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# PyBayes API Documentation

*Release 0.3-63-g5fe2330*

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September 03, 2012

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# Chapter 1

## PyBayes

### 1.1 About

PyBayes is an object-oriented Python library for recursive Bayesian estimation (Bayesian filtering) that is convenient to use. Already implemented are Kalman filter, particle filter and marginalized particle filter, all built atop of a light framework of probability density functions. PyBayes can optionally use Cython for large speed gains (Cython build can be several times faster in some situations).

PyBayes is tested with Python 2.7 and 3.2 (using 2to3). Future plans include more specialised variants of Kalman/particle filters and speed optimisations.

PyBayes is being developed by Matěj Laitl, feel free to send me a mail to matej at laidl dot cz. See ChangeLog.rst file to review a list of most important changes in recent versions.

Automatically generated **documentation** can be found at <http://strohel.github.com/PyBayes-doc/>

#### 1.1.1 Licensing

PyBayes is currently distributed under GNU GPL v2+ license. The authors of PyBayes are however open to other licensing suggestions. (Do you want to use PyBayes in e.g. BSD-licensed project? Ask!)

### 1.2 Obtaining PyBayes

PyBayes releases can be found in .tar.gz format at [github](#) or [PyPI](#). These releases bundle the Tokyo project for convenience. Binary packages for CentOS, Debian, Fedora, RHEL, OpenSUSE and Ubuntu can be downloaded from the [OpenSUSE Build Service](#); these packages are fast Cython builds. (with no requirement to install Cython for building)

Development of PyBayes happens on <http://github.com/strohel/PyBayes> using git VCS and the most fresh development sources can be obtained using git. It should be noted that PyBayes uses git submodule to bundle Tokyo library, so the proper way to clone PyBayes repository would be:

```
# cd path/to/projects
# git clone git://github.com/strohel/PyBayes.git
Cloning into PyBayes...
(...)
# cd PyBayes
# git submodule update --init
Submodule 'tokyo' (git://github.com/strohel/Tokyo.git) registered for path 'tokyo'
Cloning into tokyo...
(...)
Submodule path 'tokyo': checked out '896d046b62cf50faf7faa7e58a8705fb2f22f19a'
```

When updating your repository (using `git pull`), git should inform you that some submodules have become outdated. In that case you should issue `git submodule update`.

## 1.3 Installing PyBayes

PyBayes uses standard Python distutils for building and installation. Follow these steps in order to install PyBayes:

- download PyBayes, let's assume PyBayes-0.1.tar.gz filename
- unpack it:  

```
tar -xvf PyBayes-0.1.tar.gz
```
- change directory into PyBayes source:  

```
cd Pybayes-0.1
```
- build and install (either run as root or install to a user-writeable directory <sup>1</sup>):  

```
./setup.py install
```

**And you're done!** However, if you want PyBayes to be *considerably faster*, please read the following section.

### 1.3.1 Advanced installation options

PyBayes can use Cython to build itself into binary Python module. Such binary modules are transparent to Python in a way that Python treats them as any other modules (you can `import` them as usual). Interpreter overhead is avoided and many other optimisation options arise this way.

In order to build optimised PyBayes, you'll additionally need:

- [Cython](#) Python to C compiler, version **0.14.1** or newer
- working C compiler (GCC on Unix-like systems, MinGW or Microsoft Visual C on Windows <sup>2</sup>)
- [NumPy](#) numerical library for Python, version 1.5 or greater (NumPy is needed also in Python build, but older version suffice in that case)

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<sup>1</sup> <http://docs.python.org/install/#alternate-installation>

<sup>2</sup> <http://docs.cython.org/src/quickstart/install.html>

- On some Debian-based Linux distributions (Ubuntu) you'll need python-dev package that contains `Python.h` file that is needed by PyBayes

Proceed with following steps:

1. Install all required dependencies. They should be already available in your package manager if you use a modern Linux Distribution.
2. Unpack and install PyBayes as described above, you should see following message during build:

```
Cython and NumPy found, enabling optimised Cython build.
```

- in order to be 100% sure that optimised build is used, you can add `--use-cython=yes` option to the `./setup.py` call. You can force pure Python mode even when Cython is installed, pass `--use-cython=no`. By default, PyBayes auto-detects Cython and NumPy presence on system.
- if you plan to profile code that uses optimised PyBayes, you may want to embed profiling information into PyBayes. This can be accomplished by passing `--profile=yes` to `./setup.py`. The default is to omit profiling information in order to avoid performance penalties.
- all standard and custom build parameters can be listed using `./setup.py --help`

The best results performance-wise are achieved when also your code that uses or extends PyBayes is compiled by Cython and uses static typing where appropriate. Remember to `cimport pybayes[.something]` everytime you `import pybayes[.something]` so that fast Cython calling convention is used.

### 1.3.2 Building Documentation

*There is no need to build documentation yourself, an online version is at <http://strohel.github.com/PyBayes-doc/>*

PyBayes uses [Sphinx](#) to prepare documentation, version 1.0 or greater is required. The documentation is built separately from the python build process. In order to build it, change directory to `doc/` under PyBayes source directory (`cd [path_to_pybayes]/doc`) and issue `make` command. This will present you with a list of available documentation formats. To generate html documentation, for example, run `make html` and then point your browser to `[path_to_pybayes]/doc/_build/html/index.html`.

PyBayes docs contain many mathematical expressions; [Sphinx](#) can use [LaTeX](#) to embed them as images into resulting HTML pages. Be sure to have LaTeX-enabled Sphinx if you want to see such nice things.

## 1.4 Testing

PyBayes comes with a comprehensive test and stress-suite that can and should be used to verify that your PyBayes build works as expected.

