

Basic Probability

1.	D1	D2	
	1	1	$(1,1), (1,3), (1,5),$
	2	2	$(2,2), (2,4), (2,6),$
	3	3	$(3,1), (3,3), (3,5),$
	4	4	$(4,2), (4,4), (4,6),$
	5	5	$(5,1), (5,3), (5,5),$
	6	6	$(6,2), (6,4), (6,6)$

Total Possible Outcomes = 36

And the Sum of no's being even = 18

$$P_1(\text{Sum of no's being even}) = \frac{18}{36} = \frac{1}{2}$$

$$P_2(\text{One of die shows 6}) = \frac{4}{36} = \frac{1}{9}$$

2) D1 D2

D1	D2	1	2	3	4	5	6
1		2	3	4	5	6	7
2		3	4	5	6	7	8
3		4	5	6	7	8	9
4		5	6	7	8	9	10
5		6	7	8	9	10	11
6		7	8	9	10	11	12

No of Equally likely outcomes = $5 + 4 + 3 + 2 + 1 = 15$

Total possible outcomes = 36

$$P(\text{Sum of no's} < 7) = \frac{15}{36} = \frac{5}{12}$$

3) $P(2H | 1H) = ?$

$$P(2H) = \frac{4}{8}$$

H H H ✓

H H T ✓

H T H ✓

$$P(1H) = \frac{7}{8}$$

H T T

T H H ✓

$$P(2H | 1H) = \frac{P(2H \cap 1H)}{P(1H)}$$

T H T

T T H

$$\frac{P(2H)}{P(1H)} = \frac{\frac{4}{8}}{\frac{7}{8}} = \frac{4}{7}$$

T T T

$$\frac{4}{7}$$

Subject: _____

4) Total Possible outcomes = $\{(A, A), (A, B), (B, A), (B, B)\}$

$$P(A) = \frac{1}{4}$$

$$P(B) = \frac{3}{4}$$

$$\therefore P(A|B) = \frac{P(A \cap B)}{P(B)} \Rightarrow \frac{P(A)}{P(B)} = \frac{\frac{1}{4}}{\frac{3}{4}} = \frac{1}{3}$$

5) Conditional, Joint and Marginal Probability

$\frac{1}{3} R$	HT	$\frac{1}{2}$	Late	$\frac{1}{2}$
	NHT	$\frac{1}{2}$	Late	$\frac{1}{4}$
$\frac{2}{3} NR$	HT	$\frac{1}{4}$	Late	$\frac{1}{4}$
	NHT	$\frac{3}{4}$	Late	$\frac{1}{8}$

(a) $P(NR \cap HT) \cap NL$

$$[P(NR) \times P(HT|NR)] \cap NL$$

$$\left[\frac{2}{3} \times \frac{1}{4} \right] \cap NL \Rightarrow \left[\frac{1}{6} \right] \cap NL \Rightarrow \frac{1}{6} \times \frac{2}{4} = \frac{1}{8}$$

$$(b) P(L) = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{3} + \frac{1}{4} \times \frac{1}{2} \times \frac{1}{3} + \frac{1}{4} \times \frac{1}{4} \times \frac{2}{3} + \frac{1}{8} \times \frac{3}{4} \times \frac{2}{3}$$

$$P(L) \Rightarrow P(RTL) + P(RNTL) + P(NRTL) + P(NRNTL)$$

$$\Rightarrow \frac{1}{12} + \frac{1}{24} + \frac{1}{24} + \frac{1}{16} \Rightarrow \frac{11}{48}$$

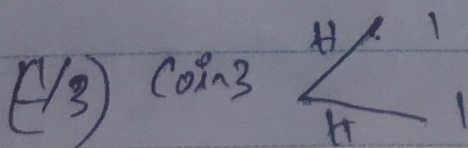
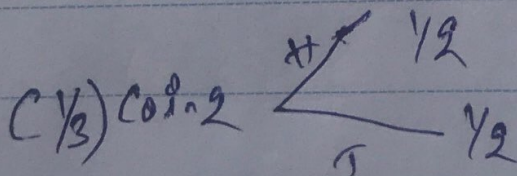
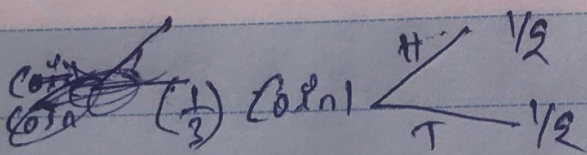
$$\downarrow$$

$$\frac{4+2+2+3}{48}$$

$$(c) P(R|L) = \frac{P(L|R) \times P(R)}{P(L)} = \frac{\frac{1}{2} \times \frac{1}{2} \times \frac{1}{3} + \frac{1}{4} \times \frac{1}{2} \times \frac{1}{3}}{11/48}$$

$$\Rightarrow \frac{\frac{1}{8}}{11/48} = \frac{6}{11}$$

6)



