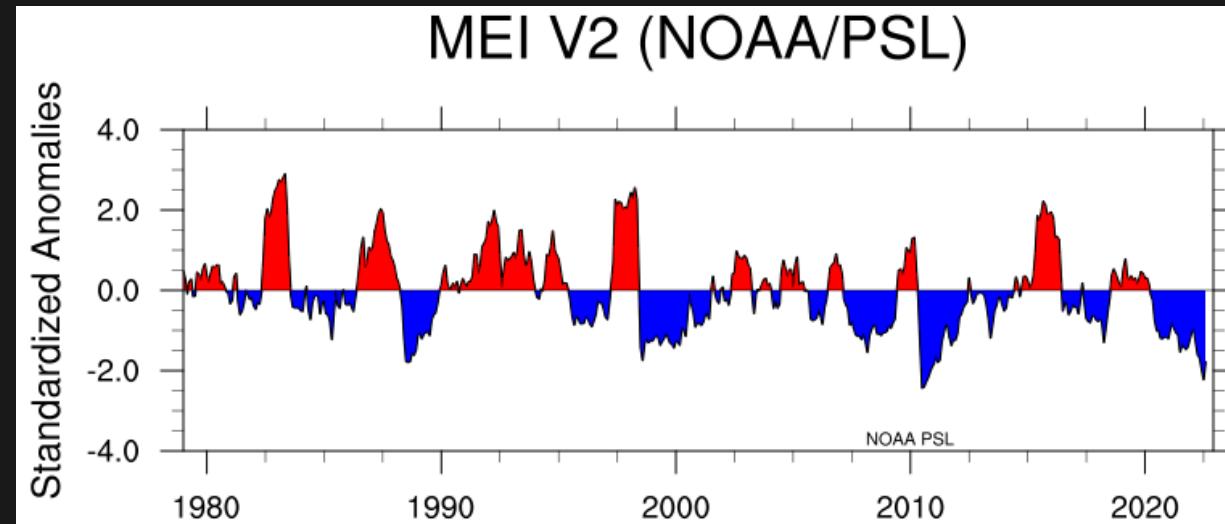
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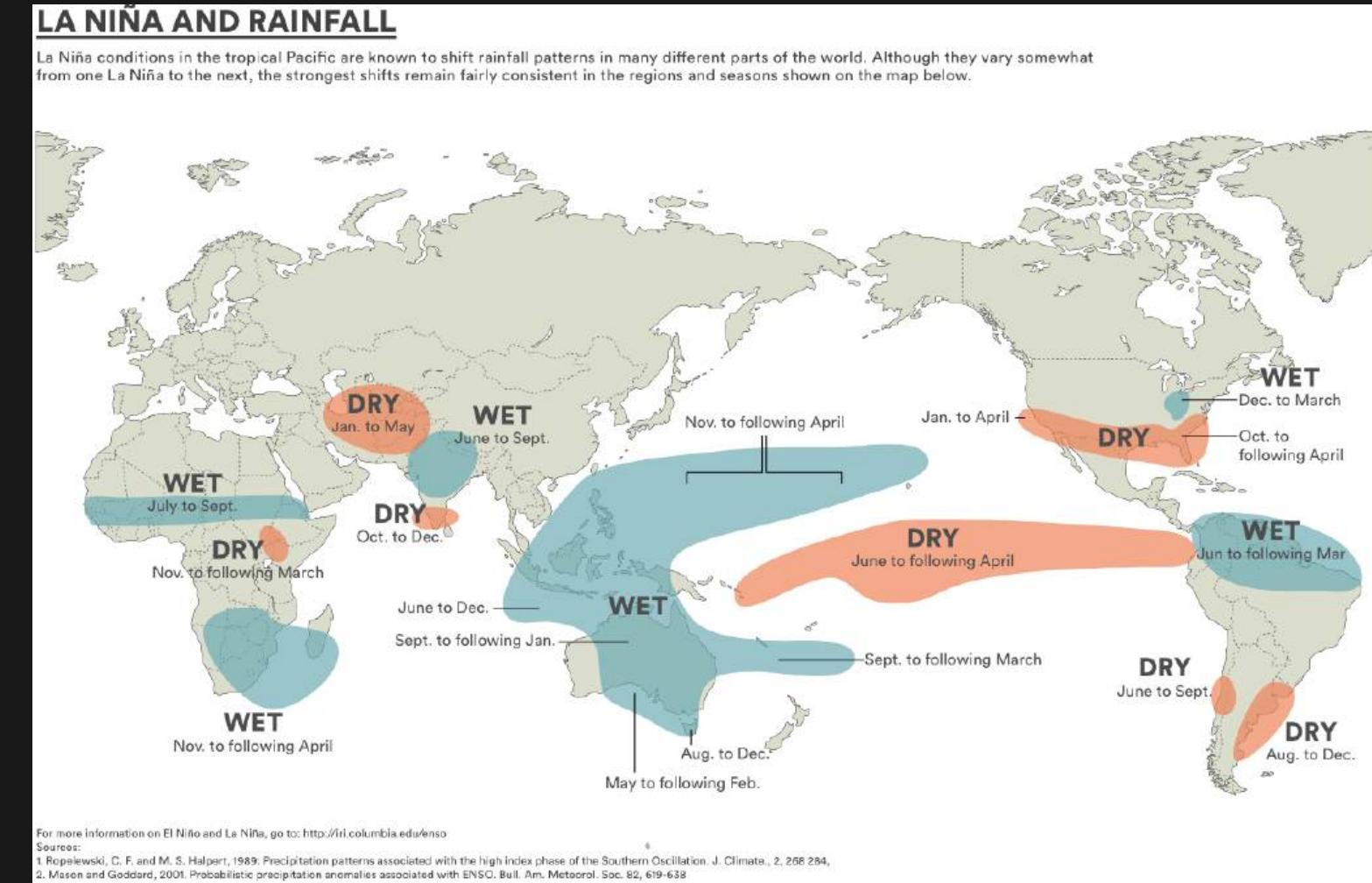
- Stronger trade winds -> warm ocean blob in the western Pacific



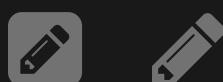
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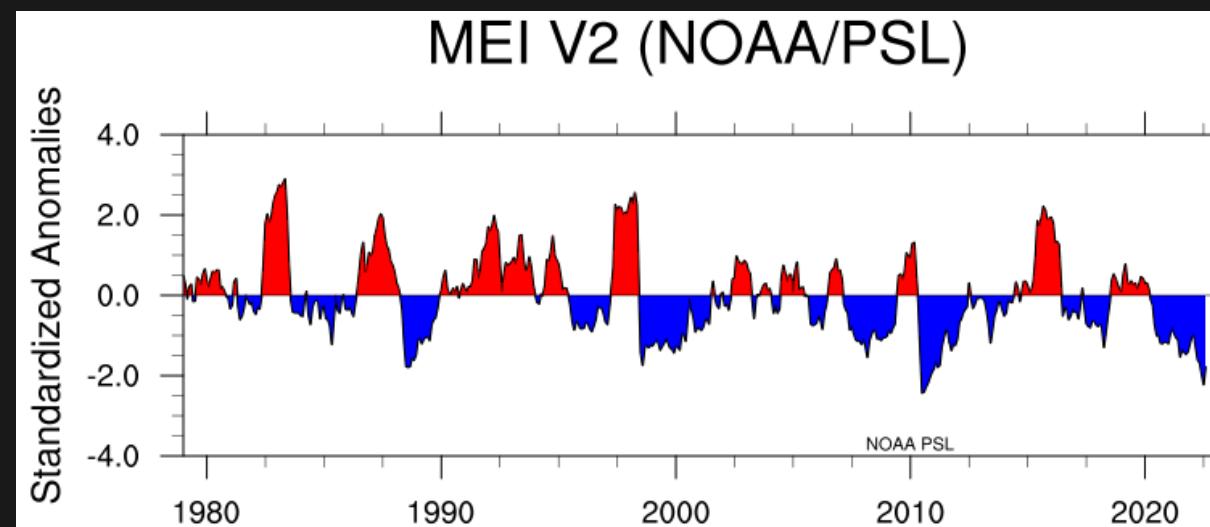
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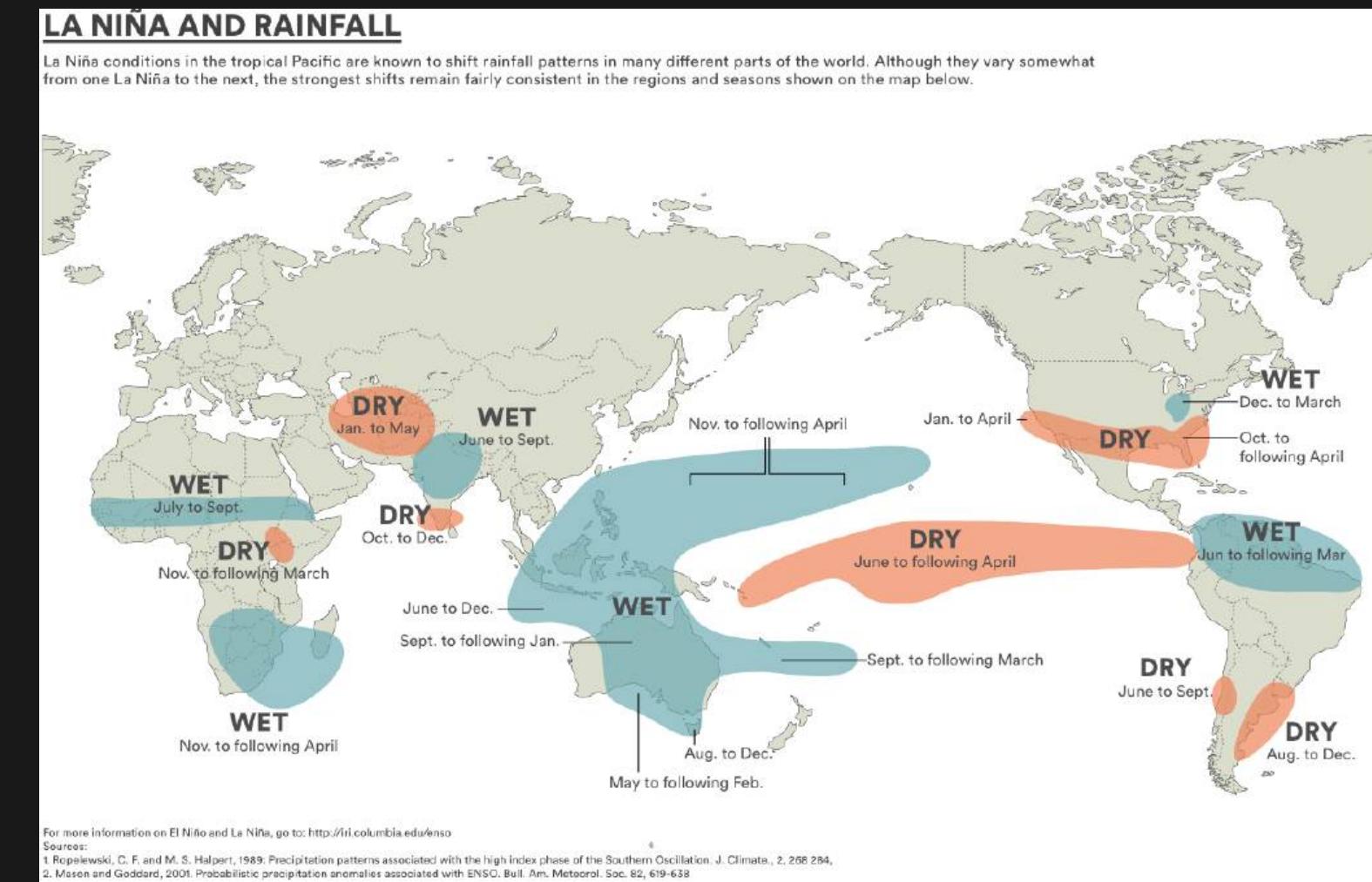
- Stronger trade winds -> warm ocean blob in the western Pacific
- Wet conditions in the West Pacific cause extreme precipitation



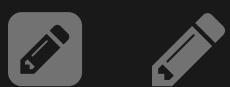
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- Stronger trade winds -> warm ocean blob in the western Pacific
- Wet conditions in the West Pacific cause extreme precipitation
- Teleconnections with Monsoon, Africa..



# Quiz time!

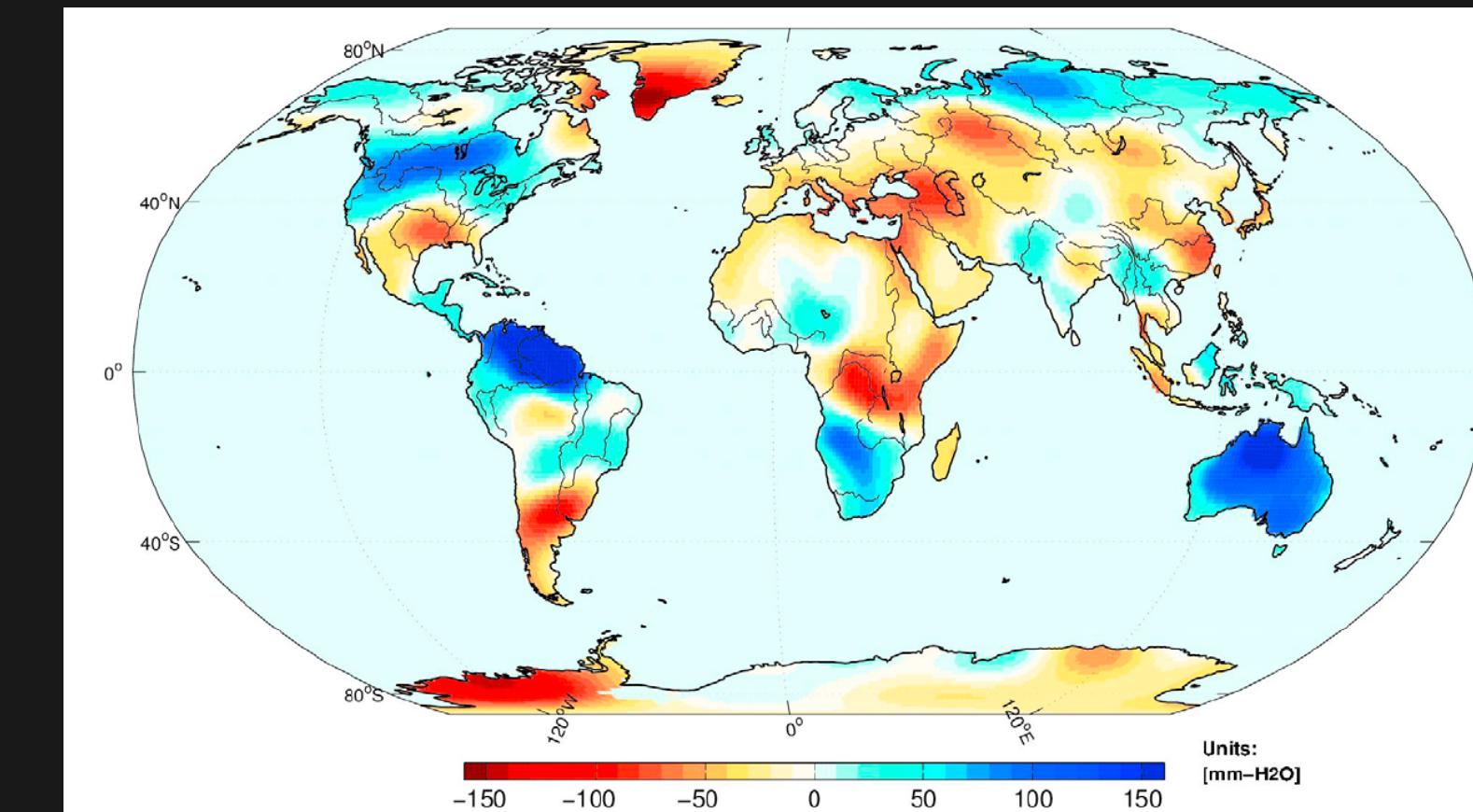
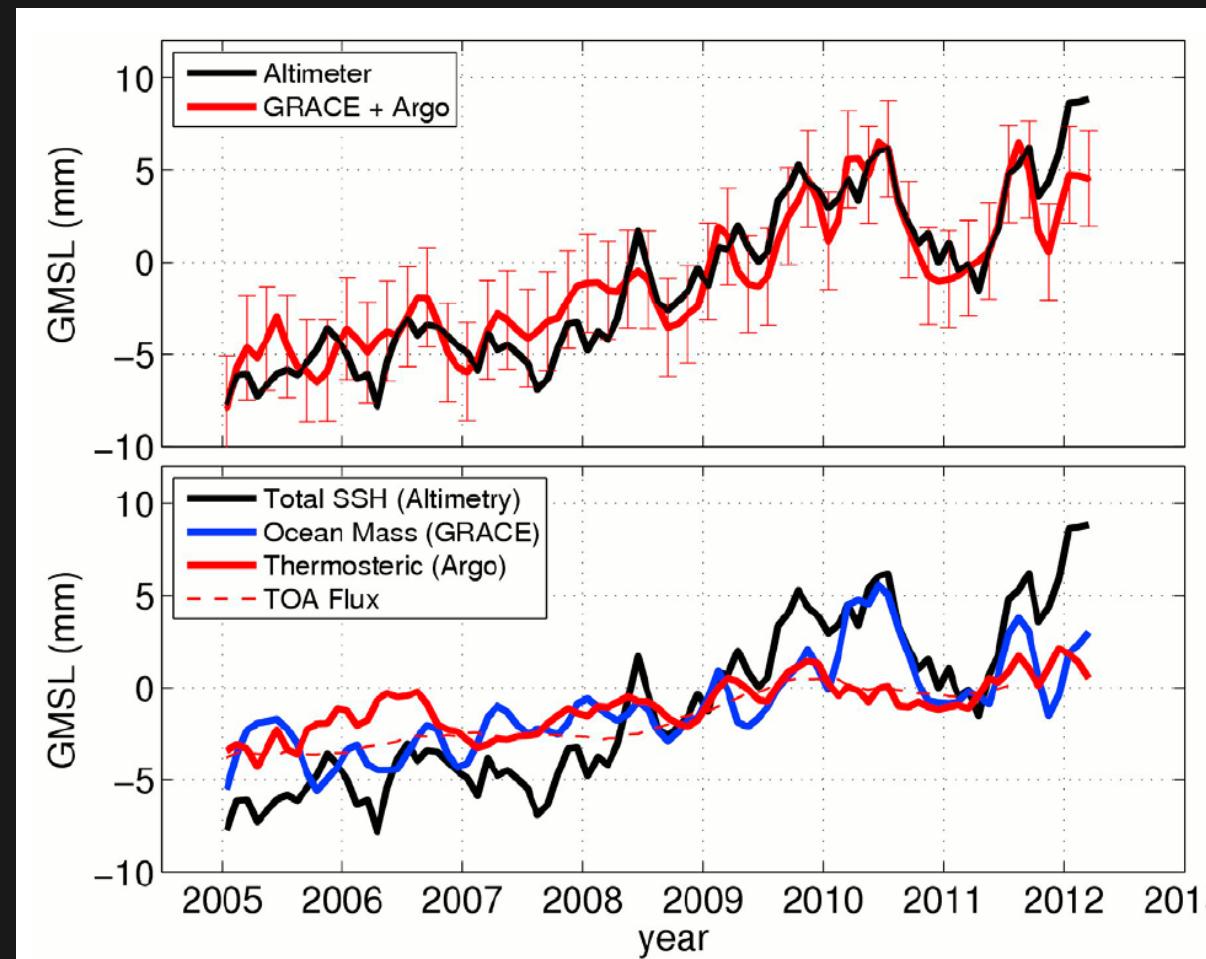
The image shows a Wooclap quiz login screen. On the left, there is a blue-tinted background image of a person holding a smartphone. Overlaid on this image is a white sidebar containing the text "Want to join an event?", the URL "www.wooclap.com/", an "Event code" input field, and a "Join" button.

The main right side of the screen displays a "Choose a method to log in" section. It includes a "Sign up" button at the top right, a "Your email address" input field with an envelope icon, and a "OR" separator. Below these are four social sign-up buttons: "Sign up with Facebook" (blue), "Sign up with Google" (blue), "Sign up with LinkedIn" (dark blue), and "Sign up with Microsoft" (blue).

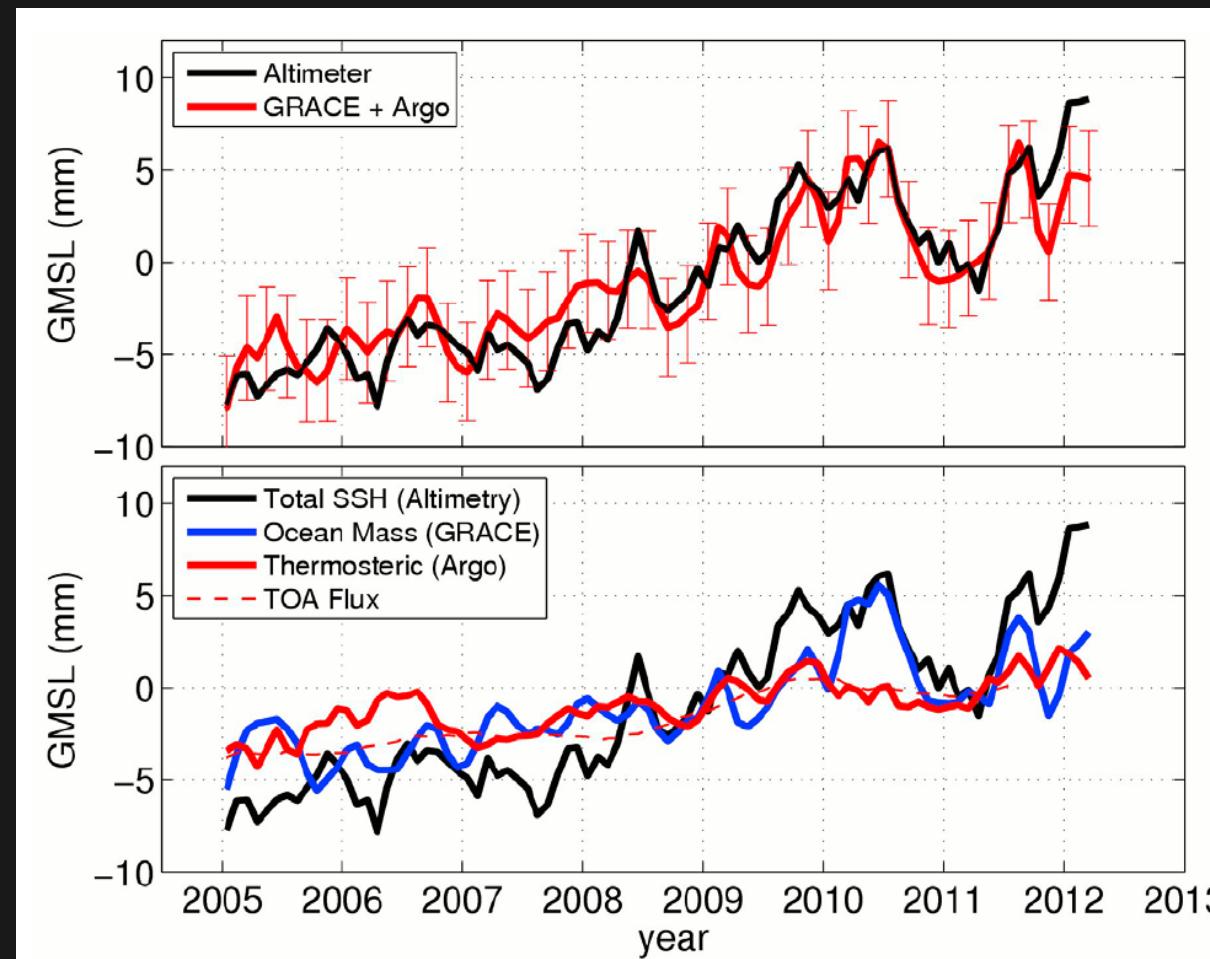
Further down, another "OR" separator leads to a "Log in with your institution" section, featuring a "Your institution" input field with a building icon. A cookie consent overlay is visible on the right, containing a circular icon with a cookie, text about cookie usage, and three buttons: "Accept all", "Reject All", and "Customise".



# 2010-2011 La Nina event

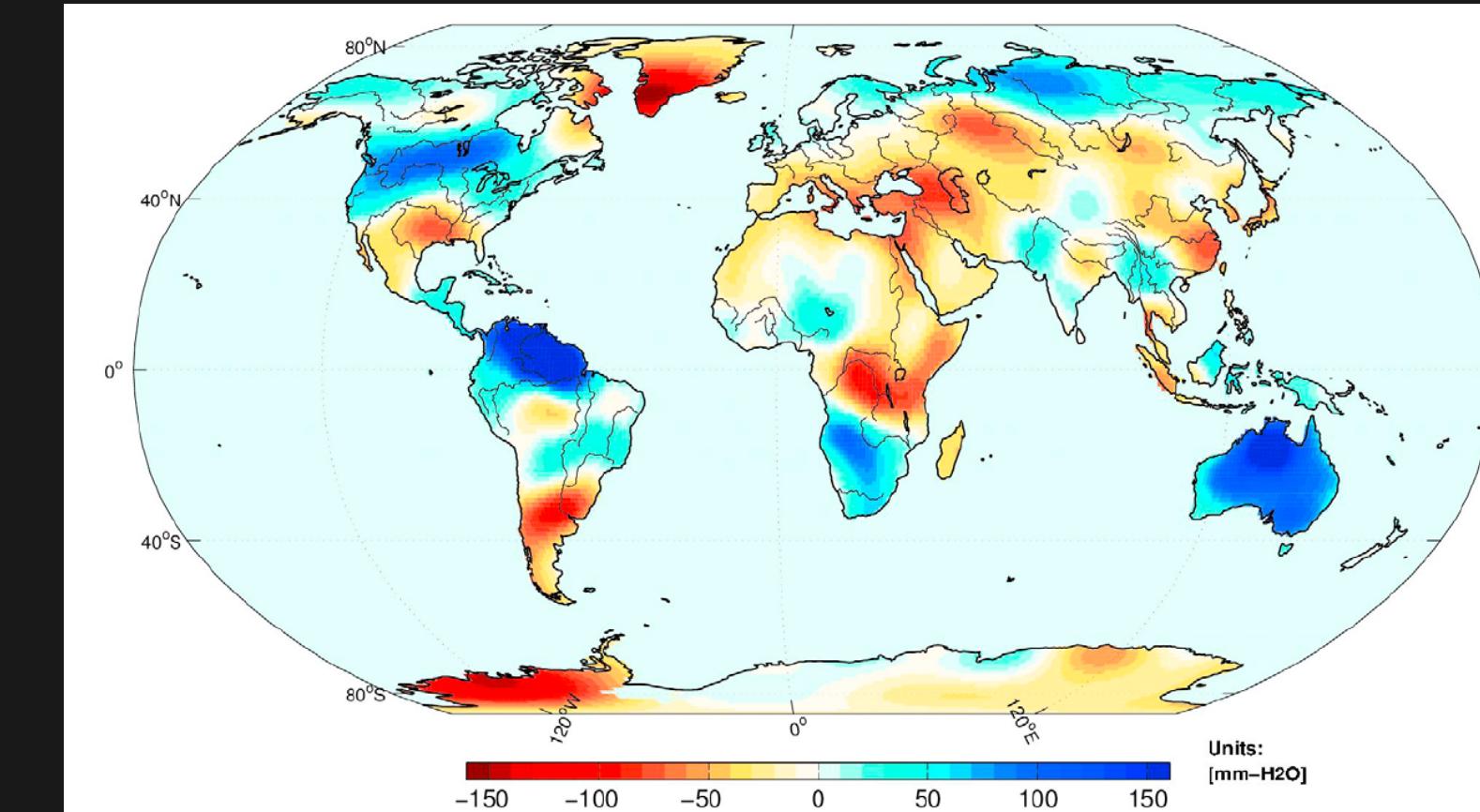


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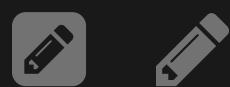


Global mean sea level variations (total, mass driven and 'steric'),  
From Böning et al. 2012