Since version 0.4, testing is integrated into the `setup.py` script and can be run without installing PyBayes. In order to run PyBayes test-suite, simply issue `./setup.py test` from within the source directory. To run tests during installation procedure, simply install like this: `./setup.py`

`build test install`. Failing tests cause installation to fail, but this can be overridden using *-non-fatal* option of the *test* command.

If you want to test your already installed PyBayes instance, simply issue `python -m pybayes.tests` anytime, anywhere. :-)

#### 1.4.1 Stress-testing

Stress testing is not yet ported to the *setup.py*, see the *support/run\_stresses.py* script.

## Chapter 2

# PyBayes Change Log

This file mentions important changes between PyBayes version that are important for its users. Most recent versions are mentioned on top.

### 2.1 Changes between 0.3 and 0.4

- Test-suite no longer needs PyBayes to be installed, yay! (no privilege problems etc.)
- Build-system was rewritten so that it is no longer an ugly hack. .pxd and .py files are now installed along .so (.dll) files for interoperability and additional openness. Better parsing of setup.py arguments and custom parameters visible in the `-help` command.
- (C)Pdf `shape()` and `cond_shape()` functions are no longer abstract and just return *self.rv.dimension* and *self.cond\_rv.dimension* respectively. CPdf subclasses therefore should not implement these methods. This is a backwards compatible change API-wise.



## Chapter 3

# Probability Density Functions

This module contains models of common probability density functions, abbreviated as pdfs.

All classes from this module are currently imported to top-level pybayes module, so instead of `from pybayes.pdfs import Pdf` you can type `from pybayes import Pdf`.

### 3.1 Random Variables and their Components

`class pybayes.pdfs.RV(*components)`

Representation of a random variable made of one or more components. Each component is represented by [RVComp](#) (page 7) class.

#### Variables

- **dimension** (*int*) – cumulative dimension; do not change
- **name** (*str*) – pretty name, can be changed but needs to be a string
- **components** (*list*) – list of RVComps; do not change

*Please take into account that all RVComp comparisons inside RV are instance-based and component names are purely informational. To demonstrate:*

```
>>> rv = RV(RVComp(1, "a"))
>>> ...
>>> rv.contains(RVComp(1, "a"))
False
```

Right way to do this would be:

```
>>> a = RVComp(1, "arbitrary pretty name for a")
>>> rv = RV(a)
>>> ...
>>> rv.contains(a)
True
```

`__init__(*components)`

Initialise random variable meta-representation.

**Parameters** `*components` ([RV](#) (page 6), [RVComp](#) (page 7) or a sequence of [RVComp](#) (page 7) items) – components that should form the random

variable. You may also pass another RVs which is a shortcut for adding all their components.

**Raises `TypeError`** invalid object passed (neither a [RV](#) (page 6) or a [RVComp](#) (page 7))

Usual way of creating a RV could be:

```
>>> x = RV(RVComp(1, 'x_1'), RVComp(1, 'x_2'))
>>> x.name
'x_1, x_2'
>>> xy = RV(x, RVComp(2, 'y'))
>>> xy.name
'x_1, x_2, y'
```

**`contains(component)`**

Return True if this random variable contains the exact same instance of the **component**.

**Parameters `component`** ([RVComp](#) (page 7)) – component whose presence is tested

**Return type** bool

**`contains_all(test_components)`**

Return True if this RV contains all RVComps from sequence **test\_components**.

**Parameters `test_components`** (sequence of [RVComp](#) (page 7) items) – list of components whose presence is checked

**`contains_any(test_components)`**

Return True if this RV contains any of **test\_components**.

**Parameters `test_components`** (sequence of [RVComp](#) (page 7) items) – sequence of components whose presence is tested

**`contained_in(test_components)`**

Return True if sequence **test\_components** contains all components from this RV (and perhaps more).

**Parameters `test_components`** (sequence of [RVComp](#) (page 7) items) – set of components whose presence is checked

**`indexed_in(super_rv)`**

Return index array such that this rv is indexed in **super\_rv**, which must be a superset of this rv. Resulting array can be used with [numpy.take\(\)](#) and [numpy.put\(\)](#).

**Parameters `super_rv`** ([RV](#) (page 6)) – returned indices apply to this rv

**Return type** 1D [numpy.ndarray](#) of ints with dimension = self.dimension

**class `pybayes.pdfs.RVComp(dimension, name=None)`**

Atomic component of a random variable.

**Variables**

- **dimension** (*int*) – dimension; do not change unless you know what you are doing
- **name** (*str*) – name; can be changed as long as it remains a string (warning: parent RVs are not updated)

`__init__(dimension, name=None)`

Initialise new component of a random variable [RV](#) (page 6).

#### Parameters

- **dimension** (*positive integer*) – number of vector components this component occupies
- **name** (*string or None*) – name of the component; default: None for anonymous component

#### Raises

- **TypeError** – non-integer dimension or non-string name
- **ValueError** – non-positive dimension

## 3.2 Probability Density Function prototype

`class pybayes.pdfs.CPdf`

Base class for all Conditional (in general) Probability Density Functions.

When you evaluate a CPdf the result generally also depends on a condition (vector) named *cond* in PyBayes. For a CPdf that is a [Pdf](#) (page 9) this is not the case, the result is unconditional.

Every CPdf takes (apart from others) 2 optional arguments to constructor: **rv** and **cond\_rv**. (both [RV](#) (page 6) or a sequence of [RVComp](#) (page 7) objects) When specified, they denote that the CPdf is associated with a particular random variable (respectively its condition is associated with a particular random variable); when unspecified, *anonymous* random variable is assumed (exceptions exist, see [ProdPdf](#) (page 13)). It is an error to pass RV whose dimension is not same as CPdf's dimension (or cond dimension respectively).

