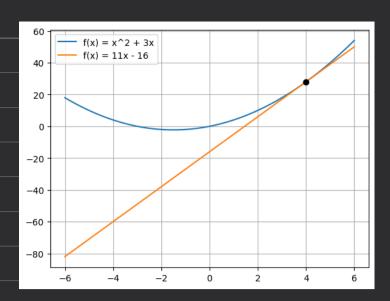
$$f'(x) = 3(x+x^{3})^{2} \cdot (1+3x^{2}) - 3x^{2}$$

$$= 3(x^{2}+2x^{4}+x^{6})(1+3x^{2}) - 3x^{2}$$

$$= 3(x^{2}+2x^{4}+x^{6}+3x^{4}+6x^{6}+3x^{8}) - 3x^{2}$$

$$= 5x^{4}+7x^{6}+3x^{8}$$



$$(1) \quad f(x) = x^2 + 3x$$

a) 
$$f(x_0 + \delta) = f(x_0) + \frac{\partial f}{\partial x}|_{x_0} - \delta$$
  $f'(x) = 2x + \delta$   
 $= 28 + 11 \cdot \delta$   $f'(4) = 11$   
 $= 28 + 11 \cdot (x - x_0)$   
 $= 28 + 11 \cdot (x - 44) = 11 \cdot (x - 16)$ 

3 
$$f(\vec{x}(\vec{p}_0 + \vec{J})) \approx f(\vec{x}(\vec{p}_0)) + [(grad f)]_{\vec{p}_0} \cdot \vec{\vec{J}}$$
  
 $f(x_1(\vec{p}), x_2(\vec{p})) = x_1(\vec{p}) + x_2^3(\vec{p})$   
=>  $grad f = [1, 3x_2^2(\vec{p})]$ 

$$\chi_1(\vec{p}) = 2pz$$

$$\chi_1(\vec{p}) = p_1 + pz^2 \qquad = 0 \qquad = 0 \qquad 2$$

$$\chi_1(\vec{p}) = p_1 + pz^2 \qquad = 0 \qquad = 0 \qquad 2$$

$$= \int \{(x_{1}(\vec{p}), x_{2}(\vec{p})) + [1, 3x_{1}^{2}(\vec{p})] \begin{bmatrix} 0 & 2 \\ 1 & 2p_{2} \end{bmatrix} \begin{bmatrix} \delta_{1} \\ \delta_{2} \end{bmatrix}$$

$$= \int \{(x_{1}(\vec{p}), x_{1}(\vec{p})) + [3x_{2}^{2}, 2 + 6p_{2}x_{2}^{2}] [\int_{J_{2}}^{J_{1}} ] (x_{2} - p_{1} + p_{2}^{2}) \}$$

$$= \int \{(x_{1}(\vec{p}), x_{2}(\vec{p})) + [3(p_{1} + p_{2}^{2})^{2}, 2 + 6p_{2}(p_{1} + p_{2}^{2})^{2}] [\int_{J_{2}}^{J_{1}} ] (x_{2} - p_{1} + p_{2}^{2}) \}$$

$$= \int \{(x_{1}(\vec{p}), x_{2}(\vec{p})) + (3(p_{1} + p_{2}^{2})^{2} \delta_{1} + 2 \delta_{2} + 6p_{2}(p_{1} + p_{2}^{2})^{2} \delta_{2}) \}$$

$$\begin{array}{ccc}
(y) & x \in \mathbb{R}^d & A \in \mathbb{R}^{d \times d} & PD \\
f(\vec{x}) & = 2\vec{x}^T A \vec{x} - 10\vec{x} \\
\frac{\partial f}{\partial \vec{x}} & = 2\vec{x}^T (A + A^T) - 10\vec{x}^T & = 4\vec{x}^T A - 10\vec{x}^T
\end{array}$$