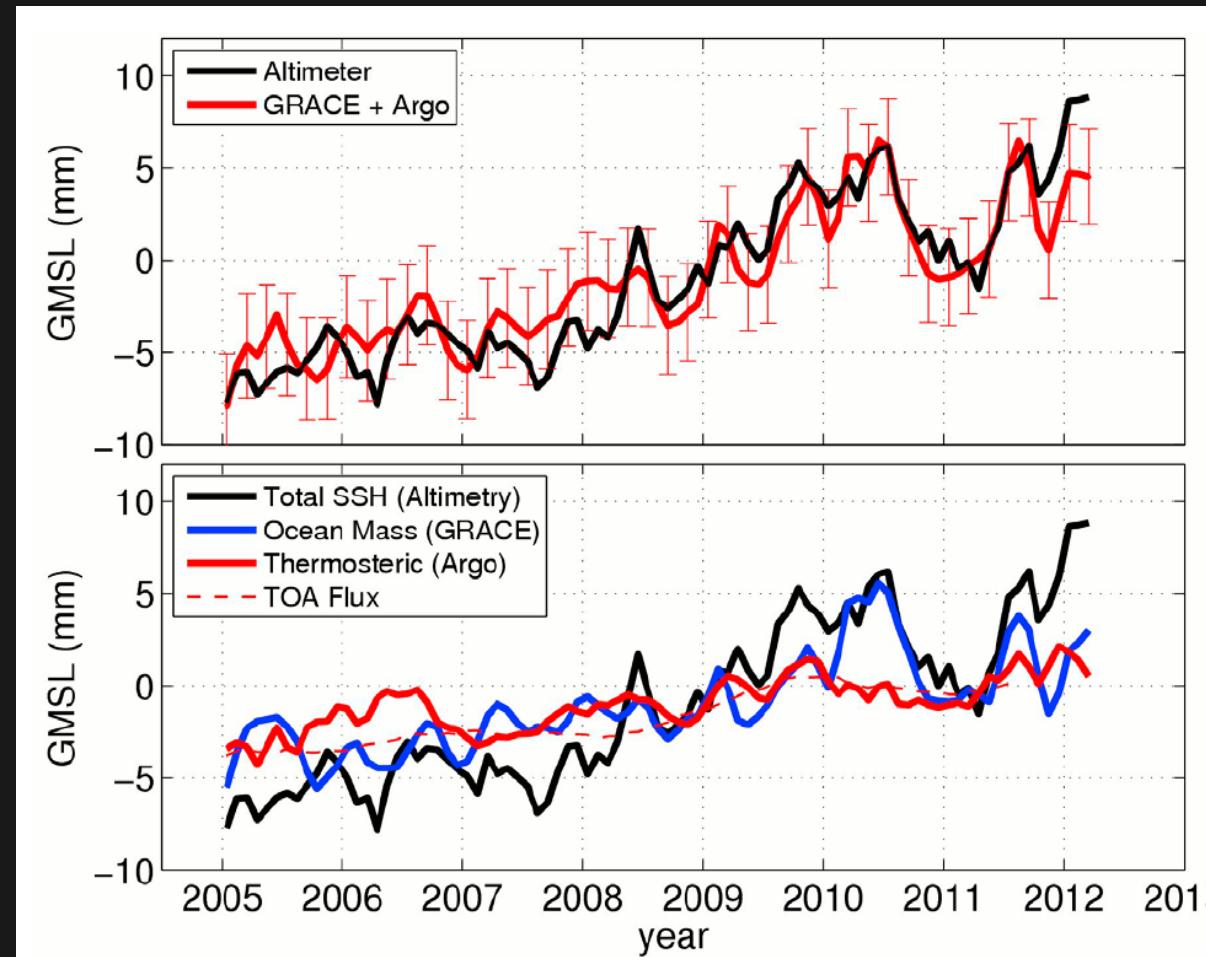
- Detectable with radar altimetry



Terrestrial water storage change (2010-2011) from GRACE, From Böning et al. 2012

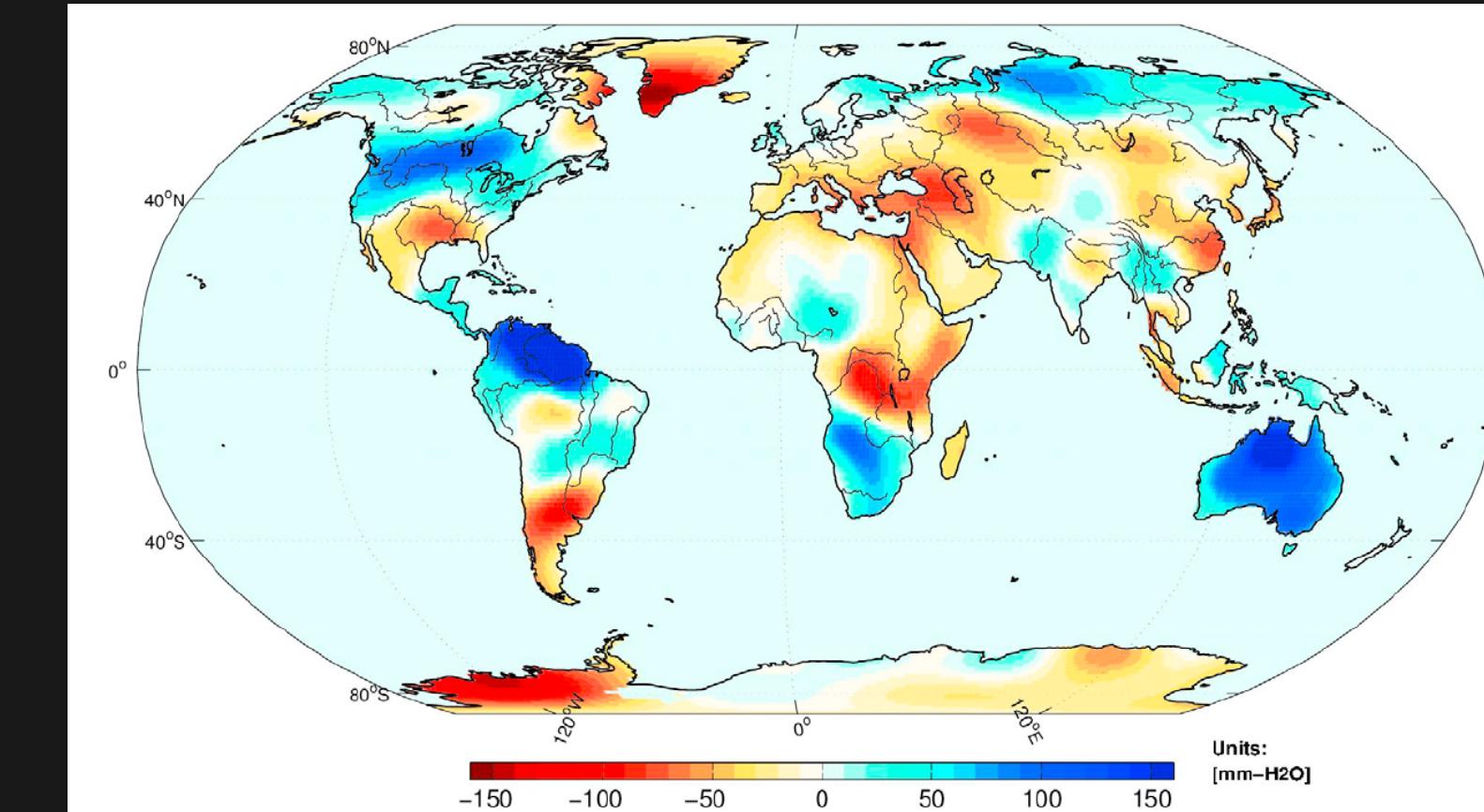


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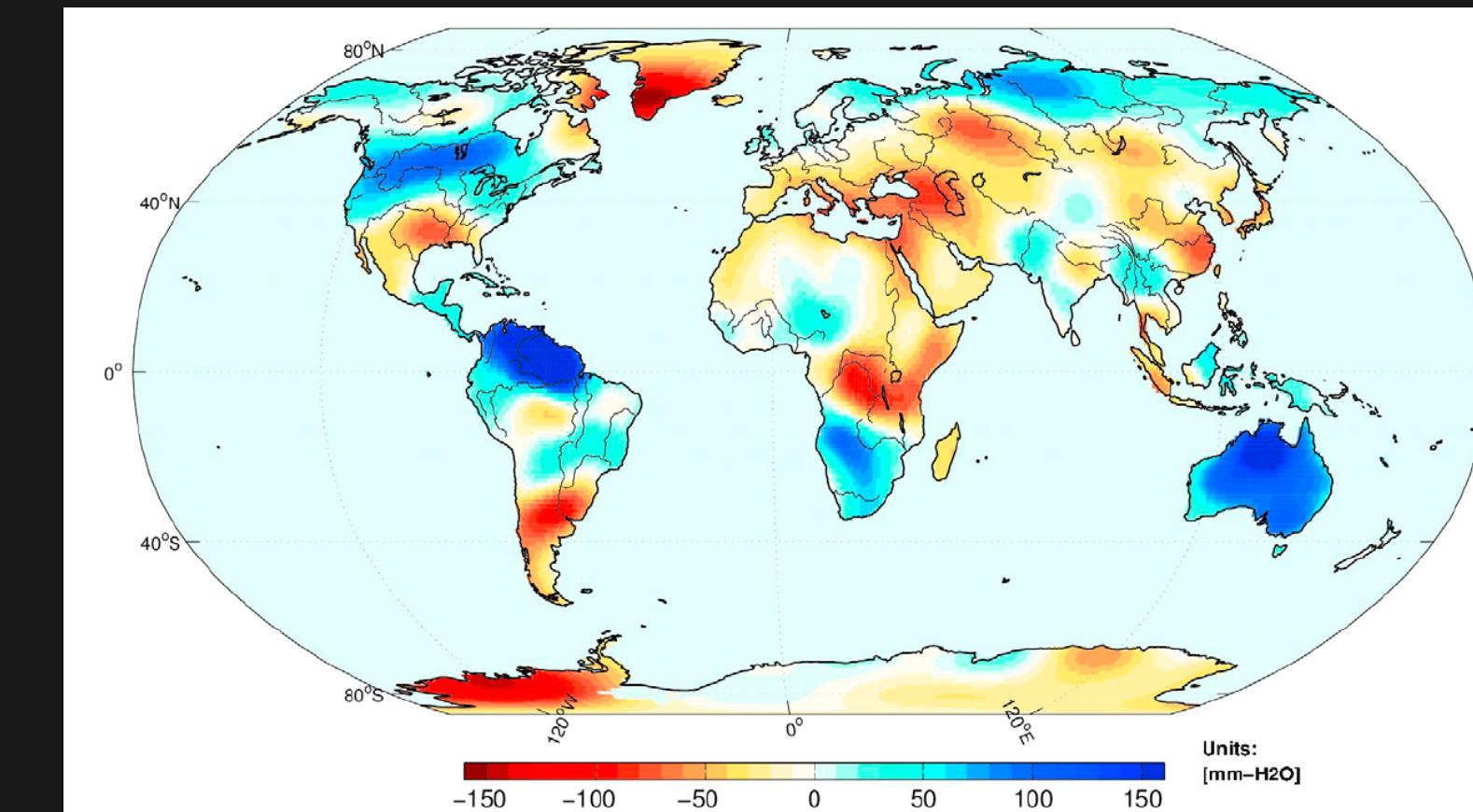
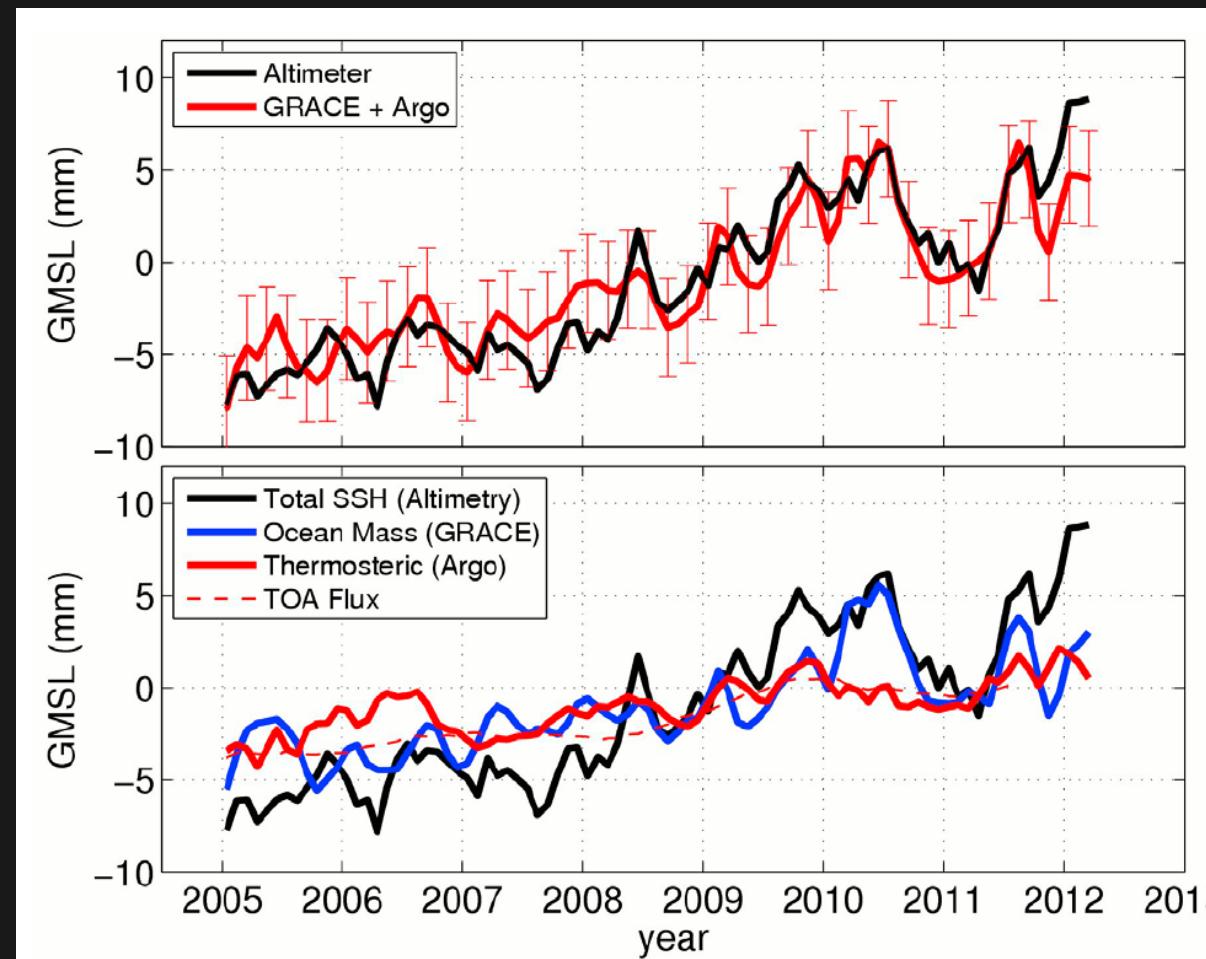
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- Can be explained by mass-driven sea level (GRACE)



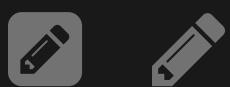
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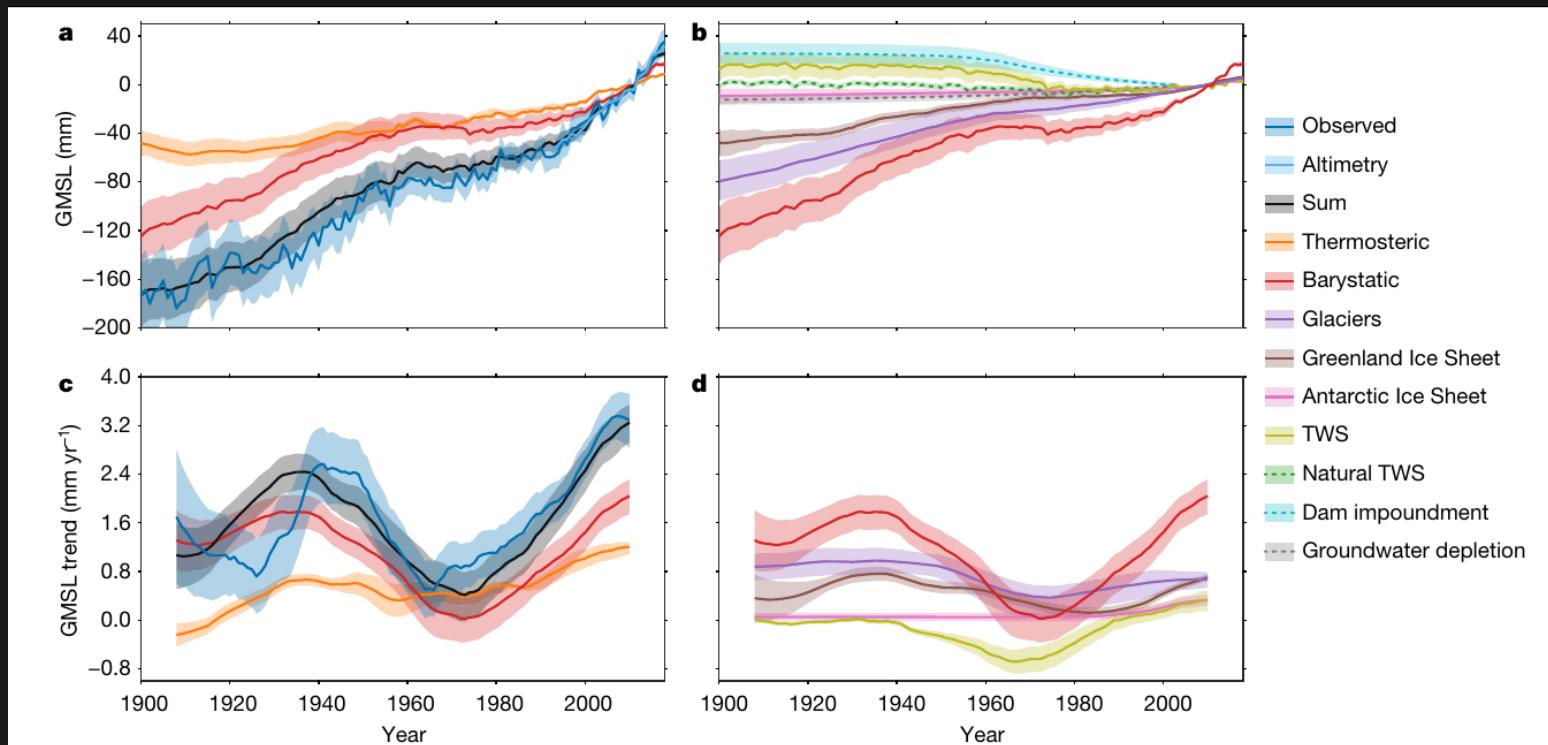
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- Can be explained by mass-driven sea level (GRACE)
- Hotspot: Australia



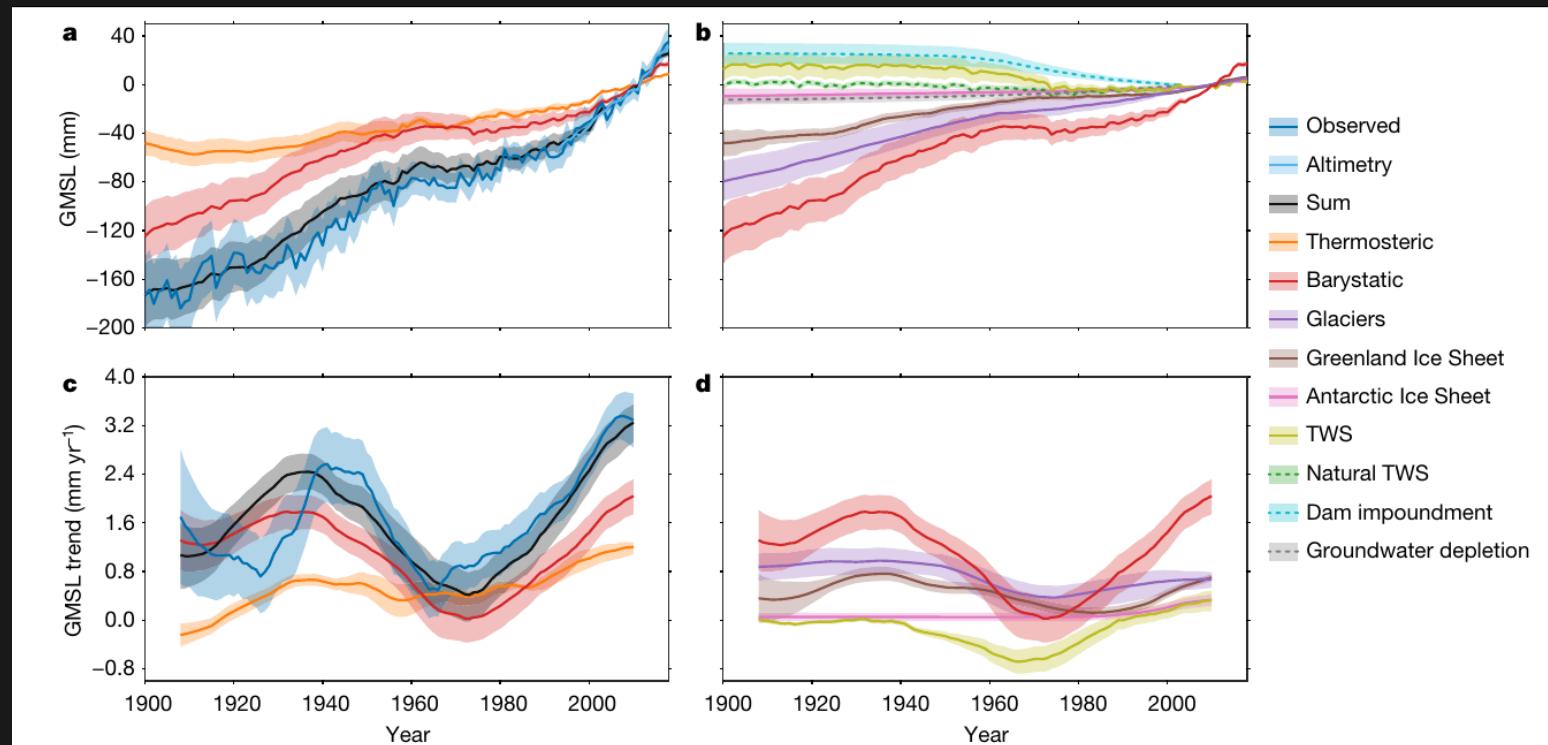
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Historic sea level can be largely explained with different (modelled) sea level contributions. From Frederikse et al. 2020



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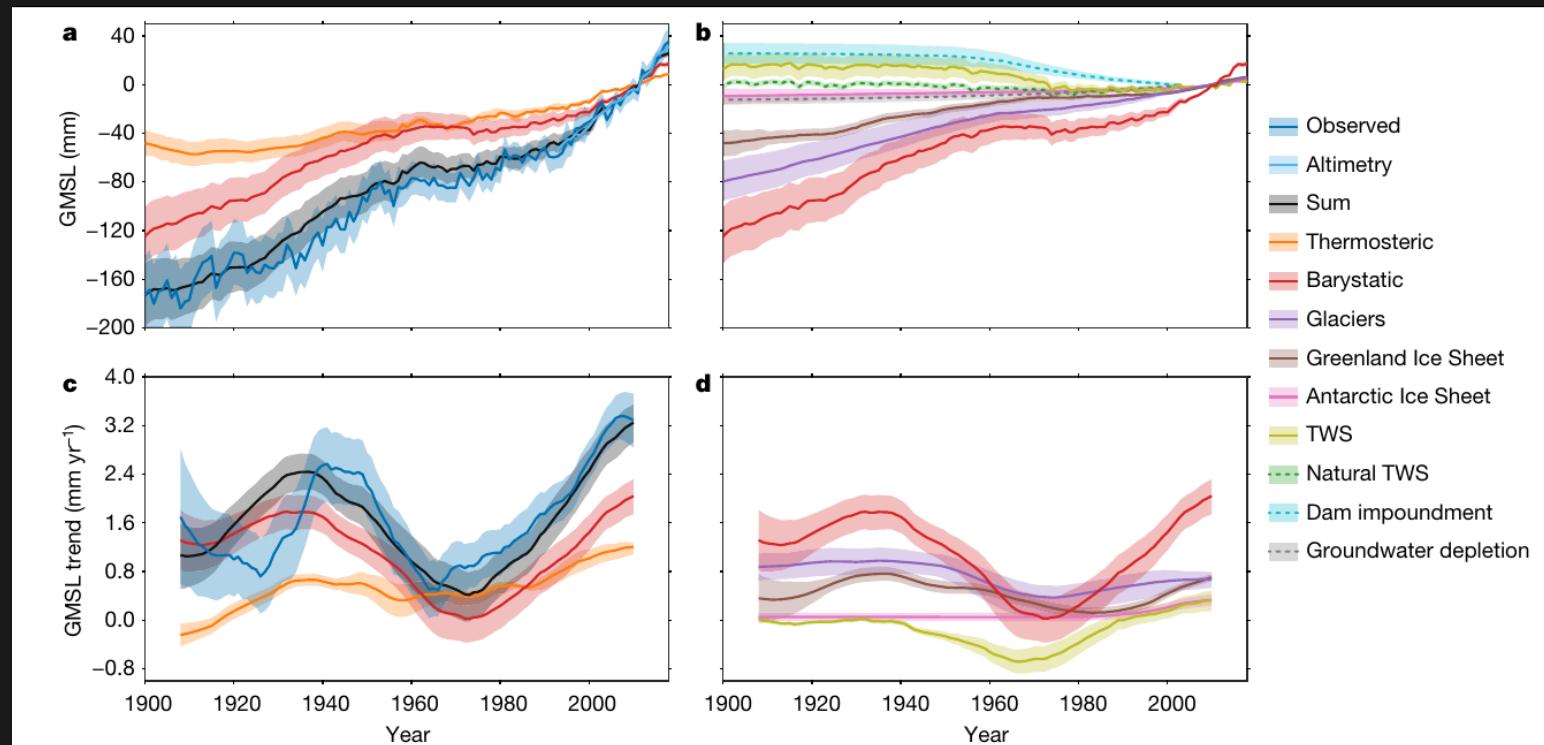


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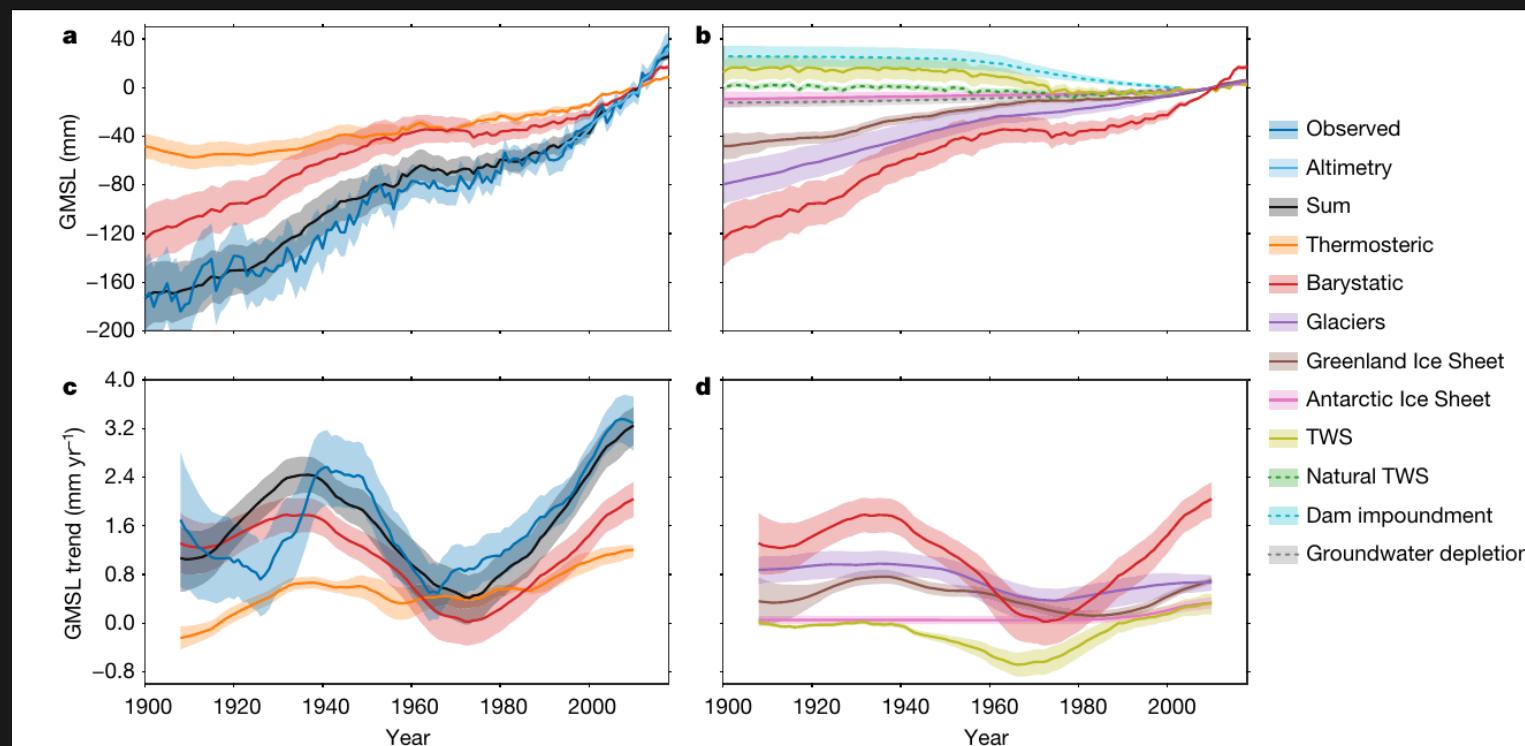


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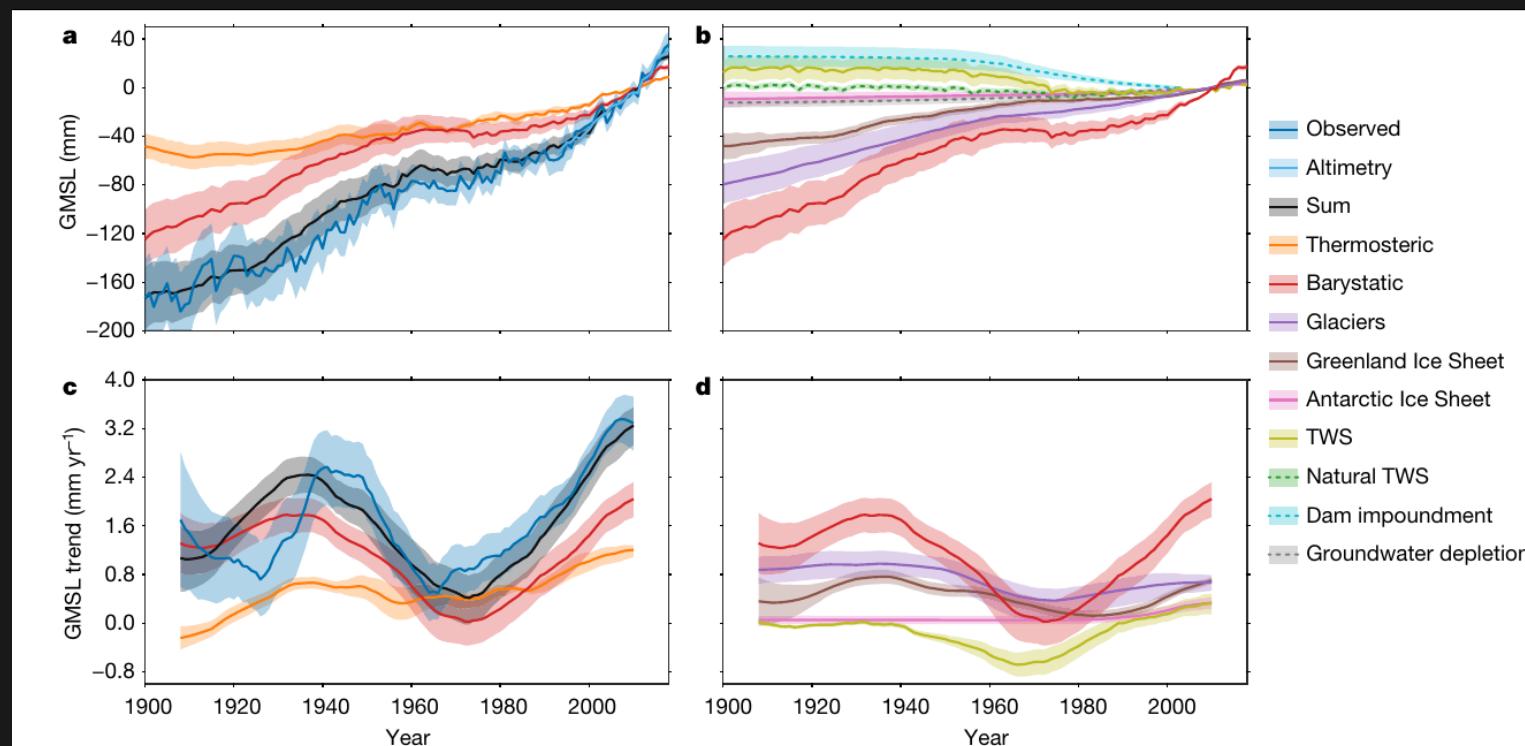