#### Variables

- **rv** (*RV*) – associated random variable (always set in constructor, contains at least one RVComp)
- **cond\_rv** (*RV*) – associated condition random variable (set in constructor to potentially empty RV)

*While you can assign different rv and cond\_rv to a CPdf, you should be cautious because sanity checks are only performed in constructor.*

While entire idea of random variable associations may not be needed in simple cases, it allows you to express more complicated situations. Assume the state variable is composed of 2 components  $x_t = [a_t, b_t]$  and following probability density function has to be modelled:

$$\begin{aligned} p(x_t|x_{t-1}) &= p_1(a_t|a_{t-1}, b_t)p_2(b_t|b_{t-1}) \\ p_1(a_t|a_{t-1}, b_t) &= \mathcal{N}(a_{t-1}, b_t) \\ p_2(b_t|b_{t-1}) &= \mathcal{N}(b_{t-1}, 0.0001) \end{aligned}$$

This is done in PyBayes with associated RVs:

```
>>> a_t, b_t = RVComp(1, 'a_t'), RVComp(1, 'b_t') # create RV components
>>> a_tp, b_tp = RVComp(1, 'a_{t-1}'), RVComp(1, 'b_{t-1}') # t-1 case
```

```
>>> p1 = LinGaussCPdf(1., 0., 1., 0., [a_t], [a_tp, b_t])
>>> # params for p2:
>>> cov, A, b = np.array([[0.0001]]), np.array([[1.]]), np.array([0.])
>>> p2 = MLinGaussCPdf(cov, A, b, [b_t], [b_tp])

>>> p = ProdCPdf((p1, p2), [a_t, b_t], [a_tp, b_tp])

>>> p.sample(np.array([1., 2.]))
>>> p.eval_log()
```

**shape()**

Return pdf shape = number of dimensions of the random variable.

**mean()** (page 9) and **variance()** (page 9) methods must return arrays of this shape. Default implementation (which you should not override) just returns `self.rv.dimension`.

**Return type** int

**cond\_shape()**

Return condition shape = number of dimensions of the conditioning variable.

Default implementation (which you should not override) just returns `self.cond_rv.dimension`.

**Return type** int

**mean(cond=None)**

Return (conditional) mean value of the pdf.

**Return type** `numpy.ndarray`

**variance(cond=None)**

Return (conditional) variance (diagonal elements of covariance).

**Return type** `numpy.ndarray`

**eval\_log(x, cond=None)**

Return logarithm of (conditional) likelihood function in point x.

**Parameters** **x** (`numpy.ndarray`) – point which to evaluate the function in

**Return type** double

**sample(cond=None)**

Return one random (conditional) sample from this distribution

**Return type** `numpy.ndarray`

**samples(n, cond=None)**

Return n samples in an array. A convenience function that just calls **shape()** (page 9) multiple times.

**Parameters** **n** (*int*) – number of samples to return

**Return type** 2D `numpy.ndarray` of shape (n, m) where m is pdf dimension

**class** `pybayes.pdfs.Pdf`

Base class for all unconditional (static) multivariate Probability Density Functions. Subclass of **CPdf** (page 8).

As in CPdf, constructor of every Pdf takes optional **rv** ([RV](#) (page 6)) keyword argument (and no `cond_rv` argument as it would make no sense). For discussion about associated random variables see [CPdf](#) (page 8).

`cond_shape()`

Return zero as Pdfs have no condition.

### 3.3 Unconditional Probability Density Functions (pdfs)

`class pybayes.pdfs.UniPdf(a, b, rv=None)`

Simple uniform multivariate probability density function. Extends [Pdf](#) (page 9).

$$f(x) = \Theta(x - a)\Theta(b - x) \prod_{i=1}^n \frac{1}{b_i - a_i}$$

#### Variables

- **a** – left border
- **b** – right border

You may modify these attributes as long as you don't change their shape and assumption **a** < **b** still holds.

`__init__(a, b, rv=None)`

Initialise uniform distribution.

#### Parameters

- **a** (1D `numpy.ndarray`) – left border
- **b** (1D `numpy.ndarray`) – right border

**b** must be greater (in each dimension) than **a**. To construct uniform distribution on interval  $[0,1]$ :

```
>>> uni = UniPdf(np.array([0.]), np.array([1.]), rv)
```

`class pybayes.pdfs.AbstractGaussPdf`

Abstract base for all Gaussian-like pdfs - the ones that take vector mean and matrix covariance parameters. Extends [Pdf](#) (page 9).

#### Variables

- **mu** – mean value
- **R** – covariance matrix

You can modify object parameters only if you are absolutely sure that you pass allowable values - parameters are only checked once in constructor.

`class pybayes.pdfs.GaussPdf(mean, cov, rv=None)`

Unconditional Gaussian (normal) probability density function. Extends [AbstractGaussPdf](#) (page 10).

$$f(x) \propto \exp(-(x - \mu)' R^{-1} (x - \mu))$$

```
__init__(mean, cov, rv=None)
    Initialise Gaussian pdf.
```

#### Parameters

- **mean** (1D `numpy.ndarray`) – mean value; stored in **mu** attribute
- **cov** (2D `numpy.ndarray`) – covariance matrix; stored in **R** attribute

Covariance matrix **cov** must be *positive definite*. This is not checked during initialisation; it fail or give incorrect results in `eval_log()` (page 9) or `sample()` (page 9). To create standard normal distribution:

```
>>> # note that cov is a matrix because of the double [[ and ]]
>>> norm = GaussPdf(np.array([0.]), np.array([[1.]])
```

```
class pybayes.pdfs.LogNormPdf(mean, cov, rv=None)
    Unconditional log-normal probability density function. Extends AbstractGaussPdf (page 10).
```

More precisely, the density of random variable  $Y$  where  $Y = \exp(X)$ ;  $X \sim \mathcal{N}(\mu, R)$

```
__init__(mean, cov, rv=None)
    Initialise log-normal pdf.
```

#### Parameters

- **mean** (1D `numpy.ndarray`) – mean value of the **logarithm** of the associated random variable
- **cov** (2D `numpy.ndarray`) – covariance matrix of the **logarithm** of the associated random variable