Subject: _____

$$(a) P(H) = \frac{1}{2} \times \frac{1}{3} + \frac{1}{2} \times \frac{1}{3} + 1 \times \frac{1}{3}$$

$$\Rightarrow \frac{1}{6} + \frac{1}{6} + \frac{1}{3} = \frac{2}{6} + \frac{1}{3}$$

$$\Rightarrow \frac{2}{3}$$

$$(b) P(2H/H) = \frac{P(H/2H) \times P(2H)}{P(H)}$$

$$\Rightarrow \frac{1 \times \frac{1}{3}}{\frac{2}{3}} \Rightarrow \frac{1}{2}$$

7) I guess this question is complete. kindly advise if I am missing something.

$$8) P(W) = 1/9 \quad P(T/W) = 5/6 \quad P(T/NW) = 1/6$$

$$P(NW) = 8/9$$

$$P(W/T) = \frac{P(T/W) \times P(W)}{P(T)}$$

$$\Rightarrow \frac{\frac{5}{6} \times \frac{1}{9}}{\frac{5}{6} \times \frac{1}{9} + \frac{1}{6} \times \frac{8}{9}} = \frac{5}{13}$$

$$9) P(T/b) = 4/5 \quad P(T/Nb) = 1/5 \quad P(b) = 1/6 \quad P(Nb) = 5/6$$

$$\Rightarrow P(b/T) = \frac{P(T/b) \times P(b)}{P(T)}$$

$$\Rightarrow \frac{4/5 \times 1/6}{4/5 \times 1/6 + 1/5 \times 5/6}$$

$$\frac{4/30}{9/30}$$

$$\Rightarrow \frac{4/30}{9/30}$$

$$\Rightarrow 4/9$$

$$10) P(M/S) = 40/100 \quad P(M) = 60/100$$

$$P(S/M) = \frac{P(M/S) \times P(S)}{P(M)} \Rightarrow \frac{P(M/S)}{P(M)}$$

$$\Rightarrow \frac{40/100}{60/100} = 2/3$$

11)

$$(a) P(M \cap G) = P(M) \times P(G/M)$$

$$\Rightarrow \frac{60}{100} \times \frac{19}{60}$$

$$\Rightarrow \frac{19}{100} \therefore \text{It is a joint Probability}$$

Subject: _____

$$(b) P(H) = \frac{60}{100} = 3/5$$

$$(d) P(F/Pa) = \frac{P(Pa/F) \times P(F)}{P(Pa)}$$

$$= \frac{\frac{28}{40} \times \frac{40}{100}}{\frac{69}{100}} = \frac{28}{69} \therefore \text{it is Conditional Probability}$$

$$(c) P(A) = \frac{31}{100} \therefore \text{it is marginal Probability}$$

2) Bayes Theorem

$$P(F) = 0.1 \quad P(NF) = 0.9 \quad P(F/\text{Positive}) = ?$$

$$\frac{P(\text{Positive}/F) \times P(F)}{P(\text{Positive})}$$

$$= \frac{92}{100} \times 0.1$$

$$\frac{\frac{92}{100} \times 0.1 + \frac{10}{100} \times 0.9}{1} = 0.50$$

13. I am not able to understand this question.

14	S	NS
Positive Prob	99%	1%
Negative	0%	100%

$$P(S) = \frac{1}{10,000} = 0.0001$$

$$P(NS) = 0.9999$$

$$P(S/\text{Positive}) = ?$$

$$\frac{P(\text{Positive}/S) \times P(S)}{P(\text{Positive})}$$

$$= \frac{99}{100} \times 0.0001$$

$$\frac{99}{100} \times 0.0001 + \frac{1}{100} \times 0.9999$$

$$= 0.0098$$

THE END

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