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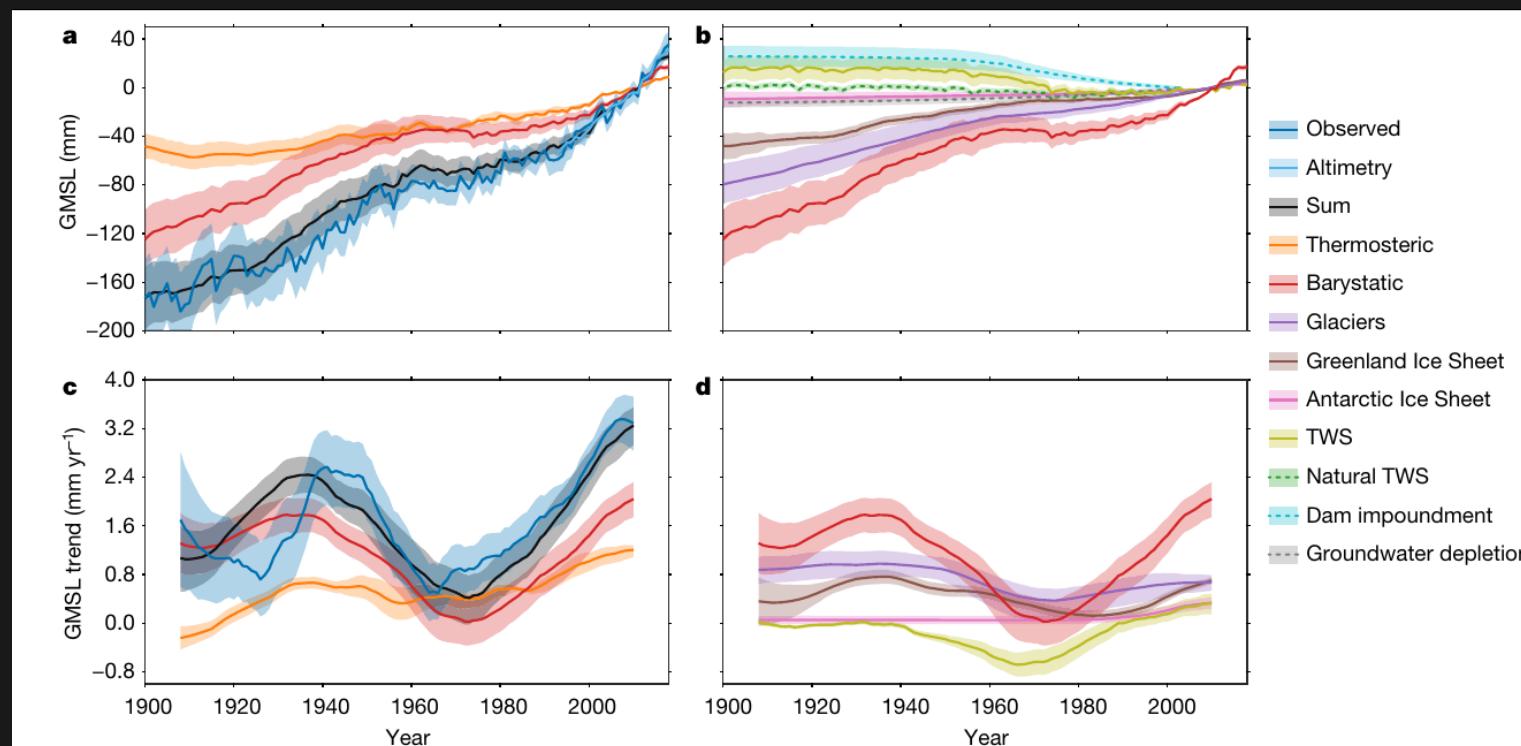


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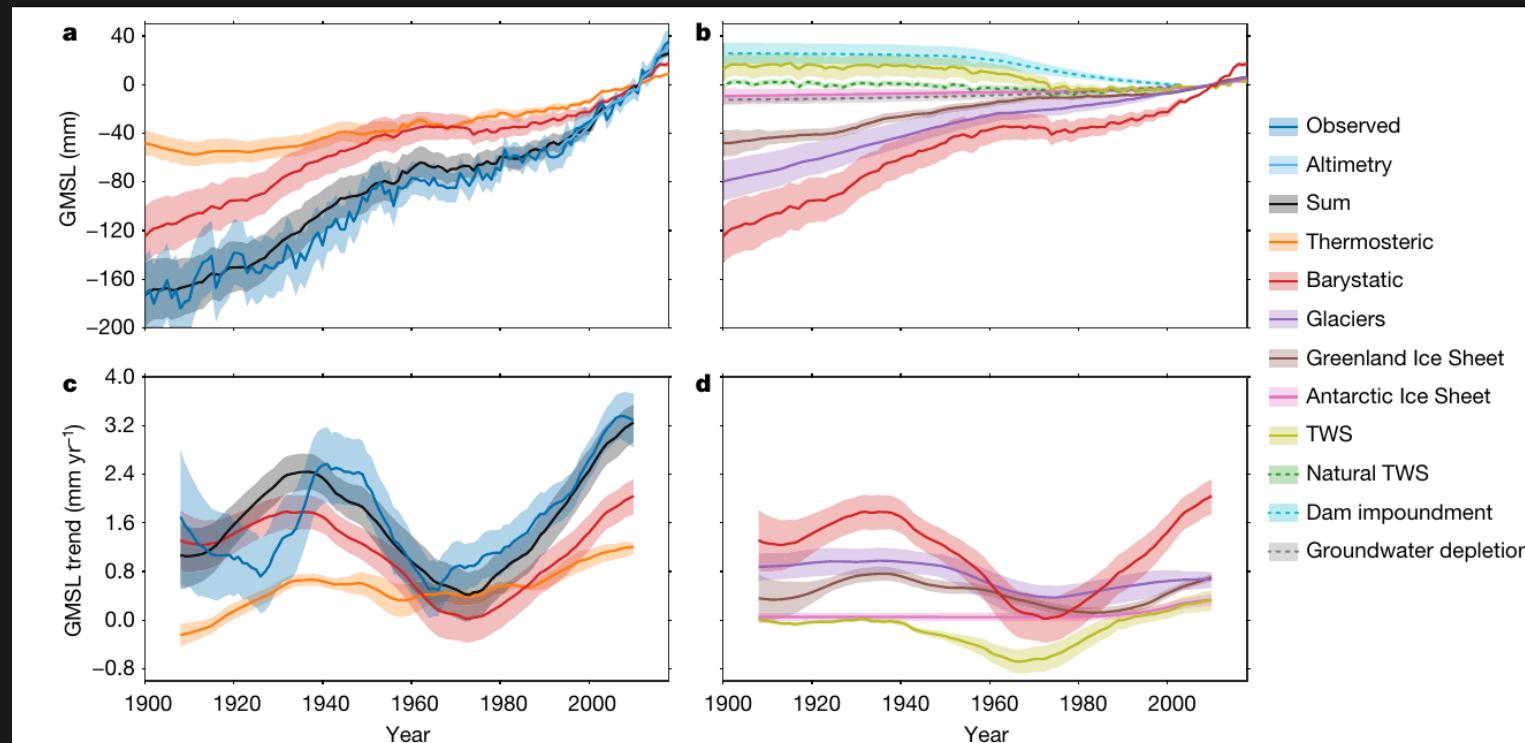


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- Recent accelerations from icesheets and glaciers -> (observable by GRACE since 2002)



# Ocean mass from GRACE (Theory)

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**Methods for inferring regional surface-mass anomalies from Gravity Recovery and Climate Experiment (GRACE) measurements of time-variable gravity**

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Department of Physics and Cooperative Institute for Research in Environmental Sciences, University of Colorado, Boulder, USA

Received 8 May 2001; revised 9 March 2002; accepted 14 March 2002; published 19 September 2002.

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$$\widetilde{\Delta\sigma}_{\text{region}} = \sum_{l,m} \frac{K_l}{\Omega_{\text{region}}} (W_{lm}^c \Delta C_{lm} + W_{lm}^s \Delta S_{lm}). \quad (27)$$



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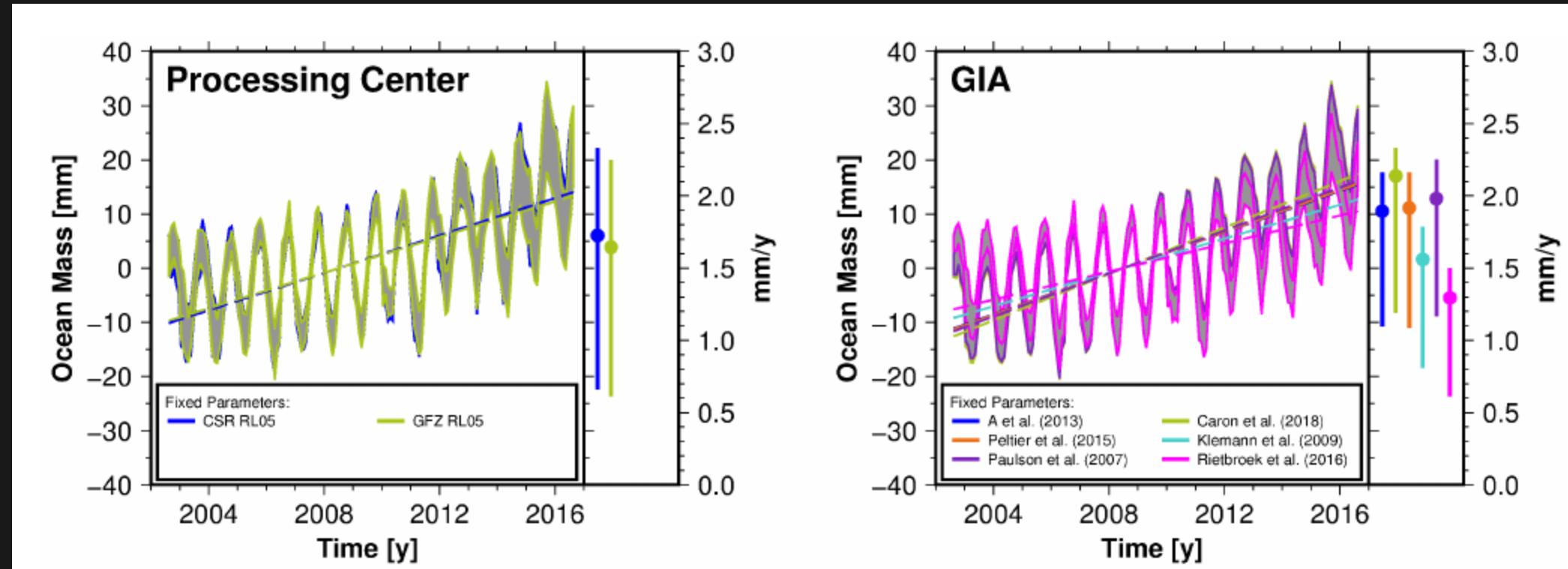
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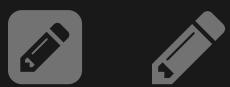
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- Averaging can be done purely in the spectral domain
  - dot product of smoothed basin coefficients with GRACE-TWS coefficients



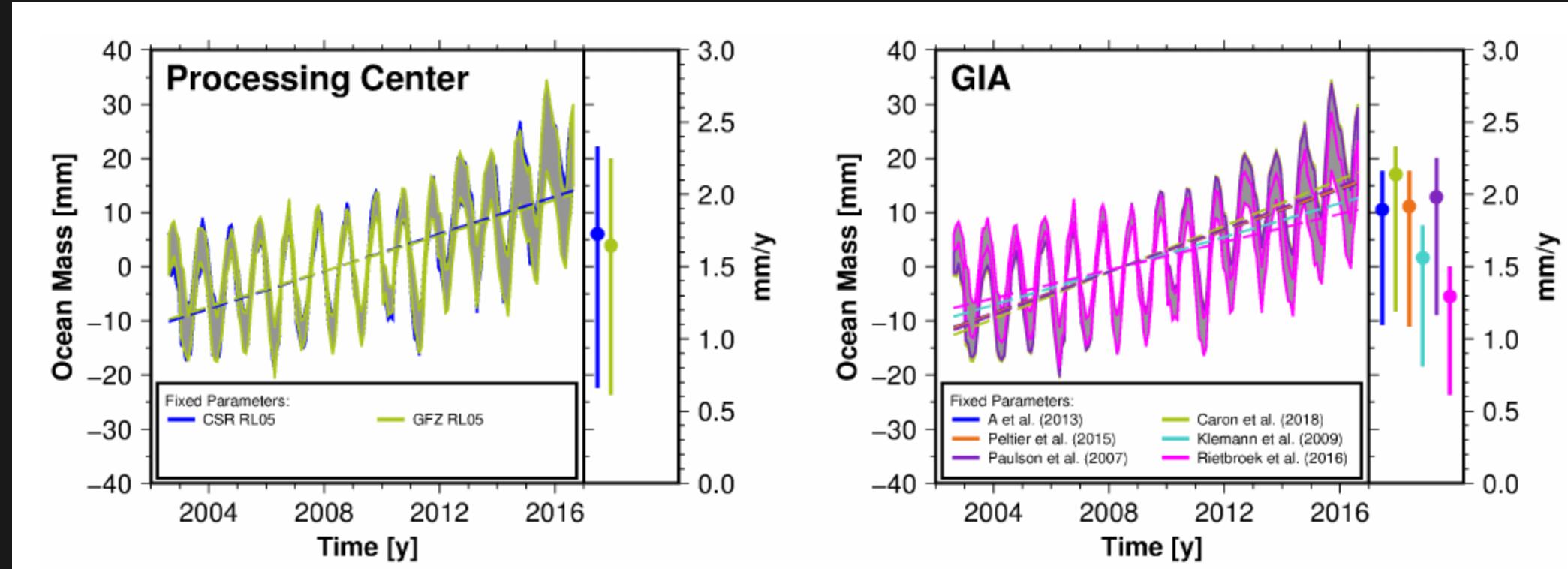
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Effect of different processing choices on ocean mass estimates, from Uebbing et al. 2019

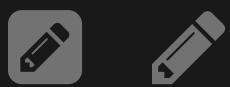


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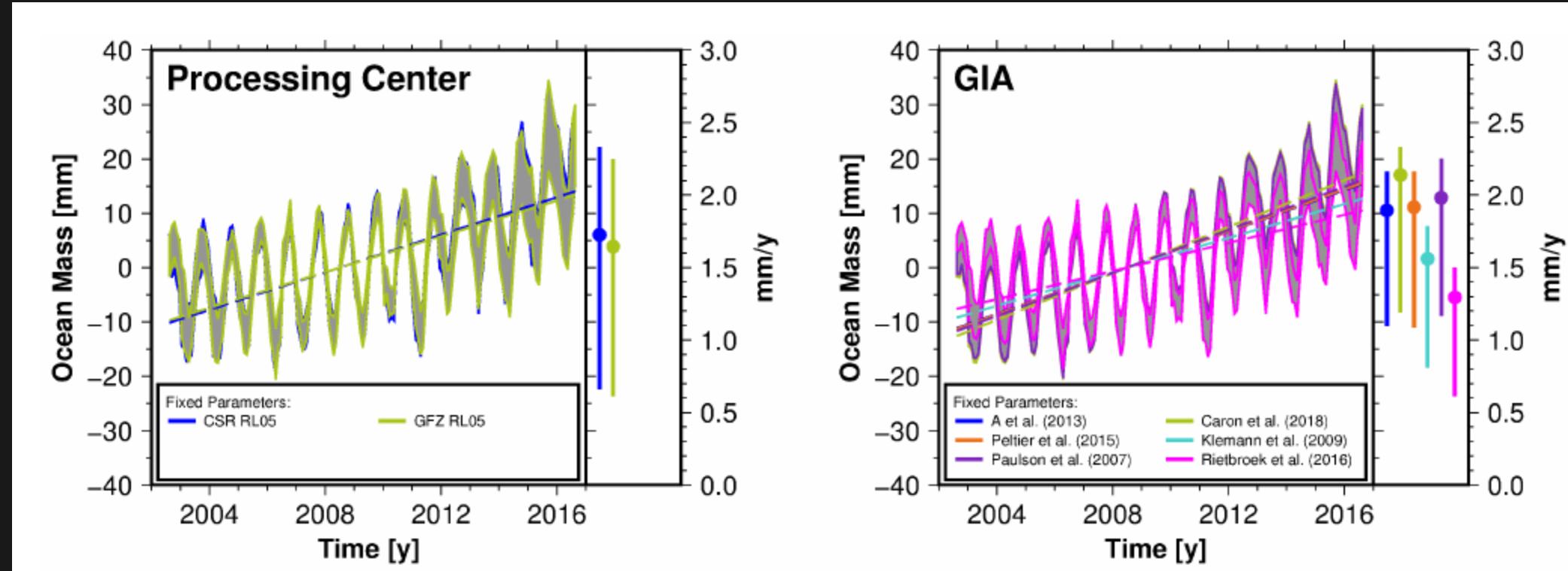


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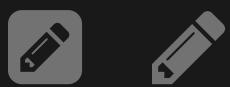


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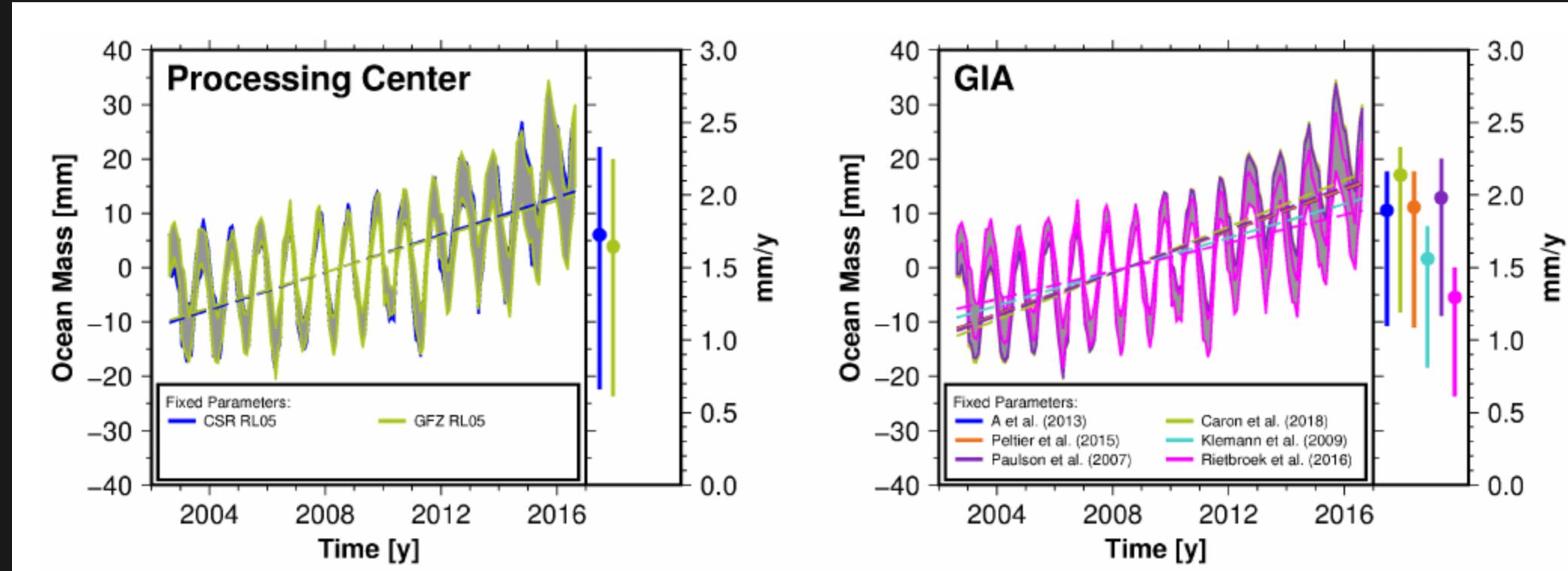


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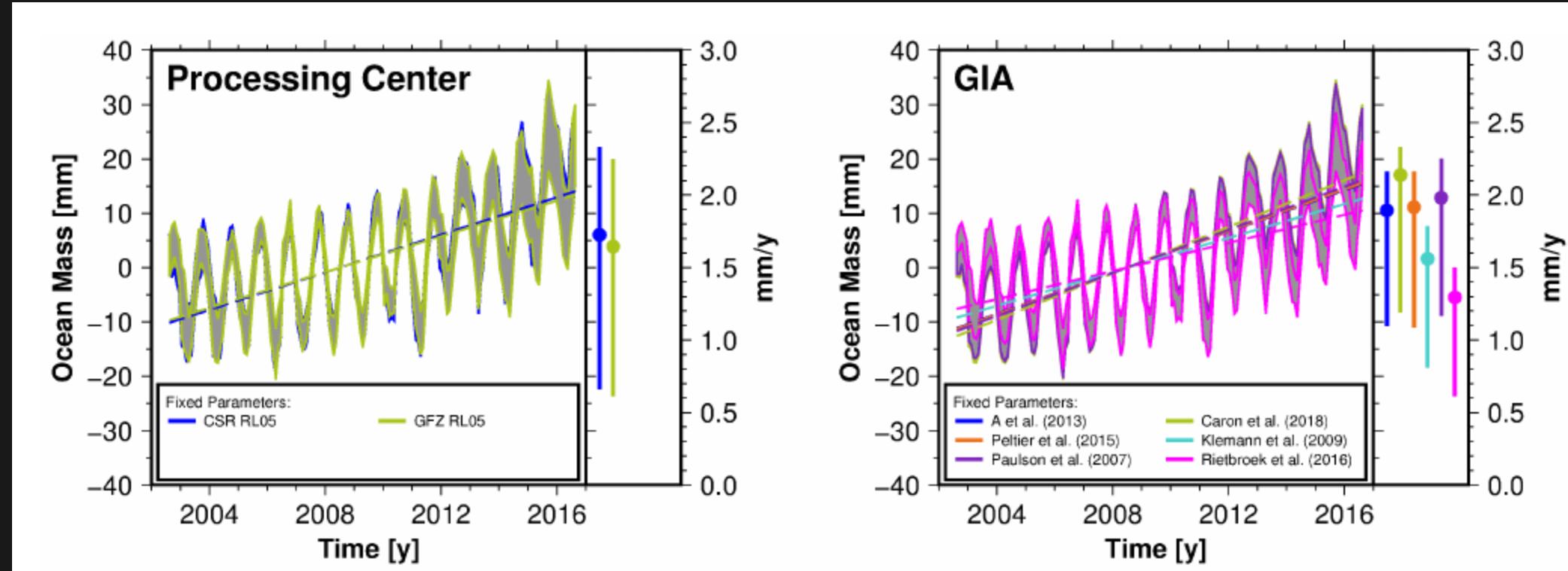


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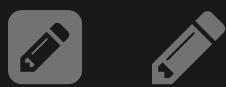


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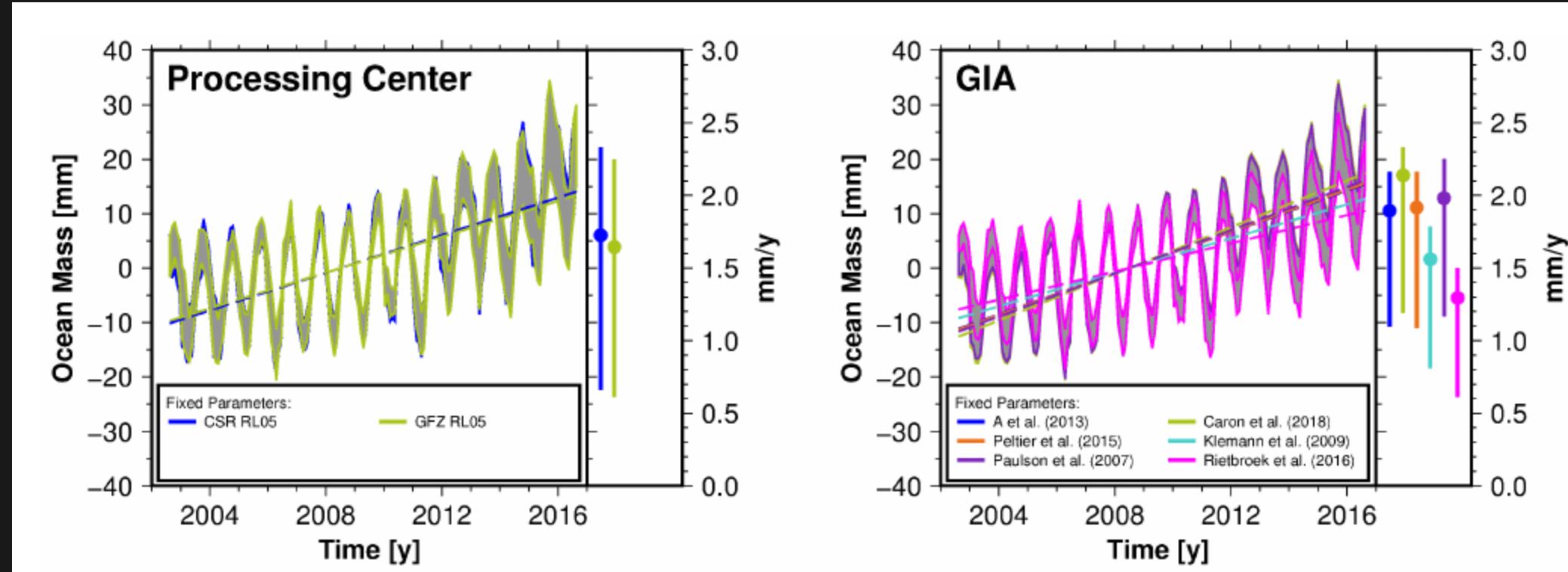


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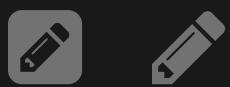


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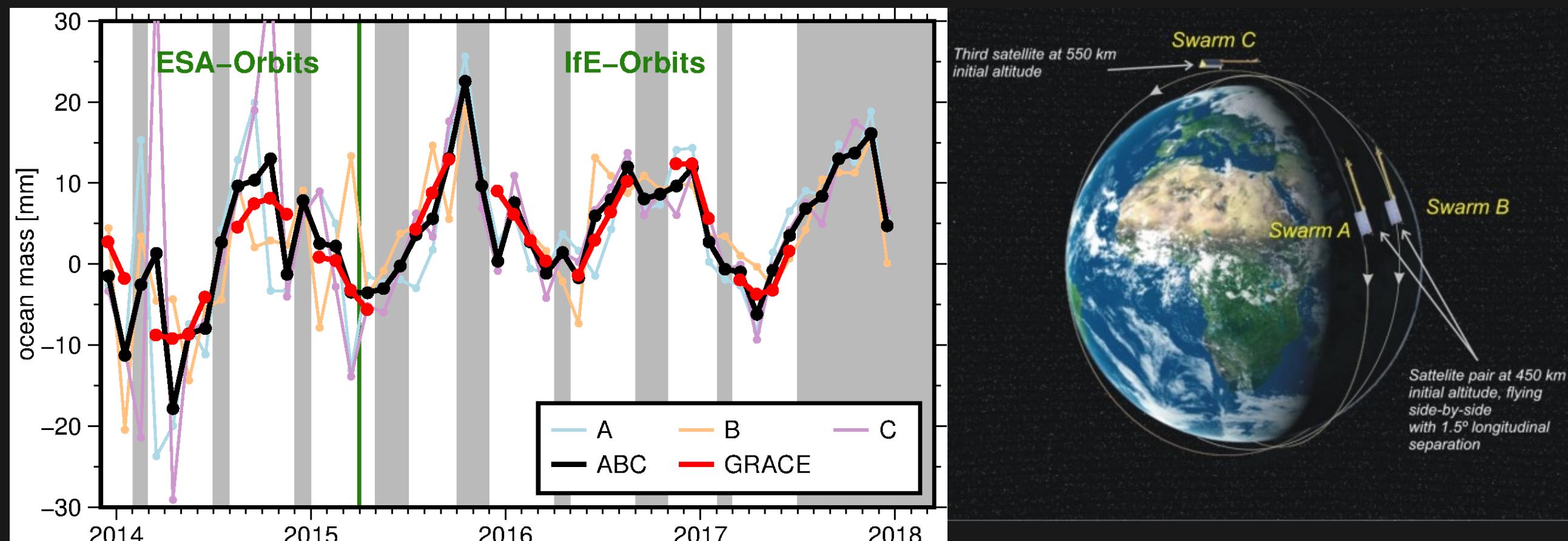


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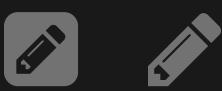
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  - Current mass trends  $\sim$ 1.5-2mm/yr (c.f. total trend  $\sim$ 3.3 mm/yr)



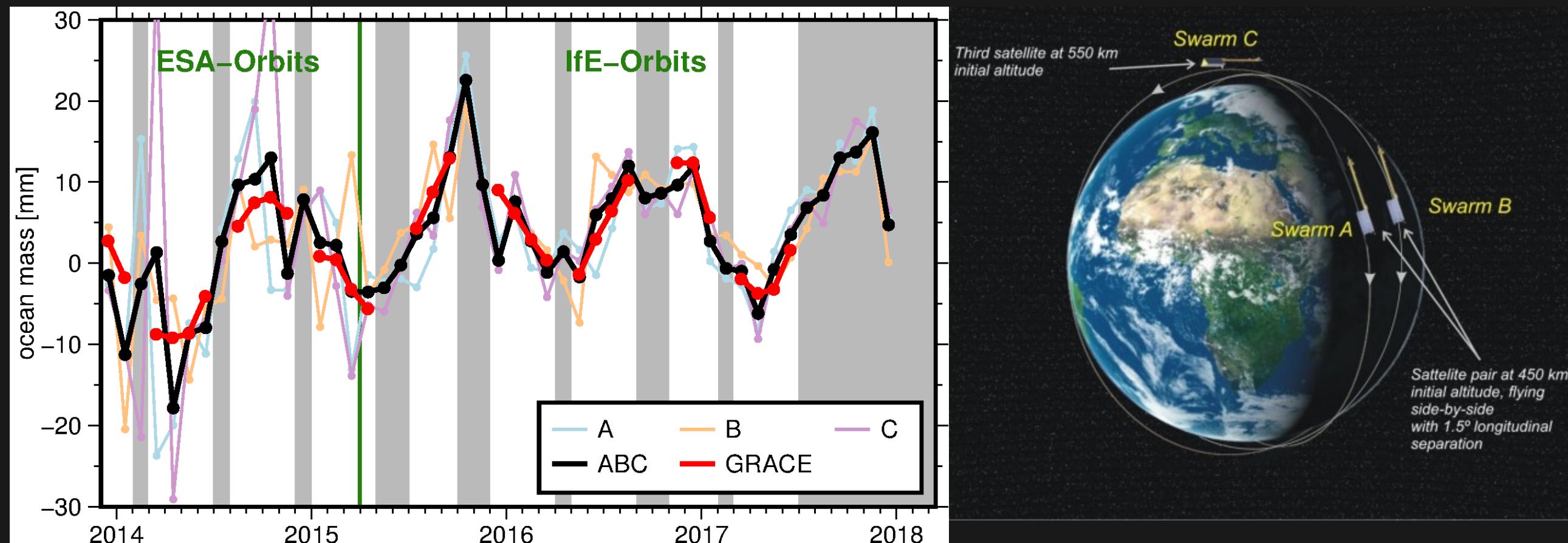
# Ocean mass from the SWARM Mission



Comparison of ocean mass from GRACE and the SWARM (A,B,C satellites). Update of Luck et al. 2018