A current limitation is that `LogNormPdf` is only univariate. To create standard log-normal distribution:

```
>>> lognorm = LogNormPdf(np.array([0.]), np.array([[1.]]) # note the shape of covariance
```

```
class pybayes.pdfs.GammaPdf(k, theta, rv=None)
    Gamma distribution with shape parameter  $k$  and scale parameter  $\theta$ . Extends Pdf (page 9).
```

$$f(x) = \frac{1}{\Gamma(k)\theta^k} x^{k-1} e^{-\frac{x}{\theta}}$$

```
__init__(k, theta, rv=None)
    Initialise Gamma pdf.
```

#### Parameters

- **k** (*double*) –  $k$  shape parameter above
- **theta** (*double*) –  $\theta$  scale parameter above

```
class pybayes.pdfs.InverseGammaPdf(alpha, beta, rv=None)
    Inverse gamma distribution with shape parameter  $\alpha$  and scale parameter  $\beta$ . Extends Pdf (page 9).
```

If random variable  $X \sim \text{Gamma}(k, \theta)$  then  $Y = 1/X$  will have distribution  $\text{InverseGamma}(k, 1/\theta)$  i.e.  $\alpha = k, \beta = 1/\theta$

$$f(x) = \frac{\beta^\alpha}{\Gamma(\alpha)} x^{-\alpha-1} e^{-\frac{\beta}{x}}$$

`__init__(alpha, beta, rv=None)`  
Initialise Inverse gamma pdf.

#### Parameters

- **alpha** (*double*) –  $\alpha$  shape parameter above
- **beta** (*double*) –  $\beta$  scale parameter above

`class pybayes.pdfs.AbstractEmpPdf`

An abstraction of empirical probability density functions that provides common methods such as weight normalisation. Extends [Pdf](#) (page 9).

**Variables** **weights** (*numpy.ndarray*) – 1D array of particle weights  $\omega_i \geq 0 \forall i; \sum \omega_i = 1$

`normalise_weights()`

Multiply weights by appropriate constant so that  $\sum \omega_i = 1$

**Raises** **AttributeError** when  $\exists i : \omega_i < 0$  or  $\forall i : \omega_i = 0$

`get_resample_indices()`

Calculate first step of resampling process (dropping low-weight particles and replacing them with more weighted ones).

**Returns** integer array of length n:  $(a_1, a_2 \dots a_n)$  where  $a_i$  means that particle at  $i$ th place should be replaced with particle number  $a_i$

**Return type** *numpy.ndarray* of ints

*This method doesnt modify underlying pdf in any way - it merely calculates how particles should be replaced.*

`class pybayes.pdfs.EmpPdf(init_particles, rv=None)`

Weighted empirical probability density function. Extends [AbstractEmpPdf](#) (page 12).

$$p(x) = \sum_{i=1}^n \omega_i \delta(x - x^{(i)})$$

where  $x^{(i)}$  is value of the  $i^{th}$  particle

$$\omega_i \geq 0 \text{ is weight of the } i^{th} \text{ particle} \quad \sum \omega_i = 1$$

**Variables** **particles** (*numpy.ndarray*) – 2D array of particles; shape: (n, m)  
where n is the number of particles, m dimension of this pdf

You may alter particles and weights, but you must ensure that their shapes match and that weight constraints still hold. You can use [normalise\\_weights\(\)](#) (page 12) to do some work for you.

`__init__(init_particles, rv=None)`  
Initialise empirical pdf.

**Parameters** `init_particles` (`numpy.ndarray`) – 2D array of initial particles; shape  $(n, m)$  determines that  $n$   $m$ -dimensioned particles will be used. *Warning: EmpPdf does not copy the particles - it rather uses passed array through its lifetime, so it is not safe to reuse it for other purposes.*

`resample()`

Drop low-weight particles, replace them with copies of more weighted ones. Also reset weights to uniform.

`transition_using(i, transition_cpdf)`

Transition  $i$ -th particle from  $t - 1$  to  $t$  by sampling from `transition_cpdf`  $p(x_t|x_{t-1})$

**class** `pybayes.pdfs.MarginalizedEmpPdf`(`init_gausses`, `init_particles`, `rv=None`)

An extension to empirical pdf (`EmpPdf` (page 12)) used as posterior density by `MarginalizedParticleFilter` (page 21). Extends `AbstractEmpPdf` (page 12).

Assume that random variable  $x$  can be divided into 2 independent parts  $x = [a, b]$ , then probability density function can be written as

$$p(a, b) = \sum_{i=1}^n \omega_i \left[ \mathcal{N} \left( \hat{a}^{(i)}, P^{(i)} \right) \right]_a \delta(b - b^{(i)})$$

where  $\hat{a}^{(i)}$  and  $P^{(i)}$  is mean and covariance of  $i^{th}$  gauss pdf

$b^{(i)}$  is value of the (second part of the)  $i^{th}$  particle

$\omega_i \geq 0$  is weight of the  $i^{th}$  particle  $\sum \omega_i = 1$

### Variables

- **gausses** (`numpy.ndarray`) – 1D array that holds `GaussPdf` (page 10) for each particle; shape:  $(n)$  where  $n$  is the number of particles
- **particles** (`numpy.ndarray`) – 2D array of particles; shape:  $(n, m)$  where  $n$  is the number of particles,  $m$  dimension of the “empirical” part of random variable

You may alter particles and weights, but you must ensure that their shapes match and that weight constraints still hold. You can use `normalise_weights()` (page 12) to do some work for you.

*Note: this pdf could have been coded as ProdPdf of EmpPdf and a mixture of GaussPdfs. However it is implemented explicitly for simplicity and speed reasons.*

`__init__`(`init_gausses`, `init_particles`, `rv=None`)

Initialise marginalized empirical pdf.