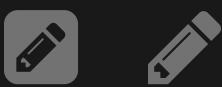


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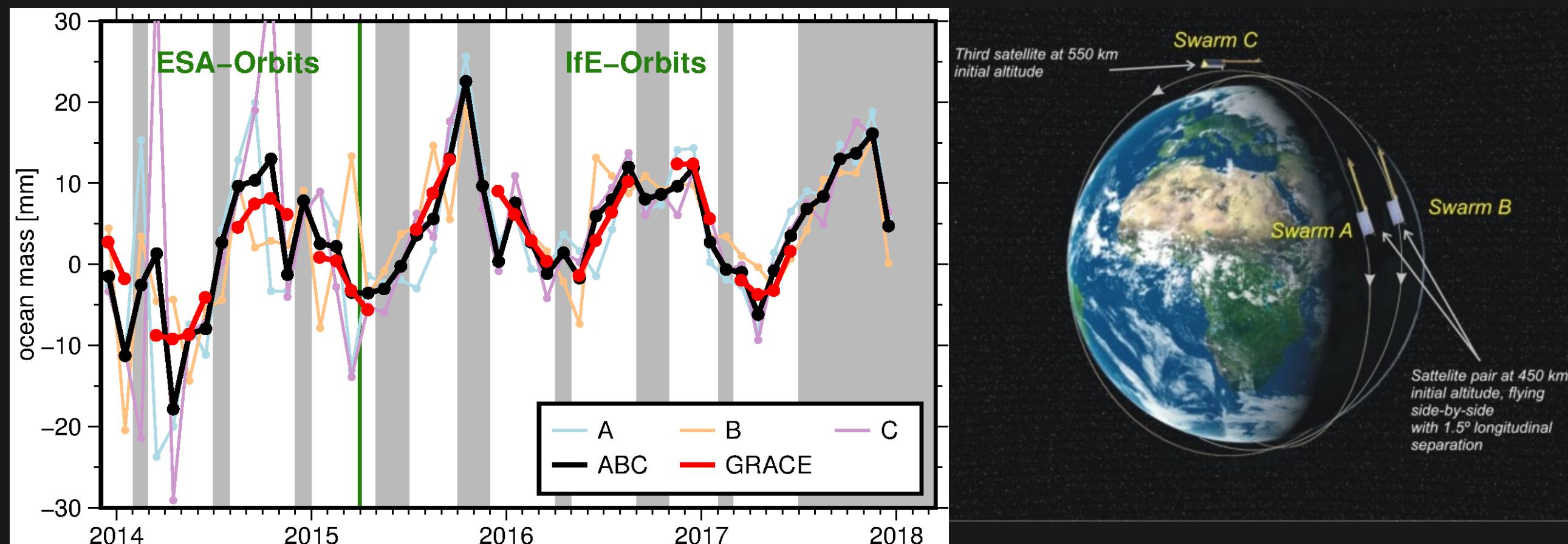


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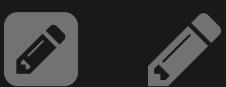


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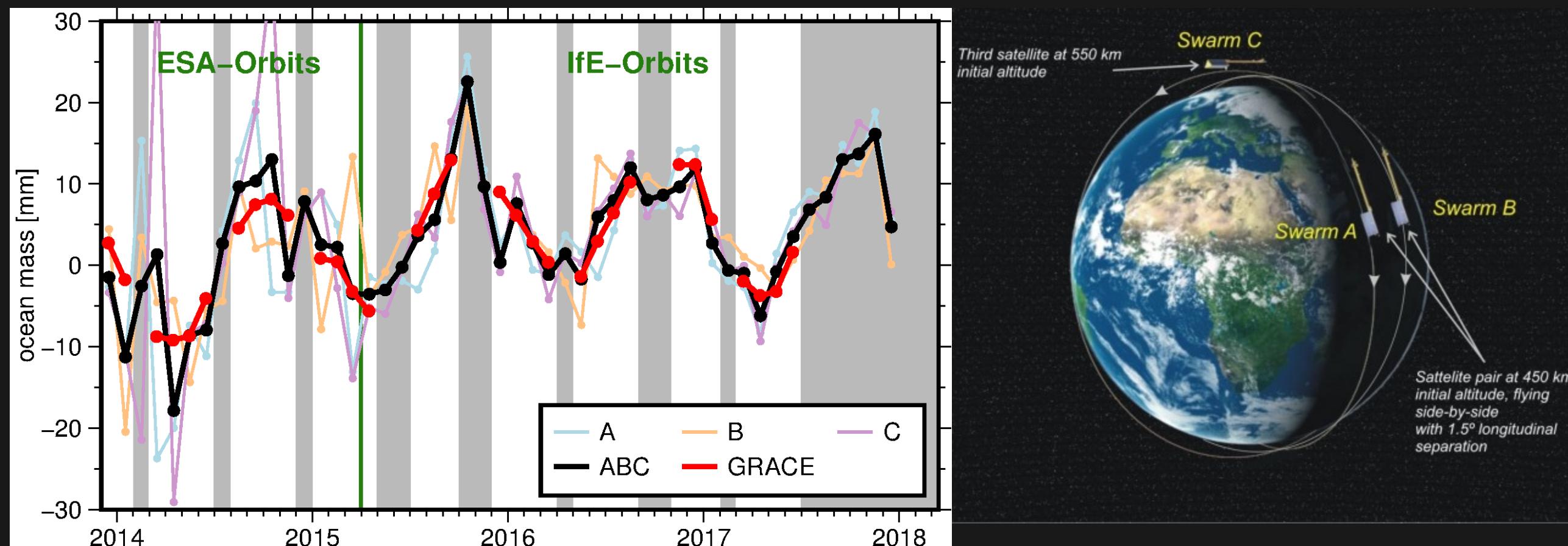


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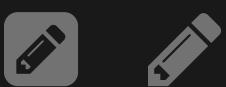


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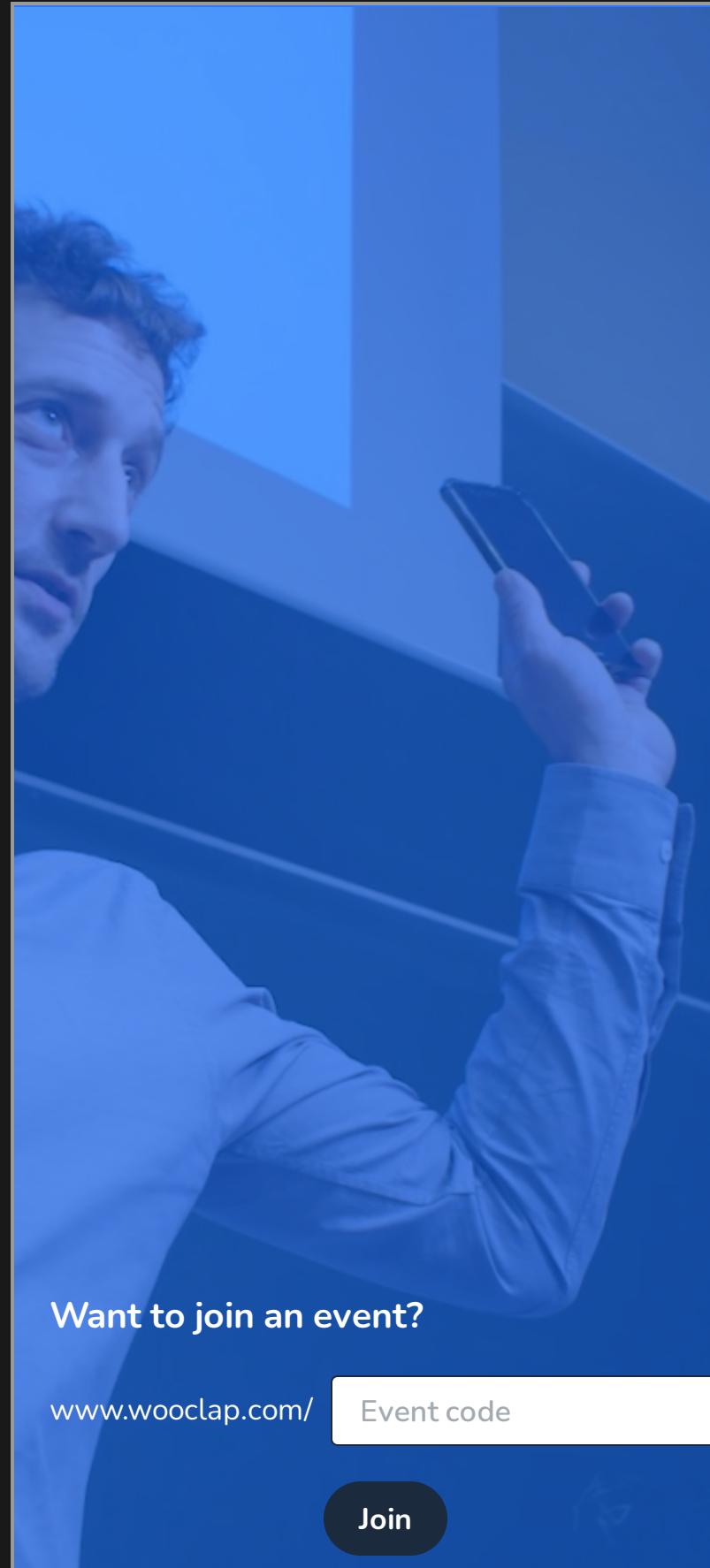


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- Precise (kinematic) orbits contain information on low-resolution gravity changes -> ocean scales
- Principle is useful for filling gaps and potentially pre-GRACE era



# Does Greenland induce regional sea level changes?



Want to join an event?

[www.wooclap.com/](http://www.wooclap.com/)

Event code

Join



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Your email address

OR

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Sign up with LinkedIn

Sign up with Microsoft

OR

Log in with your institution

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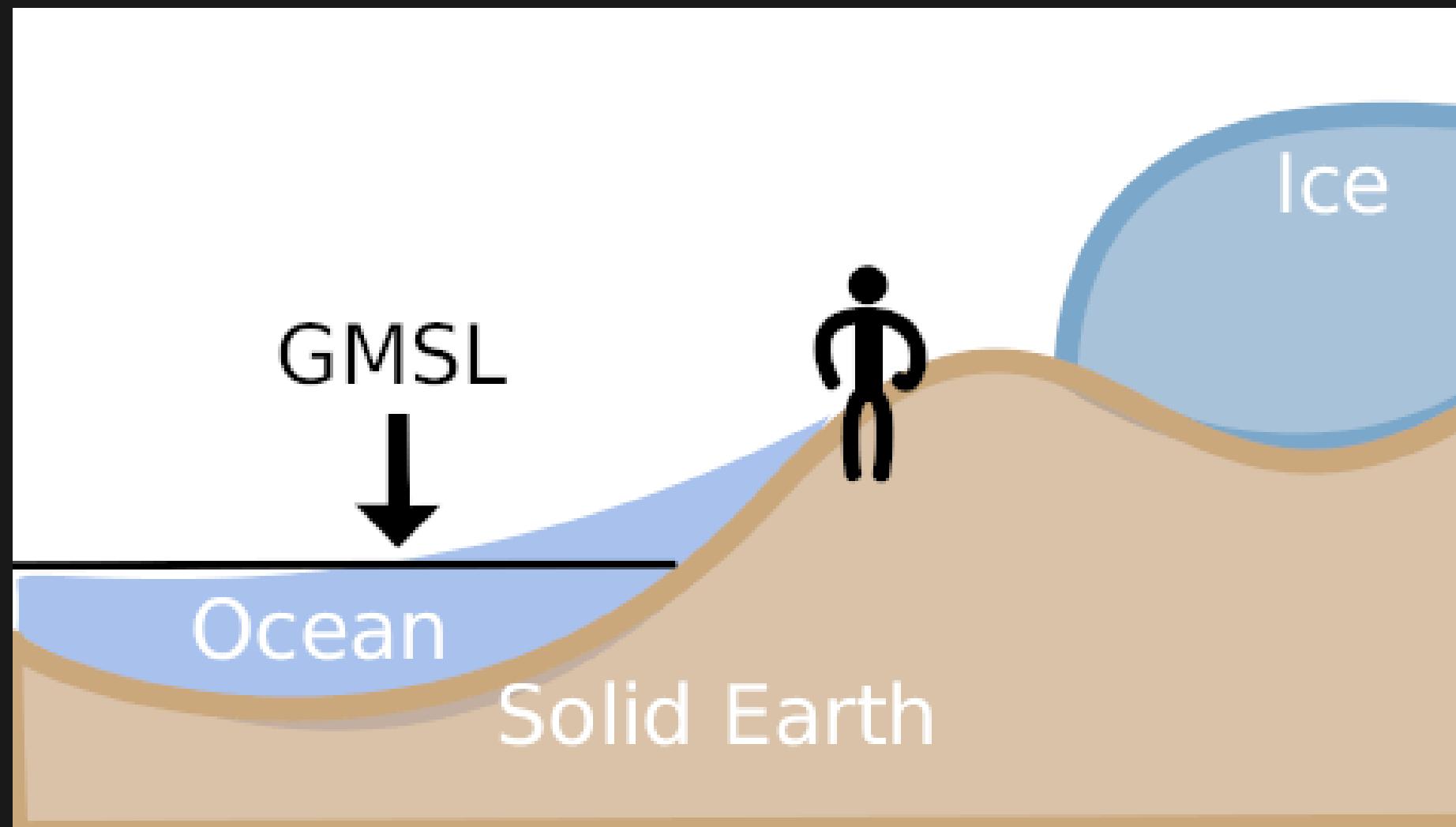
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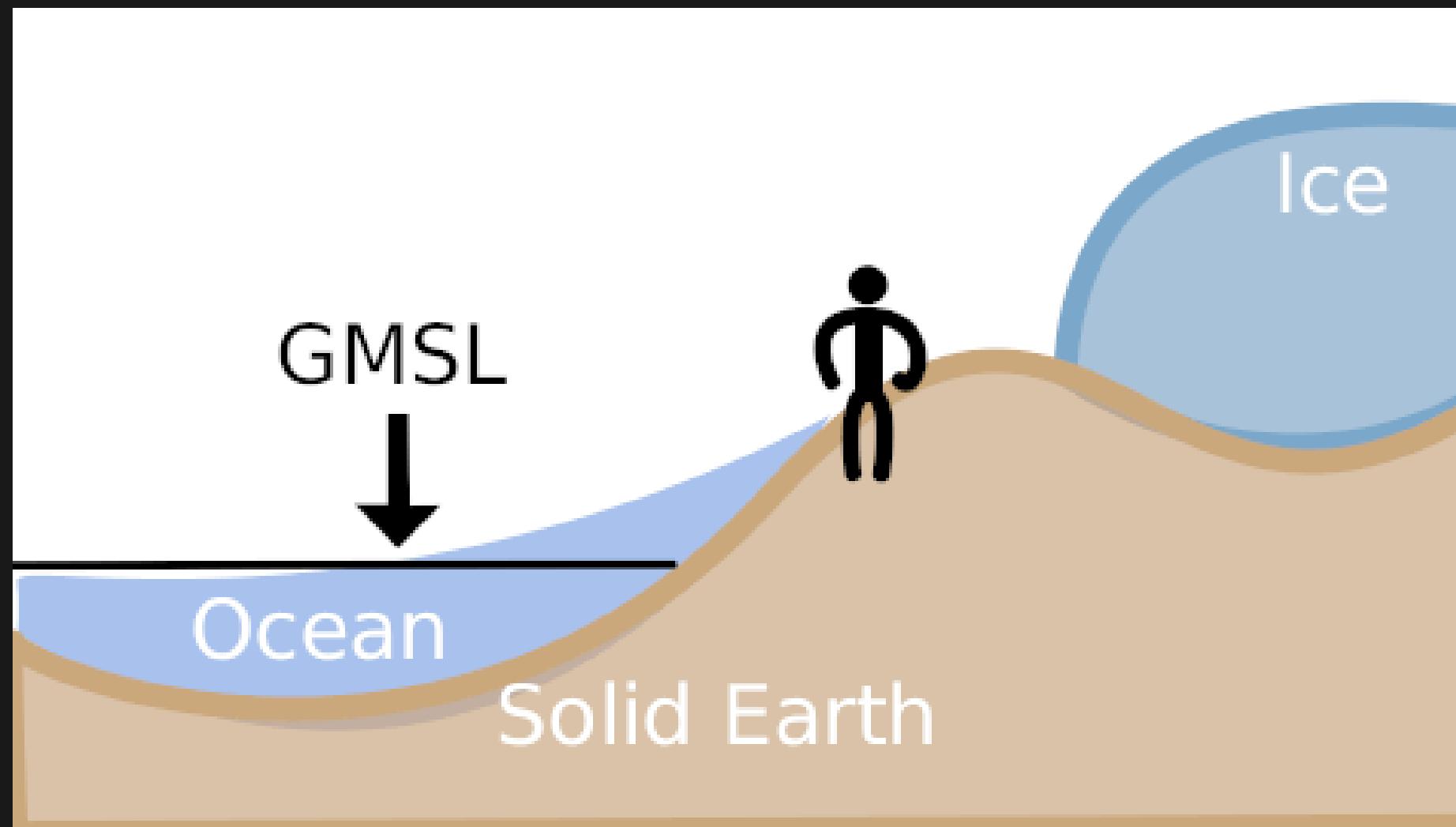
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Relative sea level is affected by self attraction and loading (SAL)..

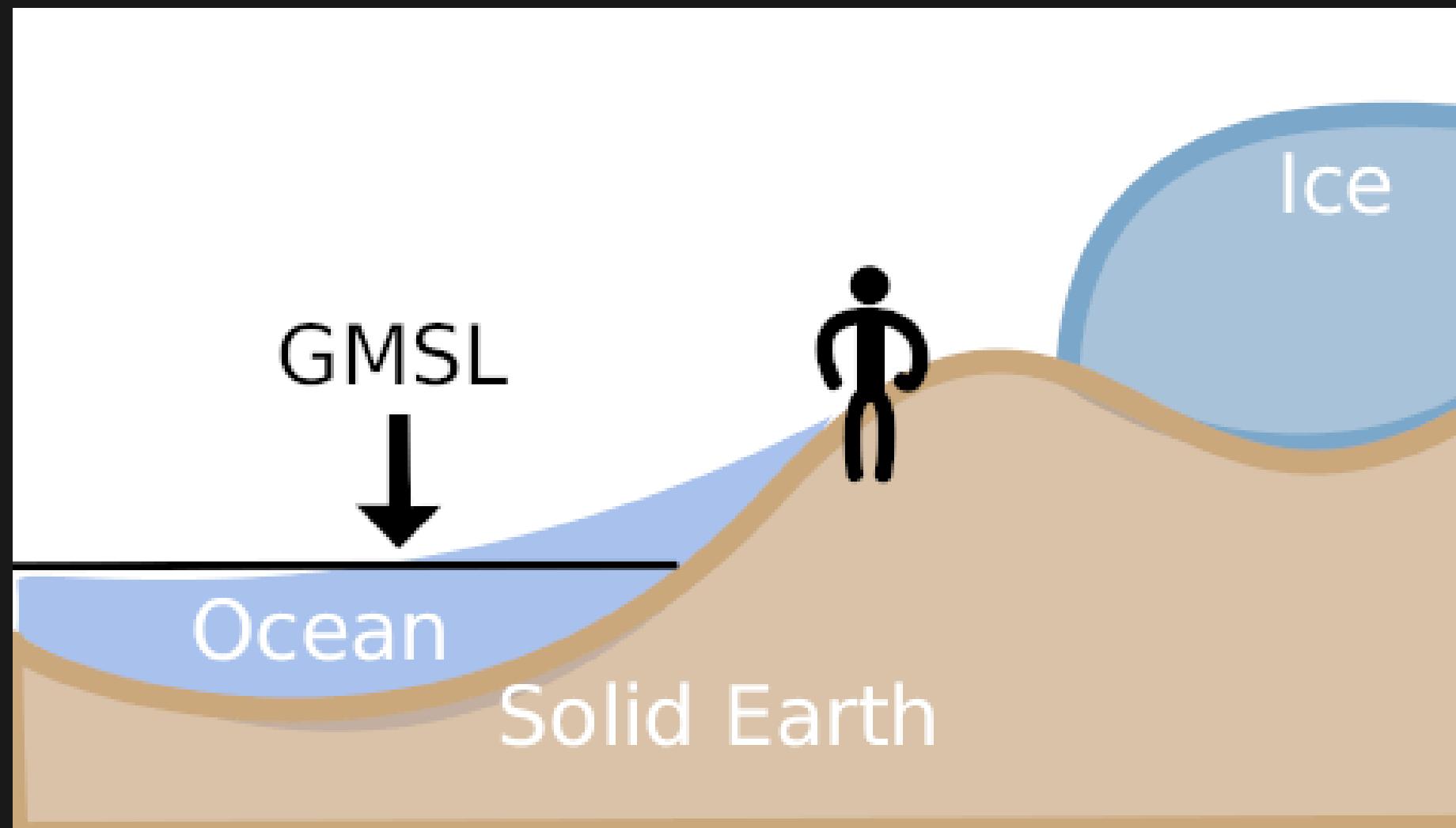


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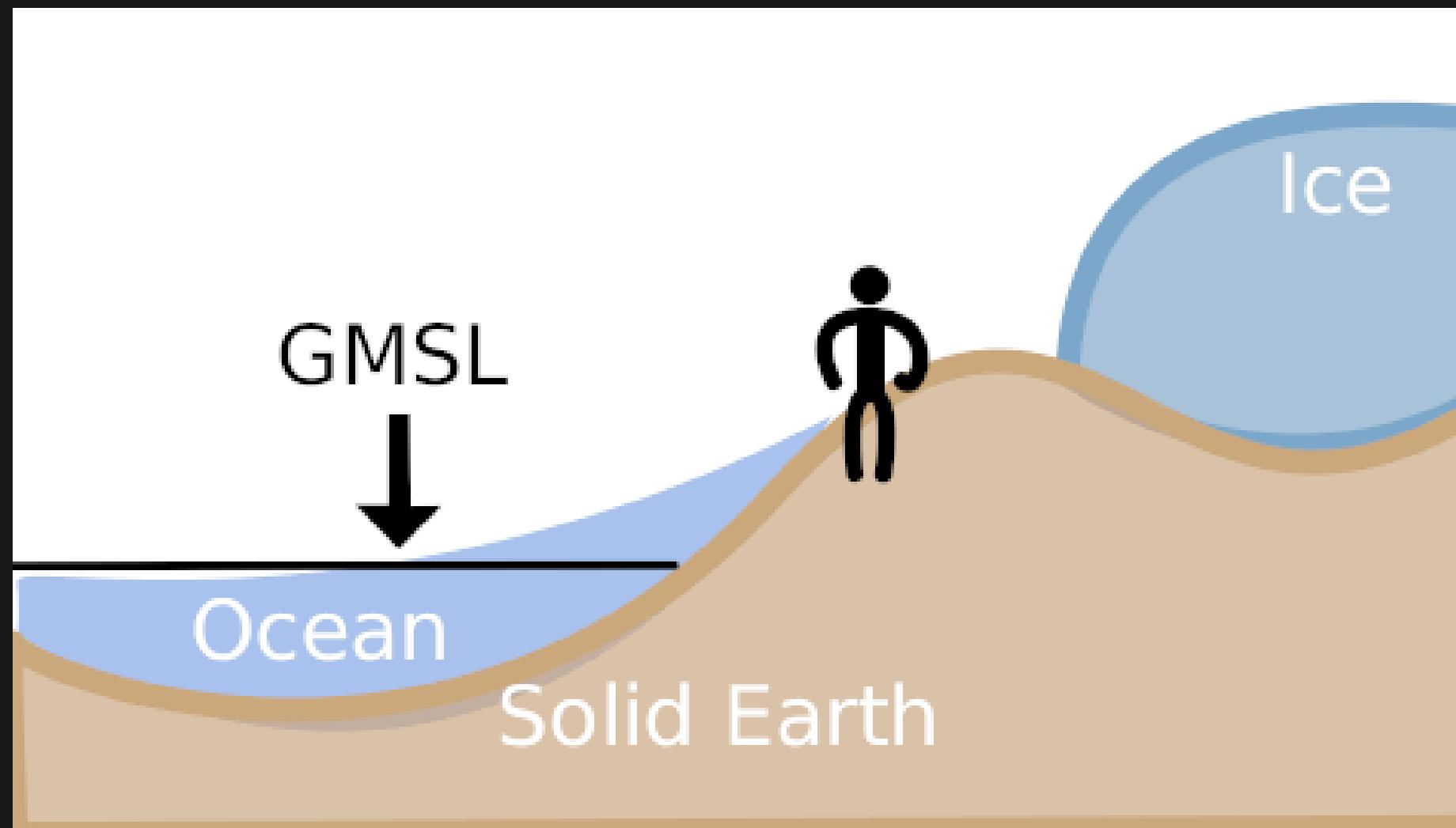
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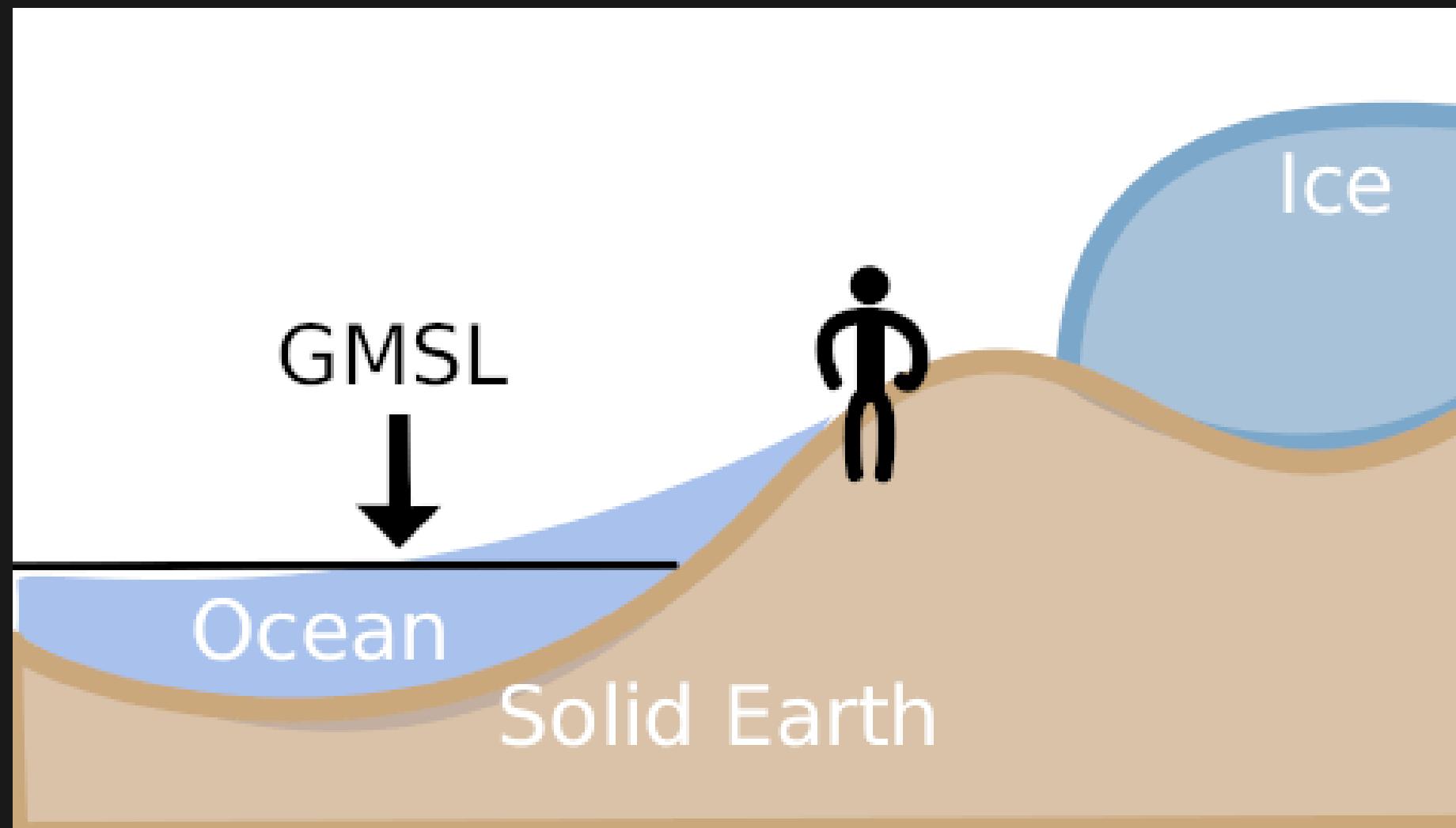
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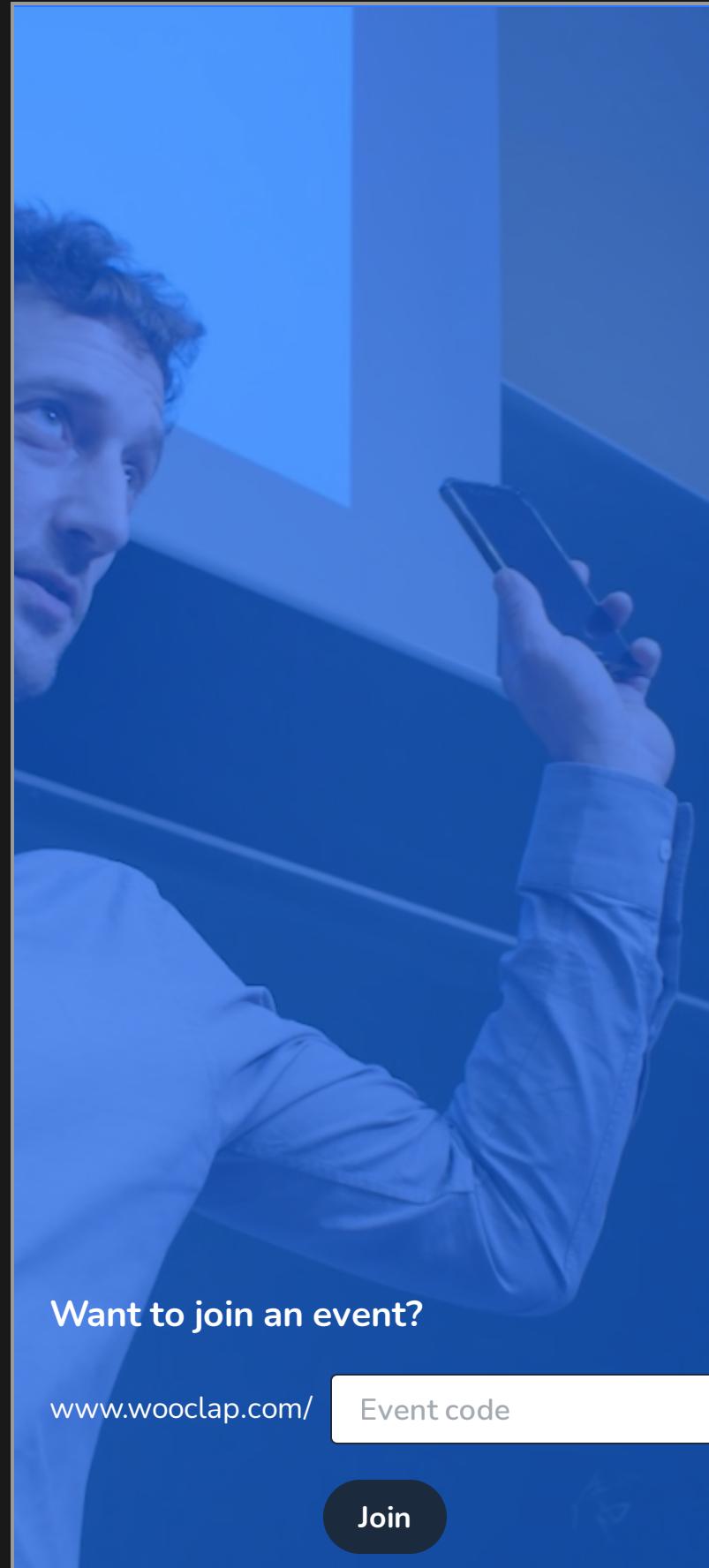
- Theory goes back to 1888 (Woodward)
- Modelled as a passive ocean response (no currents)
- mass conserving

# Relative sea level is affected by self attraction and loading (SAL)..



- Theory goes back to 1888 (Woodward)
- Modelled as a passive ocean response (no currents)
- mass conserving
- Takes into account the deformation of the Earth

# Other factors affecting relative sea level?



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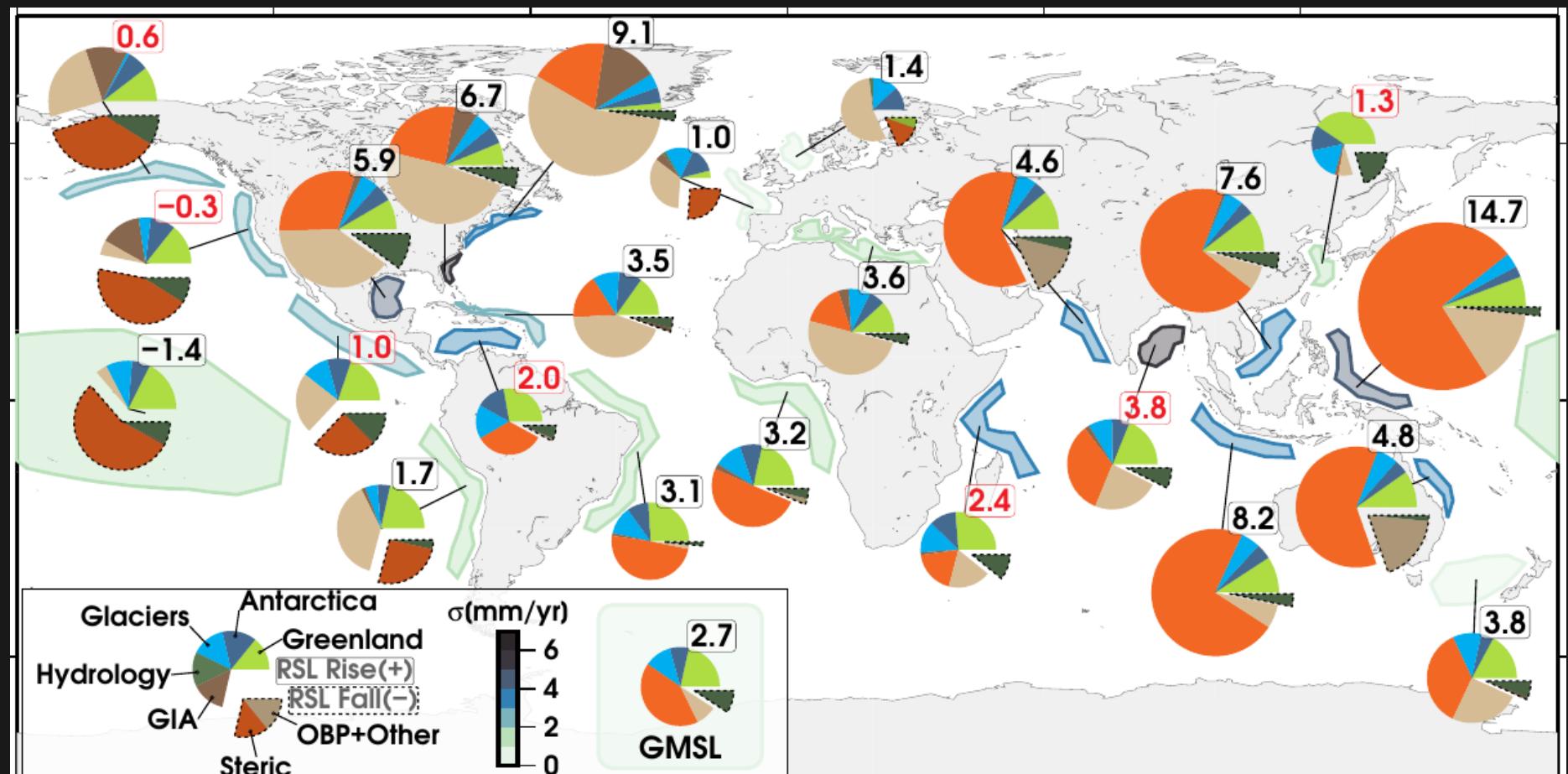
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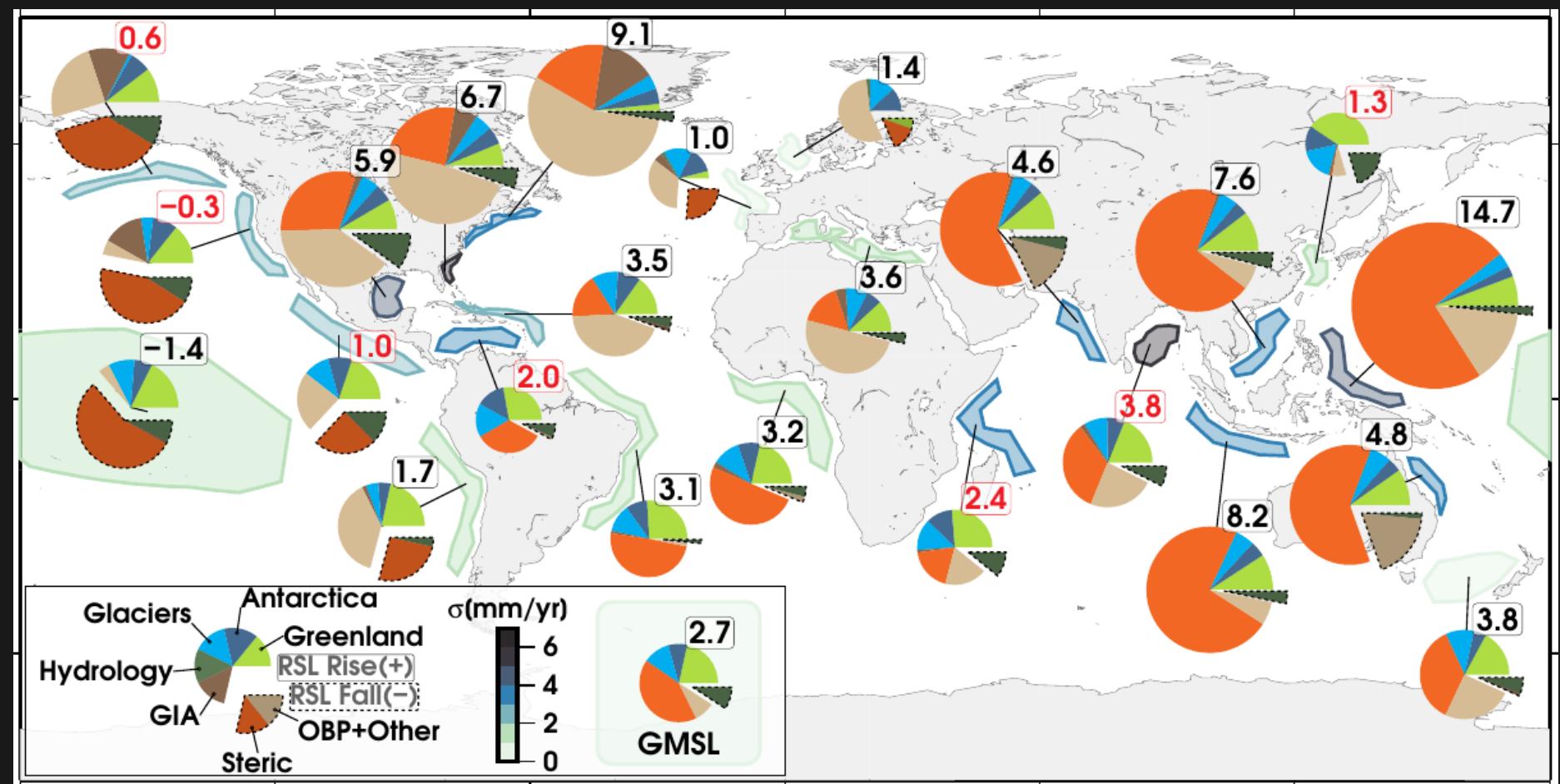
# Regional sea level budgets



Regional sea level budgets from Rietbroek et al. 2016

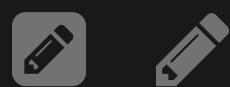


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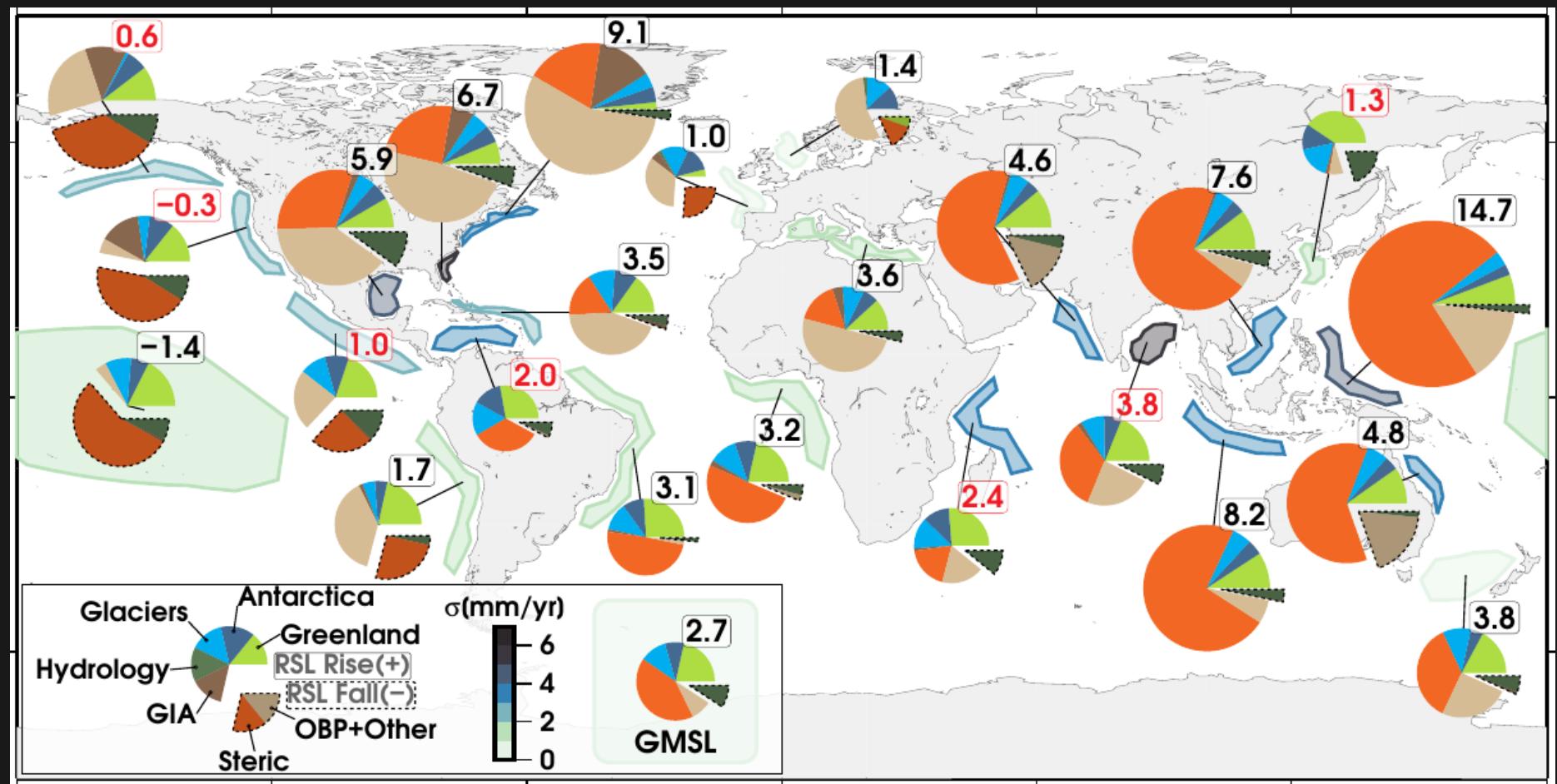


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- Sea level rise is not uniform



# Regional sea level budgets

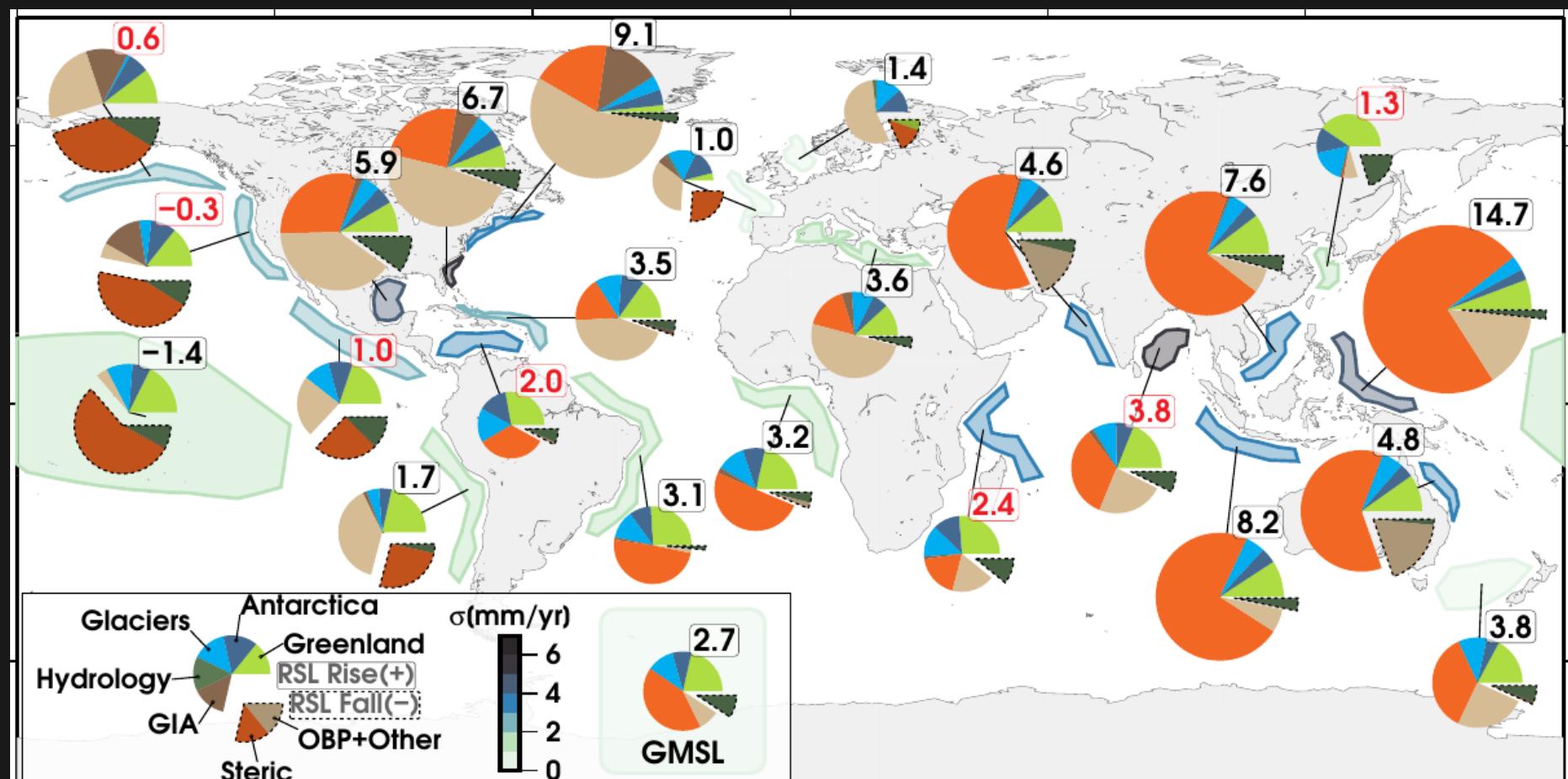


Regional sea level budgets from Rietbroek et al. 2016

- Sea level rise is not uniform
- SAL effects

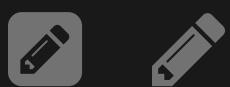


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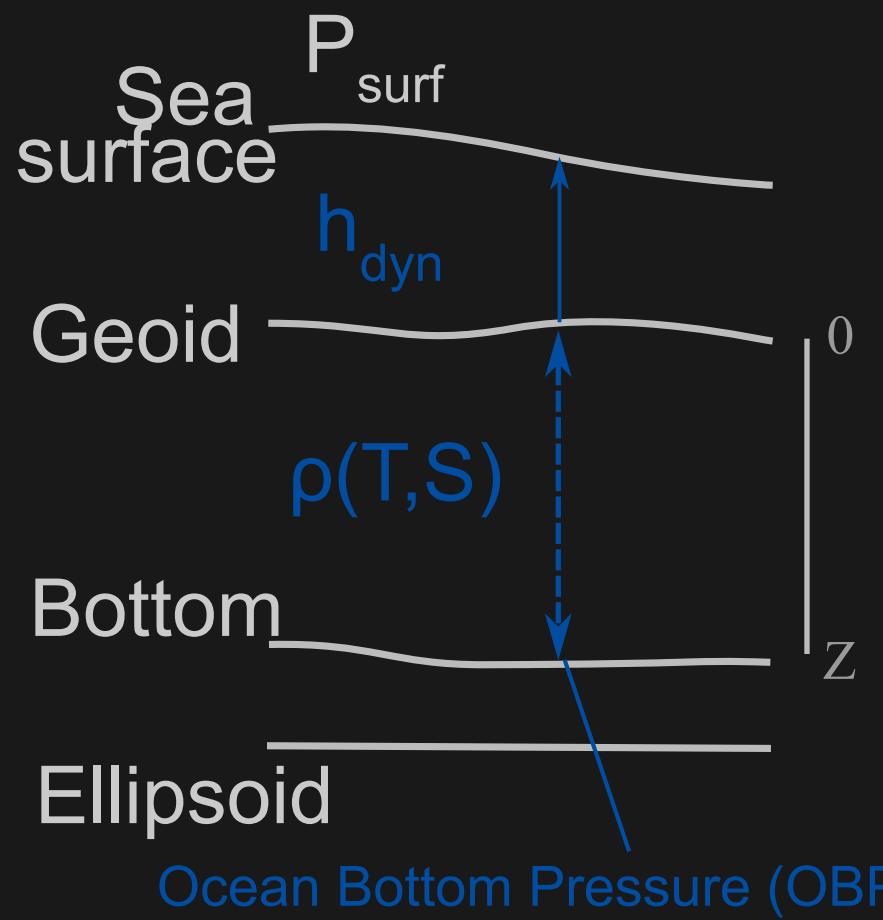
- Sea level rise is not uniform
- SAL effects
- Thermosteric and ocean bottom pressure changes play a larger role in the regional budgets



# Churning the ocean (forcing from wind stress, density contrasts)

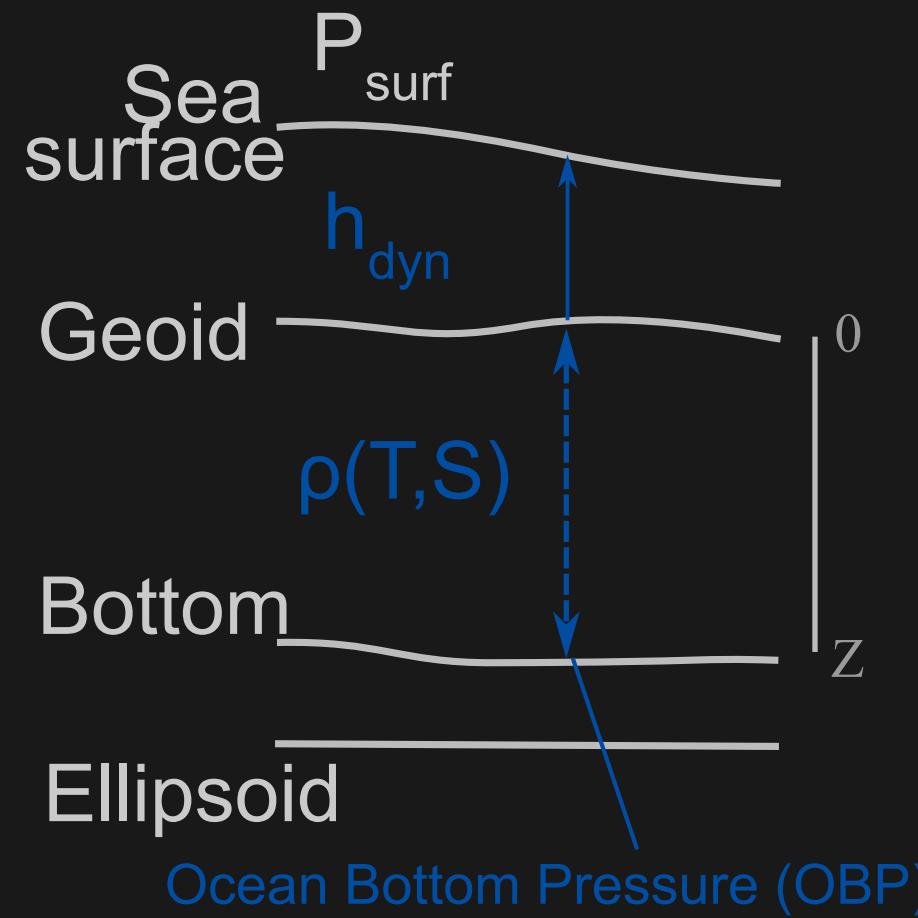


# Integrating the water column to obtain ocean bottom pressure

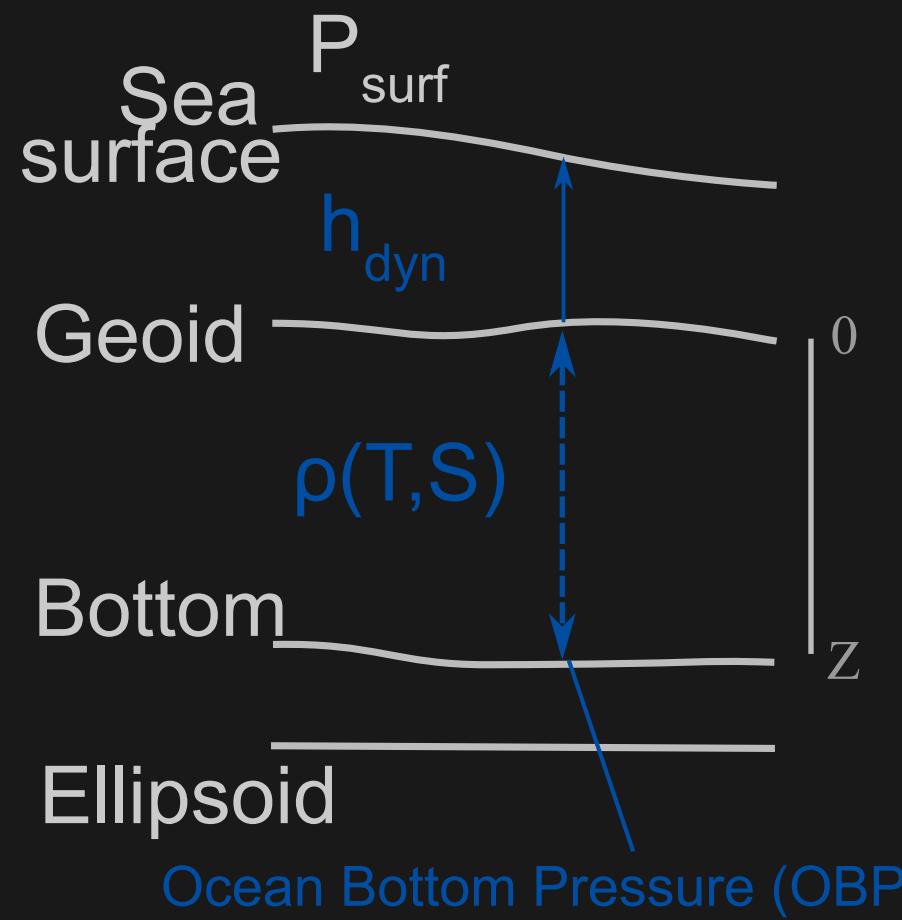


# Integrating the water column to obtain ocean bottom pressure

$$P_{OBP} = P_{surf} + g \int_{-Z}^0 \rho(z, T, S) dz \\ + g \rho_{sea} h_{dyn}$$



# Integrating the water column to obtain ocean bottom pressure

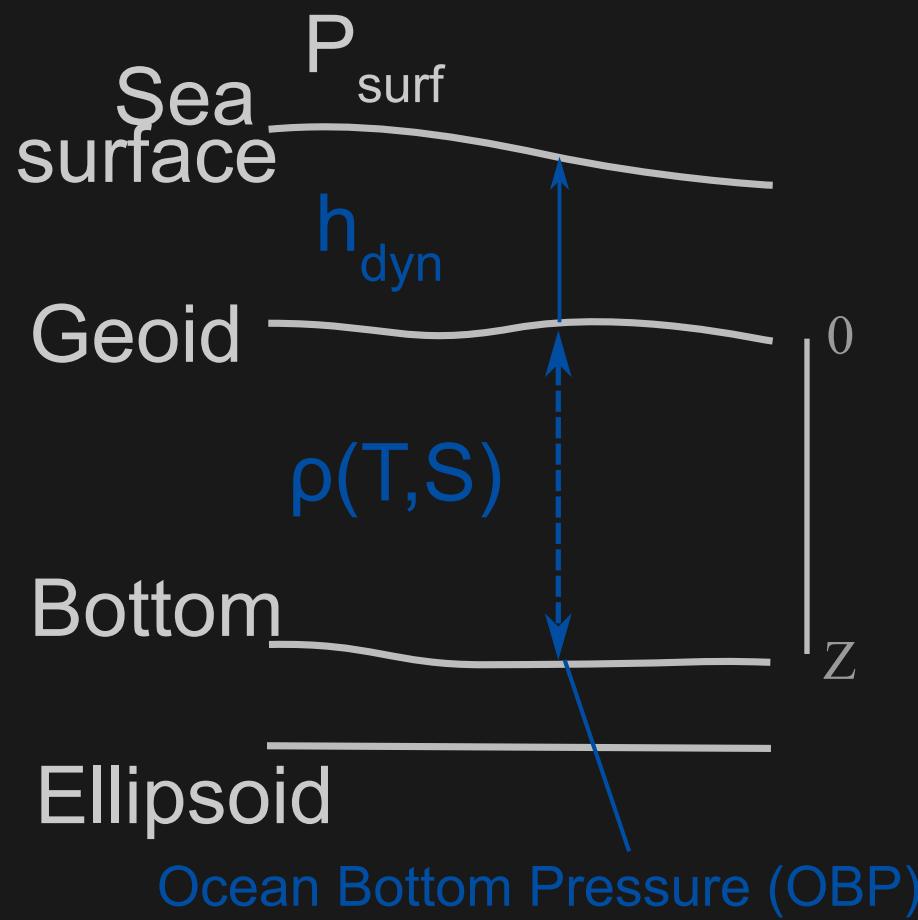


$$P_{OBP} = P_{surf} + g \int_{-Z}^0 \rho(z, T, S) dz + g \rho_{sea} h_{dyn}$$

Steric change only (no OBP change):

$$0 = g \int_{-Z}^0 \delta \rho(z, T, S) dz + g \rho_{sea} \delta h_{ster}$$

# Integrating the water column to obtain ocean bottom pressure



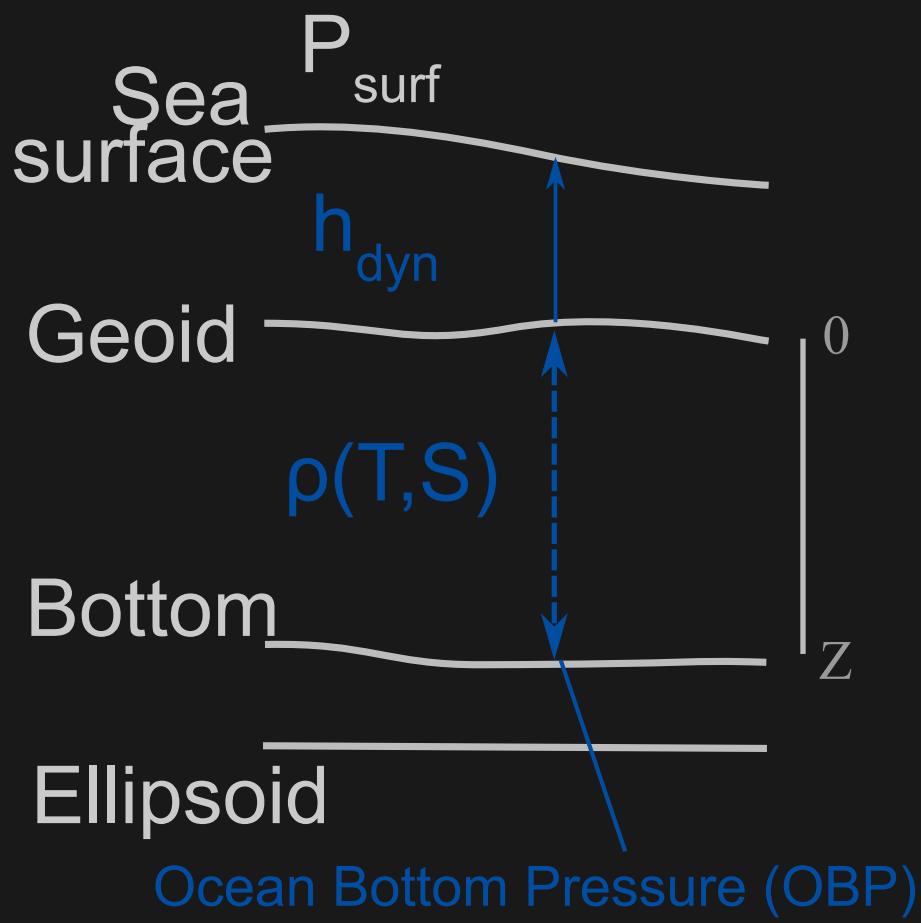
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$$\delta h_{ster} = -\frac{1}{\rho_{sea}} \int_{-Z}^0 \delta \rho(z, T, S) dz$$