### Parameters

- **init\_gausses** (`numpy.ndarray`) – 1D array of `GaussPdf` (page 10) objects, all must have the dimension
- **init\_particles** (`numpy.ndarray`) – 2D array of initial particles; shape  $(n, m)$  determines that  $n$  particles whose *empirical* part will have dimension  $m$

*Warning: MarginalizedEmpPdf does not copy the particles - it rather uses both passed arrays through its lifetime, so it is not safe to reuse them for other purposes.*



**class** pybayes.pdfs.ProdPdf(*factors*, *rv=None*)

Unconditional product of multiple unconditional pdfs.

You can for example create a pdf that has uniform distribution with regards to x-axis and normal distribution along y-axis. The caller (you) must ensure that individual random variables are independent, otherwise their product may have no mathematical sense. Extends Pdf (page 9).

$$f(x_1x_2x_3) = f_1(x_1)f_2(x_2)f_3(x_3)$$

**\_\_init\_\_**(*factors*, *rv=None*)

Initialise product of unconditional pdfs.

**Parameters** *factors* (sequence of Pdf (page 9)) – sequence of sub-distributions

As an exception from the general rule, ProdPdf does not create anonymous associated random variable if you do not supply it in constructor - it rather reuses components of underlying factor pdfs. (You can of course override this behaviour by passing custom *rv*.)

Usual way of creating ProdPdf could be:

```
>>> prod = ProdPdf((UniPdf(...), GaussPdf(...))) # note the double (( and ))
```

### 3.4 Conditional Probability Density Functions (cpdfs)

In this section, variable *c* in math expressions denotes condition.

**class** pybayes.pdfs.MLinGaussCPdf(*cov*, *A*, *b*, *rv=None*, *cond\_rv=None*, *base\_class=None*)

Conditional Gaussian pdf whose mean is a linear function of condition. Extends CPdf (page 8).

$$f(x|c) \propto \exp(-(x - \mu)' R^{-1} (x - \mu)) \quad \text{where } \mu = Ac + b$$

**\_\_init\_\_**(*cov*, *A*, *b*, *rv=None*, *cond\_rv=None*, *base\_class=None*)

Initialise Mean-Linear Gaussian conditional pdf.

**Parameters**

- **cov** (2D `numpy.ndarray`) – covariance of underlying Gaussian pdf
- **A** (2D `numpy.ndarray`) – given condition *c*,  $\mu = Ac + b$
- **b** (1D `numpy.ndarray`) – see above
- **base\_class** (*class*) – class whose instance is created as a base pdf for this cpdf. Must be a subclass of `AbstractGaussPdf` (page 10) and the default is `GaussPdf` (page 10). One alternative is `LogNormPdf` (page 11) for example.

```
class pybayes.pdfs.LinGaussCPdf(a, b, c, d, rv=None, cond_rv=None,
                               base_class=None)
```

Conditional one-dimensional Gaussian pdf whose mean and covariance are linear functions of condition. Extends [CPdf](#) (page 8).

$$f(x|c_1c_2) \propto \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right) \quad \text{where} \quad \mu = ac_1 + b \quad \text{and} \quad \sigma^2 = cc_2 + d$$

```
__init__(a, b, c, d, rv=None, cond_rv=None, base_class=None)
```

Initialise Linear Gaussian conditional pdf.

#### Parameters

- **a, b** (*double*) – mean =  $a \cdot \text{cond\_1} + b$
- **c, d** (*double*) – covariance =  $c \cdot \text{cond\_2} + d$
- **base\_class** (*class*) – class whose instance is created as a base pdf for this cpdf. Must be a subclass of [AbstractGaussPdf](#) (page 10) and the default is [GaussPdf](#) (page 10). One alternative is [LogNormPdf](#) (page 11) for example.

```
class pybayes.pdfs.GaussCPdf(shape, cond_shape, f, g, rv=None, cond_rv=None,
                             base_class=None)
```

The most general normal conditional pdf. Use it only if you cannot use [MLinGaussCPdf](#) (page 14) or [LinGaussCPdf](#) (page 14) as this cpdf is least optimised. Extends [CPdf](#) (page 8).

$$f(x|c) \propto \exp\left(-(x-\mu)'R^{-1}(x-\mu)\right)$$

where  $\mu = f(c)$  (interpreted as n-dimensional vector)  
 $R = g(c)$  (interpreted as n\*n matrix)

```
__init__(shape, cond_shape, f, g, rv=None, cond_rv=None, base_class=None)
```

Initialise general gauss cpdf.

#### Parameters

- **shape** (*int*) – dimension of random variable
- **cond\_shape** (*int*) – dimension of conditioning variable
- **f** (*callable*) –  $\mu = f(c)$  where  $c = \text{condition}$
- **g** (*callable*) –  $R = g(c)$  where  $c = \text{condition}$
- **base\_class** (*class*) – class whose instance is created as a base pdf for this cpdf. Must be a subclass of [AbstractGaussPdf](#) (page 10) and the default is [GaussPdf](#) (page 10). One alternative is [LogNormPdf](#) (page 11) for example.