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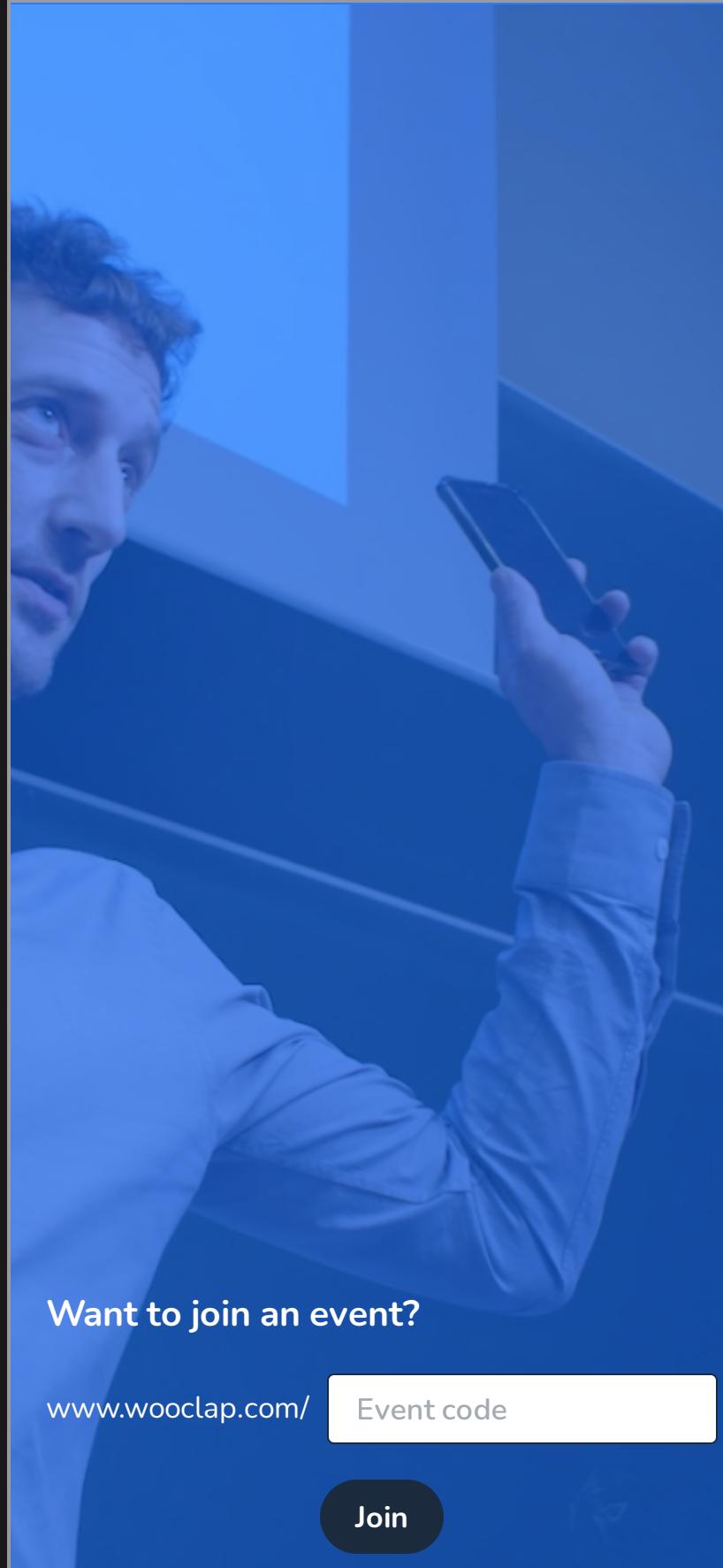
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$$0 = g \int_{-Z}^0 \delta \rho(z, T, S) dz + g \rho_{sea} \delta h_{ster}$$

$$\delta h_{ster} = -\frac{1}{\rho_{sea}} \int_{-Z}^0 \delta \rho(z, T, S) dz$$

- $\delta h_{ster}$  visible to GRACE! ( $P_{OBP} = 0$ )
- $\delta h_{ster}$  visible by radar altimetry!
- Density  $\uparrow$  results in  $\downarrow$  of sea level
- Wind driven (quick)  $\rightarrow$  change in  $h_{dyn}$
- Density driven (slow)  $\rightarrow$   $h_{dyn} \sim h_{ster}$

# Quiz time! (again)



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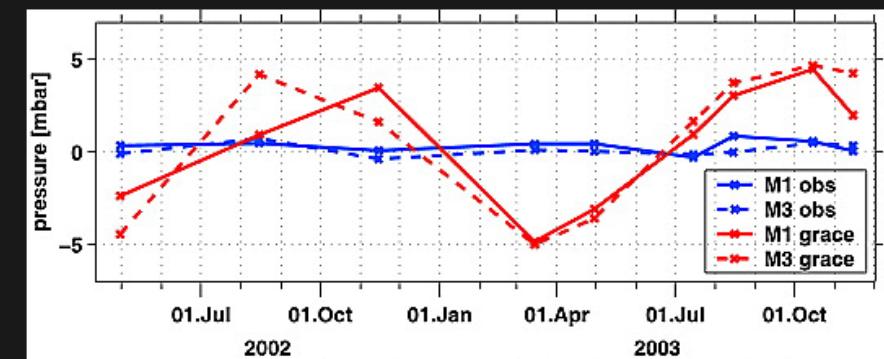
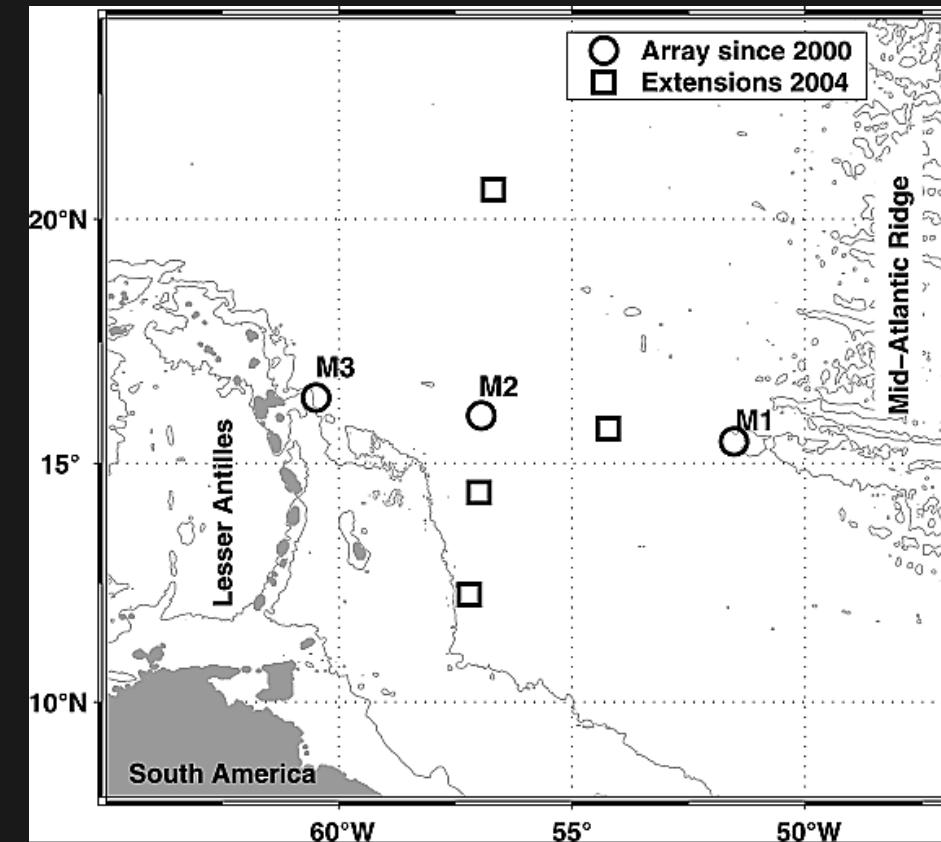
**Accept all**

**Reject All**

**Customise**

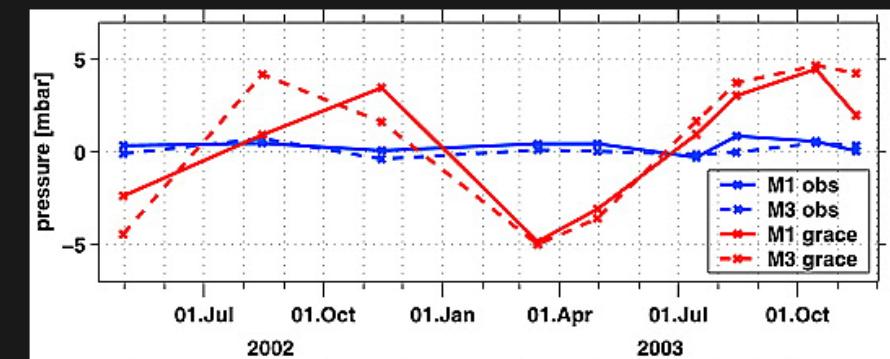
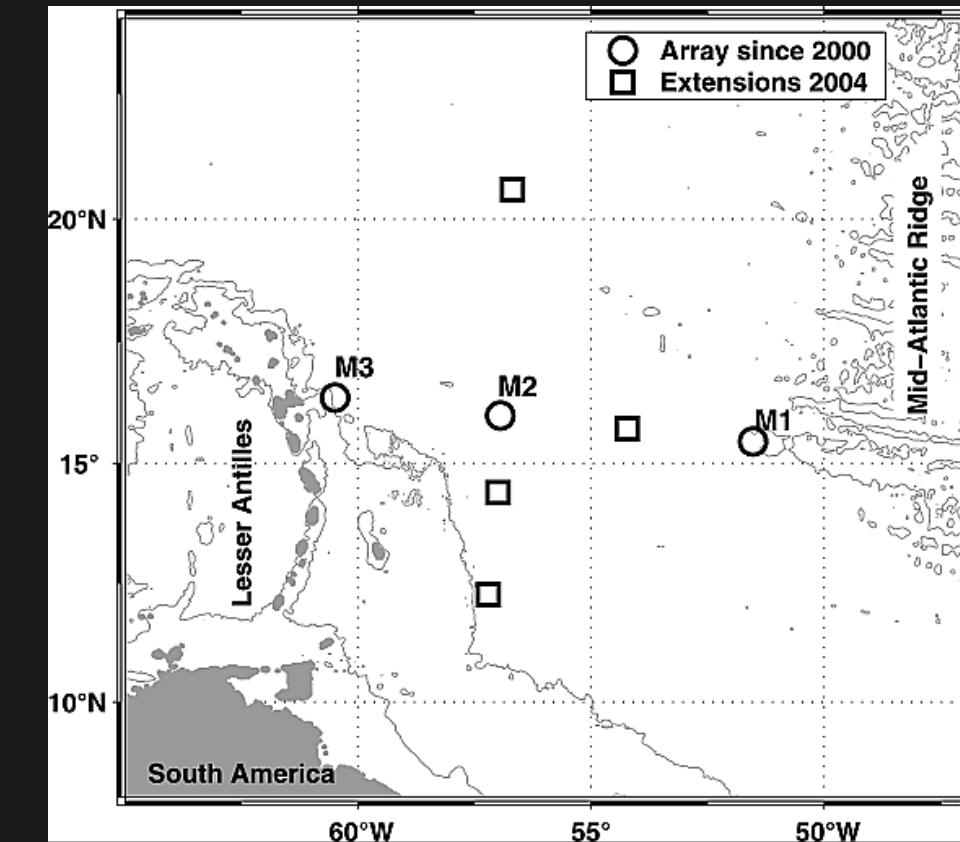


# Early GRACE validation of ocean bottom pressure changes (Kanzow et al. 2005)



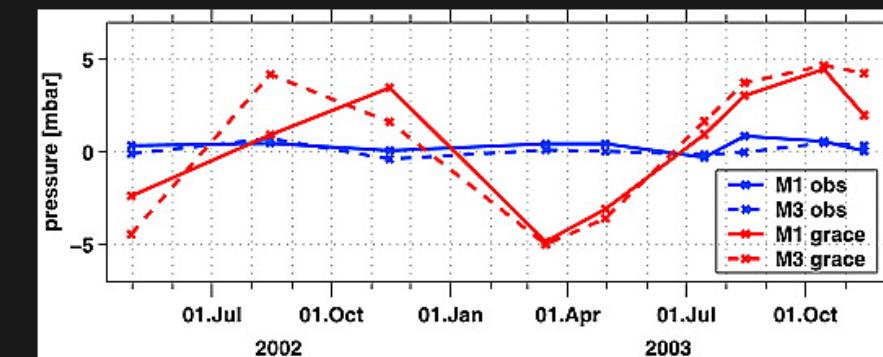
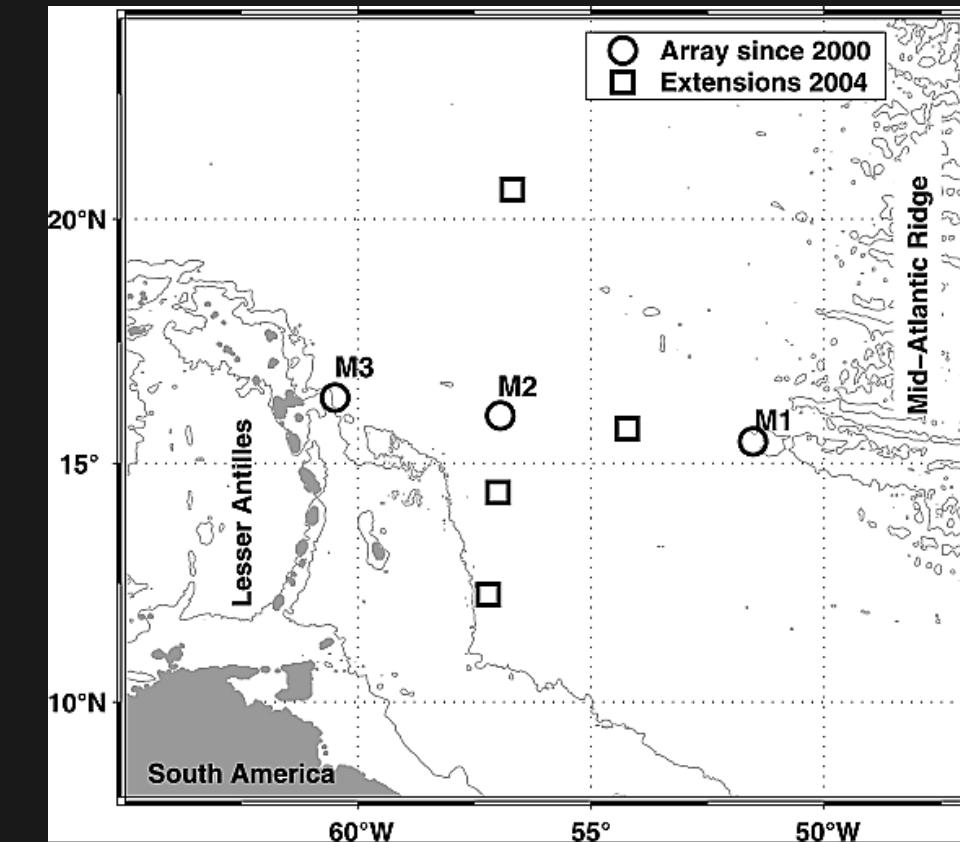
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- In situ validation with pressure sensors



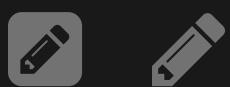
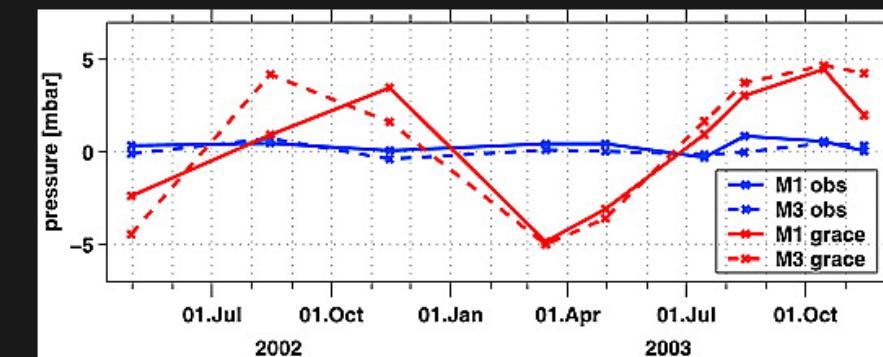
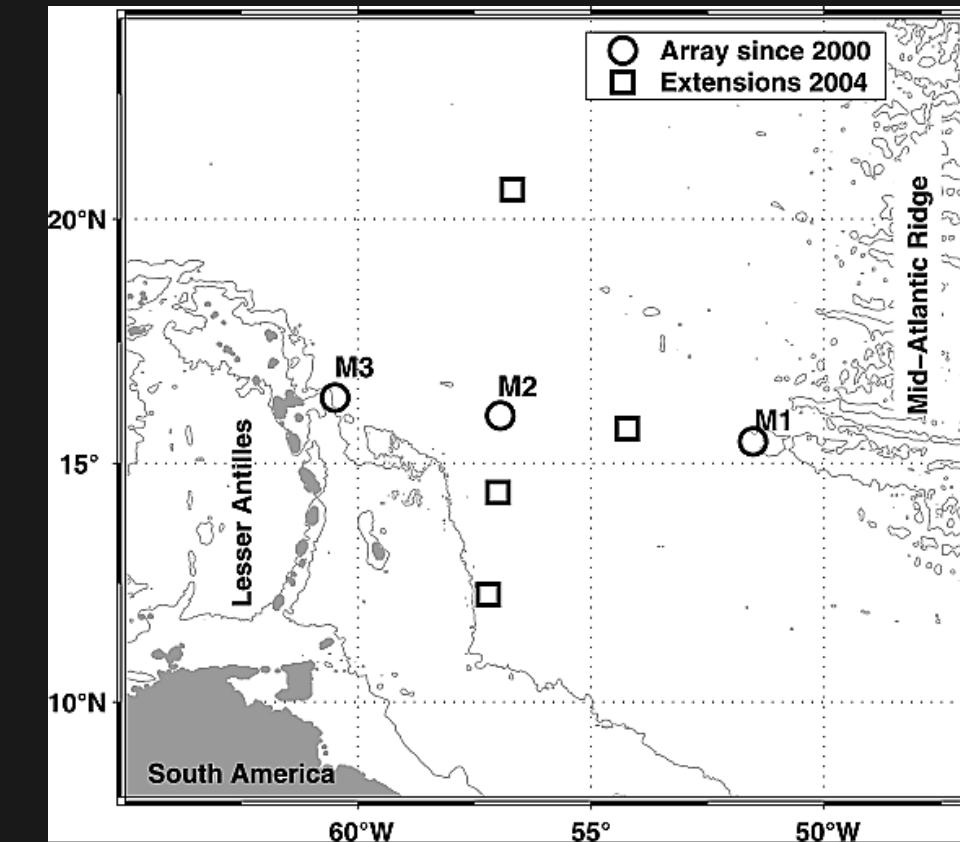
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- In situ validation with pressure sensors
- GRACE fluctuations were too large



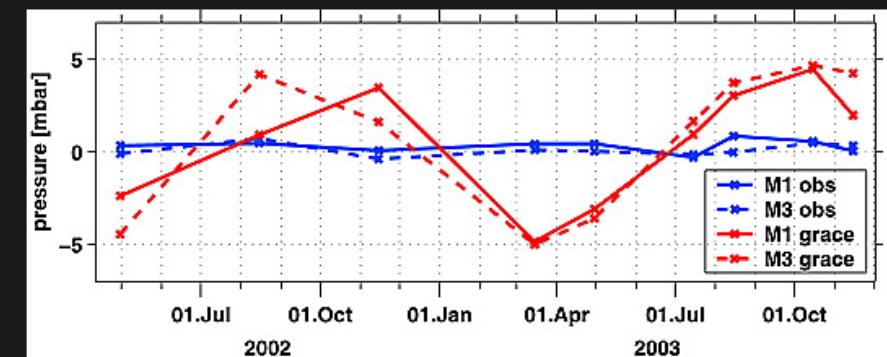
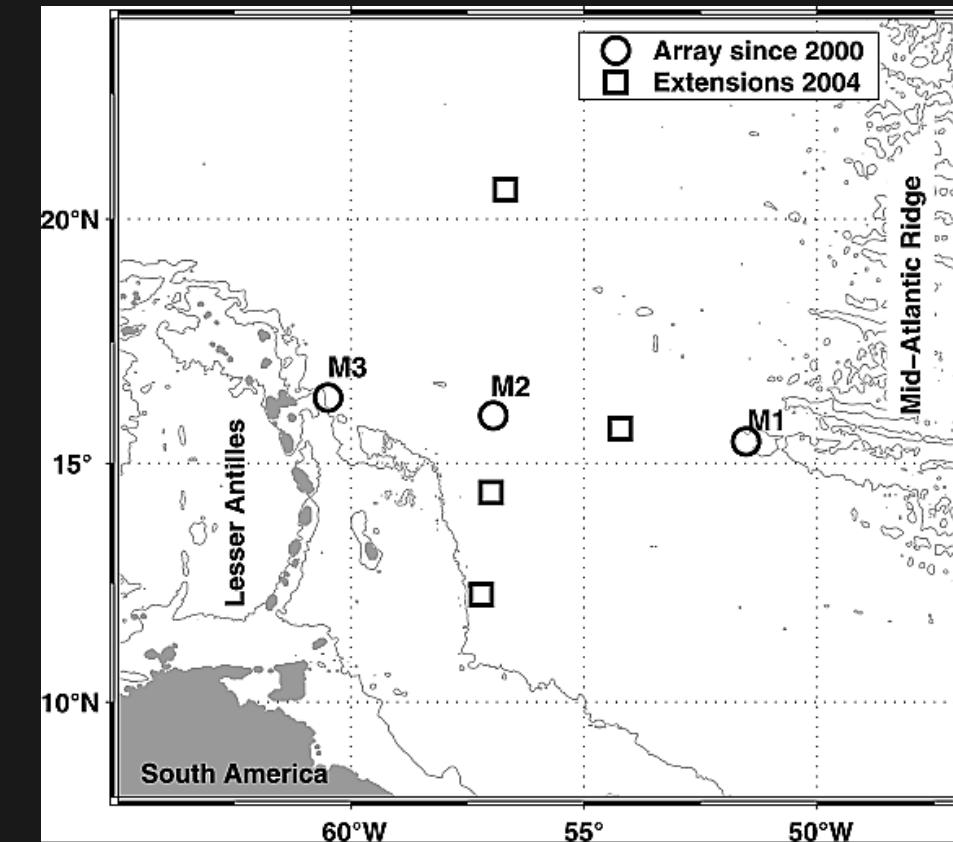
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- In situ validation with pressure sensors
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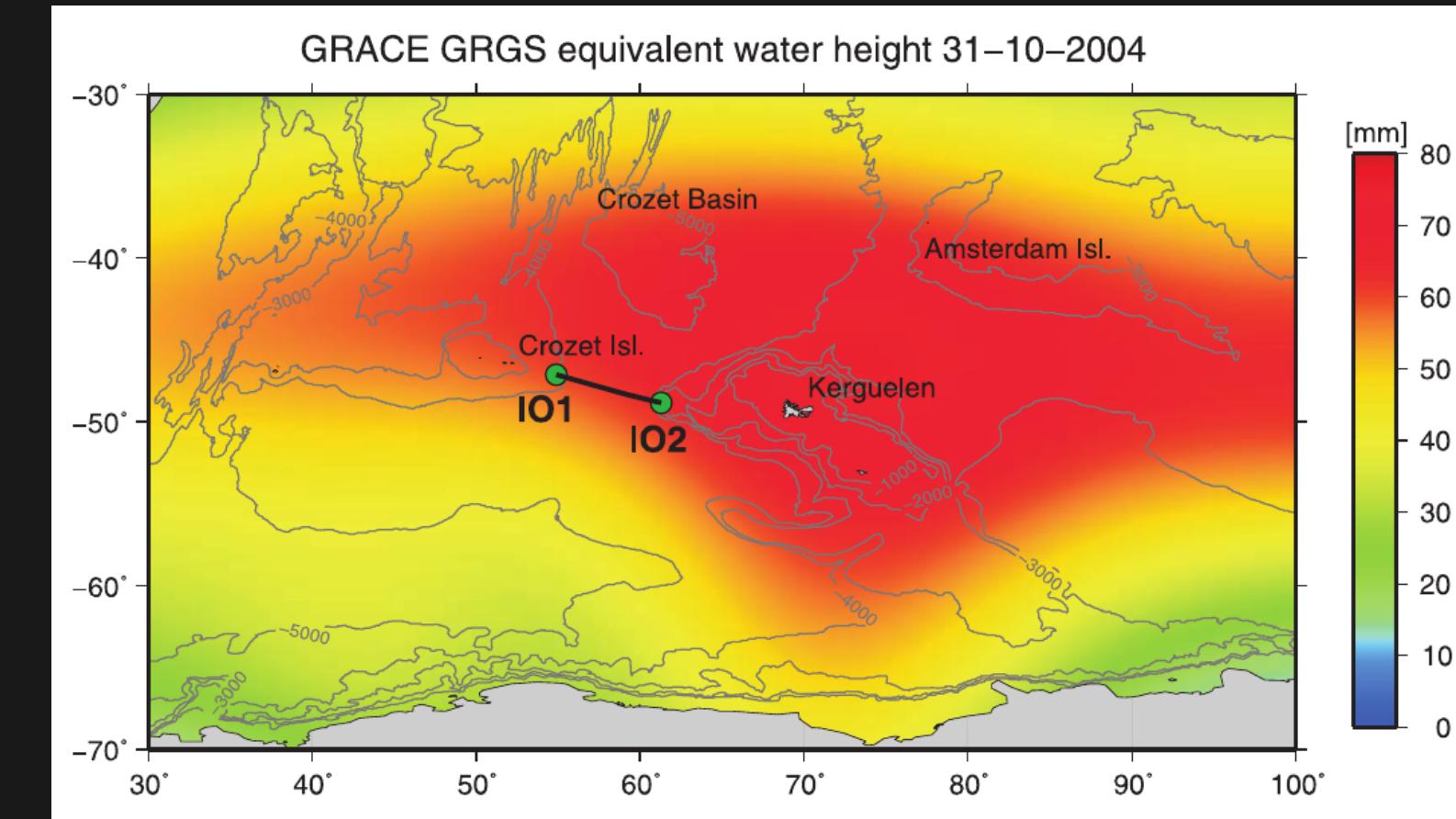
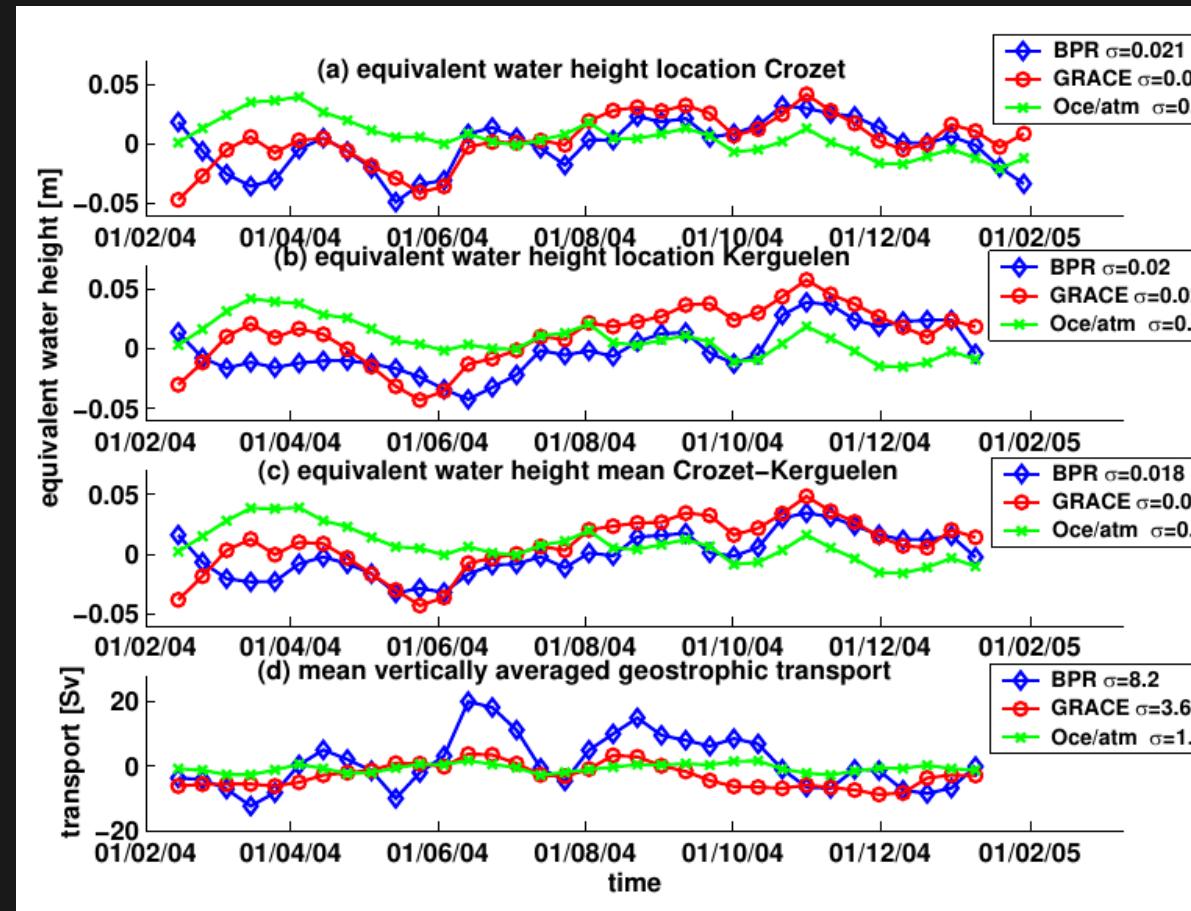


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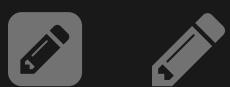
- In situ validation with pressure sensors
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  - Signal leakage
  - Processing errors