*Please note that the way of specifying callback function f and g is not yet fixed and may be changed in future.*

```
class pybayes.pdfs.GammaCPdf(gamma, rv=None, cond_rv=None)
```

Conditional pdf based on [GammaPdf](#) (page 11) tuned in a way to have mean  $\mu$  and standard deviation  $\gamma\mu$ . In other words,  $\text{GammaCpdf}(\mu, \gamma) = \text{GammaPdf}(k = \gamma^{-2}, \theta = \gamma^2\mu)$

The  $\gamma$  parameter is specified in constructor and the  $\mu$  parameter is the conditioning variable.

```
__init__(gamma, rv=None, cond_rv=None)
    Initialise conditional gamma pdf.
```

**Parameters** `gamma` (*float*) –  $\gamma$  parameter above

```
class pybayes.pdfs.InverseGammaCPdf(gamma, rv=None, cond_rv=None)
    Conditional pdf based on InverseGammaPdf (page 11) tuned in a way to have
    mean  $\mu$  and standard deviation  $\gamma\mu$ . In other words,  $\text{InverseGammaCpdf}(\mu, \gamma) =$ 
 $\text{InverseGammaPdf}(\alpha = \gamma^{-2} + 2, \beta = (\gamma^{-2} + 1)\mu)$ 
```

The  $\gamma$  parameter is specified in constructor and the  $\mu$  parameter is the conditioning variable.

```
__init__(gamma, rv=None, cond_rv=None)
    Initialise conditional inverse gamma pdf.
```

**Parameters** `gamma` (*float*) –  $\gamma$  parameter above

```
class pybayes.pdfs.ProdCPdf(factors, rv=None, cond_rv=None)
    Pdf that is formed as a chain rule of multiple conditional pdfs. Extends CPdf (page 8).
```

In a simple textbook case denoted below it isn't needed to specify random variables at all. In this case when no random variable associations are passed, ProdCPdf ignores rv associations of its factors and everything is determined from their order. ( $x_i$  are arbitrary vectors)

$$p(x_1 x_2 x_3 | c) = p(x_1 | x_2 x_3 c) p(x_2 | x_3 c) p(x_3 | c)$$

$$\text{or } p(x_1 x_2 x_3) = p(x_1 | x_2 x_3) p(x_2 | x_3) p(x_3)$$

```
>>> f = ProdCPdf((f1, f2, f3))
```

For less simple situations, specifying random value associations is needed to establish data-flow:

$$p(x_1 x_2 | y_1 y_2) = p_1(x_1 | y_1) p_2(x_2 | y_2 y_1)$$

```
>>> # prepare random variable components:
>>> x_1, x_2 = RVComp(1), RVComp(1, "name is optional")
>>> y_1, y_2 = RVComp(1), RVComp(1, "but recommended")

>>> p_1 = SomePdf(..., rv=[x_1], cond_rv=[x_2])
>>> p_2 = SomePdf(..., rv=[x_2], cond_rv=[y_2, y_1])
>>> p = ProdCPdf((p_2, p_1), rv=[x_1, x_2], cond_rv=[y_1, y_2]) # order of
>>> # pdfs is insignificant - order of rv components determines data flow
```

Please note: this will change in near future in following way: it will be always required to specify *rvs* and *cond\_rvs* of factor pdfs (at least ones that are shared), but product *rv* and *cond\_rv* will be inferred automatically when not specified.

```
__init__(factors, rv=None, cond_rv=None)
    Construct chain rule of multiple cpdfs.
```

**Parameters** `factors` (sequence of [CPdf](#) (page 8)) – sequence of densities that will form the product

Usual way of creating ProdCPdf could be:

```
>>> prod = ProdCPdf([MLinGaussCPdf(..), UniPdf(..)], rv=[..], cond_rv=[..])
```

## Chapter 4

# Bayesian Filters

This module contains Bayesian filters.

All classes from this module are currently imported to top-level pybayes module, so instead of `from pybayes.filters import KalmanFilter` you can type `from pybayes import KalmanFilter`.

### 4.1 Filter prototype

`class pybayes.filters.Filter`

Abstract prototype of a bayesian filter.

`bayes(yt, cond=None)`

Perform approximate or exact bayes rule.

#### Parameters

- **yt** (1D `numpy.ndarray`) – observation at time t
- **cond** (1D `numpy.ndarray`) – condition at time t. Exact meaning is defined by each filter

**Returns** always returns True (see `posterior()` (page 18) to get posterior density)

`posterior()`

Return posterior probability density funcion (`Pdf` (page 9)).

**Returns** posterior density

**Return type** `Pdf` (page 9)

*Filter implementations may decide to return a reference to their work pdf - it is not safe to modify it in any way, doing so may leave the filter in undefined state.*

`evidence_log(yt)`

Return the logarithm of *evidence* function (also known as *marginal likelihood*) evaluated in point yt.

**Parameters** **yt** (`numpy.ndarray`) – point which to evaluate the evidence in

**Return type** double

This is typically computed after `bayes()` (page 18) with the same observation:

```
>>> filter.bayes(yt)
>>> log_likelihood = filter.evidence_log(yt)
```

## 4.2 Kalman Filter

`class pybayes.filters.KalmanFilter(A, B=None, C=None, D=None, Q=None, R=None, state_pdf=None)`

Implementation of standard Kalman filter. `cond` in `bayes()` (page 20) is interpreted as control (intervention) input  $u_t$  to the system.

Kalman filter forms *optimal Bayesian solution* for the following system:

$$\begin{aligned}x_t &= A_t x_{t-1} + B_t u_t + v_{t-1} & A_t &\in \mathbb{R}^{n,n} & B_t &\in \mathbb{R}^{n,k} & n &\in \mathbb{N} & k &\in \mathbb{N}_0 \text{ (may be zero)} \\y_t &= C_t x_t + D_t u_t + w_t & C_t &\in \mathbb{R}^{j,n} & D_t &\in \mathbb{R}^{j,k} & j &\in \mathbb{N} & j &\leq n\end{aligned}$$

where  $x_t \in \mathbb{R}^n$  is hidden state vector,  $y_t \in \mathbb{R}^j$  is observation vector and  $u_t \in \mathbb{R}^k$  is control vector.  $v_t$  is normally distributed zero-mean process noise with covariance matrix  $Q_t$ ,  $w_t$  is normally distributed zero-mean observation noise with covariance matrix  $R_t$ . Additionally, initial pdf (`state_pdf`) has to be Gaussian.

`__init__(A, B=None, C=None, D=None, Q=None, R=None, state_pdf=None)`  
Initialise Kalman filter.