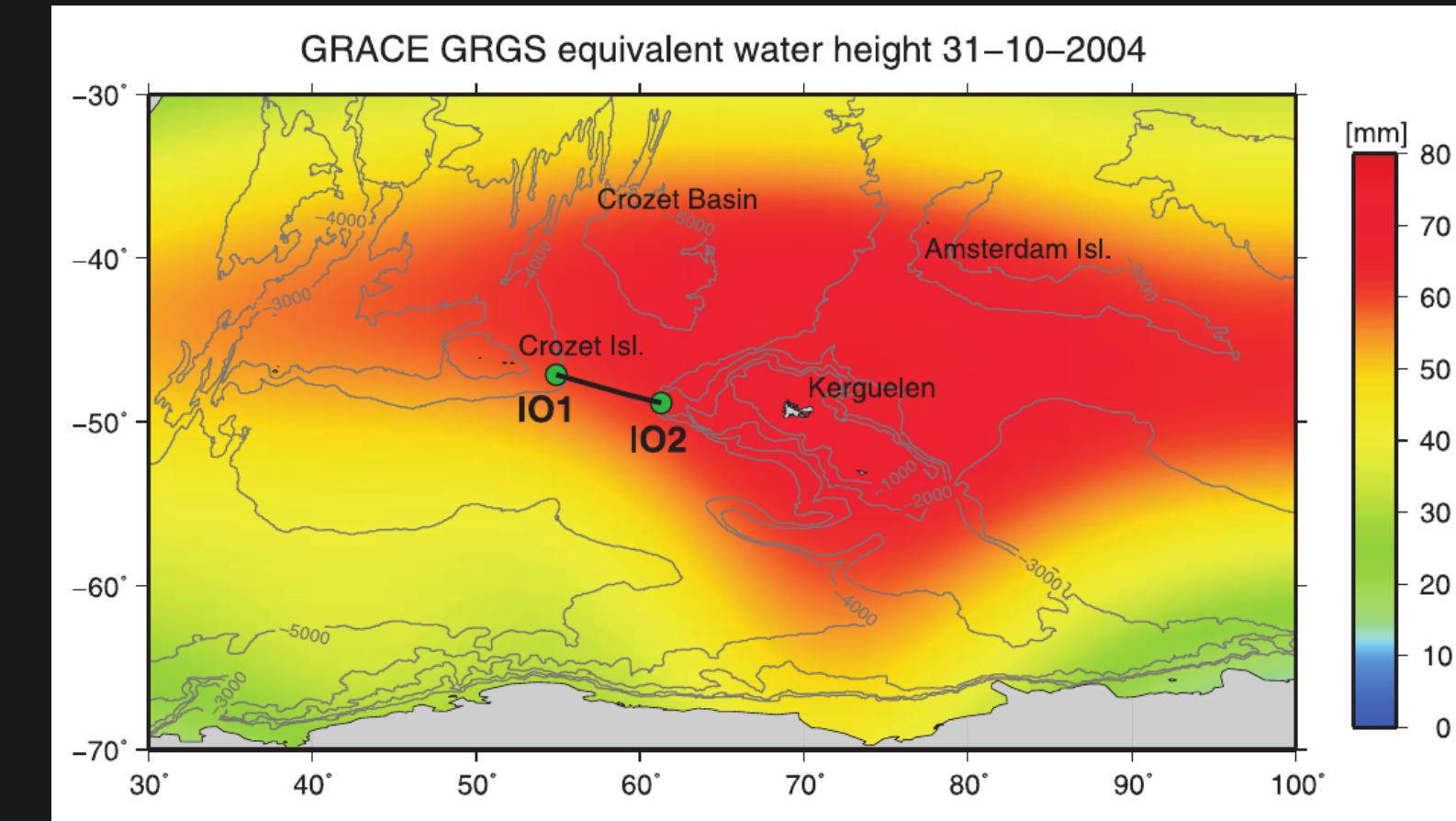
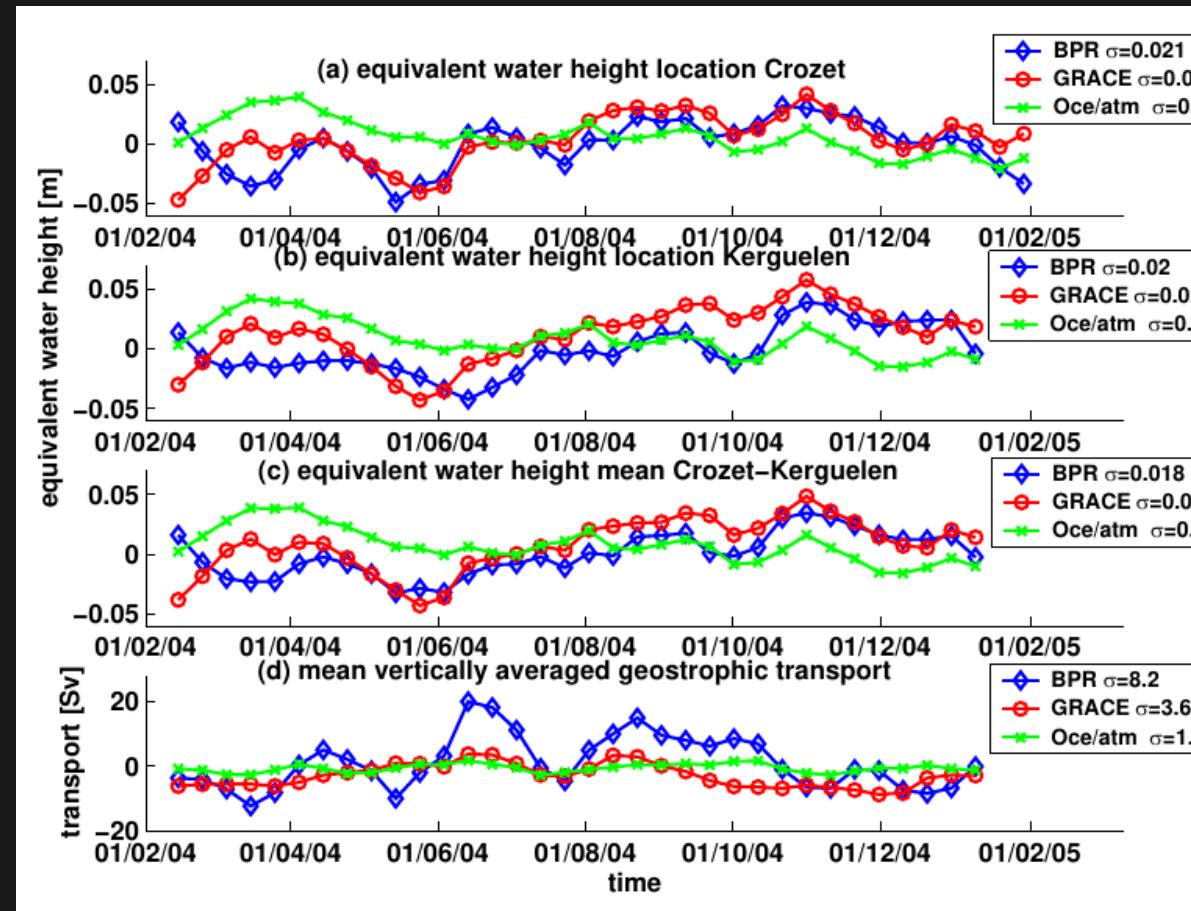
# Validation in the Southern Ocean



From Rietbroek et al. 2016



# Validation in the Southern Ocean

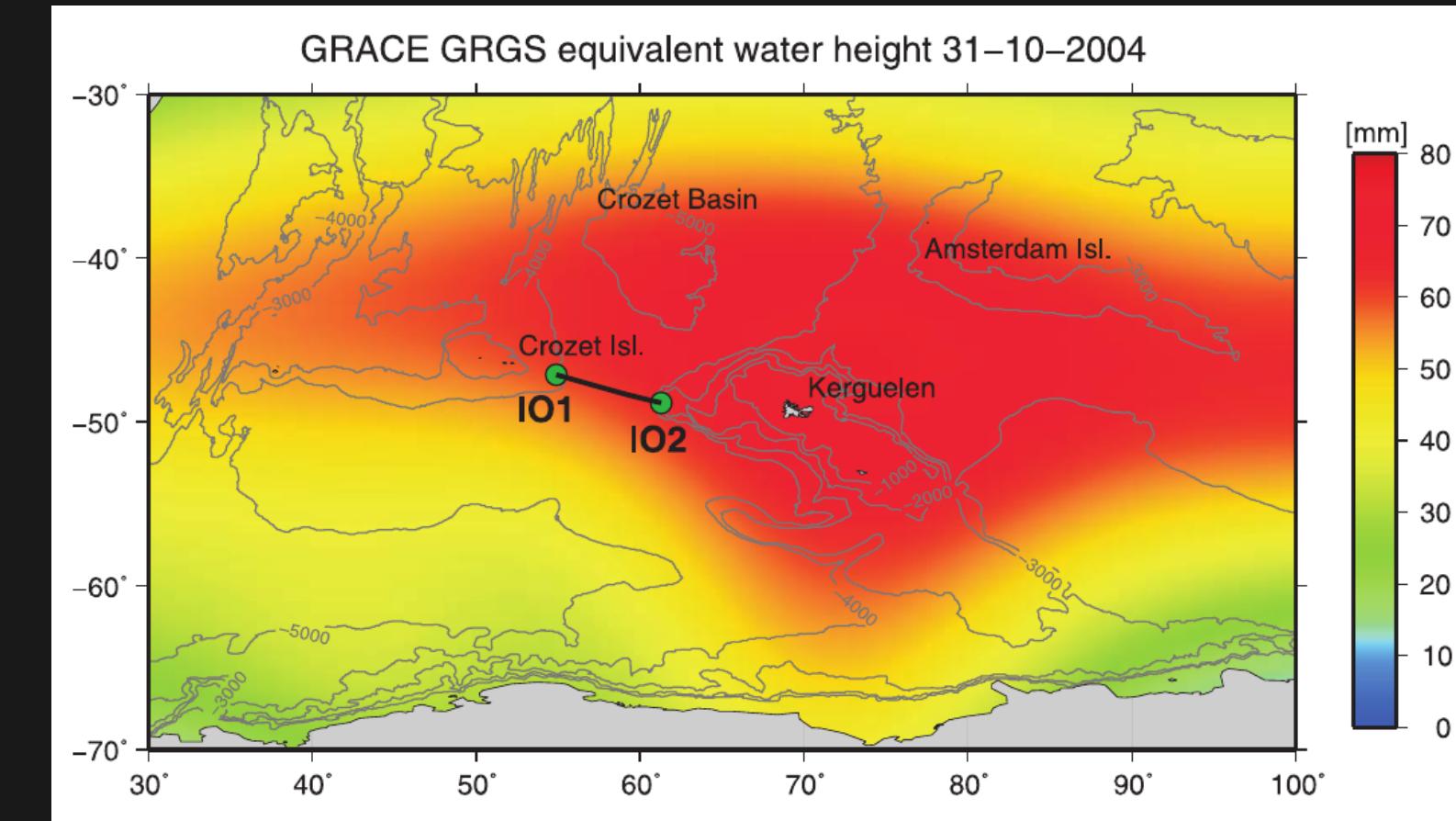
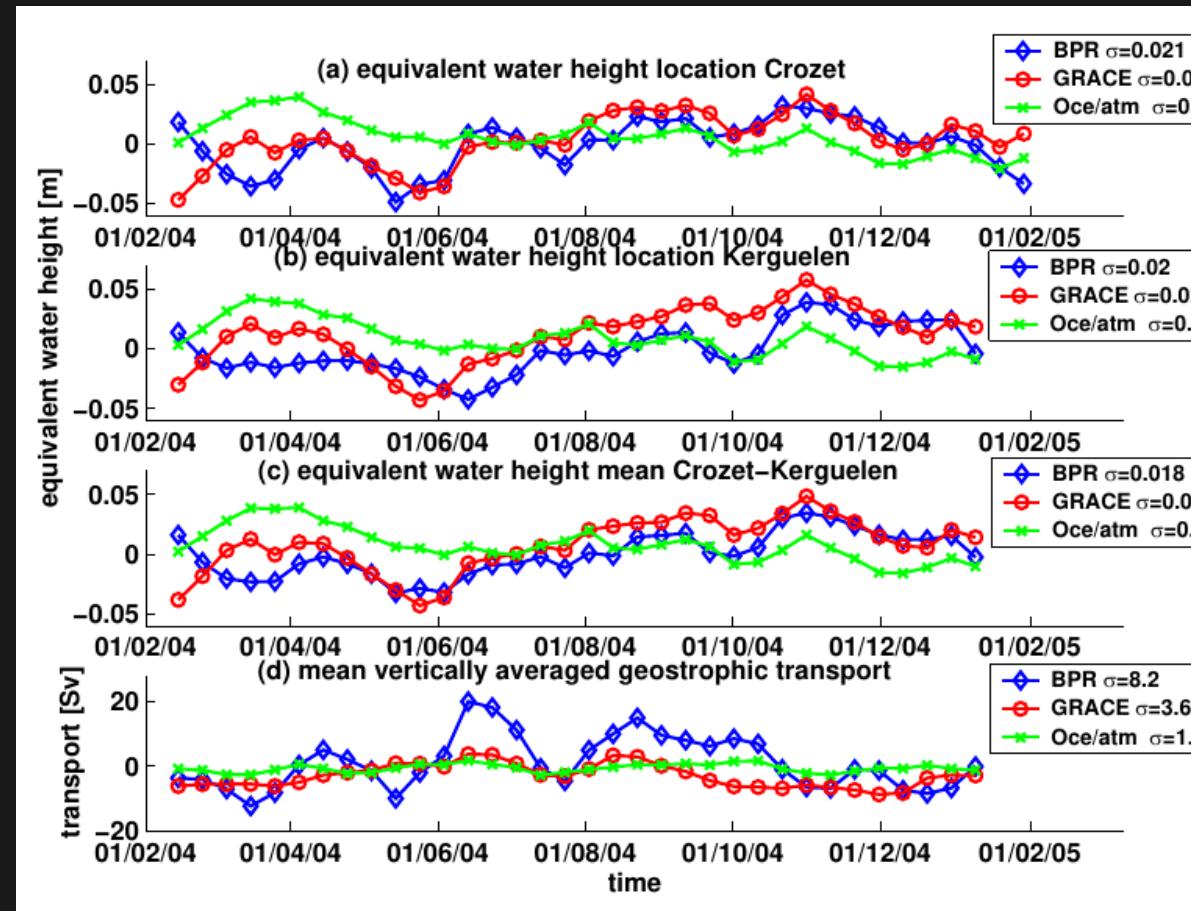


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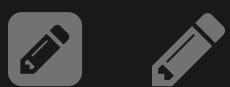


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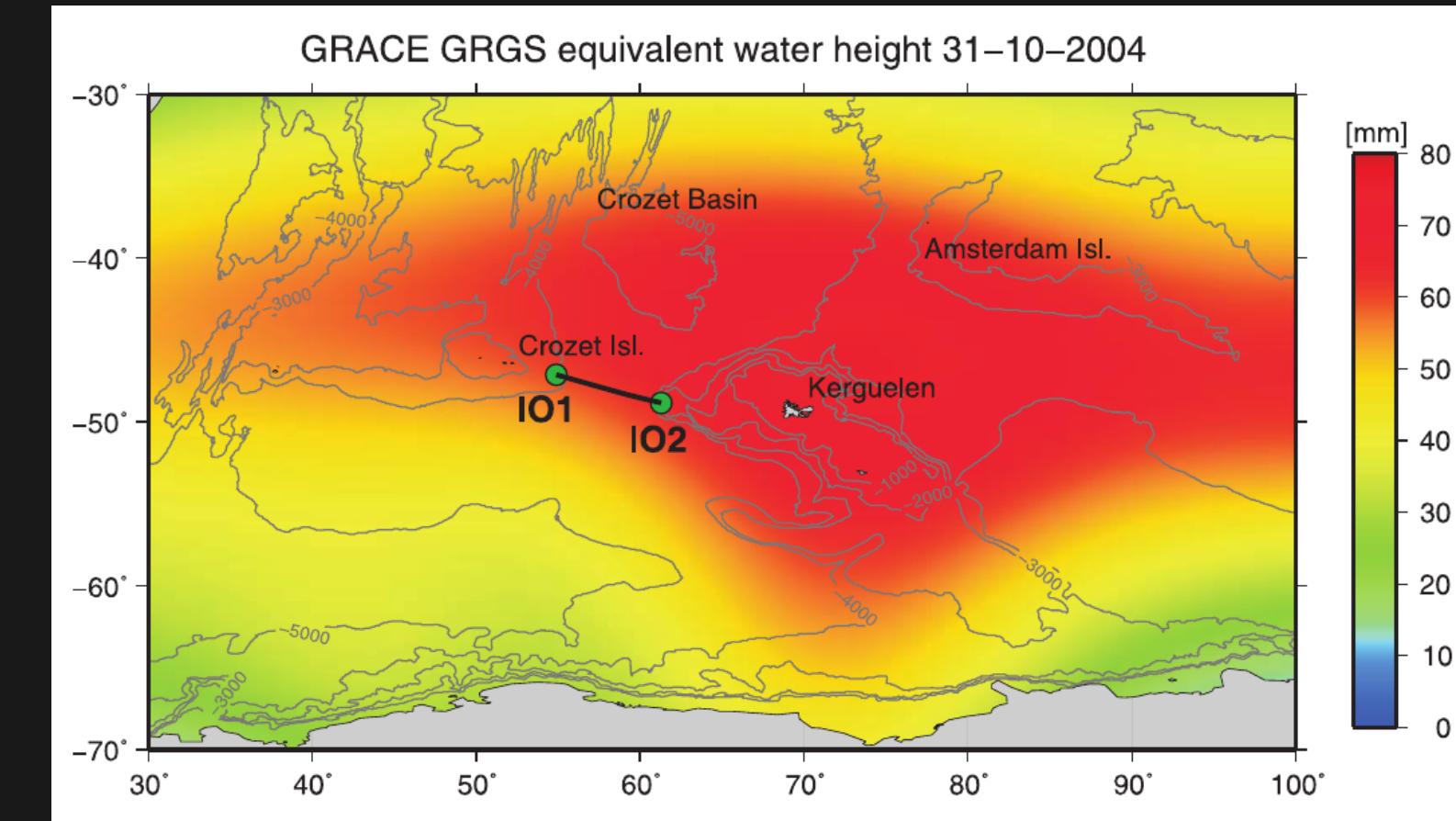
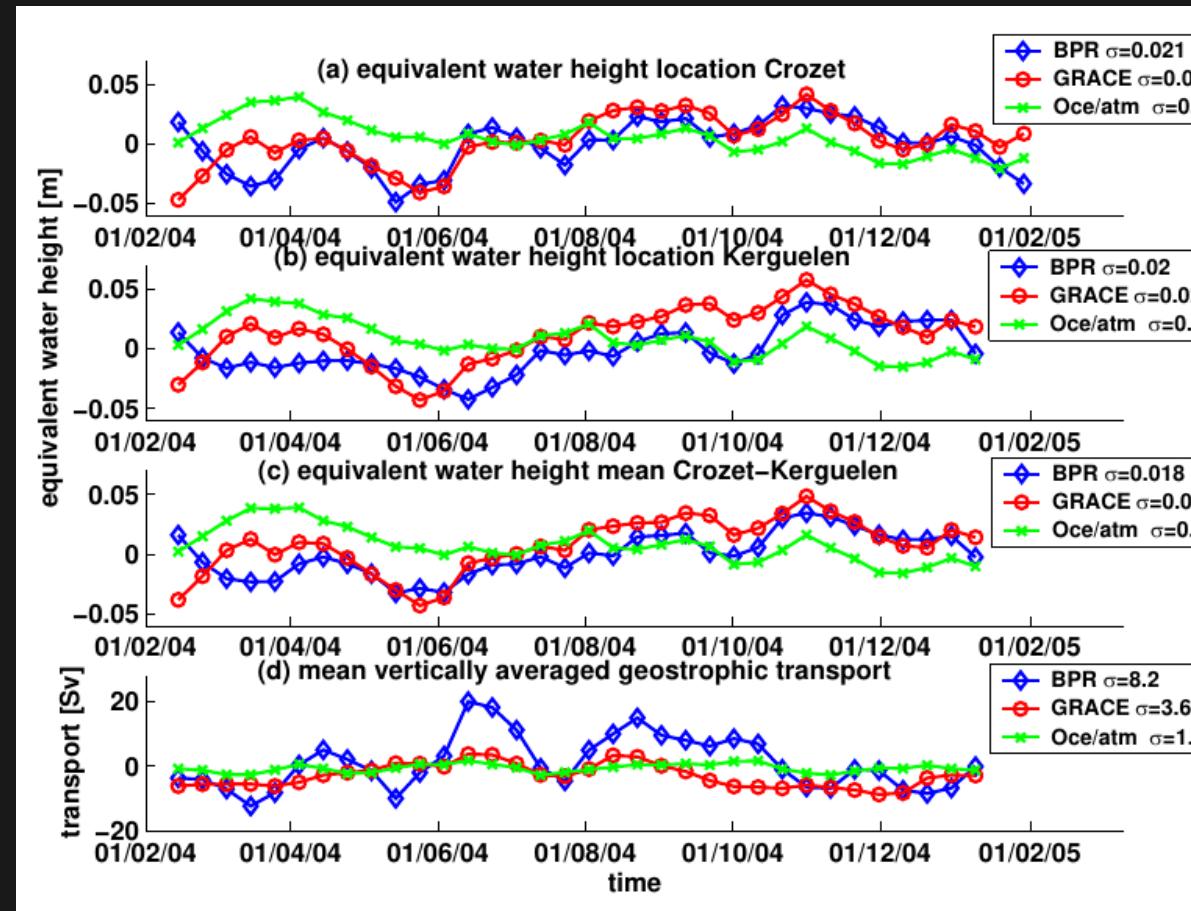


From Rietbroek et al. 2016

- In situ validation with pressure sensors
- 10-day GRACE solution was better than background model



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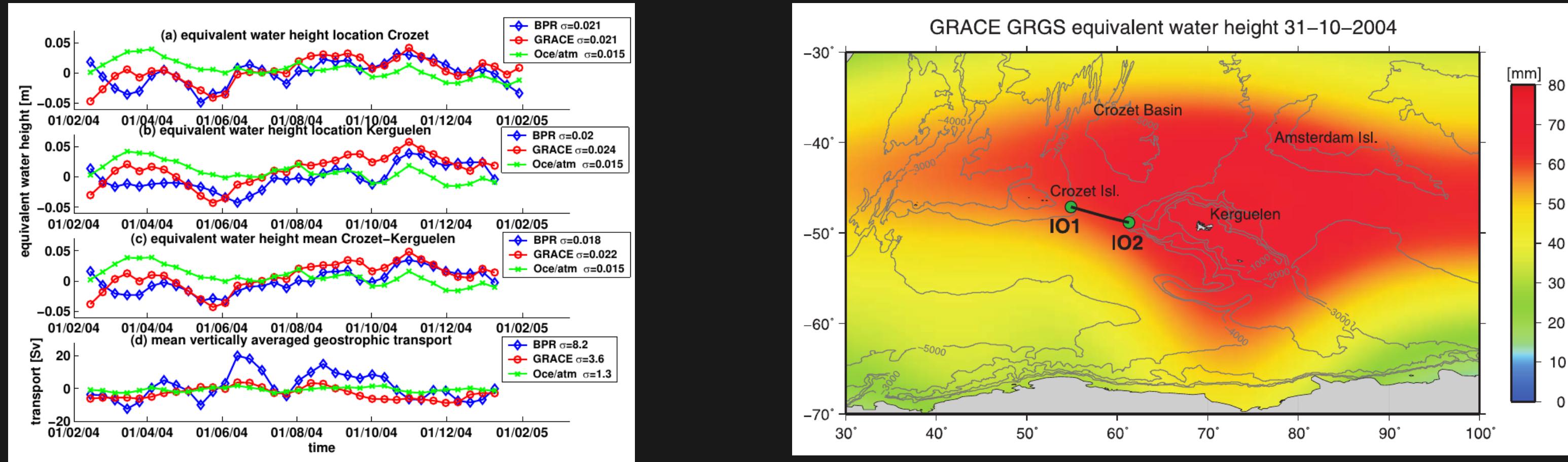


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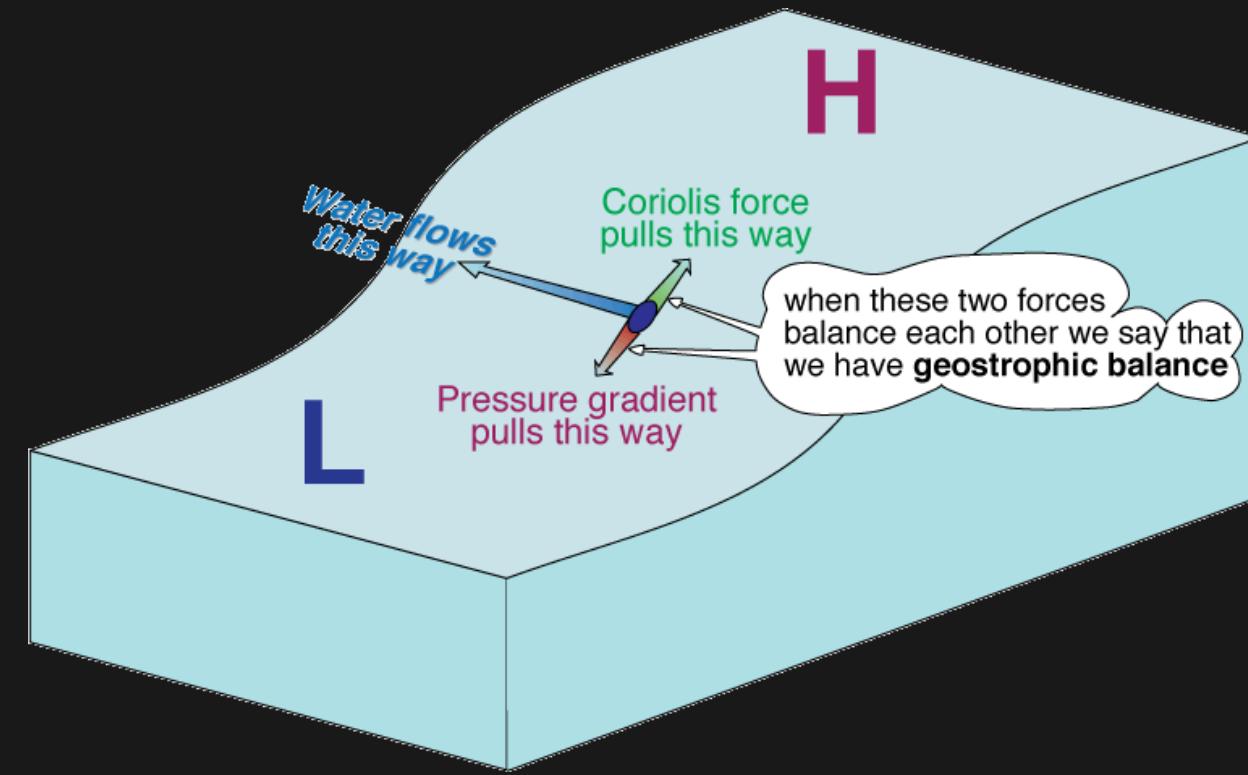
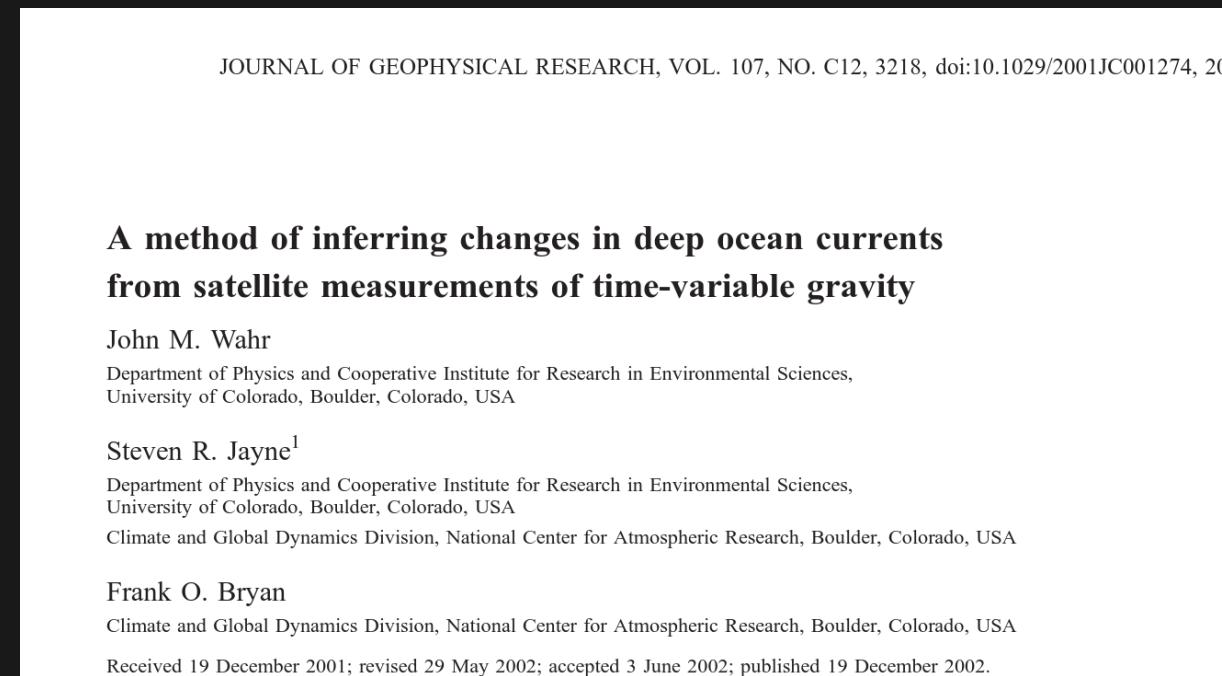


From Rietbroek et al. 2016

- In situ validation with pressure sensors
- 10-day GRACE solution was better than background model
- Large scale ocean signals picked up
- Due to smoothing geostrophic bottom currents not resolved



# Geostrophic currents from time variable gravity



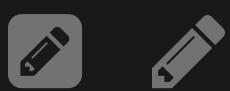
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the effects of friction and external forcing are less important,  
(1) reduces to the geostrophic approximation:

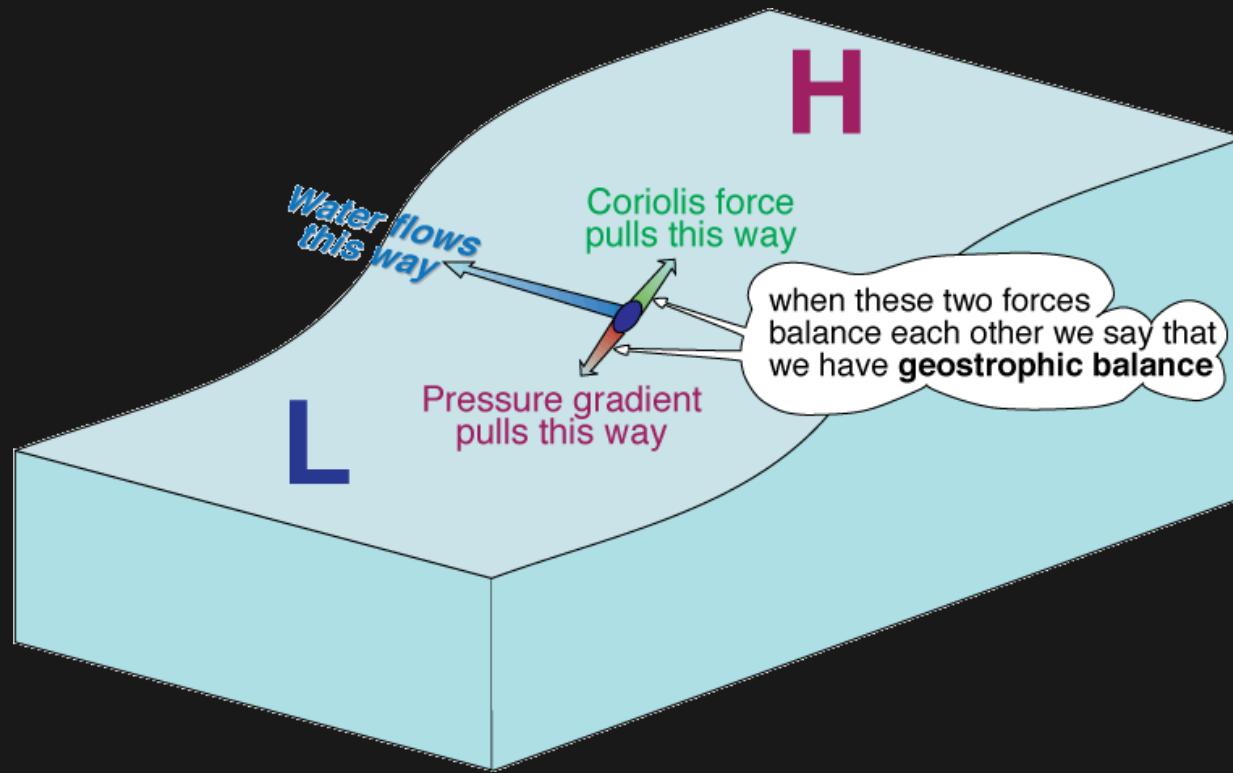
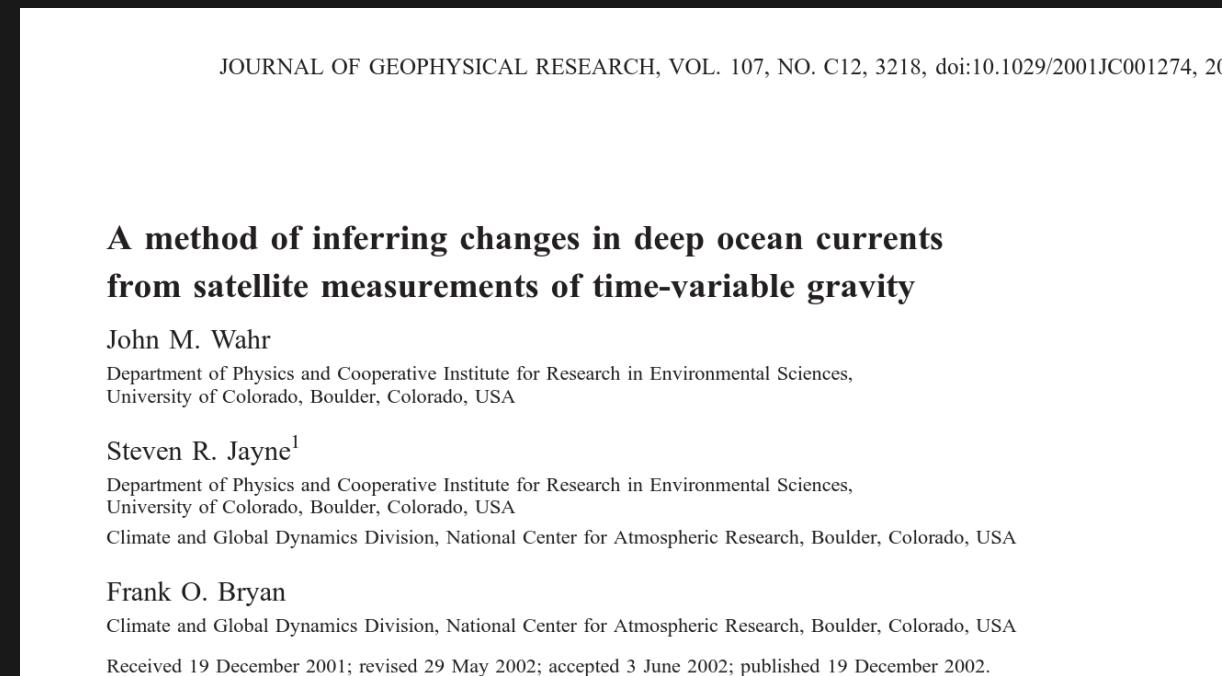
**Pressure gradient**

$$2\rho_0\Omega \times \mathbf{v} \approx -\nabla P \quad (2)$$

Earth rotation vector      ↑ velocity



# Geostrophic currents from time variable gravity



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- Assume horizontal constant velocities

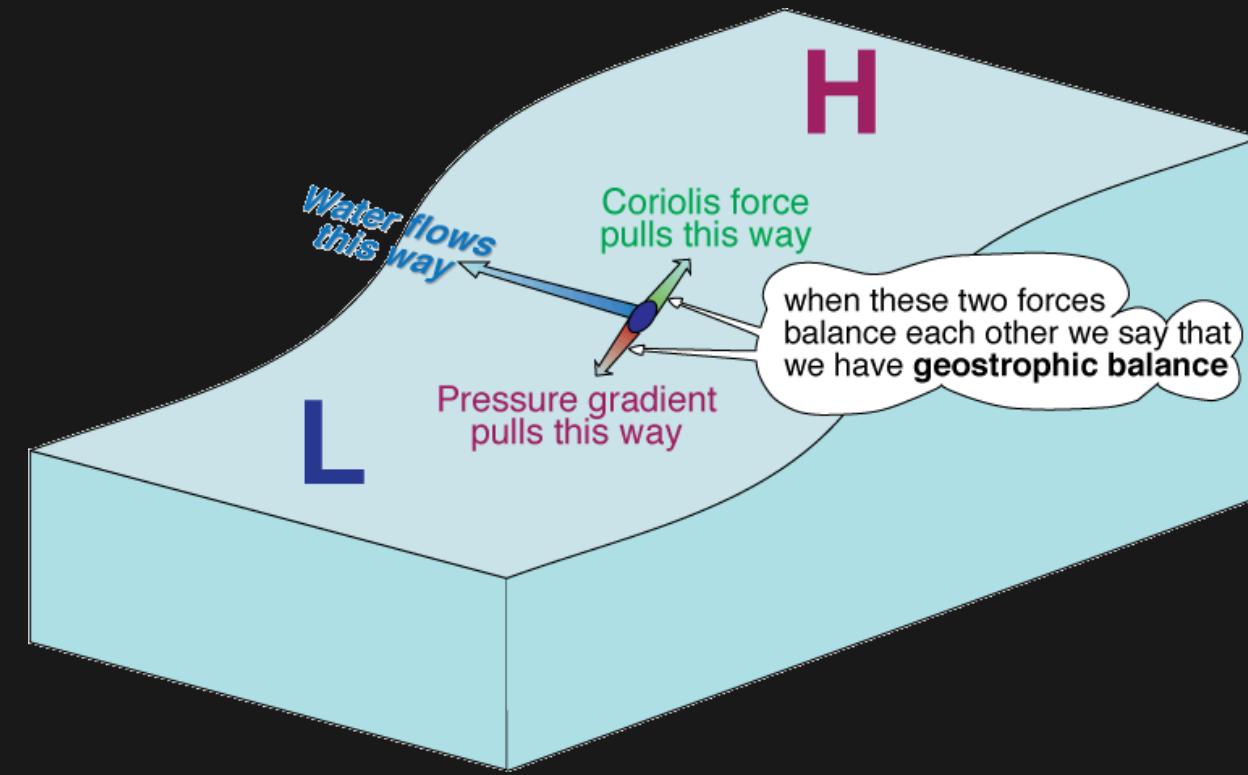
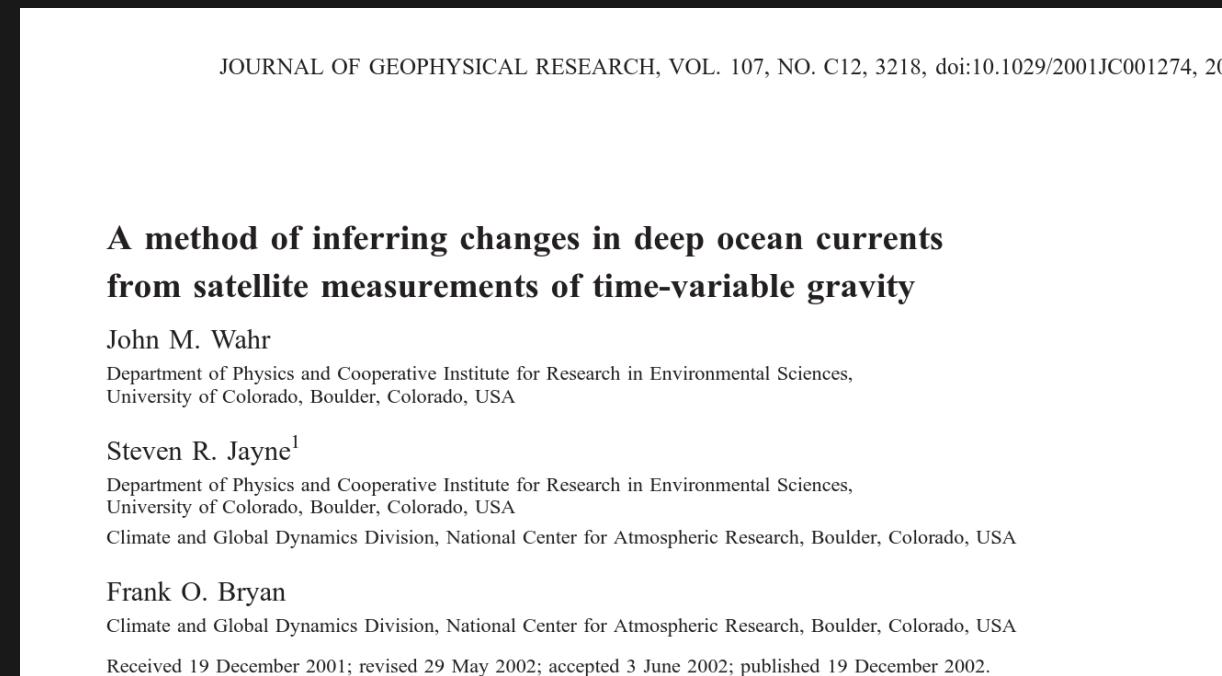
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Earth rotation vector      ↑ velocity



# Geostrophic currents from time variable gravity



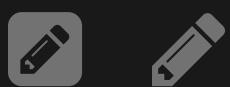
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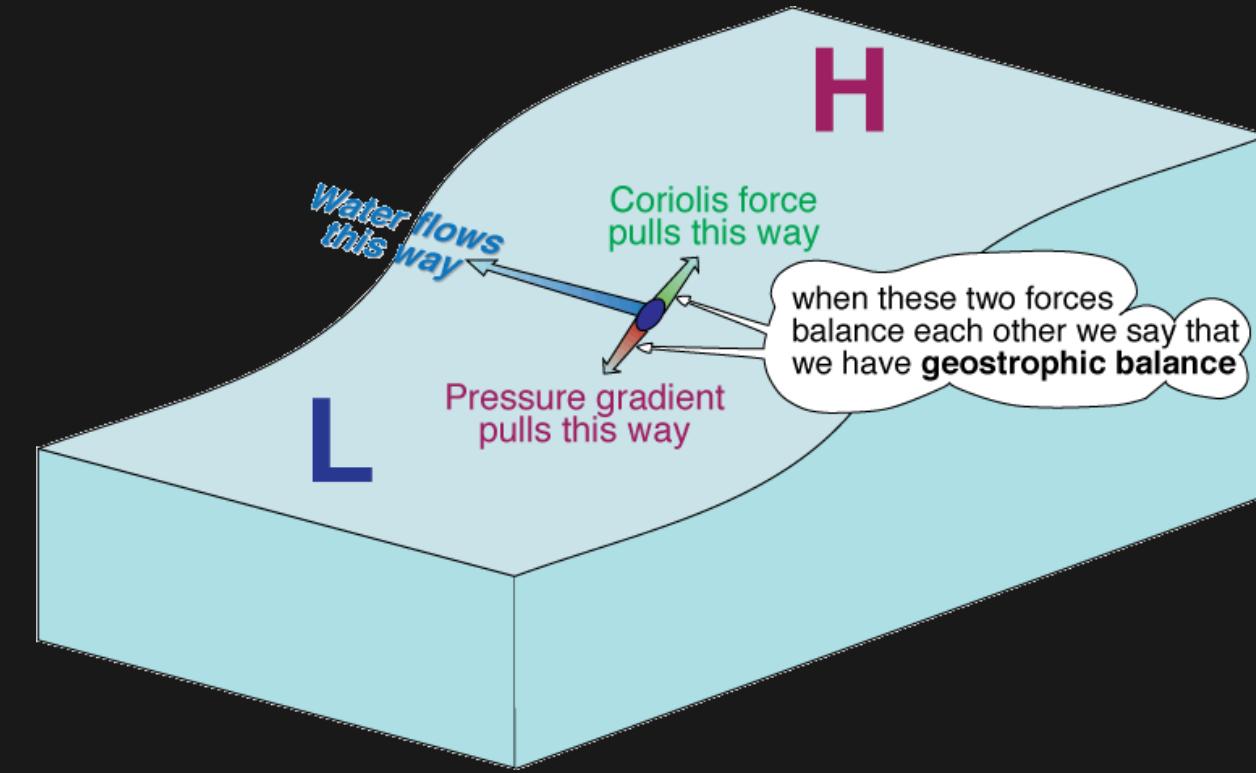
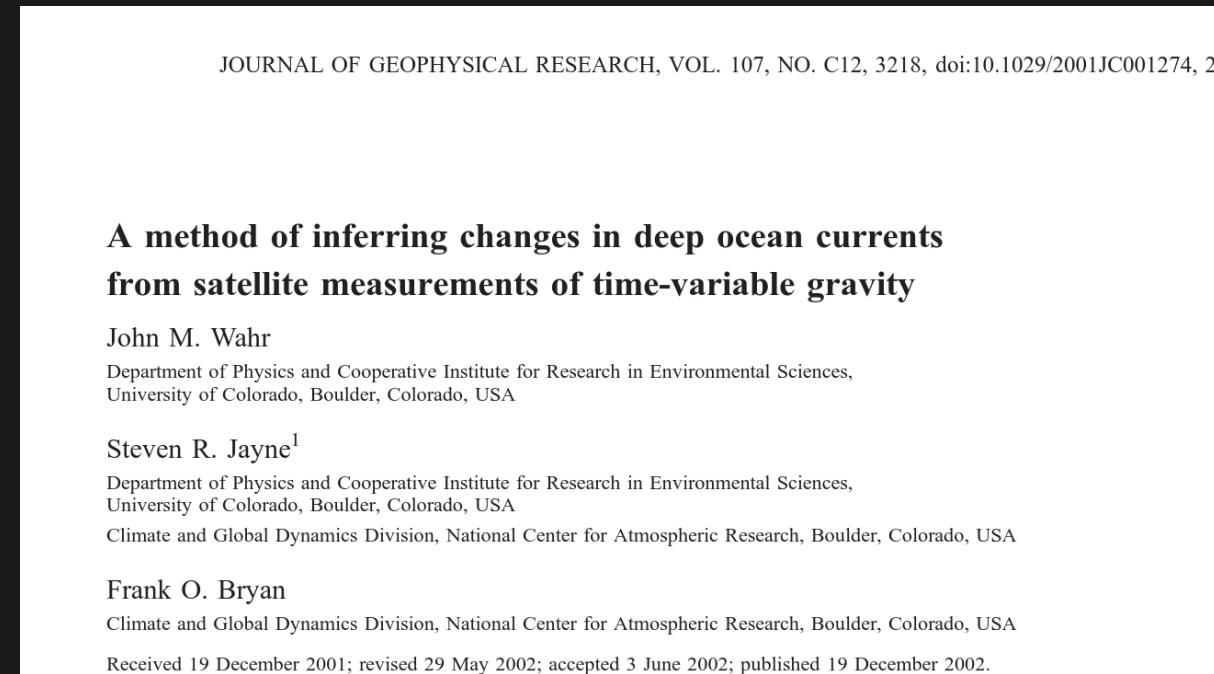
$$\text{Pressure gradient} \\ 2\rho_0 \Omega \times \mathbf{v} \approx -\nabla P \quad (2)$$

Earth rotation vector      ↑ velocity

- Assume horizontal constant velocities
- cross-product  $\rightarrow$  latitude dependency



# Geostrophic currents from time variable gravity



CC-NC-SA, <https://www.seos-project.eu>

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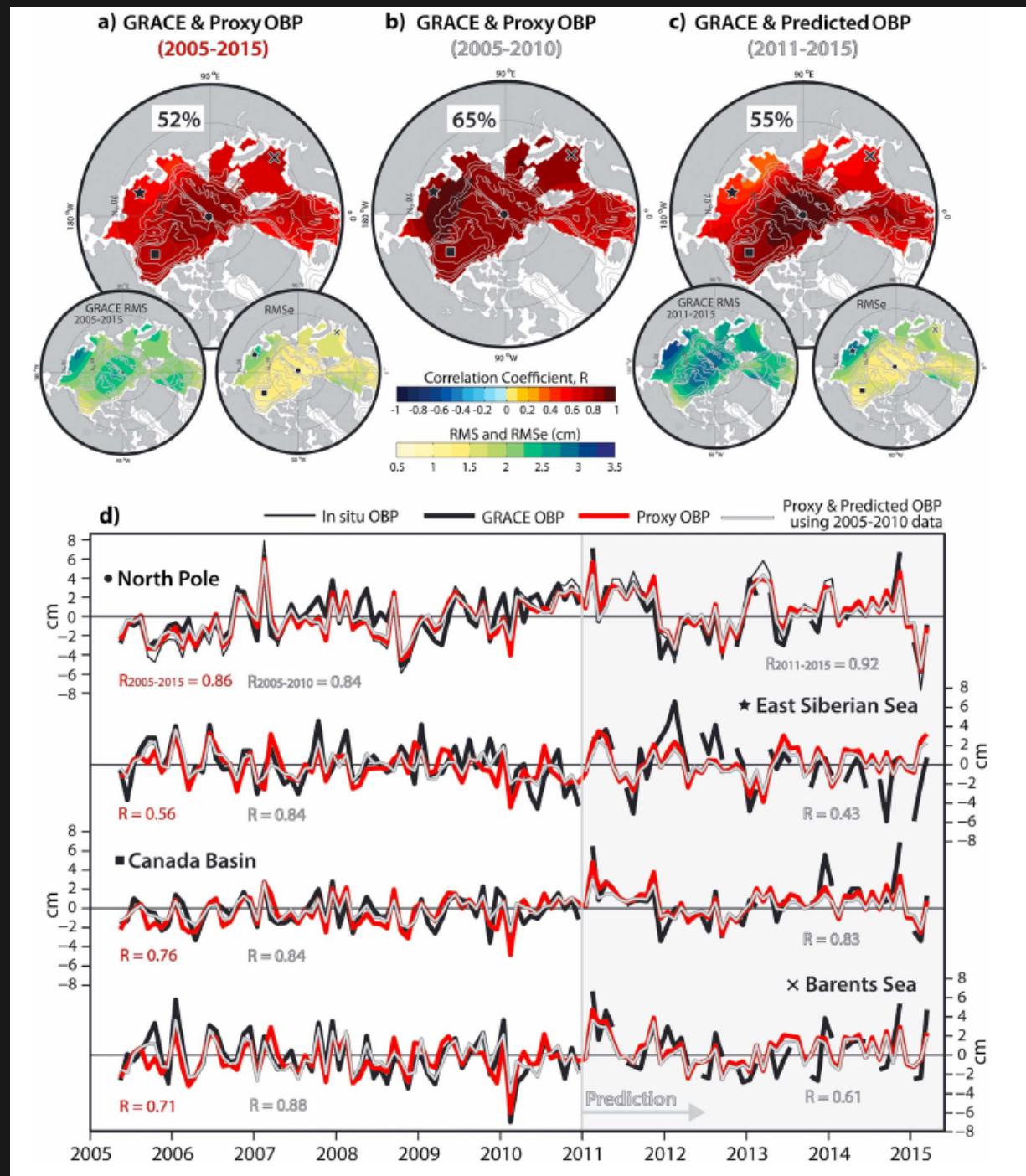
Earth rotation  
vector



- Assume horizontal constant velocities
- cross-product  $\rightarrow$  latitude dependency
- Velocity is orthogonal to gradient!



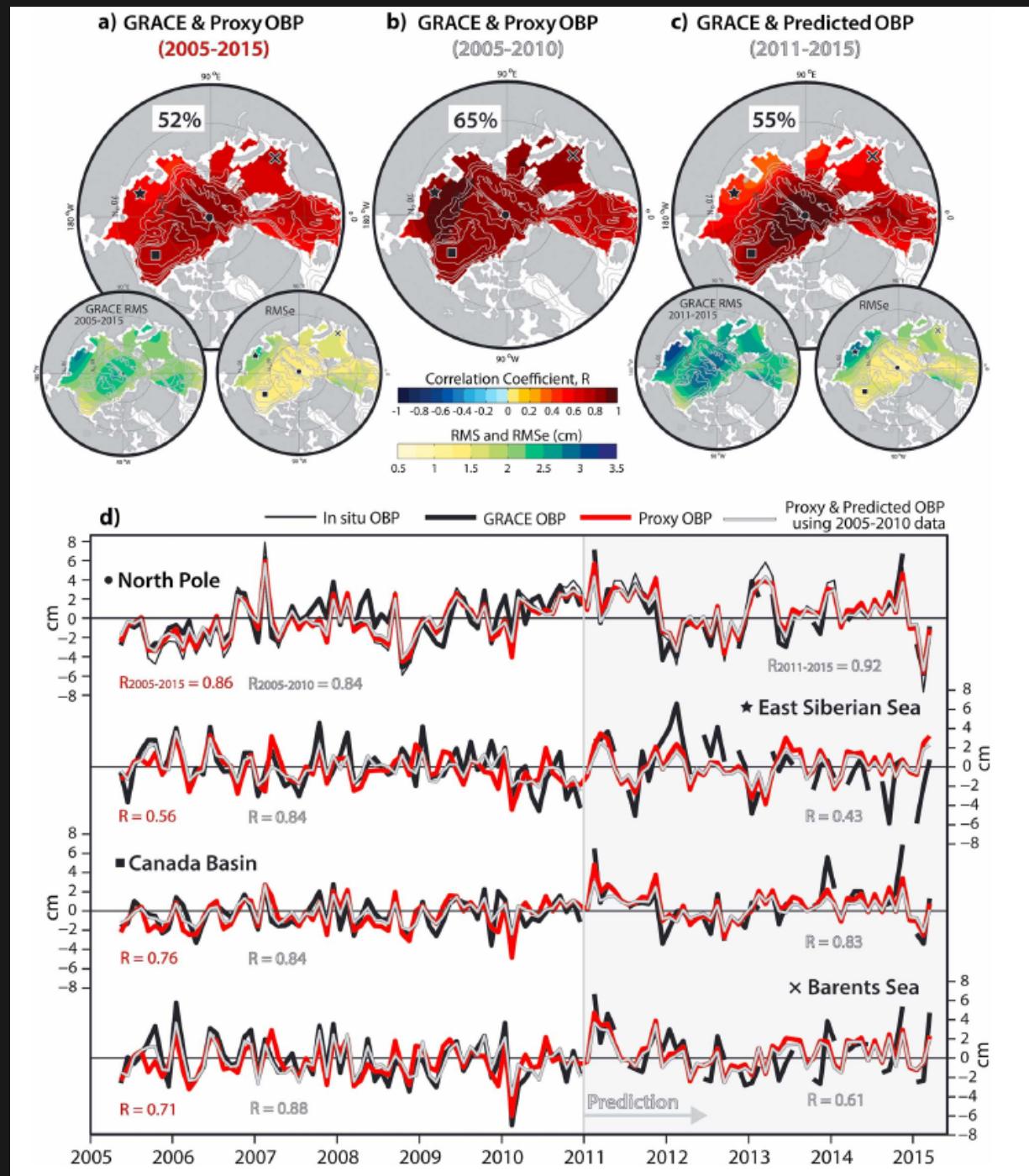
# Arctic Ocean Bottom pressure variations well captured by GRACE



From Peralta-ferriz et al. 2016



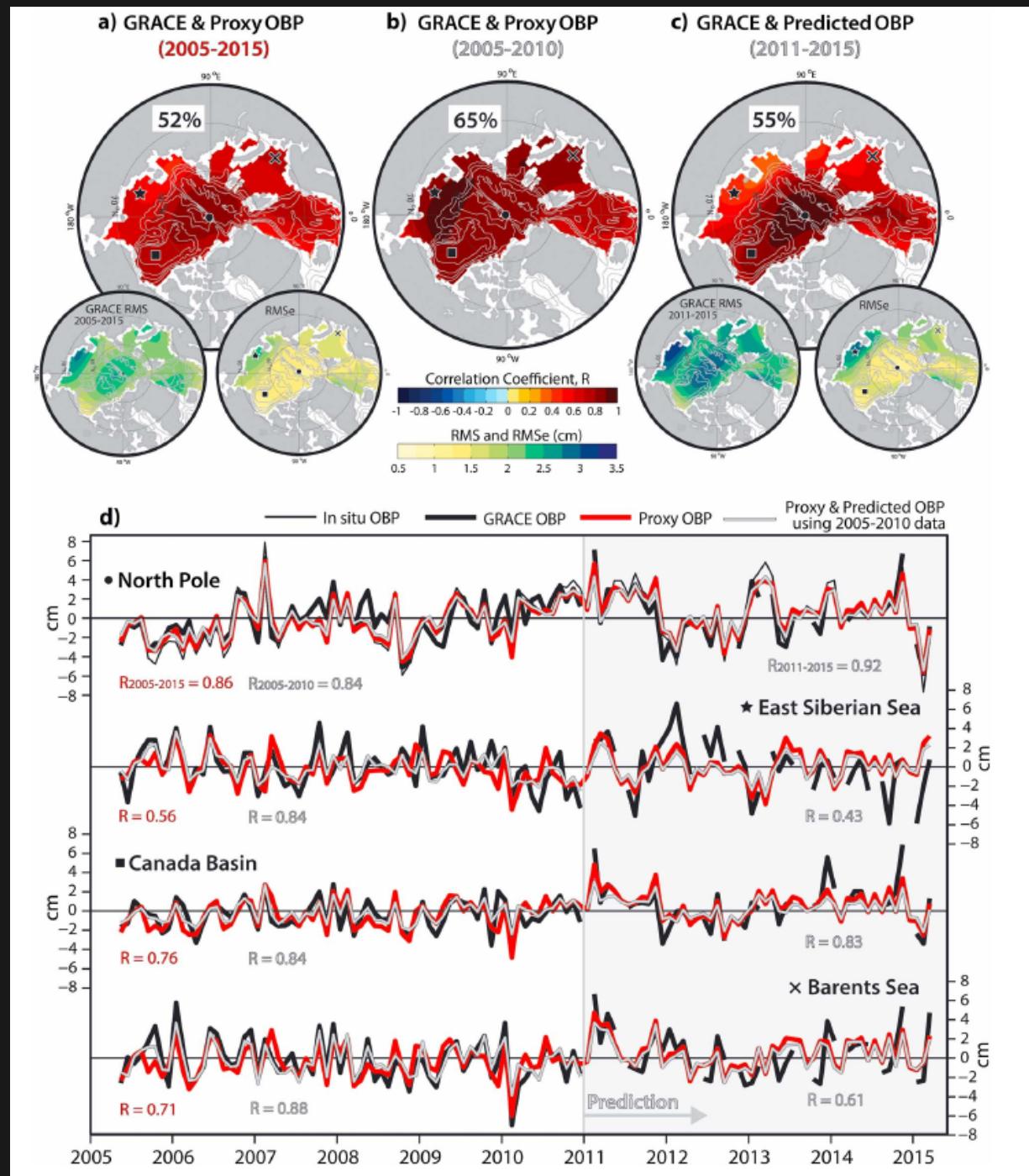
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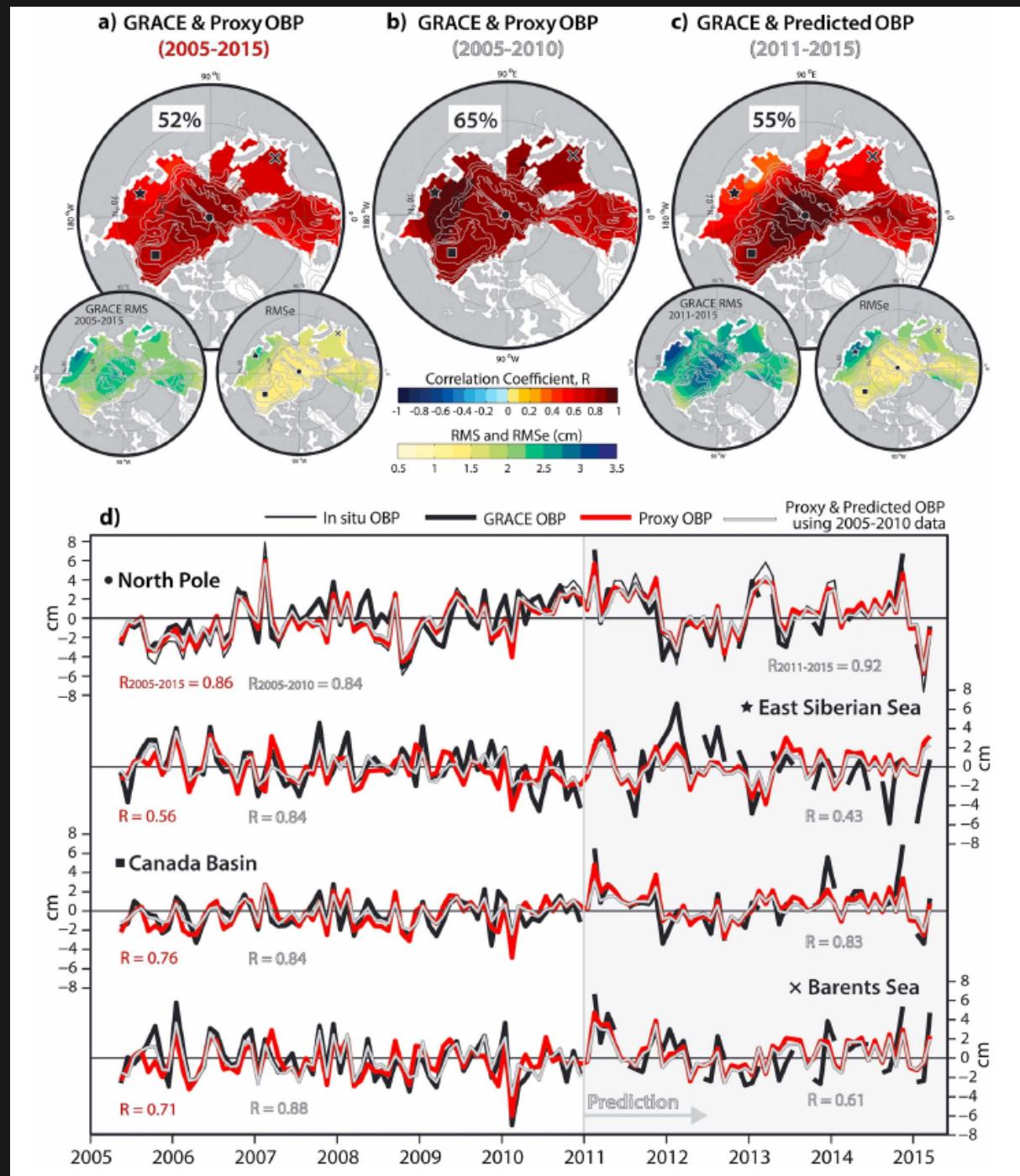
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- In situ OBP well captured by GRACE
- Coherent OBP signals in the Arctic

# Arctic Ocean Bottom pressure variations well captured by GRACE



From Peralta-ferriz et al. 2016

- In situ OBP well captured by GRACE
- Coherent OBP signals in the Arctic
- Comparison showed that a single in situ OBP can serve as proxy for the entire Arctic



# What have you learned?

- Adding mass to the ocean
  - Observable in time-variable gravity
  - GRACE (1.5 - 2 mm/yr global mean ocean mass change)
  - Different causes have non-uniform contributions (Ice sheets, hydrology, dam impoundment,..)
  - Regional sea level also influenced by: Self attraction and loading
- Churning the Ocean (currents and wind)
  - Integration of the water column -> OBP
  - OBP changes due to dynamic height differences and column density change
  - Steric sea level: density driven dynamic height changes under the assumption of no OBP change
  - Pressure gradients cause circulation (surface gradient may be different from bottom)



## Outlook

- Still many ocean applications unexplored (geostrophic currents!)
- Added value comes from combined data e.g. altimetry, Argo, etc.