### Parameters

- **A** (2D `numpy.ndarray`) – process model matrix  $A_t$  from [class description](#) (page 19)
- **B** (2D `numpy.ndarray`) – process control model matrix  $B_t$  from [class description](#) (page 19); may be None or unspecified for control-less systems
- **C** (2D `numpy.ndarray`) – observation model matrix  $C_t$  from [class description](#) (page 19); must be full-ranked
- **D** (2D `numpy.ndarray`) – observation control model matrix  $D_t$  from [class description](#) (page 19); may be None or unspecified for control-less systems
- **Q** (2D `numpy.ndarray`) – process noise covariance matrix  $Q_t$  from [class description](#) (page 19); must be positive definite
- **R** (2D `numpy.ndarray`) – observation noise covariance matrix  $R_t$  from [class description](#) (page 19); must be positive definite
- **state\_pdf** (`GaussPdf` (page 10)) – initial state pdf; this object is referenced and used throughout whole life of `KalmanFilter`, so it is not safe to reuse state pdf for other purposes

All matrices can be time-varying - you can modify or replace all above stated matrices providing that you don't change their shape and all constraints still hold. On the other hand, you **should not modify** `state_pdf` unless you really know what you are doing.

```
>>> # initialise control-less Kalman filter:
>>> kf = pb.KalmanFilter(A=np.array([[1.]]),
                        C=np.array([[1.]]),
                        Q=np.array([[0.7]]), R=np.array([[0.3]]),
                        state_pdf=pb.GaussPdf(...))
```

```
bayes(yt, cond=array([], dtype=float64))
    Perform exact bayes rule.
```

#### Parameters

- **yt** (1D `numpy.ndarray`) – observation at time  $t$
- **cond** (1D `numpy.ndarray`) – control (intervention) vector at time  $t$ . May be unspecified if the filter is control-less.

**Returns** always returns `True` (see `posterior()` (page 18) to get posterior density)

## 4.3 Particle Filter Family

```
class pybayes.filters.ParticleFilter(n, init_pdf, p_xt_xtp, p_yt_xt, proposal=None)
```

Standard particle filter (or SIR filter, SMC method) implementation with resampling and optional support for proposal density.

Posterior pdf is represented using `EmpPdf` (page 12) and takes following form:

$$p(x_t|y_{1:t}) = \sum_{i=1}^n \omega_i \delta(x_t - x_t^{(i)})$$

```
__init__(n, init_pdf, p_xt_xtp, p_yt_xt, proposal=None)
    Initialise particle filter.
```

#### Parameters

- **n** (*int*) – number of particles
- **init\_pdf** (`Pdf` (page 9)) – either `EmpPdf` (page 12) instance that will be used directly as a posterior (and should already have initial particles sampled) or any other probability density which initial particles are sampled from
- **p\_xt\_xtp** (`CPdf` (page 8)) –  $p(x_t|x_{t-1})$  cpdf of state in  $t$  given state in  $t-1$
- **p\_yt\_xt** (`CPdf` (page 8)) –  $p(y_t|x_t)$  cpdf of observation in  $t$  given state in  $t$
- **proposal** (`Filter` (page 18)) – (optional) a filter whose posterior will be used to sample particles in `bayes()` (page 21) from (and to correct their weights). More specifically, its `bayes` (page 18)  $(y_t, x_{t-1}^{(i)})$

method is called before sampling  $i$ -th particle. Each call to `bayes()` should therefore reset any effects of the previous call.

`bayes(yt, cond=None)`

Perform Bayes rule for new measurement  $y_t$ ; `cond` is ignored.

**Parameters** `cond` (*numpy.ndarray*) – optional condition that is passed to  $p(x_t|x_{t-1})$  after  $x_{t-1}$  so that it can be rewritten as:  $p(x_t|x_{t-1}, c)$ .

The algorithm is as follows:

- 1.generate new particles:  $x_t^{(i)} = \text{sample from } p(x_t^{(i)}|x_{t-1}^{(i)}) \quad \forall i$
- 2.recompute weights:  $\omega_i = p(y_t|x_t^{(i)})\omega_i \quad \forall i$
- 3.normalise weights
- 4.resample particles

```
class pybayes.filters.MarginalizedParticleFilter(n,          init_pdf,          p_bt_btp,
                                                kalman_args,
                                                kalman_class=<class      'py-
                                                bayes.filters.KalmanFilter'>)
```

Simple marginalized particle filter implementation. Assume that the state vector  $x$  can be divided into two parts  $x_t = (a_t, b_t)$  and that the pdf representing the process model can be factorised as follows:

$$p(x_t|x_{t-1}) = p(a_t|a_{t-1}, b_t)p(b_t|b_{t-1})$$

and that the  $a_t$  part (given  $b_t$ ) can be estimated with (a subclass of) the `KalmanFilter` (page 19). Such system may be suitable for the marginalized particle filter, whose posterior pdf takes the form

$$p = \sum_{i=1}^n \omega_i p(a_t|y_{1:t}, b_{1:t}^{(i)}) \delta(b_t - b_t^{(i)})$$

$p(a_t|y_{1:t}, b_{1:t}^{(i)})$  is posterior pdf of  $i^{th}$  Kalman filter

where  $b_t^{(i)}$  is value of the (b part of the)  $i^{th}$  particle

$\omega_i \geq 0$  is weight of the  $i^{th}$  particle  $\sum \omega_i = 1$

**Note:** currently  $b_t$  is hard-coded to be process and observation noise covariance of the  $a_t$  part. This will be changed soon and  $b_t$  will be passed as condition to `KalmanFilter.bayes()` (page 20).

```
__init__(n, init_pdf, p_bt_btp, kalman_args, kalman_class=<class 'py-
        bayes.filters.KalmanFilter'>)
```

Initialise marginalized particle filter.

#### Parameters

- **n** (*int*) – number of particles
- **init\_pdf** (*Pdf* (page 9)) – probability density which initial particles are sampled from. (both  $a_t$  and  $b_t$  parts)
- **p\_bt\_btp** (*CPdf* (page 8)) –  $p(b_t|b_{t-1})$  cpdf of the (b part of the) state in  $t$  given state in  $t-1$



- **kalman\_args** (*dict*) – arguments for the Kalman filter, passed as dictionary; *state\_pdf* key should not be specified as it is supplied by the marginalized particle filter
- **kalman\_class** (*class*) – class of the filter used for the  $a_t$  part of the system; defaults to [KalmanFilter](#) (page 19)

**bayes**(*yt*, *cond=None*)

Perform Bayes rule for new measurement  $y_t$ . Uses following algorithm:

- 1.generate new  $b$  parts of particles:  $b_t^{(i)} = \text{sample from } p(b_t^{(i)}|b_{t-1}^{(i)}) \quad \forall i$
- 2.set  $Q_i = b_t^{(i)} \quad R_i = b_t^{(i)}$  where  $Q_i, R_i$  is covariance of process (respectively observation) noise in  $i$ th Kalman filter.
- 3.perform Bayes rule for each Kalman filter using passed observation  $y_t$
- 4.recompute weights:  $\omega_i = p(y_t|y_{1:t-1}, b_t^{(i)})\omega_i$  where  $p(y_t|y_{1:t-1}, b_t^{(i)})$  is *evidence (marginal likelihood)* pdf of  $i$ th Kalman filter.
- 5.normalise weights
- 6.resample particles

## Chapter 5

# PyBayes Development

This document should serve as a reminder to me and other possible PyBayes hackers about PyBayes coding style and conventions.

### 5.1 General Layout and Principles

PyBayes is developed with special dual-mode technique - it is both perfectly valid pure Python library and optimised cython-built binary python module.

PyBayes modules are laid out with following rules:

- all modules go directly into `pybayes/<module>.py` (pure Python file) with cython augmentation file in `pybayes/module.pxd`
- in future, bigger independent units can form subpackages
- `pybayes/wrappers/` subpackage is special, it is the only package whose modules have different implementation for cython and for python. It is accomplished by `.py` (Python) and `.pyx`, `.pxd` (Cython) files.

### 5.2 Tests and Stress Tests

All methods of all PyBayes classes should have a unit test. Suppose you have a module `pybayes/modname.py`, then unit tests for all classes in `modname.py` should go into `pybayes/tests/test_modname.py`. You can also write stress test (something that runs considerably longer than a test and perhaps provides a simple benchmark) that would go into `pybayes/tests/stress_modname.py`.

### 5.3 Imports and cimports

**No internal module can import `pybayes`!** That would result in an infinite recursion. External PyBayes clients can and should, however, only `import pybayes` (and in future also `import pybayes.subpackage`). From inside PyBayes just import relevant pybayes modules, e.g. `import pdfs`. Notable exception from this rule is `cimport`, where (presumably due to a cython bug) `from a.b cimport c` sometimes doesn't work and one has to type `from pybayes.a.b cimport c`.

Imports in \*.py files should adhere to following rules:

- import first system modules (sys, io..), then external modules (matplotlib..) and then pybayes modules.
- **instead of** importing **numpy** directly use `import wrappers._numpy as np`. This ensures that fast C alternatives are used in compiled mode.
- **instead of** importing **numpy.linalg** directly use `import wrappers._linalg as linalg`.
- use `import module [as abbrev]` or, for commonly used symbols from module `import symbol`.
- `from module import *` shouldn't be used.

Following rules apply to \*.pxd (cython augmentation) files:

- no imports, just cimports.
- use same import styles as in associated .py file. (from module cimport vs. cimport module [as abbrev])
- for numpy use `cimport pybayes.wrappers._numpy as np`
- for numpy.linalg use `cimport pybayes.wrappers._linalg as linalg`

*Above rules do not apply to pybayes/tests. These modules are considered external and should behave as a client script.*

## 5.4 Releasing PyBayes

Things to do when releasing new version (let it be **X.Y**) of PyBayes:

### 5.4.1 Before Tagging

1. Set fallback version to **X.Y** in *setup.py* (around line 15)
2. Set version to **X.Y** in *support/python-pybayes.spec*
3. Ensure *ChangeLog.rst* mentions all important changes
4. (Optional) update **short description** in *setup.py* **AND** *support/python-pybayes.spec*
5. (Optional) update **long description** in *setup.py* **AND** *README.rst* **AND** *support/python-pybayes.spec*

### 5.4.2 Tagging

1. Check everything, run tests and stresses for Python 2.7, 3.2 in both pure/Cython mode
2. `git tag -s vX.Y`
3. `git-archive-all.sh --format tar --prefix PyBayes-X.Y/ dist/PyBayes-X.Y.tar`
4. `gzip dist/PyBayes-X.Y.tar`
5. `./setup.py register`

(do not use `./setup.py upload`, it does not work as some files are not in MANIFEST etc.)

### 5.4.3 Publishing

1. Upload `PyBayes-X.Y.tar.gz` to <https://github.com/strohel/PyBayes/downloads> and <http://pypi.python.org/pypi/PyBayes>
2. Build and upload docs: `cd ../pybayes-doc && ./synchronize.sh`
3. Upload updated *python-pybayes.spec* file to <https://build.opensuse.org/package/files?package=python-pybayes&project=home%3Astrohel>
4. If **short description** of PyBayes changed, update it manually at following places:
  - <https://github.com/strohel/PyBayes>
5. If **long description** of PyBayes changed, update it manually at following places:
  - <https://build.opensuse.org/package/show?package=python-pybayes&project=home%3Astrohel>
  - [http://scipy.org/Topical\\_Software](http://scipy.org/Topical_Software)
  - <http://www.ohloh.net/p/pybayes>

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